

1. (a) Looking at the differential equation dI/dt , we find that $I(t)$ will be increasing when $aSI > rI$ and decreasing when $rI > aSI$. From dI/dt , we can conclude the spread of the disease depends on the interactions between the susceptible and the infected with some transmission rate a . By this model, since the number of infected goes up with the interactions between S and I , quarantining would reduce the amount of interactions, thus, reducing the rate at which I grows.

(b)

$$\begin{aligned}\frac{dS}{dt} &= -aSI, & \frac{dI}{dt} &= aSI - rI \\ \frac{dIdt}{dtdS} &= \frac{aSI - rI}{-aSI} \\ &= \frac{aSI}{-aSI} + \frac{rI}{aSI} \\ &= -1 + \frac{rI}{aSI} \\ &= -1 + \frac{r}{aS} \\ &= -1 + \frac{1}{R_0 S}\end{aligned}$$