

exercise4

Lee Rui (BA19008042)

2020/3/27

```
rm(list = ls())
setwd("E:/RStudio/workspace/ecology")
data <- read.csv("exercise4/percep_data.csv")
mydata <- data[1:1000,c(1, 2, 3)]
names(mydata) <- c("X1", "X2", "y")
str(mydata)

## 'data.frame':    1000 obs. of  3 variables:
##  $ X1: num  -0.58 -0.7 0.617 -0.384 0.103 ...
##  $ X2: num  -0.52 0.217 0.256 -0.716 0.527 ...
##  $ y : int  -1 -1 1 -1 1 -1 -1 -1 1 -1 ...
```

Sort the data by “y” from small to large

```
mydata <- mydata[order(mydata$y),]
for (i in 1:1000){
  if (mydata[i,3] > 0){
    num = i
    break
  }
}

g1_x = mydata[1:num-1,1]
g1_y = mydata[1:num-1,2]
g2_x = mydata[num:1000,1]
g2_y = mydata[num:1000,2]
g_x = c(g1_x, g2_x)
g_y = c(g1_y, g2_y)
group = mydata$y
print(g_x)

##      [1] -0.580332229 -0.700408393 -0.383554021 -0.669665385 -0.924211684
##      [6] -0.893007390 -0.747517828 -0.969455949  0.212477822 -0.067018274
##     [11] -0.845380255 -0.070843342 -0.161002714 -0.847237288 -0.538870153
##     [16] -0.796104809  0.312884902 -0.952179132 -0.555047904  0.027254277
##     [21] -0.201685828  0.614560655 -0.303915638 -0.745993299 -0.594036328
##     [26] -0.661723996  0.655322408 -0.012181714 -0.300574421  0.177990529
##     [31]  0.164390196 -0.082830399 -0.679185029 -0.207624209 -0.029622243
##     [36] -0.653184939 -0.727843930 -0.932441863 -0.709648260 -0.262066213
##     [41] -0.128924456 -0.652841405  0.133513165  0.309207475  0.471734496
##     [46]  0.168329255 -0.679675893  0.498291621  0.021842169 -0.662531914
##     [51] -0.969802656  0.172361911  0.520983047  0.009372056 -0.028214697
##     [56]  0.235774269 -0.130581330 -0.955704043 -0.491060224 -0.891019150
```

```

## [61] 0.178745360 -0.212209630 0.041795839 0.111030995 -0.124411177
## [66] 0.283784857 -0.166099959 -0.315088346 -0.830380953 0.129859228
## [71] 0.052712458 -0.031044246 -0.599721087 0.464988472 -0.035812174
## [76] -0.739608680 -0.209620364 0.311338193 -0.493997291 0.252401895
## [81] -0.671518746 -0.686676425 -0.936032108 -0.510550155 0.367339595
## [86] -0.826208770 0.217190416 0.504245621 0.296146520 -0.794670000
## [91] 0.741823995 0.336200786 -0.654568986 -0.246696351 -0.444534361
## [96] -0.863172337 -0.526602338 -0.919577098 -0.774254259 -0.371410395
## [101] 0.259062315 -0.782329143 -0.329103272 0.037174952 -0.922831454
## [106] -0.499206846 0.466347251 0.699940872 -0.046789649 -0.974437356
## [111] -0.169687034 -0.204699697 -0.223160031 -0.202537509 0.620094142
## [116] 0.043000923 0.348489683 -0.379673912 0.419640260 0.182189302
## [121] 0.241317721 -0.742440020 0.113006205 -0.641043318 -0.403210716
## [126] -0.994074475 -0.063866402 -0.019371397 0.364074961 -0.027474417
## [131] 0.180817684 -0.936607894 -0.328059698 -0.735465886 -0.514475176
## [136] -0.686662948 -0.816306446 -0.211106422 0.345657145 -0.957116118
## [141] -0.947068227 -0.140775172 -0.896823365 -0.848902832 -0.206187144
## [146] 0.165387341 -0.260593829 -0.565067444 0.391064555 -0.201906139
## [151] -0.247436375 -0.155606141 -0.645391389 0.095639043 -0.914976891
## [156] -0.089692972 -0.445442307 -0.092253339 -0.412230505 0.280022554
## [161] -0.772558860 -0.317060656 -0.427522399 -0.845484805 -0.819221074
## [166] 0.456802012 -0.209790305 -0.689747316 -0.119930612 -0.253897336
## [171] -0.641686664 -0.570967958 -0.545758299 -0.115310044 0.053186549
## [176] -0.323417496 -0.141921432 -0.364992660 -0.821142353 -0.655381416
## [181] 0.304634633 -0.365465459 -0.728927127 0.385169975 0.188504144
## [186] 0.124964156 -0.352389164 0.434121532 -0.768223628 -0.036338809
## [191] -0.832893942 -0.217558372 -0.445880481 -0.377475702 -0.044101676
## [196] -0.852990613 -0.798988577 -0.835976070 -0.448127987 -0.686201458
## [201] 0.297108687 -0.158558780 -0.416690049 -0.822917893 -0.067795461
## [206] -0.839224492 0.190852643 -0.178901900 -0.456978573 0.108187420
## [211] -0.607726229 -0.253882249 -0.195342080 -0.042486992 -0.193772476
## [216] -0.856056809 0.026147165 -0.653958161 0.416520590 0.308608411
## [221] -0.972264203 -0.748728958 -0.870237883 0.300926180 0.551333887
## [226] 0.696451934 -0.467352808 -0.172944556 -0.015172399 -0.211980343
## [231] -0.307366263 0.401981569 0.494755397 -0.627593298 -0.646065289
## [236] -0.802083119 -0.673365920 -0.344081173 -0.107657734 -0.129669155
## [241] 0.175481335 -0.842352185 -0.307359297 -0.009464754 -0.697997046
## [246] 0.038687191 -0.399294488 0.369750724 0.412766828 -0.154997888
## [251] -0.795236657 -0.165362463 0.000334154 -0.113829067 -0.253295537
## [256] -0.266737649 0.575917895 -0.355796588 -0.946214764 -0.757178127
## [261] 0.012263365 -0.678252286 -0.180667686 -0.716173588 -0.895842977
## [266] -0.928286566 0.035431514 0.015473441 -0.361613856 0.223643867
## [271] -0.974288764 -0.900005416 -0.166460627 -0.802627985 0.658867585
## [276] -0.054149183 -0.107479451 -0.254147325 -0.596835584 -0.768822022
## [281] -0.392734643 -0.811788584 -0.166963488 0.265736505 -0.645530737
## [286] -0.601138547 0.389303598 0.232397514 -0.806690948 0.182137072
## [291] -0.409485518 -0.564986074 0.035444822 0.471500428 -0.573094180
## [296] -0.432867255 0.191168467 -0.594515572 0.093331449 -0.208790140
## [301] -0.967117591 -0.559325628 -0.924592285 0.234079776 -0.858373559
## [306] 0.112455057 -0.518298279 -0.970944117 -0.377414336 0.070039710
## [311] -0.037824427 -0.213020124 0.067258903 -0.724717168 0.688810281
## [316] 0.087264478 -0.158909296 -0.769724817 0.055806912 0.095415584
## [321] -0.658431144 -0.628058108 -0.314984113 -0.144179220 -0.314583454
## [326] 0.441003655 -0.158952710 -0.315962978 0.345497573 -0.687195288

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## [331] -0.126628440 -0.179661683 -0.088183258 0.181202901 0.282010744
