# SmartCheck: Automatic and Efficient **Counterexample Reduction and Generalization**

# UNPUBLISHED DRAFT

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#### **Abstract**

QuickCheck, developed by Claessen and Hughes, is a powerful library for automatic test-case generation. Because QuickCheck performs random testing, some of the counterexamples discovered are very large. QuickCheck provides an interface for the user to write shrink functions to attempt to reduce the size of counterexamples. Hand-written implementations of shrink can be complex, inefficient, and consist of significant boilerplate code. Furthermore, shrinking is only one aspect in debugging: counterexample generalization is the process of extrapolating from individual counterexamples to a class of counterexamples, often requiring a flash of insight from the programmer. To improve counterexample reduction and generalization, we introduce SmartCheck. SmartCheck is a debugging tool that reduces algebraic data using generic search heuristics to efficiently find smaller counterexamples. In addition to shrinking, SmartCheck also automatically generalizes counterexamples to formulas representing classes of counterexamples. SmartCheck has been implemented for Haskell and is freely available.

#### Introduction 1.

The QuickCheck testing framework was a revolutionary stepforward in type-directed random testing [3, 4]. Originally designed for Haskell, QuickCheck has been ported to other languages and is a now a widely-used testing tool. Because QuickCheck generates random values for testing, counterexamples it finds may be substantially larger than a minimal counterexample. In their original QuickCheck paper [3], the authors report the following user experience by Andy Gill:

Sometimes the counterexamples found are very large and it is difficult to go back to the property and understand why it is a counterexample.

That is, automated testing helps find a counterexample, but it may be a very large counterexample. We are left facing the shrinking problem: assume there exist a set of inputs  $i_0, i_1, \ldots, i_n$ , such that for program P (modeled as a function mapping inputs to output) and property  $\phi$ ,  $\phi(P(i_0, i_1, \dots, i_n))$  is false. The shrinking

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problem is to find the smallest set of inputs  $i'_0, i'_1, \ldots, i'_n$ , according to some measure, such that  $\phi(P(i_-0, i_-1, ..., i_-n))$  is also

In general, the problem too expensive to solve, since it requires showing that for a set of failing inputs, there exist no strictly smaller inputs that also cause the property to fail. Such a demonstration requires exhaustive testing or proof. Solutions to the shrinking problem are therefore approximated to efficiently discover sufficiently small inputs causing the input to fail. Usually, the shrunk inputs are derived algorithmically (but perhaps nondeterministically) from a known larger set of inputs resulting in failure, and the inputs may not be minimal.

To address the shrinking problem, QuickCheck defines a type class Arbitrary that presents a method arbitrary for generating random values of a given type. Gill added another method to the type class:

```
smaller :: a -> [a]
```

The purpose of smaller is to generate strictly smaller values, according to some measure, from a given counterexample. These new values are then tested to attempt to find a smaller counterexample. Today, smaller is called shrink.

In industrial uses, shrinking is essential. In describing commercial applications of QuickCheck, Hughes has noted that "without it [shrinking], randomly generated failing cases would often be so large as to be almost useless." [10]. Hughes et al. also give an extended example in which shrinking is essential in debugging telecom software [1].

Defining an efficient and effective shrink method requires a good understanding of how shrinking in QuickCheck works and the semantics of the property and program being evaluated. Bad definitions can be so slow or so ineffective at shrinking that they

In addition, shrinking is one side of the coin when it comes to making counterexamples more understandable: the other side is extrapolation from individual counterexamples to a class of counterexamples. This leap of abstraction is often implicitly made by the programmer in determining the reason why counterexamples fail the property. For example, the following is a relatively small counterexample returned when QuickChecking a property in (a bug-injected version of) Xmonad, a popular X11 window manager written in Haskell [18]:

```
StackSet {current = Screen {workspace = Workspace
{tag = NonNegative {getNonNegative = 0}, layout =
-1, stack = Just (Stack {focus = 'S', up = "",
down = ""})}, screen = 1, screenDetail = 1},
visible = [Screen {workspace = Workspace {tag
= NonNegative {getNonNegative = 2}, layout =
```

```
-1, stack = Nothing}, screen = 2, screenDetail
= -1},Screen {workspace = Workspace {tag =
NonNegative {getNonNegative = 3}, layout = -1,
stack = Nothing}, screen = 0, screenDetail =
-1}], hidden = [Workspace {tag = NonNegative
{getNonNegative = 1}, layout = -1, stack =
Just (Stack {focus = '\NUL', up = "", down =
""})},Workspace {tag = NonNegative {getNonNegative}
= 4}, layout = -1, stack = Just (Stack {focus =
'I', up = "", down = ""})}], floating = fromList
[]}
```

(This counterexample uses Haskell's default Show instances, which uses record syntax.) Programmers may be familiar with having to debug a "wall of text" as shown above. What if instead a formula like the following were returned, stating that for any well-typed values  $x_0$ ,  $x_1$ ,  $x_2$ , and  $x_3$ , tested, a counterexample is found?

```
forall values x0 x1 x2 x3:
   StackSet
   (Screen (Workspace x0 (-1) (Just x1)) 1 1)
   x2 x3 (fromList [])
```

The formula quantifies away all the irrelevant portions of the data structure with respect to the property, so that the user can focus on the heart of the problem in a class of counterexamples. Given a program and large counterexample, *SmartCheck* returns such a formula.

**SmartCheck** Motivated by the problems of reducing and generalizing large counterexamples, we developed SmartCheck. SmartCheck takes a counterexample produced by some oracle and generically minimizes and generalizes the counterexample.

As shown in the motivating example in Section 2, SmartCheck can shrink more than an order-of-magnitude faster than even the most efficient hand-written shrink implementations for some properties and programs. As well, the time required to shrink scales linearly with the size of the counterexample—other common shrink implementations often scale in polynomial time or worse. (Shrinking time is important in real-world uses; see Section 7 for examples.)

After presenting some preliminary definitions in Section 3, in Section 4, we describe SmartCheck's generic counterexample reduction algorithm. The algorithm is particularly novel in that it generates new random sub-values during the reduction phase (see related work in Section 8).

SmartCheck implements three novel approaches to automatically generalize counterexamples, which are described in Section 5. The first algorithm universally quantifies sub-values that always fail in tests. The second algorithm existentially quantifies sub-values for types in which every possible variant fails the property. For example, finding counterexamples (Left 2) and (Right True) for the type

Either Int Bool

means there exists a counterexample regardless of the variant chosen. Existential generalization is useful for large sum types, as found in abstract syntax tree (AST) definitions, for example.

The third algorithm automatically strengthens properties by omitting "similar" counterexamples to the ones previously observed. The algorithm is motivated by noting that there are often multiple ways in which a property may fail; for example, a property stating that pretty-printing an AST and then parsing it results in the original AST may fail due to multiple bugs. During testing, it is useful to discover counterexamples arising from each bug in one go. In practice, the problem is solved by discovering a counterexample cex, abstracting it, and then adding a new precondition

to the property that informally says "omit counterexamples of form cex." Adding preconditions manually is laborious and may cause the programmer to make premature fixes to the program, if she believes she has isolated the error before she actually does.

