

$$f(x) = \frac{e^x}{1+e^x}$$

1.  $\lim_{x \rightarrow \infty} f(x) = \lim_{x \rightarrow \infty} \frac{e^x}{1+e^x}$  By L'Hopital's rule:  $\lim_{x \rightarrow \infty} \frac{e^x}{1+e^x} = \lim_{x \rightarrow \infty} \frac{e^x}{e^x} = 1$  Thus, the limit is 1.
2.  $\lim_{x \rightarrow -\infty} \frac{e^x}{1+e^x}$  If we plug in negative, we find that the equation looks like:  $\lim_{x \rightarrow -\infty} \frac{\frac{1}{e^x}}{1+\frac{1}{e^x}}$  and as this equation goes to infinity,  $\frac{1}{e^x}$  is going to go to zero. Thus,  $\lim_{x \rightarrow -\infty} \frac{e^x}{1+e^x} = \frac{0}{1+0} = 0$
3. The derivative of  $f$  is  $\frac{e^x}{e^{2x}+2e^x+1}$  Since  $e^x$  is never negative, we can conclude that the numerator is never negative, and for the same reason, the denominator is not negative, as we are adding only positive numbers.