## [336] 0.153671760 0.620897359 -0.549778792 -0.888157069 0.321892867
## [341] -0.461256960 -0.264689643 -0.284150278 0.765190511 -0.741085878
## [346] -0.748162873 -0.483040136 0.445254738 0.045465385 -0.860957781
## [351] -0.416511309 -0.718017798 -0.064132224 0.117409077 -0.881507226
## [356] -0.326711051 -0.750778860 -0.571088917 -0.906473081 -0.286386711
## [361] -0.641660280 -0.781221180 0.397195697 -0.558807834 0.193122434
## [366] -0.387582598 -0.420757418 -0.966231763 0.116030682 -0.350187365
## [371] 0.062884708 -0.682551017 -0.401300504 -0.159472918 0.692469806
## [376] -0.827573081 0.285814634 -0.170037101 -0.235924248 -0.789530714
## [381] -0.913625308 -0.882604131 -0.123552807 -0.115001661 -0.729208708
## [386] -0.625490915 -0.601441060 0.187301796 -0.625599968 0.330187223
## [391] -0.749915121 -0.708846171 -0.290408871 -0.530922749 0.746768342
## [396] -0.944784558 -0.349192686 -0.184933668 0.306502727 -0.419161390
## [401] -0.662244672 0.245345186 -0.924199512 -0.520749620 0.141922093
## [406] -0.558310262 -0.718951023 -0.353766682 0.083370241 0.165908242
## [411] -0.902190282 -0.833461824 -0.401139818 -0.935742204 -0.773890657
## [416] 0.155522502 -0.267749361 -0.656409097 -0.548493402 0.005637744
## [421] -0.623664577 0.193454072 -0.709607192 0.622961145 -0.587941859
## [426] -0.772632896 -0.106580826 -0.282237823 -0.420275256 0.675568823
## [431] -0.332328035 -0.010200853 -0.339268897 -0.697159376 0.063798551
## [436] -0.149303484 0.071928496 -0.273868570 -0.443125974 0.199992094
## [441] -0.466650018 -0.405830210 -0.663891094 0.081889824 -0.196830544
## [446] 0.249348830 -0.404209675 -0.297410359 -0.376978803 0.217374588
## [451] -0.925128179 -0.771201064 0.499127375 -0.780692267 -0.305354987
## [456] -0.080387612 -0.791710288 -0.004393333 -0.616765269 -0.179444063
## [461] 0.200991023 -0.385387314 -0.190839613 0.277464658 -0.489161934
## [466] -0.815507501 0.023013493 -0.403525979 -0.634905955 -0.732205941
## [471] -0.915674248 -0.902312712 -0.559450231 -0.712596677 0.447495591
## [476] 0.132552444 -0.036978606 -0.424367876 -0.314046890 -0.712853417
## [481] -0.241534478 -0.568683981 -0.414000700 -0.239742117 -0.324528561
## [486] -0.208028026 0.840509628 0.141464219 -0.422471884 -0.094710995
## [491] -0.932614278 -0.477744627 -0.165755649 0.101332703 -0.963075801
## [496] -0.864184003 -0.175750089 -0.375405491 -0.370674771 -0.250561224
## [501] -0.976006721 -0.949363505 -0.191098937 -0.787015597 -0.859230338
## [506] -0.249137735 -0.700804804 -0.390214302 -0.293462123 0.298451326
## [511] 0.314188981 -0.285026094 -0.691558615 -0.239902932 -0.174967562
## [516] -0.703233708 -0.369599388 -0.223754765 -0.514713384 -0.155804209
## [521] 0.792885573 -0.302076167 -0.615199013 0.093260398 -0.482591934
## [526] -0.365064777 0.109752625 -0.697287773 -0.856599043 -0.880615717
## [531] -0.822679487 -0.320862388 -0.251871119 0.564032251 0.102640499
## [536] -0.554506344 -0.850256227 -0.479235939 -0.271657098 0.214704994
## [541] -0.402360349 -0.494843251 0.407675811 -0.004288866 0.357268584
## [546] -0.092123169 0.574561055 -0.365274219 -0.423066940 -0.166714074
## [551] 0.922230838 -0.193874396 -0.444780488 0.100524891 0.312744911
## [556] 0.263368541 -0.998518443 0.090781895 -0.545345797 -0.327256690
## [561] -0.961206979 0.950067932 -0.519171910 0.351340038 -0.886740738
## [566] 0.297438289 0.056049726 -0.652629828 0.253545141 -0.522627722
## [571] -0.734579715 -0.163512648 -0.853652426 0.060748849 -0.040044416
## [576] -0.543203233 0.297929912 -0.233382013 0.259712565 -0.253748919
## [581] -0.192967595 -0.543764659 -0.615920154 -0.296641224 0.098852753
## [586] -0.618308517 -0.693263447 -0.876938911 0.756681340 0.712198121
## [591] -0.813686469 0.197707428 -0.561940813 -0.961478478 -0.865332700
## [596] -0.805343785 -0.509284019 0.613209374 -0.530029545 0.158138046

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## [601] -0.122007295 -0.549008537 -0.866411627 -0.399490101 -0.155724308
## [606] -0.458632750 -0.421568671 -0.588181201 0.518976761 -0.047392850
## [611] -0.883109126 -0.511075464 0.285739308 -0.928251764 -0.807711298
## [616] -0.183885921 0.422554926 -0.027609547 0.597560266 -0.359902762
## [621] -0.850962342 -0.679619643 0.310512355 0.879252173 0.260837032
## [626] 0.066803083 -0.887660014 -0.744614456 -0.755401384 -0.427124362
## [631] 0.081702865 0.626338821 -0.572181598 -0.605421676 -0.359128957
## [636] -0.452135180 -0.167388875 -0.675963644 -0.502464008 -0.082102047
## [641] 0.291148275 -0.824148617 -0.408202096 -0.753623002 -0.385308473
## [646] -0.610716824 -0.335364092 0.311873815 -0.606699381 0.439094439
## [651] 0.913315999 0.015714832 -0.869335719 0.410711158 -0.622861284
## [656] -0.071611420 -0.073301136 -0.584423991 -0.425665190 0.586914383
## [661] 0.268797752 -0.227074812 -0.738260977 -0.738537821 -0.717623139
## [666] 0.108787790 -0.659649092 -0.585486952 0.617452960 0.102860314
## [671] 0.495805302 0.717524145 0.590579726 0.731425554 0.483921118
## [676] 0.665881643 0.713695913 0.932679267 0.550222915 0.192508432
## [681] 0.652458721 0.582303554 0.815841476 0.224820658 0.369213326
## [686] 0.476629192 0.475745307 0.216011198 0.964336313 0.250117260
## [691] 0.233915106 0.678698656 0.568139121 0.821559003 0.919404368
## [696] 0.417619857 0.392067277 0.524906655 0.894747502 0.428347597
## [701] 0.810716338 -0.081888004 0.905405383 0.739087285 0.970142080
## [706] 0.892603375 0.919931365 0.725802282 0.658469780 0.821923941
## [711] 0.816940960 0.722909905 0.908834677 0.742041501 0.772651761
## [716] 0.464171179 0.723530638 0.891825687 0.864651679 0.801288861
## [721] 0.987301196 -0.467118425 0.688494379 0.608086800 0.398938740
## [726] 0.927521297 0.939185260 0.642987972 0.804794711 0.613654878
## [731] 0.729745180 