We describe our implementation based on generic programming in Section 6; the implementation is open-source. In Section 7, we discuss some of our experiences with using SmartCheck, including checking properties from XMonad and a natural language processing library.

# 2. A Motivating Example

```
type I = [Int16]
data T = T I I I I I

toList :: T -> [[Int16]]
toList (T i0 i1 i2 i3 i4) = [i0, i1, i2, i3, i4]

pre :: T -> Bool
pre t = all ((< 256) . sum) (toList t)

post :: T -> Bool
post t = (sum . concat) (toList t) < 5 * 256

prop :: T -> Property
prop t = pre t ==> post t
```

Figure 1: Example program and property.

In this section, we motivate in more detail the challenges in shrinking counterexamples by comparing manual approaches using QuickCheck to SmartCheck. (We focus on shrinking rather than generalization here since counterexample generalization is unique to SmartCheck.) We will show how a small data type and simple property can result in large counterexamples without any shrinking. Then we show the difficulty in designing an efficient shrink implementation manually, which is required when using QuickCheck; we will show a poor design before arriving at a "canonical" manual solution. However, even the canonical solution produces significantly larger counterexamples and takes significantly longer to produce them than SmartCheck, even though SmartCheck's shrinking strategy is completely automatic and generic.

Consider the example in Figure 1. Data type T is a product type containing five lists of signed 16-bit integers.

Now suppose we are modeling some program that serializes values of type T. The input to the program satisfies the invariant pre, that the sum of values in each list of Int16s is less than or equal to 256. Assuming this, we want to show post holds, that the sum of all the values from T is less than 5\*256, where five is the number of fields in T. At first glance, the property seems reasonable. But we have forgotten about underflow; for example, the value

```
T [-20000] [-20000] [] [] []
```

satisfies pre but fails post (the ==> operator in the figure is implication from the OuickCheck library).

Despite the simplicity of the example, a typical counterexample returned by QuickCheck can be large. With standard settings and no shrinking, the average counterexample discovered contains just over 80 Int16 values, and over five percent contain over 100 values. Thus, it pays to define shrink!

<sup>&</sup>lt;sup>1</sup> All examples and algorithms in this paper are presented in Haskell 2010 [8] plus the language extensions of existential type quantification and scoped type variables.

We might first naively try to shrink counterexamples for a data type like T by taking the cross-product of shrunk values over the arguments to the constructor T. This can be expressed using Haskell's list-comprehension notation:

While the above definition appears reasonable on first glance, there are two problems with it. First, the result of (shrink t) is null if any list contained in t is null, in which case t will not be shrunk. More troublesome is that with QuickCheck's default Arbitrary instances, the length of potential counterexamples returned by shrink can easily exceed  $10^{10}$ , which is an intractable number of tests for QuickCheck to analyze. The reason for the blowup is that shrinking a list [a] produces a list [[a]], a list of lists; each list is a new shrinking of the original list. Then, we take the crossproduct of the generated lists. For the example above, with some counterexamples, the shrinking stage may appear to execute for hours, consuming ever more memory, without returning a result.

The first way we will control the complexity is focusing on structurally shrinking the data type rather than shrinking the base types. We prevent QuickCheck from using its default shrink instance for Int16 by defining a newtype:

```
newtype J = J { getInt :: Int16 }
```

Next, a programmer might try to control the complexity by truncating lists using truncation where

```
take n ls
```

returns the first n elements 1s. The trade-off is quicker shrinking with a lower probability of finding a smaller counterexample. For example, we might redefine shrink as follows:

Call this version "truncated shrink". Truncation controls the blowup of the input-space, but the downside is that potentially smaller counterexamples may be omitted.

Someone who understands the semantics of QuickCheck's shrink implementation defines a shrink instance as follows:<sup>2</sup>

This "tuple shrink" definition does not suffer the same shortcomings: it shrinks a value even if it contains an empty list, and the combinatorial blowup of shrink candidates is avoided, since a pair (a,b) is shrunk by attempting to shrink a while holding b constant, then attempting to shrink b while holding a constant (and is generalized from pairs to arbitrary tuples). Thus, each argument to T is independently shrunk.

Finally, with this combination of shrinking tuples and disabling shrinking for Int16 values, we have an efficient and effective shrinking approach.

The results of our discussion above are summarized in Table 2 and the corresponding graph in Figure 2. They show three approaches to shrinking with QuickCheck: no shrinking (QC none), to provide a baseline, truncated shrinking (QC trunc) with Int16 shrinking disabled, in which each list is truncated to 10 elements,

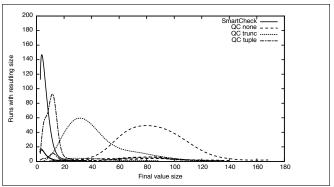


Figure 2: Results for 1000 tests of the program in Figure 1.

	QC none	QC trunc	QC tuple	SmartCheck
Mean	83, 0.013s	40, 0.064s	10, 0.031s	6, 0.021s
Std. dev.	22, 0.014	20, 0.334	4, 0.039	4, 0.009
95%	119, 0.023s	84, 0.153s	16, 0.052s	13, 0.036s

**Table 1.** Summarizing data for the graph in Figure 2. Entries contain execution time (in seconds) and counterexample sizes (counting Int16 values).

and tuple shrinking (QC tuple), also with Int16 shrinking disabled. We omit SmallCheck, since as noted, it is not even feasible for the example with default instances.<sup>3</sup> We graph the final counterexample size, measured in the total number of Int16 values, and execution time for counterexample discovery and shrinking. Figure 2 shows how many of the 1000 runs resulted in a final value of a particular size, fitting the data with a Bezier curve.

In Table 2, we summarize the graphed values and provide execution time in seconds as well. For both execution time and final value size, we summarize the mean, median, standard deviation, and the results at the 95th percentile. (While we provide the standard deviations, note that the plots are not necessarily Gaussian.)

SmartCheck produces consistently small counterexamples and does so quickly—even smaller and faster than the best hand-tuned solution—all without writing any problem-specific code. Note that the "no shrinking" example provides a lower-bound on execution time (only including counterexample discovery time) and an upper-bound on counterexample size. In this example, the hand-written "tuple shrink" algorithm is only slightly slower and produces slightly larger results. In Section 7.3, we provide additional benchmarks, but now we turn to the design of SmartCheck.

We now describe in detail SmartCheck's algorithm for generic shrinking.

# 3. Preliminaries

SmartCheck focuses on algebraic data types represented as "sums of products" including recursive and mutually recursive types. We sometimes refer to the elements of a sum type as a *variant* that is *tagged* by a constructor. For example, the type

contains two variants, tagged by the constructors Just and Nothing, respectively.

To present the algorithms in the following sections, we provide some definitions in the form of methods of a SubTypes type class.

<sup>&</sup>lt;sup>2</sup> The following approach was suggested to the author by John Hughes.