0.295689749 0.346240358 0.682439948 0.587901326
## [736] -0.004112198 0.749939844 0.540782292 0.926566520 0.803408851
## [741] 0.505890977 0.455412403 0.859034390 0.288439938 0.506295346
## [746] 0.176569473 0.909958834 0.443776780 0.257965944 0.636095771
## [751] 0.634709449 0.641266505 0.838697677 0.258704986 0.445580781
## [756] 0.798803652 0.864364909 0.853916025 0.916603066 0.881752174
## [761] 0.867052207 -0.391734914 0.865338917 0.799224332 0.606619583
## [766] 0.984023750 0.865926477 0.964862464 0.785717427 0.259316275
## [771] 0.285496207 0.720984917 0.705606468 0.775837755 0.843479035
## [776] 0.829673521 0.238637483 0.978575439 0.913979881 0.583926806
## [781] -0.050259219 -0.029360380 0.991417036 -0.060254995 0.692808133
## [786] -0.035165094 0.782367188 0.133189930 0.854801175 0.619836284
## [791] 0.841352789 0.582125020 0.969806652 0.676268001 0.804554337
## [796] 0.436217048 0.555555487 0.489192200 0.894542849 0.777457165
## [801] 0.591089583 0.663318397 0.427442965 0.699602025 0.876730374
## [806] 0.881163103 0.291357895 0.145928355 0.997131149 0.341296653
## [811] 0.703390837 0.984792263 -0.344307624 0.721074105 0.294930345
## [816] 0.474986978 -0.019181719 0.175069337 0.659952105 0.356974509
## [821] 0.409245794 0.906489435 0.864253255 0.575288488 0.755117604
## [826] 0.547547050 0.940818330 0.962734676 0.254520348 0.960789610
## [831] 0.432844357 0.654123909 0.871460822 0.075991365 0.651641415
## [836] 0.579835237 0.075459165 0.267797037 0.148971590 0.492552690
## [841] 0.762729859 0.735864696 -0.133472593 0.529953276 0.372720274
## [846] 0.885861657 0.467847235 0.175147638 0.666771272 0.706905389
## [851] 0.921012893 0.862954224 0.820175318 0.598397850 0.838917051
## [856] 0.512478007 0.793667857 -0.358524807 0.286051426 0.503908926
## [861] 0.766913780 0.395648678 0.330393946 0.734578698 0.830322354
## [866] 0.587589887 0.848788150 0.577934735 0.758437932 0.950971244

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## [871] 0.679835126 0.303365529 0.766944304 0.726523405 0.686285680
## [876] 0.739346062 0.713007276 0.706848277 0.676630160 0.157903188
## [881] 0.620536485 0.630384073 0.433166596 0.623042396 0.960544850
## [886] 0.715408551 0.698854843 0.710342670 0.820727269 0.485013281
## [891] 0.926851451 0.704234743 0.231711307 0.809317084 0.666857583
## [896] 0.785270240 0.130067189 0.618908106 0.894779993 0.020842439
## [901] 0.997732540 0.363069845 0.620408148 0.997525715 0.720659013
## [906] 0.834827844 0.780129303 0.384541863 0.932570448 0.100769422
## [911] 0.662887472 0.555710516 0.430679534 0.357212817 0.753994210
## [916] 0.598761067 0.103908985 0.935290516 0.025553748 0.988902126
## [921] 0.618051430 0.789193399 0.863632367 0.702681357 0.714228435
## [926] 0.934796846 0.308086152 0.719759024 0.859053405 0.645949415
## [931] 0.778692973 0.350962407 0.898676416 0.435821219 0.713049050
## [936] 0.408234312 0.796753211 0.753026501 0.860338372 0.890994592
## [941] 0.910200815 0.670767310 0.803446386 -0.681976813 0.462360063
## [946] 0.916078371 0.867017545 0.601604638 0.232870690 0.617103974
## [951] 0.065653211 0.824116913 0.918424270 0.829126610 0.539831813
## [956] 0.597670494 -0.164067451 0.015252130 0.428780785 0.767178330
## [961] 0.685353305 0.731710804 0.767946739 0.875615617 0.349175095
## [966] 0.530546459 0.820267855 0.514998773 0.038780489 0.699823687
## [971] 0.486799459 0.289754946 0.492070521 0.589714910 0.702352426
## [976] 0.793462679 0.799033222 0.390658394 0.976742982 0.432787957
## [981] 0.908759137 0.072954751 0.756588583 0.784670779 0.563193537
## [986] 0.179956783 0.737284963 0.906559011 0.543397749 0.982478278
## [991] 0.852748033 0.825467063 0.810363557 0.558737156 0.605552093
## [996] 0.247469838 0.353707701 0.893961554 -0.005746083 0.715176346
```

```
print(g_y)
```

```
## [1] -0.520060800 0.216898262 -0.716119123 -0.661911467 0.219849278
## [6] -0.323050076 0.062956920 -0.821005984 -0.617250544 0.708718831
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## [161] 0.071361611 -0.728153464 -0.951042099 0.209286518 0.326196240
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## [176] -0.307402492 -0.226861500 0.283244786 0.197494596 0.342223645
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## [656] 0.695685639 -0.355957849 -0.268144275 0.059151990 0.258170787
## [661] -0.622171651 0.661991755 0.193185961 0.753349645 -0.322147505
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##	[671]	0.126515564	0.006217932	0.210865924	-0.141368161	0.026528165
##	[676]	0.864044283	0.543138566	0.328687133	0.487012210	0.912417329
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##	[691]	0.370796625	0.949524050	-0.239302429	-0.423959335	0.904345962
##	[696]	0.721651301	0.650060738	0.490952435	-0.078120872	0.570296464
##	[701]	0.379089095	0.990677473	0.003475682	-0.346851362	-0.490274876
##	[706]	-0.536043346	0.601172948	-0.381070763	-0.180011577	0.023627734
##	[711]	-0.116696401	0.062092841	0.680339125	0.244969238	-0.059989562
##	[716]	0.258330247	0.957842875	0.954186702	-0.411840392	0.809423285
##	[721]	-0.976969884	0.237393077	0.780501649	0.136515779	0.089251147
##	[726]	0.755107615	0.137896969	-0.339167501	0.182725348	-0.211894020
##	[731]	0.650074730	0.527281617	0.559506963	0.704061119	0.476055068
##	[736]	0.845152196	0.084661852	0.998507265	-0.487342141	0.515165016
##	[741]	0.833694918	0.325944389	0.124108083	0.398114526	0.284480453
##	[746]	0.737750959	0.304821161	0.633925620	0.989178611	0.211457719
##	[751]	0.825290927	0.918122925	0.746123890	0.729409860	0.911970732
##	[756]	-0.279276364	-0.142546262	-0.694271658	0.964274762	-0.373701741
##	[761]	0.472401611	-0.520413981	0.457547305	-0.163420991	0.440232443
##	[766]	0.976642538	-0.337261036	0.108103652	-0.569219601	