<sup>&</sup>lt;sup>3</sup> All results reported in the paper are with a GHC-7.6.3-compiled program, using -02, on a 2.8 GHz 4 core i7 with 16GB memory under OSX v. 10.9.2.

(SmartCheck requires instances to be defined for data being analyzed; in Section 6, we describe how instances for the type class are derived automatically.)

```
type Idx = Int
type Size = Int
data SubVal = forall a. SubTypes a => SubVal a

class Arbitrary a => SubTypes a where
    size :: a -> Size
    index :: a -> Idx -> Maybe SubVal
    replace :: a -> Idx -> SubVal -> a
    constr :: a -> String
    constrs :: a -> [String]
    opaque :: a -> Bool
    subVals :: a -> Tree SubVal
```

The SubTypes type class requires QuickCheck's Arbitrary as a super-class. SubTypes has the following methods:

- size returns the size of a value—intuitively, the number of constructors contained within it,
- index returns a *sub-value* at a breadth-first index in a value,
- replace replaces a sub-value at a particular focus (returning the original value if the index is out-of-bounds),
- constr returns a string representation of the constructor tagging the value,
- constrs returns the list of all possible constructors from the value's type,
- opaque is false when the type of the value is an "interesting type"; informally, this is a type other than a primitive type like Int, Char, or Bool. See Section 4.2.2 for a full discussion.
- subVals returns a tree of all non opaque-type sub-values. A
  tree is a value with the type

```
data Tree a = Node { rootLabel :: a
    , subForest :: [Tree a] }
```

To illustrate typical evaluations of the methods, consider a binary tree type:

```
data T = L \mid B T T
```

and the value tree, labeled with indexes in a breadth-first order:

```
tree = B_0 (B_1 L_3 (B_4 L_6 L_8)) (B_2 L_5 L_7)
```

Here are example applications of SubTypes methods; in the following, we show the indexes with respect to the value tree:

The SubVal type is an existential data type, used as a generic container for sub-values from a counterexample. We will sometimes refer to the unwrapped value returned by index a i as the *ith sub-value of a*, so for example, (B<sub>4</sub> L<sub>6</sub> L<sub>8</sub>) is the 4th sub-value of tree. An invariant of index is that for any value a, and for the smallest  $i \geq 0$  such that

```
index a i == Nothing then for all 0 \le j < i, index a j /= Nothing
```

We use this invariant as a termination case in recursive algorithms over the sub-values of a value. (Rather than indexes into a data-structure, an alternative representation is to use a zipper data structure [9] to traverse data. We have chosen explicit indexes to write simple tail-recursive algorithms that can easily be transcribed to imperative languages.)

In our implementation, constr and constrs depends on GHC Generics [15], which we describe in Section 6. For simplicity, we omit here Generics-specific super-class constraints on the SubTypes class. Moreover, our presentation simplifies the implementation (Section 6) somewhat to improve the presentation.

# 4. Shrinking Data

In this section, we describe how to efficiently and generically shrink algebraic data values. Recall the basic idea behind the shrink method of the Arbitrary class: generate a list of values, each of which is smaller than the current counterexample. Each of the new values generated may not bear any relationship to the original counterexample other than being smaller. SmartCheck pursues an approach that searches for smaller but structurally similar counterexamples, as we make precise below.

We describe the algorithm in Section 4.1 and then describe algorithmic details in Section 4.2. Some optimizations to the reduction algorithm are described in Section 4.3.

# 4.1 Reduction Algorithm Overview

The algorithm we present for efficiently searching for new counterexamples is an instance of greedy breadth-first search over a tree structure that represents a value. At each node, during the traversal, we generate arbitrary structurally smaller sub-values and build a new value from that, leaving the remainder of the tree unchanged. Intuitively, by a *structurally smaller value*, we mean one with fewer constructors. We continue until we reach a fixed-point.

Figure 3 shows the reduction algorithm. In this algorithm and subsequent algorithms in the paper, functions in **bold font** are left undefined but their implementation is described in the text. The function reduce takes flags to customize the algorithm's behavior, a counterexample cex, and the property prop. The reduction begins at the first proper sub-value of cex; call it v. When the index idx becomes out-of-bounds and returns Nothing, the algorithm terminates. Otherwise, a list of new random values are generated.

```
sizedArbitrary :: SubTypes a => Size -> a -> IO a
```

generates a new value v' having the same type as v and that is strictly smaller (with respect to the size method) than v. Just like QuickCheck's arbitrary method, sizedArbitrary generates successively larger counterexamples when generating new values with which to replace a sub-value.

The flag scMaxReduce is the maximum number of tries to discover a new counterexample by replacing v in cex and testing it. The result of pass prop cex' for

```
getSize :: SubVal -> Size
getSize (SubVal a) = size a
newVals :: Size -> Int -> SubVal -> IO [SubVal]
newVals sz tries (SubVal a) =
 replicateM tries s where
  s = liftM SubVal (sizedArbitrary sz a)
reduce :: SubTypes a
 => ScArgs -> (a -> Property) -> a -> IO a
reduce args prop cex = reduce' 1
 where
 reduce' idx
    | Just v <- index cex idx
    = do vs <- newVals (getSize v)</pre>
                 (scMaxReduce args) v
         maybe (reduce' (idx+1)) (reduce args prop)
               (test cex idx vs prop)
    | otherwise = return cex
test :: SubTypes a => a -> Idx -> [SubVal]
    -> (a -> Property) -> Maybe a
test cex idx vs prop = go vs
 where
 go []
             = Nothing
  go (v:vs') =
    let cex' = replace cex idx v in
    if pass prop cex' then go vs'
      else Just cex'
```

Figure 3: Counterexample reduction algorithm.

```
pass :: (a -> Property) -> a -> Bool
```

holds if cex' satisfies the property prop. The property may be a conditional, in which case the value must pass the precondition as well as the consequent for pass to return True. If no failure is found, we move to the next sub-value of cex and continue. However, if a new smaller counterexample cex' is found, we start a new breadth-first traversal of cex', attempting to shrink it further.

The algorithm is guaranteed to terminate: informally, the measure for the function is that either the index increases or the size of the counterexample being evaluated decreases. The algorithm's complexity is  $\mathcal{O}(n^2)$ , where n is the number of constructors in the counterexample, assuming that generating new sub-values and testing them is done in constant time.

#### 4.2 Reduction Algorithm Details

Having described the reduction algorithm, there are two important details about its design we describe below.

# 4.2.1 Variant Counterexample Hypothesis

A motivation for the design of the reduction algorithm is something we call the *variant counterexample hypothesis*: in the search space of possible values from a given type T, if a known counterexample cex is a variant v of T, then it is most probable that other counterexamples are also from variant v. As an example supporting the hypothesis, consider a property about unintended variable capture over a language's parse tree represented by a sum type with constructors for module imports, function definitions, and global-variable assignments, respectively. A function definition counterexample can only be reduced to smaller function definition counterexamples, the only construct in which variable capture is possible.

Recall that the algorithm begins at the *first* sub-value of the counterexample rather than the 0th sub-value. The 0th sub-value of cex is cex itself. No invariant of the algorithm would be violated by beginning with the 0th sub-value, and in particular, the algorithm

would still terminate. However, we begin with a strict sub-value because of the hypothesis.

The hypothesis may be incorrect for some properties, in which case SmartCheck may potentially fail to discover a smaller counterexample. However, in Sections 5.2 and 5.3, we describe an approaches to generalize counterexamples based on discovering new counterexample variants. These generalization techniques are executed in an (optional) generalization phase, run after the reduction phase, in which this hypothesis is implemented.

#### 4.2.2 Opaque Types

SmartCheck focuses on efficiently shrinking and generalizing large data structures. It is not intended as a general replacement for QuickCheck's shrink method. Consequently, SmartCheck ignores "primitive" types without value constructors, such as Char, Int, and Word16. Our experience is that for the kinds of properties with counterexamples that contain massive data structures, shrinking primitive types does not significantly help in understanding them. Furthermore, by ignoring these types by fiat, shrinking time is dependent only on the size of a data structure as measured by the number of constructors.

We generalize the idea of ignoring primitive types by introducing the concept of *opaque types*. If the reduction algorithm encounters a opaque type, it is ignored. Opaque types include the primitive types mentioned above, but in the user can declare any substructure in a data type to be a opaque type by providing custom instances. Doing so effectively treats values from that type as "black boxes", making SmartCheck more efficient if the user knows that some portion of the structure cannot be shrunk or is irrelevant to the property.

Opaque types can be conditional. For example, the user may want lists to be shrunk in general, unless the element of the list are opaque themselves. Such a definition is possible.

Opaque types are defined by providing the method for opaque in the SubTypes type class.

<<re>ference into with QC, no int shrinking>>

# 4.3 Reduction Algorithm Optimizations

The reduction algorithm description above omits some details and optimizations we describe here.

#### 4.3.1 Sub-value Counterexample Hypothesis

Sometimes, a counterexample fails a property due to a sub-value nested deep inside the counterexample. The rest of the value is irrelevant. We call this the *sub-value counterexample hypothesis*. Thus, one way to efficiently search the space of potential counterexamples is to test a counterexample's (well-typed) sub-values.

For example, consider a simple calculator language containing constants, addition, and division, together with an evaluator that checks if the divisor is 0 and returning Nothing in that case:

Now consider the property prop\_div, claiming that if divSubTerms holds on an expression, then the evaluator returns Just a value:

```
divSubTerms :: Exp -> Bool
divSubTerms (C _) = True
```

```
reduceOpt :: forall a . SubTypes a
 => ScArgs -> (a -> Property) -> a -> IO a
reduceOpt args prop cex = reduce' 1
 where
 reduce' idx
    | Just v <- index cex idx
    = maybe (test' v idx) (reduceOpt args prop)
            (testHole v)
    | otherwise = return cex
 test' v idx = do
   vs <- newVals (getSize v) (scMaxReduce args) v
   maybe (reduce' (idx+1)) (reduceOpt args prop)
          (test cex idx vs prop)
 testHole (SubVal a) = do
    a' <- cast a :: Maybe a
    if pass prop a' then Nothing else Just a'
```

**Figure 4:** Reduction algorithm with the sub-value counterexample optimization.

```
odivSubTerms (Div _ (C 0)) = False
divSubTerms (Add e0 e1) = divSubTerms e0
&& divSubTerms e1
divSubTerms (Div e0 e1) = divSubTerms e0
&& divSubTerms e1
```

```
prop_div e = divSubTerms e ==> eval e /= Nothing
```

Testing prop\_div, we might have a counterexample like the following:

```
Add (Div (C 5) (C (-12))) (Add (Add (C 2) (C 4)) (Add (C 7) (Div (Add (C 7) (C 3)) (Add (C (-5)) (C 5)))))
```

The cause is that divSubTerms fails to check whether the divisor evaluates to zero. In the counterexample, the culprit is a buried subvalue:

```
Div (Add (C 7) (C 3)) (Add (C (-5)) (C 5))
```

Thus, when attempting to shrink an Exp value, it pays to test whether a sub-value itself fails the property.

Generalizing the scenario, during the reduction algorithm's breadth-first search through a counterexample cex's sub-values, we may happen upon a sub-value cex' that has the same type as cex and fails the property (while passing any preconditions). In this case, we can return cex' directly, and rerun the reduction algorithm on cex'. In Figure 4, we show an updated reduction algorithm, reduceOpt, that implements this optimization. The function testHole tests the current sub-value and if it fails the property, the function tests the sub-value directly.

#### 4.3.2 Bounding Counterexample Exploration

SmartCheck's implementation contains flags to allow the user to customize its behavior. Three flags that are relevant to the reduction algorithm are the following:

```
scMaxReduce :: Int
scMaxSize :: Int
scMaxDepth :: Maybe Int
```

The scMaxReduce flag controls the number of values generated by the reduction algorithm for each sub-value analyzed. scMaxSize controls the maximum size of values generated to replace sub-values by the reduction algorithm. Thus, new sub-values must be strictly smaller than the minimum of scMaxSize and the size of the sub-value being replaced. Finally, scMaxDepth determines the maximum depth in the counterexample the reduction algorithm

should analyze. A value of Nothing means that the counterexample should be exhaustively reduced, as the algorithm is presented in Figure 3. For example, the depth of a list is determined by its length, and the depth of the binary tree defined in Section 4.1 is determined by the function depth:

```
depth L = 0 depth (B t0 t1) = 1 + max (depth t0) (depth t1)
```

Of the flags, scMaxDepth is the most important for controlling efficiency, particularly for large product types with significant "fan out". The number of sub-values of a product type value can grow exponentially with respect to the depth. Furthermore, note that as the reduction algorithm descends further, there is less chance to reduce the size of the value overall, since smaller and smaller sub-values are replaced.

# 5. Counterexample Generalization

Small counterexamples make debugging easier, but they are just half the battle. To go from a specific counterexample to the required fix in a program, the programmer must have a flash of insight in which she generalizes the counterexample to a set of counterexamples for which the program and property fails. The generalization step is an important yet under-appreciated step in the debugging process. A characterizing formula reduces the noise in favor of the signal by abstracting away portions of large counterexample that are irrelevant to why it violates the property.

The characterization of counterexamples that most helps the programmer should strike a middle ground. A single counterexample is too specific. On the other hand, the property itself is a formula that over-approximates the failing inputs. In this section, we describe two kinds of formula that fall between these two extremes that we call universal and existential sub-value generalization, respectively. We then describe a third approach to generalization to automatically strengthen a property's precondition to obtain new counterexamples.

# 5.1 Universal Sub-Value Generalization

Consider again the calculator language from Section 4.3.1. The property prop\_div is violated for any numerator, so we might generalize a counterexample like

```
Div (Add (C 7) (C 3)) (Add (C (-5)) (C 5)) by the formula forall x . Div x (Add (C (-5)) (C 5))
```

since any dividend results in divide-by-zero for the given divisor. Not only do the generalizations assist the programmer's insight, but they reduce the sheer size of the counterexample. We call the kind of formula just shown *universal sub-value generalization* and it is implemented in SmartCheck.