0.663784514
##	[771]	0.745614666	0.342293553	0.998249357	0.694374177	0.130481393
##	[776]	0.857235936	0.957305740	0.093922688	-0.584665076	0.200815263
##	[781]	0.824439001	0.874982257	-0.735353446	0.857656231	0.130653759
##	[786]	0.960680781	0.949396250	0.488479604	0.117862285	-0.055926994
##	[791]	0.953840174	0.728897199	-0.372975930	-0.011812624	-0.469219475
##	[796]	0.693312942	0.993895215	0.062456799	0.945861024	0.693414099
##	[801]	0.996598321	0.434381749	0.964030581	0.666341014	0.926313023
##	[806]	-0.206052613	0.448619929	0.753419418	0.402011848	0.170206147
##	[811]	0.030819084	-0.916195359	0.677392859	-0.299231005	0.777166802
##	[816]	-0.020399182	0.902274304	0.743021103	-0.021176300	0.786562252
##	[821]	0.658312617	0.133702015	0.821915611	0.367614727	0.605955094
##	[826]	0.748798162	0.582246713	-0.528136979	0.988005612	-0.940716783
##	[831]	0.494993256	0.462796115	0.155290544	0.933355894	-0.116873843
##	[836]	-0.166444305	0.705376599	0.989803529	0.584806842	0.948842148
##	[841]	0.515625393	0.982212059	0.082028260	0.124056763	0.162781337
##	[846]	-0.624557129	0.650717532	0.459680556	0.152670416	0.689671190
##	[851]	-0.568312019	0.063845251	-0.102498620	-0.317533011	0.825685657
##	[856]	0.442064298	0.225044248	0.540217252	0.953721613	0.833817434
##	[861]	-0.555910063	0.830626545	0.385193678	-0.357916143	0.618011242
##	[866]	-0.090293236	0.187612670	0.462356817	0.220347025	0.636172570
##	[871]	0.677663043	0.363955160	-0.425954423	0.393559975	-0.262762553
##	[876]	0.821125699	-0.013138385	0.357303659	0.226316792	0.440407671
##	[881]	0.731562082	0.446064488	0.026255057	-0.085150302	-0.292597850
##	[886]	0.330876373	0.265174883	0.147881248	-0.377024920	0.119305778
##	[891]	-0.658000898	-0.470168019	0.925997048	-0.023902066	-0.202867223
##	[896]	-0.216340049	0.637359911	-0.331724546	0.699055102	0.844656488
##	[901]	0.219557220	0.579903816	0.150328055	0.379149677	0.183646823
##	[906]	-0.476220626	-0.232361719	0.051394356	0.226864411	0.968912669
##	[911]	0.308394417	0.869250764	0.783861426	0.927254533	0.894979039
##	[916]	0.821052843	0.910478256	-0.508277486	0.771791840	-0.933615211
##	[921]	-0.021498451	0.078903731	0.448218092	0.316143179	0.574156435
##	[926]	-0.498768267	0.309079474	0.762135282	-0.393938632	-0.109420694
##	[931]	-0.437783598	0.167571427	0.355459576	0.993208495	0.614604194
##	[936]	0.517470724	-0.106448260	0.278844422	-0.403630945	0.595760830


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## [941] -0.768536740 -0.015899629 0.476982128 -0.137629990 -0.079218015
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## [956] 0.950977972 0.997553027 0.916786597 0.298661910 0.989902428
## [961] -0.284839513 0.094149063 0.007195421 -0.429885716 0.158199611
## [966] 0.297186636 -0.115286239 0.910834371 0.993983089 -0.195010530
## [971] 0.750727096 0.261477361 0.443947403 -0.031126470 -0.116524510
## [976] -0.476734445 0.594195400 0.204504129 0.631474056 0.777222957
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## [986] 0.584534413 -0.136514551 0.518319314 0.636010607 -0.013855288
## [991] 0.137555285 0.951856345 0.661778382 0.923314955 -0.278932694
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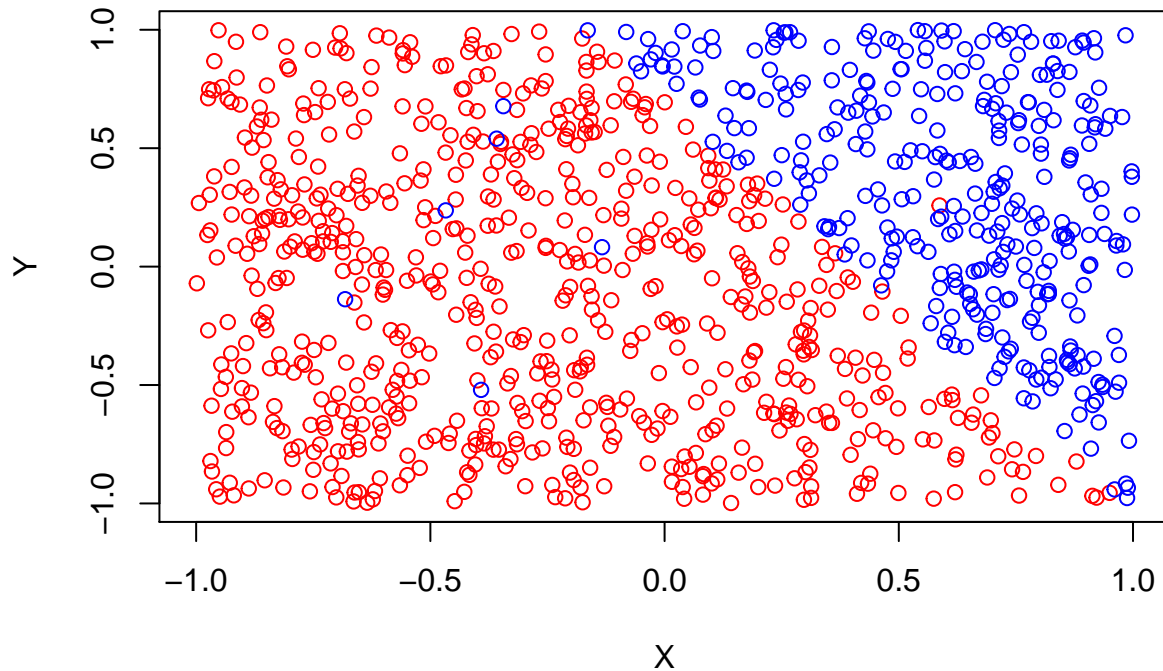
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print(group)
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## [25] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [49] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [73] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [97] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [121] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [145] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [169] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [193] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [217] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [241] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [265] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [289] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [313] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [337] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [361] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [385] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [409] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [433] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [457] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [481] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [505] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [529] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [553] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [577] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [601] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [625] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [649] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 1 1 1 1
## [673] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [697] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [721] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [745] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [769] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [793] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [817] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [841] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [865] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [889] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [913] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [937] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
```

```
## [961] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [985] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
```