An extrapolation algorithm performs universal sub-value generalization. The basic idea is as follows: for a counterexample cex and a property prop, a breadth-first search over the sub-values of the cex is performed. For each sub-value, the algorithm generates new sub-values and replaces them in cex to create a list of new potential counterexamples. If no new value satisfies the property, then we extrapolate, claiming that for *any* new value replacing that sub-value in cex, the property will fail.

The extrapolation algorithm is shown in Figure 5; let sketch its specification. The algorithm is similar to the reduction algorithm in Figure 3 (and in the implementation, the algorithms are generalized and combined). The function extrapolate returns a list of indexes to be generalized in the original counterexample. In the recursive function extrapolate, there is a function guard with a call

```
subTree cex idx0 idx1
```

```
subTrees :: SubTypes a => a -> Idx -> [Idx] -> Bool
subTrees cex idx = any (subTree cex idx)
extrapolate :: SubTypes a
 => ScArgs -> a -> (a -> Property) -> IO [Idx]
extrapolate args cex prop = extrapolate' 1 []
 where
 extrapolate' idx idxs
    | subTrees cex idx idxs
   = extrapolate' (idx+1) idxs
    | Just v <- index cex idx = mkNewVals v
    | otherwise = return idxs
   where
   mkNewVals v = do
     vs <- newVals (scMaxSize args)</pre>
                    (scMaxForall args) v
      extrapolate' (idx+1)
        (if allFail args cex idx vs prop
           then idx:idxs else idxs)
allFail :: SubTypes a => ScArgs -> a -> Idx
  -> [SubVal] -> (a -> Property) -> Bool
allFail args cex idx vs prop =
 length res >= scMinForall args && and res
 where
 res = mapMaybe go vs
      = fail prop . replace cex idx
```

Figure 5: Universal sub-value generation algorithm.

```
where subTree has the type
subTree :: SubTypes a => a -> Idx -> Idx -> Bool
The value
subTree cex idx0 idx1
```

is true if in cex, the value at index idx0 is a child of index idx1 in a tree representation of cex (i.e., subVals cex). The subTrees guard prevents the algorithm from trying to generalize sub-values that are abstracted away already since their parents have been generalized. New sub-values are generated by newVals, shown in Figure 3.

The function allFail takes a counterexample cex, an index into cex, a list of new sub-values, and a property. It returns true if no new values satisfy the property. The function

```
fail :: (a -> Property) -> a -> Maybe Bool
```

is roughly the dual of pass in the reduction algorithm: (fail prop cex) returns (Just True) if cex passes prop's precondition but fails the property; (Just False) if cex non-trivially satisfies prop, and Nothing if cex fails prop's precondition.

Like in the reduction algorithm user-specified flags bound the behavior of the algorithm. We bound the size of values to generate by the flag scMaxSize, which is independent of the size of the particular sub-value. The flag scMaxForall is the analogue of the scMaxReduce flag, determining the number of values generated in trying to generalize a value. The flag scMinForall is the minimum number of Just False results required from fail to extrapolate from failed tests to a universal claim. So, for example, if scMaxForall is set to 30 and scMinForall is set to 20, we generate 30 new values, 20 of which must pass the precondition but fail the property to claim the counterexample can be generalized.

The algorithm's complexity is  $\mathcal{O}(n)$ , where n is the number of constructors in the counterexample. Again, we assume that the cost for each generating random values and testing them at each index is constant.

**Soundness** The extrapolation algorithm is unsound in two ways. First, it extrapolates from a set of counterexamples to a universal claim, similar to QuickSpec or Daikon [5, 7]. By tuning the parameters, the risk of an unsound generalization is reduced by requiring more or larger values to fail the property.

In some cases, a formula may be returned that is overly general. For example, consider the counterexample in which both arguments of the outermost Add constructor contain values causing the failure:

```
Add (Div (C 1) (Add (C (-2)) (C 2)))
(Div (C 0) (Add (C (-1)) (C 1)))
```

Since no matter what random value the first field of Add is replaced with, the property fails by the second field and vice versa for the second. The universal generalization algorithm might return the formula

```
forall values x0 \ x1 . Add x0 \ x1
```

An over-generalized formula is only a problem when generalizing without minimizing the counterexample first, as pointed out to the author by John Hughes, so in practice with SmartCheck, this form of unsoundness does not arise. However, if one were to generalize without shrinking first, the reader should read a universally quantified formula as shorthand for quantifying each variable independently and taking the conjunction of formulas. For example, instead of

# 5.2 Existential Sub-Value Generalization

Sum types denote choice in a data type. Sometimes, a property over a sum type fails because there is a bug for some of the variants but not others. For example, recall again the calculator language from Section 4.3.1. The no-division-by-zero property fails only for values that contain a variant tagged with the Div constructor. Recall again the generalized counterexample from Section 5:

```
forall x . Div x (Add (C (-5)) (C 5))
```

Because the divisor does not generalize, we know there is something special about it that causes failure. But we might wonder if there is something special about variants tagged by the Add constructor, or might we finding failing sub-values with the other variants.

We therefore introduce another kind of generalization we call existential sub-value generalization. In this generalization, if there is a counterexample containing every possible variant as a sub-value, then we abstract it. For example, suppose that divSubTerms had no equation

```
divSubTerms (Div _ (C 0)) = False
```

Then the following would all counterexamples:

```
Div (Add (C 3) (C 2)) (C 0)
Div (C 7) (Add (C (-5)) (C 5))
Div (C (-2)) (Div (C 0) (C 1))
```

Because there are only three variants in the type, we have found counterexamples built from each of them in the divisor. We therefore can claim the following formula holds:

```
subConstr :: SubVal -> String
subConstr (SubVal a) = constr a
subConstrs :: SubVal -> [String]
subConstrs (SubVal a) = constrs a
sumTest :: SubTypes a => ScArgs -> a
 -> (a -> Property) -> [Idx] -> IO [Idx]
sumTest args cex prop exIdxs = sumTest' 1 []
 where
 sumTest' idx idxs
   | subTrees cex idx (exIdxs ++ idxs)
    = sumTest' (idx+1) idxs
    | Just v <- index cex idx = fromSumTest v
    | otherwise = return idxs
   where
    fromSumTest v = do
      vs <- newVals (scMaxSize args)
              (scMaxExists args) v
      sumTest' (idx+1)
        (if constrFail cex idx vs prop
           (subConstr v) (subConstrs v)
           then idx:idxs else idxs)
constrFail :: SubTypes a => a -> Idx -> [SubVal]
 -> (a -> Property) -> String -> [String] -> Bool
constrFail cex idx vs prop con allCons =
 constrFail' [con] vs
 where
 constrFail' cons vs'
    | length cons == length allCons = True
                                    = False
    | null vs'
   | go v == Just True
   = constrFail' (c:cons) (tail vs')
    | otherwise
   = constrFail' cons (tail vs')
   where
   v = head vs'
    c = subConstr v
    go = fail prop' . replace cex idx
   prop' a = c 'notElem' cons ==> prop a
```

Figure 6: Universal sub-value generation algorithm.

We therefore present an existential sub-value generalization algorithm that performs constructor generalization. Like with the other algorithms, this algorithm also performs a breadth-first search over a counterexample.

We show the algorithm in Figure 6. The function sumTest takes a set of flags, a counterexample, a property, and a list of indexes that have already been generalized—perhaps by the extrapolation algorithm in Figure 5. The list of course may be empty if no sub-values have been previously extrapolated. In a call to subTrees, discussed in Section 5.1, the guard prevents constructor generalization if the current index is a sub-value of a previously generalized value. Otherwise, a list of well-typed new values are generated by a call to newVals, as shown in Figure 3. In the arguments to newVals, we bound the size of values generated with scMaxSize as before, and bound the number of values generated with the flag scMaxExists. Because values are randomly generated, for "wide" sum-types (i.e., with a large number of constructors), scMaxExists should be large enough to ensure with high probability that each variant is generated.

The function constrFail returns true if we replace the subvalue at index idx in counterexample cex with every possible variant given the type and construct a counterexample to the property. There are four guards to the recursive function constrFail': the first guard holds if the list of constructors tagging variants in which

a counterexample is found is equal in size to the list of all possible constructors for the type. The second guard tests whether the set of test values is null; if so (and if the first guard fails), then we have exhausted test values before finding all possible failing variants. Third, for a specific sub-value v, we test whether it fails the property. If so, we add its constructor to the list of constructors. Otherwise, we simply recurse. Note in the definition of prop', we add an additional precondition that the current constructor is not an element of constructors already seen. Thus, (go v) returns

```
Just True

if

replace cex idx v
```

passes this precondition (and any other preconditions of prop), but fails the property.

Unlike universal sub-value generalization, existential sub-value generalization is sound. The existential claim is only that for each variant, there exists at least one counterexample, so inductive reasoning is not required.

This algorithm's complexity is also  $\mathcal{O}(n)$ , where n is the number of constructors in the counterexample.

#### 5.3 Automated Precondition Strengthening

The universal and existential generalization algorithms generalize a counterexample, but in the "neighborhood" of the original counterexample. In particular, all generalizations are from the same variant as the original counterexample. To help the programmer in the generalization step, we would also like a way to test the property again, ensuring we get counterexamples (if they exist) outside of the neighborhood of the original one.

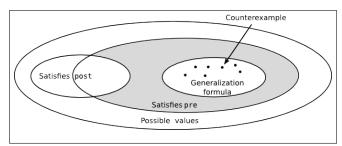


Figure 7: Counterexample generalization.

Figure 7 illustrates a property of the form (pre ==> post). Points are specific counterexamples that satisfy the precondition but fail the post-condition, and the enclosing oval represents the generalization of counterexamples resulting from either universal or existential generalization. Our goal is to find additional counterexamples in the shaded region. As new counterexamples are discovered in the shaded region (and generalized), the counterexample space becomes covered until no more classes of counterexamples exist or it becomes too difficult for the testing framework to discover them

Figure 8 shows the shape-matching algorithm used for precondition strengthening. The function takes a candidate counterexample and a list of previous counterexamples, together with the indexes at which they have been generalized. The basic idea of the algorithm is to determine whether two values have the same "shape". Intuitively, we consider two values to have the same shape if in their respective tree representations, their constructors at each node in the tree match, ignoring all opaque types (Section 4.2.2). That is, for values a and b.

```
subVals a == subVals b
```

```
matchesShapes :: SubTypes a
 => a -> [(a,[Idx])] -> Bool
matchesShapes d = any (matchesShape d)
matchesShape :: SubTypes a
 => a -> (a, [Idx]) -> Bool
matchesShape a (b, idxs)
 | constr a /= constr b = False
 | Just a' <- aRepl
 = let x = subForest (subVals a') in
   let y = subForest (subVals b) in
   all foldEqConstrs (zip x y)
  | otherwise = False
 where
 updateA idx d =
   fmap (replace d idx) (index b idx)
  aRepl = foldl go (Just a) idxs where
   go ma idx | Just x <- ma = updateA idx x
                           = Nothing
             | otherwise
 foldEqConstrs ( Node (SubVal 10) sts0
                , Node (SubVal 11) sts1 )
    | constr 10 == constr 11 =
     all foldEqConstrs (zip sts0 sts1)
    l otherwise
                             = False
```

**Figure 8:** Shape matching algorithm.

Furthermore, indexes that have been universally generalized (and all their children) match any value, since a universally generalized index indicates that counterexamples have been found for any possible constructor. In our implementation, we also consider existentially generalized indexes to match any value. Doing so is a design choice that is more aggressive about covering the space of counterexamples at the risk of omitting some.

To understand the shape matching algorithm, consider a few values of type Exp, defined in Section 4.3.1:

```
e0 = Div (C 1) (C 2)
e1 = Div (C 1) (C 3)
e2 = Div (Add (C 1) (C 2)) (C 7)
e3 = Div (Div (C 8) (C 2)) (C 7)

Then the following hold:

matchesShape e0 (e1, []) == True
matchesShape e1 (e2, []) == False
matchesShape e1 (e2, [0]) == True
matchesShape e3 (e2, [0]) == True
```

The first equation holds because we ignore opaque types, so the arguments to C are considered equal. The second equation fails because at index 0, e1 contains the constructor C and e2 contains the constructor Add. However, index 0 has been generalized, then we ignore the sub-value at index 0, and they match (the third equation). The same reasoning holds for the fourth equation.

# 6. Implementation and Usage

The implementation of SmartCheck is written in Haskell and is designed to test Haskell programs. The source code is licensed BSD3 and is freely available.<sup>4</sup>

SmartCheck generically operates over arbitrary algebraic data and so uses a generics library to encode generic traversals. Specifically, SmartCheck uses "GHC Generics", a recently-developed generics library for Haskell [15]. The generics library allows algebraic data types to automatically derive the type class SubTypes presented in Section 3. One limitation with GHC Generics is that it does not (currently) support generalized algebraic data types [12].

The data type to be tested must derive the Typeable, and Generic type classes. Deriving Typeable and Generic require using the GHC language extensions DeriveDataTypeable and DeriveGeneric, respectively. Typeable is used for dynamic typing in defining the replace method of SubTypes since it is unknown at compile-time whether the value to be replaced and replacing value have the same types. However, through SmartCheck's interface, run-time failures due to type-mismatches will not occur. Additionally, like with QuickCheck, deriving Show is required to print counterexamples discovered.

Then, the user simply declares, for a data type D,

```
instance Subtypes D
```

Default instances are provided for common Prelude types and some additional ones, including all types for which QuickCheck provides instances

SmartCheck does not implement a counterexample discovery algorithm or an arbitrary method. Any initial counterexample can be passed in or generated, and the algorithm depends on QuickCheck's arbitrary to generate new well-typed values.