Color points based on the value of “y”

```
plot(g_x, g_y, type='n', xlab='X', ylab='Y')
points(g1_x, g1_y, col='red')
points(g2_x, g2_y, col='blue')
```



Initial weight

```
theta0 = 0.1
theta1 = 0.2
theta2 = 0.3
```

```
M = 15          # number of epochs to run
eta = 0.005     # learning rate
th = 0.9        # threshold to stop
verbose = F     # whether detailed weight update info is printed
```

Iteration

```
for (i in 1:M){
  print(paste('Epoch starts: ', i))

  ## We reshuffle the order of the datapoint for each epoch.
```

```

index = 1:1000
index = sample(index)

for (j in index){
  y_j = theta0 + theta1*g_x[j] + theta2*g_y[j]

  if (y_j >= 0){
    pred_j = 1
  }else{
    pred_j = -1}

  theta0 = theta0 + eta*(group[j] - pred_j)*1.0
  theta1 = theta1 + eta*(group[j] - pred_j)*g_x[j]
  theta2 = theta2 + eta*(group[j] - pred_j)*g_y[j]

  if (verbose == T){
    print(paste(' -> updating data point ', j, ' : '))
    print(paste(' -> theta0: ', theta0))
    print(paste(' -> theta1: ', theta1))
    print(paste(' -> theta2: ', theta2))
  }
}

y_all = theta0 + theta1*g_x + theta2*g_y
y_pred = y_all
y_pred[y_all >= 0] = 1
y_pred[y_all < 0] = -1

acc = sum(y_pred == group)/length(group)
print(paste('Epoch ends: ', i, ' WITH accuracy: ', acc))

if (acc >= th){
  break
}
}

```

```

## [1] "Epoch starts: 1"
## [1] "Epoch ends: 1 WITH accuracy: 0.985"

```

```

y_all = theta0 + theta1*g_x + theta2*g_y
print(y_all)

```

```

##      [1] -0.3132087894 -0.2430225552 -0.2913138649 -0.3543922006 -0.2977032351
##      [6] -0.3634981320 -0.2754506375 -0.4497048660 -0.1312442962 -0.0205776858
##     [11] -0.2483624435 -0.1593573087 -0.1003540538 -0.2574775140 -0.1127100310
##     [16] -0.4004819568 -0.1485462180 -0.1992851314 -0.1889990207 -0.1395720973
##     [21] -0.1612195472 -0.0250355932 -0.2573888330 -0.1952956253 -0.2032766481
##     [26] -0.3919315269 -0.0279287270 -0.1638498044 -0.2131396457 -0.0093885106
##     [31] -0.0811314203 -0.0163070894 -0.1451658550 -0.2541261064 -0.1200249084
##     [36] -0.2088720589 -0.3685404153 -0.3611854116 -0.3558094970 -0.0627175951
##     [41] -0.2572356558 -0.3651362597 -0.1482508379 -0.1386806210 -0.0819948998
##     [46] -0.1258071116 -0.3221218895 -0.0583534052 -0.0766808711 -0.1858785774
##     [51] -0.3179741056 -0.0746468884 -0.0179737478 -0.0826145699 -0.0859030064
##     [56] -0.1671097795 -0.1027239875 -0.3299646027 -0.3175592457 -0.3119476059