The kinds of programs SmartCheck is specialized for are ones that operate over a large data structure together with smaller inputs. Therefore, properties provided to SmartCheck are expected to be of the form

```
Testable prop => a -> prop
```

where a is the type of the value for SmartCheck to analyze, and prop is a testable property, as defined by QuickCheck; morally, these are functions (or degenerately, values) that evaluate to a Boolean value.

If QuickCheck is used to discover a counterexample, all arguments except the first are shrunk, if their types have shrink methods defined for them. The first argument is returned to SmartCheck to be shrunk or generalized according to the algorithms described earlier.

A read-eval-print loop is presented to the user, allowing her to iterate shrink and generalize counterexamples, and then generate new counterexamples after strengthening the property's precondition as described in Figure 5.3.

SmartCheck is executed using

```
> smartCheck args prop
```

where args (the arguments) are passed in, and prop is the property being tested.

The interface types and functions for SmartCheck with analogous behavior to QuickCheck's are prefixed with an sc to avoid name space collisions with QuickCheck. Others are specialized for SmartCheck; e.g., enabling or disabling universal or existential extrapolated, number of extrapolation rounds, and limits on the depth and size of the values to generate.

Counterexamples can be optionally shown in a tree format by setting the format field of the arguments to be equal to PrintTree. for example, the tree format shows a counterexample like

```
Div (C 1) (Add (C 0) (C 2))
```

<sup>&</sup>lt;sup>4</sup>https://github.com/leepike/SmartCheck.git

```
as

Div | | +- C 1 | | '- Add | | +- C 0 | | | | '- C 2
```

We find that for very large and nested data structures, a tree representation aids in visually parsing the value.

# 7. Experiments

We describe two experiments using SmartCheck, including an XMonad property and a property about a natural language processing library.

#### 7.1 XMonad

Recall from the introduction the XMonad example. The XMonad window manager is a large software project with many contributors, so naturally, a QuickCheck test harness is included to help ensure new commits do not introduce bugs. At the heart of XMonad is a StackSet data type that encodes the relationship between windows, work spaces, and which window has the focus. XMonad contains properties to ensure the correct manipulation of StackSets. Due to having one large data-structure that is essential to the entire program, XMonad is a perfect candidate for SmartCheck.

XMonad passes all of its QuickCheck tests, but let us see what might happen to a new contributor if things go awry. Suppose a developer defines a deletion function to delete a window, if it exists. There is a deletion function that exists in XMonad, which is quite complex, given the amount of state that is managed by StackSet. However, one function used in deletion is to filter the stack of windows associated with each workspace defined:

```
removeFromWorkspace ws =
  ws { stack = stack ws >>= filter (/= w) }
```

Now, suppose the programmer makes a simple typo and instead writes

```
removeFromWorkspace ws =
  ws { stack = stack ws >>= filter (== w) }
```

When testing the property prop\_delete, which says that deleting the focused window of the current stack removes it from the StackSet x.

```
prop_delete x =
    case peek x of
    Nothing -> True
    Just i -> not (member i (delete i x))
```

QuickCheck returns the large value shown in the introduction. That value is a relatively small counterexample, but even the smallest StackSet values are somewhat visually overwhelming due to the number of fields within it. Recall the value returned by SmartCheck after generalization:

```
forall values x0 x1 x2 x3:
   StackSet
   (Screen (Workspace x0 (-1) (Just x1)) 1 1)
   x2 x3 (fromList [])
```

Let us examine what was generalized. In our test run, we chose to treat data maps as opaque, so the forth element of StackSet is not generalized, but is simply the empty map, so looks uninteresting. The second and third fields of StackSet are generalized, but the first one is not. So there is something particular about it. So the

culprit is one of the small constants (1 and -1) or having a Just value rather than a Nothing: it turns out that what matters is having a Just value, which is the stack field that deletion works on!

#### 7.2 Natural Language Processing

In 2012, a question was posted on the programming message board Stack Overflow asking about how to shrink large nested data types.<sup>5</sup> The poster writes:

... I tend to get an incomprehensible page full of output. ... Implementing the shrink function for each of my types seems to help a little, but not as much as I'd like. ... If I try to tune my shrink implementations, I also find that QC starts taking a very long time.

```
<<how long unanswered?>>
```

The question relates to the Geni natural language processing (NLP) package implemented in Haskell [13]. Specifically, counterexamples to a property attempting to show that a macro expansion function is its own inverse are enormous, requiring 200-300 80-character lines to print.

Using SmartCheck, we are able to reduce counterexamples to around 25 80-character lines of output. Most of the savings in the counterexample size were due to universal generalization, like in the XMonad case: entire record fields are abstracted away. From that, we (syntactically) shrunk the counterexample by-hand further by naming common sub-expressions.

We were able to send a substantially reduced and generalized counterexample to the message poster, making the cause of the bug more obvious. The author responded:

...While your improved shrinking may not have gone 'all' the way to the bottom, it got me a *huge* chunk of the way there!

Recall that through the entire process, we never had to learn how GenI works, what the property meant, or how to write a custom shrink method!

"Retro-fitting" SmartCheck to GenI, which is a large software system, required some boilerplate work. Fortunately, because the program already uses QuickCheck, arbitrary instances were already defined, but we had to hunt down the data types used to write instance Subtypes D, for each data type D (indeed, the job could have largely been done with Sed and Awk).

#### 7.3 Benchmarks

Unfortunately, no set of testing benchmarks exists over which to compare different test-case generation and minimization approaches. Therefore, we have collected a small number of benchmarks, in addition to the more involved case-studies described earlier in this section.

The benchmarks presented, in addition to the motivating example presented in Section 2, compare standard SmartCheck against hand-written shrink implementations. The benchmarks are as follows:

• Reverse, with the false property

```
prop_rev :: [a] -> Bool
prop_rev ls = ls == reverse ls
```

(the example appears in the original QuickCheck documentation):

Div0, a division-by-zero property for a simple calculator language (introduced in Section 4.3.1);

```
<sup>5</sup>http://stackoverflow.com/questions/8788542/
how-do-i-get-good-small-shrinks-out-of-quickcheck
```

- Heap, an example from the QuickCheck test suite, in which an incorrect "to sorted list" function is checked.
- Parser, a parser/pretty-printer for a toy imperative language containing a parser bug that switches the arguments of an binary operator.

All benchmarks can be found online. We compare the size of the final counterexample returned (by counting constructors) and the time required for counterexample generation and shrinking in seconds. The results are presented in Table 2. Again, we summarize the mean, median, standard deviation, and the results at the 95th percentile. (While we provide the standard deviations, note that the plots are not necessarily Gaussian.)

		QuickCheck	SmartCheck
	Mean	2, 0.002s	$2,4.8 \times 10^4$ s
Reverse	Std. dev.	0, 0.002	$0, 8.1 \times 10^4$
	95%	2, 0.007s	$2,5.8 \times 10^4$ s
	Mean	10, 0.001s	5, 0.001s
Div0	Std. dev.	6, 0.002	0, 0.001
	95%	23, 0.002s	5, 0.002s
	Mean	15, 0.016s	7, 0.007s
Heap	Std. dev.	1, 0.025	2, 0.003
	95%	19, 0.045s	12, 0.015s
	Mean	191, 0.013s	16, 0.241s
Parser	Std. dev.	195, 0.018	75, 0.800
	95%	577, 0.044s	14, 0.521s

**Table 2.** Summarizing data for the graphs in Figure 2. Entries contain execution time (in seconds) and counterexample sizes (counting constructors).

The *Reverse* benchmark essentially provides a lower-bound on the benefit of using SmartCheck to discover small counterexamples, since a list of length two falsifies the property (SmartCheck is still useful in generalizing the counterexample, however!). Perhaps surprisingly, SmartCheck still slightly outperforms QuickCheck. The other two benchmarks have much larger counterexamples, where SmartCheck's benefits are more pronounced. For example, consider the parser example in which the initial counterexample to shrink may be in a large parse tree. SmartCheck performs significantly better than optimal hand-written shrink instances, but even SmartCheck can sometimes return large counterexamples—this is why the mean counterexample size is larger than the size at the 95th percentile: there are a small number of large values not successfully shrunk by SmartCheck.

# 8. Related Work

Other researchers have also investigated counterexample shrinking. Zeller and Hildebrandt describe an application of greedy search to shrink counterexamples they call "delta-debugging" (DD) [19]. The authors apply their work to shrinking HTML inputs to crash Mozilla and shrinking C programs to trigger a bug in GCC. Subsequent generalizations are reported by Misherghi and Su in which they perform greedy search on tree-structured data; they call their approach hierarchical delta-debugging (HDD) [16].

HDD is most similar to SmartCheck's reduction algorithm, with an important difference: HDD (and DD) is deterministic, so the algorithm only succeeds in reducing the counterexample only if a new counterexample can be constructed from the original one. Our approach combines the speed of delta debugging with the power of QuickCheck to *randomly* discover structurally smaller counterexamples; in short, this is the first treatment we know of that integrates counterexample generation with counterexample reduction. Furthermore, neither paper explores the idea of counterexample generalization.

Within the functional programming community, one of the few treatments of generic shrinking is as a motivation for generic programming in Haskell's "Scrap your boilerplate" generic programming library [14]. There, the motivation was not to design new approaches to counterexample reduction, but simply to derive instances for the shrink method.

SmallCheck is another testing framework for Haskell for which shrinking is irrelevant: SmallCheck is guaranteed to return a smallest counterexample, if one exists [17]. SmallCheck does this by enumerating all possible inputs, ordered from smallest to largest, up to some user-defined bound.

While SmallCheck is effective for testing many programs and properties (in accordance with the *small scope hypothesis* [11]), counterexamples to even relatively simple properties may be practically infeasible to discover due to the size of the input space. For example, SmallCheck does not find a counterexample to the example presented in Section 2 after running it for several minutes.

Besides QuickCheck and SmallCheck, another testing framework related to SmartCheck is the recent Haskell library Feat [6]. Feat provides automated enumerations of algebraic data types in Haskell, allowing for fast access to very large indexes. For example, from the enumeration of ([Bool])

Accessing the  $10^{1000}$ th element takes under 0.1 seconds in interpreted Haskell. Feat combines some advantages of SmallCheck and QuickCheck, since the user can choose to exhaustively test an enumeration up to some depth, like with SmallCheck, or she can create a uniform distribution of test cases up to some depth.

Feat is used to discover counterexamples, not shrink them. However, shrinking is less necessary with Feat, since discovered counterexamples are often small, if one is found. For example, on the overflow example in Section 2, with a limit of 100 test cases, Feat finds a counterexample just two percent of the time, whereas QuickCheck finds one nearly 100%. Even at a limit of 10000, a counterexample is found about 50% of the time (with a correspondingly longer search time). Sampling from a uniform distribution does not work so well here. Feat does a better job of discovering counterexamples in the parser benchmark, but the size of the average counterexample contains 500 constructors, with a standard deviation of 500 (compared with 16 and 75, respectively, for SmartCheck). Still, Feat is powerful at what it does well and can be seamlessly used with SmartCheck, since it just defines the arbitrary method.

Finally, SmartCheck bears some similarity to QuickSpec, a testing-based library that infers equational properties about programs [5] insofar as they both attempt to generalize counterexamples based on specific inputs. QuickSpec attempts to infer equational properties of programs through random testing. Similarly, Daikon infers assertions for C, C++, Java, and Perl by observing relationships between variables in executions of a program [7]. SmartCheck does not attempt to infer properties like these tools do, so it is in one sense less general. However, SmartCheck's three kinds of counterexample generalization are novel.

# 9. Conclusions and Future Work

We have presented new approaches for generically shrinking and generalizing counterexamples over algebraic data. SmartCheck automates the laborious task of shrinking, and extrapolating from

 $<sup>^6\,\</sup>mathrm{https://github.com/leepike/SmartCheck/tree/master/regression}$ 

counterexamples, and in our experience, performs better and faster than hand-written shrink functions.

We envision a number of potential extensions and improvements to SmartCheck. First, we have considered only the simplest kind of data, algebraic data types. As noted in Section 6, SmartCheck does not work with GADTs currently, due to limitations with GHC Generics. It would be interesting to see if the approaches described here could be extended to function types as well—we are particularly motivated by Claessen's recent work in shrinking and showing functions [2].

Lazy SmallCheck can test partially-defined inputs by detecting the evaluation of undefined values [17]. This capability is useful in shrinking, too. For example, the universal sub-value generalization algorithm (Section 5.1) could be extended to shortcut testing and generalize a sub-value if it is not evaluated in testing the property. Not only does this shortcut the generalization phase, but it gives a *proof* that the sub-value can be generalized.

SmartCheck displays (generalized) counterexamples in a form similar to default Show instances or in a tree form, which can be helpful to parse the components of the value. Better approaches for showing large data types are needed. In particular, an interactive web-based viewer with hyperlinks to close or expand sub-values would be particularly useful.

Another aspect of displaying large counterexamples that we have not explored is to exploit sharing. Constructs might be repeated that can be abstracted out. For example, instead of a counterexample like

```
Add (Div (C 1) (Add (C (-2)) (C 2)))
(Div (C 1) (Add (C (-1)) (C 1)))
```

we might instead return

```
Add (div (-2) 2) (div (-1) 1)
where div x y = Div (C 1) (Add (C x) (C y))
```

Discovering and exploiting sharing automatically is future work.

Debugging is a difficult task. Functional programming has been at the forefront of testing research, with tools like QuickCheck and SmallCheck. We were motivated to build a tool like SmartCheck just because of how effective QuickCheck is at discovering counterexamples automatically—there would be no such problem of having very large counterexamples if inputs were written by hand. We hope SmartCheck and the ideas in this paper continue the tradition of highly-automated testing and debugging in the functional programming community, and beyond!

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