```

```

## [61] -0.0570195492 -0.2846185976 -0.2223659053 -0.1635719983 -0.2084469528
## [66] -0.0431927454 -0.0450517447 -0.2790641729 -0.3137340253 -0.1267016047
## [71] -0.0480607220 -0.0272818706 -0.2595806484 0.0001698190 -0.2212880546
## [76] -0.2248561836 -0.2493459536 -0.1280909227 -0.2052785716 -0.0023879791
## [81] -0.1692641551 -0.2715123727 -0.4340580458 -0.1340963128 -0.0235543765
## [86] -0.2539277243 -0.0699788433 -0.0040405252 -0.0752020618 -0.4054945108
## [91] -0.0332488577 -0.0060013671 -0.3613401818 -0.2491008816 -0.1875528511
## [96] -0.1784818669 -0.2742746058 -0.4570175481 -0.3455346925 -0.2431775228
## [101] -0.0936450562 -0.2610807953 -0.2909649995 -0.1240054950 -0.4100247441
## [106] -0.2313807263 -0.0459259362 -0.0228715132 -0.0249543745 -0.2435947757
## [111] -0.0656961797 -0.0585046663 -0.0723023119 -0.1891218513 -0.0762834374
## [116] -0.1979257326 -0.0388132931 -0.2846732393 -0.1203043478 -0.0814323492
## [121] -0.0352264915 -0.2437420315 -0.1099916652 -0.2512369779 -0.2977033604
## [126] -0.3083098352 -0.0981687781 -0.1159448543 -0.0027996449 -0.0604145102
## [131] -0.0181172990 -0.3935456701 -0.2432645921 -0.3826310522 -0.2000637223
## [136] -0.2607838459 -0.3584193678 -0.1683553619 -0.0139567477 -0.4627789408
## [141] -0.4029799482 -0.0177532611 -0.2754825329 -0.2054301357 -0.0718915978
## [146] -0.1627425935 -0.2680261582 -0.3640474186 -0.0099394419 -0.2673960915
## [151] -0.0820861720 -0.0616431600 -0.3490007538 -0.0273448314 -0.1967111275
## [156] -0.1240218108 -0.1571335864 -0.0952829988 -0.0744634189 -0.0755106835
## [161] -0.2804759987 -0.2765779278 -0.3339287441 -0.2797573571 -0.2574713571
## [166] -0.0621787020 -0.0959878206 -0.3893928762 -0.2204332923 -0.0412404078
## [171] -0.1724869142 -0.3058286009 -0.2821594900 -0.2307635409 -0.2012976245
## [176] -0.2211990813 -0.1656310142 -0.1514944738 -0.2753623417 -0.2149797932
## [181] -0.0933936923 -0.2945356464 -0.2649734592 -0.0636637389 -0.0618268733
## [186] -0.0137739190 -0.2094819464 -0.1171842892 -0.3451120827 -0.0974510910
## [191] -0.3847111316 -0.1730150361 -0.1713864615 -0.1695387778 -0.2000316467
## [196] -0.2825496610 -0.2852816193 -0.3944858942 -0.3443253818 -0.3515116489
## [201] -0.0770382236 -0.0553897653 -0.3215506273 -0.2736249212 -0.1093181636
## [206] -0.2225598271 -0.1019000662 -0.2016310307 -0.1374030671 -0.0178387786
## [211] -0.3705493782 -0.0564566196 -0.1084425669 -0.0194333146 -0.2518345276
## [216] -0.2383854614 -0.1277311097 -0.3393563202 -0.0794646867 -0.0699579486
## [221] -0.2379363299 -0.3902494140 -0.2340990012 -0.1433651052 -0.0630147462
## [226] -0.0164387502 -0.1498902014 -0.2303958155 -0.1962633810 -0.0793418937
## [231] -0.2187960101 -0.0097360294 -0.0812365934 -0.1527410552 -0.2692160835
## [236] -0.1846632878 -0.3600786272 -0.0837201048 -0.2238594813 -0.1313683132
## [241] -0.0324292735 -0.3654185645 -0.1043636890 -0.0753312810 -0.2273282554
## [246] -0.2164398063 -0.1094643122 -0.0599408410 -0.0969802078 -0.1627698983
## [251] -0.2549280435 -0.1967813863 -0.0060224844 -0.1472359413 -0.1504817586
## [256] -0.2423084722 -0.0576096299 -0.1276235127 -0.3887824887 -0.4147621279
## [261] -0.1828133049 -0.3726366766 -0.2043331060 -0.2007636055 -0.2467410470
## [266] -0.2857873125 -0.2069704850 -0.2105049057 -0.2003692408 -0.0595286469
## [271] -0.3762037861 -0.3783374853 -0.0409606707 -0.2704830161 -0.0223898078
## [276] -0.1987593167 -0.0319763042 -0.1234712589 -0.2601315944 -0.2422641289
## [281] -0.1979018056 -0.2911760989 -0.0241453048 -0.1139862928 -0.2224273267
## [286] -0.3420612899 -0.0795331998 -0.1267844925 -0.3050377612 -0.0608520381
## [291] -0.0684889856 -0.1743350633 -0.0795166915 -0.0561610275 -0.3250620743
## [296] -0.1052618395 -0.0121409092 -0.2482801769 -0.0207678419 -0.0767282397
## [301] -0.4175016977 -0.1460748273 -0.2334789682 -0.1266842376 -0.2850237264
## [306] -0.1939141707 -0.2907607030 -0.2979005396 -0.0829723046 -0.0736663734
## [311] -0.0458269229 -0.1260727302 -0.1610079388 -0.3706375460 -0.0509666865
## [316] -0.1742862705 -0.2540320435 -0.2028656924 -0.1436831179 -0.1456733065
## [321] -0.2463557330 -0.2140824544 -0.0879865509 -0.0127030161 -0.1166034408
## [326] -0.0177801084 -0.2195311464 -0.1688806767 -0.0978248657 -0.2546218725

```

```

## [331] -0.1684137737 -0.0559868847 -0.0590376331 -0.1090821110 -0.1178248360
## [336] -0.0327307692 -0.0573303552 -0.2434085134 -0.4046557342 -0.1056861456
## [341] -0.3143143916 -0.2193043638 -0.0937013437 -0.0289771919 -0.2750558364
## [346] -0.3317682187 -0.2335375678 -0.0839517919 -0.0089408369 -0.2279727997
## [351] -0.3076867220 -0.2435353084 -0.0643919655 -0.0328152824 -0.3220956358
## [356] -0.0475128871 -0.1608787857 -0.2812957327 -0.2304999050 -0.1008941299
## [361] -0.2898300297 -0.3950619096 -0.1097954970 -0.1157263184 -0.1007101787
## [366] -0.1239314934 -0.1858838123 -0.4548764006 -0.1839990743 -0.1161104575
## [371] -0.0774783429 -0.1666218850 -0.0899610080 -0.1357063565 -0.0272360514
## [376] -0.3959540432 -0.0039252230 -0.1236945332 -0.2325191158 -0.2799035569
## [381] -0.2167963145 -0.2766479651 -0.0751434821 -0.0475410488 -0.2592413489
## [386] -0.1399296846 -0.2640132822 -0.1184656714 -0.3140493867 -0.0296780689
## [391] -0.4006609706 -0.4004053106 -0.1508247688 -0.2253554992 -0.0206565280
## [396] -0.2299332812 -0.1146312746 -0.0761827780 -0.0554556239 -0.0805633904
## [401] -0.2835379026 -0.1332655138 -0.2704794154 -0.1789987245 -0.2001588351
## [406] -0.1137282270 -0.1828407092 -0.2916287186 -0.1980182528 -0.0565628998
## [411] -0.3914480174 -0.2662965114 -0.2280403596 -0.4248711780 -0.3333393399
## [416] -0.0540671130 -0.0316287913 -0.3293594703 -0.3430292728 -0.1287240271
## [421] -0.3324389958 -0.1650704326 -0.2554890694 -0.0541594205 -0.1138197321
## [426] -0.2620844685 -0.0084795309 -0.2756608422 -0.1321143910 -0.0072990471
## [431] -0.1538240842 -0.0425795660 -0.2975986854 -0.3771298801 -0.0621801885
## [436] -0.0598147895 -0.0497825744 -0.1019197723 -0.2971386601 -0.1767580317
## [441] -0.0998752306 -0.2437807553 -0.3975696337 -0.2101352704 -0.1011775018
## [446] -0.0260812687 -0.3125842466 -0.2986734531 -0.1527092981 -0.1237522574
## [451] -0.3772725830 -0.1966186981 -0.1065215747 -0.2294909189 -0.1301469343
## [456] -0.1951984018 -0.3554299300 -0.1836056537 -0.2537735329 -0.2703443258
## [461] -0.0244563276 -0.0729367128 -0.2173383878 -0.1526779866 -0.1914150404
## [466] -0.3947312172 -0.0493625283 -0.2239986208 -0.3911689326 -0.3560519310
## [471] -0.3134240441 -0.4019704838 -0.2746844317 -0.2612146461 -0.0431470319
## [476] -0.0214819410 -0.0956544746 -0.1437838241 -0.2551861439 -0.3878934340
## [481] -0.2183554244 -0.3265560962 -0.2222485934 -0.2837595593 -0.1157487192
## [486] -0.1482311183 -0.0178405363 -0.0825410367 -0.2103979964 -0.2049622180
## [491] -0.2334985954 -0.1030683267 -0.1928728076 -0.0817278063 -0.2363150578
## [496] -0.2217515451 -0.0129357124 -0.2021923054 -0.1385673239 -0.2039673459
## [501] -0.3221448359 -0.4650759295 -0.1397811298 -0.2205211909 -0.2925056763
## [506] -0.2421392367 -0.4043530171 -0.2769593130 -0.1300886098 -0.1279444052
## [511] -0.0703315055 -0.0666165348 -0.1455122745 -0.2235270864 -0.2777202307
## [516] -0.1479144406 -0.2720301486 -0.1455970232 -0.1710901791 -0.1552626576
## [521] -0.0130534653 -0.0753860476 -0.1194112227 -0.0136746870 -0.1362968656
## [526] -0.2270566051 -0.0336543755 -0.3441881419 -0.3431360499 -0.2487361249
## [531] -0.3525722283 -0.1284490608 -0.2160281655 -0.0414176263 -0.1682236978
## [536] -0.1213419330 -0.3455668625 -0.2203419030 -0.2279038911 -0.0083549428
## [541] -0.3010220293 -0.2319606395 -0.0517114829 -0.1327856055 -0.1013927086
## [546] -0.0895990956 -0.0911930094 -0.0666915808 -0.1135141636 -0.0290057215
## [551] -0.0050326145 -0.2696735263 -0.2369542184 -0.1991492339 -0.1551809690
## [556] -0.1232552700 -0.3552963562 -0.1101650874 -0.3123183067 -0.1725726632
## [561] -0.2191722683 0.0045348577 -0.1461486848 -0.1028385698 -0.2894335916
## [566] -0.1600365383 -0.0621737045 -0.3895187541 -0.1016720929 -0.3436409751
## [571] -0.2396864040 -0.1512300616 -0.4322025876 -0.0181783614 -0.0169343189
## [576] -0.1054882764 -0.0632172962 -0.2891654067 -0.1194674581 -0.1517378148
## [581] -0.2066762354 -0.2990227145 -0.3068550902 -0.2612758011 -0.0423174363
## [586] -0.3803867744 -0.1372756111 -0.2984633077 -0.0445971768 -0.0331005309
## [591] -0.4264827848 -0.0039019108 -0.2973019217 -0.2850684328 -0.3000776626
## [596] -0.1837303562 -0.3253979473 -0.0222122423 -0.2354925828 -0.1788220056

```

##	[601]	-0.2102042604	-0.3542894195	-0.3437225318	-0.2633119364	-0.0476134929
##	[606]	-0.3083460003	-0.3212530777	-0.3251931555	-0.0248173290	-0.1497385072
##	[611]	-0.3893703066	-0.1918776626	-0.0943436239	-0.4519612953	-0.1730402288
##	[616]	-0.1429323635	-0.0582215084	-0.2029298327	-0.0285046795	-0.2371471599
##	[621]	-0.3355895218	-0.2440086069	-0.0628268415	0.0050178716	-0.0558879898
##	[626]	-0.1900373670	-0.4452364880	-0.3464925630	-0.3763623454	-0.1033433446
##	[631]	-0.1996367703	-0.0323160770	-0.3150729133	-0.2420821435	-0.1648863092
##	[636]	-0.1898273112	-0.0605524263	-0.2247857700	-0.2733325618	-0.0768514939
##	[641]	-0.0656939803	-0.3093800451	-0.1251427668	-0.2721072573	-0.2958558979
##	[646]	-0.3513606291	-0.2492836582	-0.0468915285	-0.3389717721	-0.1102789706
##	[651]	-0.0062108319	-0.2190942358	-0.3266469820	-0.1287256667	-0.3862848483
##	[656]	-0.0234719793	-0.1662144823	-0.2801220937	-0.1967546716	0.0793852168
##	[661]	-0.1180494495	-0.0662930010	-0.2555475868	-0.1798046492	-0.3202122920
##	[666]	-0.0340045309	-0.2625725496	-0.2076638390	0.0866123879	-0.0033816165
##	[671]	0.0391445585	0.0774308558	0.0738851766	0.0608782098	0.0226877206
##	[676]	0.1808171073	0.1491541110	0.1740246528	0.1013258996	0.0708622561
##	[681]	0.0392465280	0.1210893612	0.2104476357	0.0678225360	0.0818402119
##	[686]	0.1473818380	0.0394499296	0.0484297979	0.1493732675	0.0252513892
##	[691]	0.0077513085	0.1955400985	0.0074377416	0.0448157443	0.2486657205
##	[696]	0.1004464930	0.0844688889	0.0956285932	0.1096329747	0.0826027258
##	[701]	0.1508297146	0.0139222728	0.1232990397	0.0349542799	0.0724084457
##	[706]	0.0471312687	0.2077647855	0.0270535544	0.0376932205	0.1054808091
##	[711]	0.0852633540	0.0863183036	0.2157479289	0.1157767745	0.0820379256
##	[716]	0.0491985584	0.2076995122	0.2486236657	0.0570613967	0.2067498163
##	[721]	0.0107634480	-0.1828340194	0.1750758719	0.0681314777	0.0102615328
##	[726]	0.2304658488	0.1498048017	0.0123432623	0.1227969972	0.0223489725
##	[731]	0.1675764418	0.0441328852	0.0609351513	0.1632405612	0.1091159949
##	[736]	0.0133686129	0.0960250522	0.1682268628	0.0620810055	0.1674474296
##	[741]	0.1373345199	0.0561936617	0.1282127789	0.0248675071	0.0631048057
##	[746]	0.0433006461	0.1652029862	0.0950113923	0.0973606249	0.0851671888
##	[751]	0.1679005650	0.1820779543	0.2073896997	0.0623860943	0.1330852637
##	[756]	0.0587964523	0.0934363752	0.0161957523	0.2560868995	0.0664315710
##	[761]	0.1773231628	-0.2668410421	0.1748911638	0.0745795453	0.1088745920
##	[766]	0.2743535763	0.0674685091	0.1520920507	0.0163356603	0.0536549774
##	[771]	0.0711727775	0.1237661695	0.2087567144	0.1849156214	0.1252470089
##	[776]	0.2202063817	0.0882901216	0.1535477267	0.0458118884	0.0708876015
##	[781]	-0.0007918654	0.0111919230	0.0444761240	0.0012436136	0.0881888321
##	[786]	0.0213615407	0.2210365882	-0.0011111871	0.1263256557	0.0449784386
##	[791]	0.2361549198	0.1419133778	0.0882008229	0.0648371289	0.0345053509
##	[796]	0.1011881953	0.1712385002	0.0288474690	0.2481656092	0.1851842388
##	[801]	0.1803496016	0.1220368778	0.1356670215	0.1623593681	0.2411362193
##	[806]	0.0889757848	0.0324209110	0.0378801110	0.1998104308	0.0070315169
##	[811]	0.0772819727	0.0183710398	-0.0930607371	0.0369658826	0.0777647888
##	[816]	0.0141379230	0.0173906192	0.0436446961	0.0595543807	0.0943059876
##	[821]	0.0898134685	0.1411903224	0.2239366152	0.0913358297	0.1678497955
##	[826]	0.1360967628	0.2103438345	0.0654612581	0.0963538812	0.0091450999
##	[831]	0.0735180831	0.1236195543	0.1354911907	0.0450200968	0.0445575905
##	[836]	0.0201766899	0.0140350026	0.0998647227	0.0158094992	0.1496355655
##	[841]	0.1574982592	0.2140330991	-0.1217473535	0.0472159235	0.0137603070
##	[846]	0.0334928481	0.1032079272	0.0053174065	0.0847605956	0.1673142379
##	[851]	0.0497559573	0.1210216741	0.0879808496	0.0042971750	0.2182113688
##	[856]	0.0859533967	0.1257859034	-0.1151247014	0.0994740658	0.1368632998
##	[861]	0.0135091863	0.1097876036	0.0334441036	0.0323471966	0.1879900282
##	[866]	0.0323912653	0.1342856272	0.1048092395	0.1164797828	0.2201407435

```
## [871] 0.1590268446 0.0239177950 0.0311045512 0.1320675047 0.0333396729
## [876] 0.1930888936 0.0736995798 0.1223184396 0.0971540650 -0.0015349537
## [881] 0.1517274533 0.1155125466 0.0101596010 0.0418124872 0.0967995644
## [886] 0.1208486033 0.1078827165 0.0948357668 0.0509630265 0.0355127888
## [891] 0.0390546248 0.0096873963 0.0823482900 0.0959455874 0.0366643138
## [896] 0.0639833887 0.0182693444 0.0074242941 0.2148219118 0.0194430923
## [901] 0.1752655119 0.0678375001 0.0730331924 0.1968134314 0.1022151327
## [906] 0.0410084241 0.0605498261 0.0015948901 0.1602174535 0.0559303660
## [911] 0.1048800309 0.1544076040 0.1120799542 0.1134055586 0.2066890542
## [916] 0.1584797641 0.0487946826 0.0613947275 0.0107412804 0.0170249585
## [921] 0.0491986374 0.1049064268 0.1732085750 0.1157223715 0.1534830459
## [926] 0.0625601832 0.0176528538 0.1802847351 0.0581063865 0.0441654261
## [931] 0.0323950782 0.0090537725 0.1692795478 0.1416778491 0.1586668811
## [936] 0.0705033641 0.0816819183 0.1230648625 0.0571108967 0.1999107160
## [941] 0.0199971206 0.0629302335 0.1622890963 -0.2864672886 0.0030699370
## [946] 0.0727948886 0.0653986726 0.1086182832 0.0923528784 0.1864249003
## [951] 0.0299667743 0.0333157716 0.2055814628 0.2200446484 0.0445258259
## [956] 0.1757950874 -0.0053723309 0.0278291637 0.0459470353 0.2227804686
## [961] 0.0301223694 0.0928226907 0.0899726140 0.0573175169 0.0073455417
## [966] 0.0707928505 0.0862729813 0.1500158824 0.0440672798 0.0458408814
## [971] 0.1214072749 0.0066990302 0.0811857798 0.0409217268 0.0570853178
## [976] 0.0307585350 0.1770663100 0.0238216967 0.2258475224 0.1117004238
## [981] 0.1248867290 0.0145296603 0.1698695450 0.1151190243 0.0470410482
## [986] 0.0233983724 0.0629771394 0.1932605337 0.1198112120 0.1399218653
## [991] 0.1284855570 0.2319768094 0.1890013124 0.1624693927 0.0112819653
## [996] 0.0654914727 0.0464885207 0.0628836667 0.0135622825 0.0179054632
```

```
y_pred = y_all
y_pred[y_all >= 0] = 1
y_pred[y_all < 0] = -1
print(y_pred)
```

```
## [1] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [25] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [49] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [73] -1 1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [97] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [121] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [145] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [169] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [193] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [217] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [241] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [265] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [289] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [313] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [337] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [361] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [385] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [409] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [433] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [457] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [481] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [505] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [529] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
```

```

## [553] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [577] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [601] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 1
## [625] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
## [649] -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 1 -1 -1 -1 -1 -1 -1 -1 1 -1 1 1
## [673] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [697] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [721] 1 -1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [745] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 -1 1 1 1 1 1 1
## [769] 1 1 1 1 1 1 1 1 1 1 1 1 -1 1 1 1 1 1 1 -1 1 1 1
## [793] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 -1 1 1 1
## [817] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [841] 1 1 -1 1 1 1 1 1 1 1 1 1 1 1 1 1 -1 1 1 1 1 1 1
## [865] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 -1 1 1 1 1 1 1 1
## [889] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [913] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [937] 1 1 1 1 1 1 1 -1 1 1 1 1 1 1 1 1 1 1 1 -1 1 1 1
## [961] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [985] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1

```

```

acc = sum(y_pred == group)/length(group)
print(acc)

```

```

## [1] 0.985

```

```

plot(g_x, g_y, type='n', xlab='X', ylab='Y')
points(g1_x, g1_y, col='red')
points(g2_x, g2_y, col='blue')
abline(a = -1.0*theta0/theta2, b = -1.0*theta1/theta2, col='dark green', lwd=3, lty=2)

```