

List of Depths: Given a binary tree, design an algorithm that creates a linked list of all the nodes at each depth.

If you have a tree of depth  $D$ , you will have  $D$  number of linked lists.

Ex)

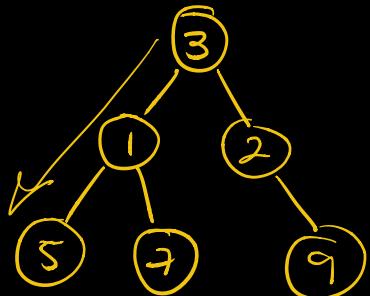
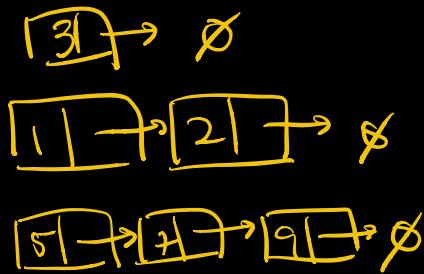


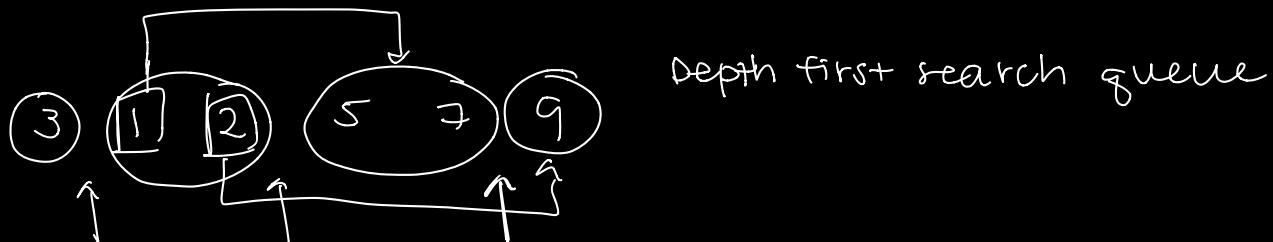
Fig 1.  
A binary tree



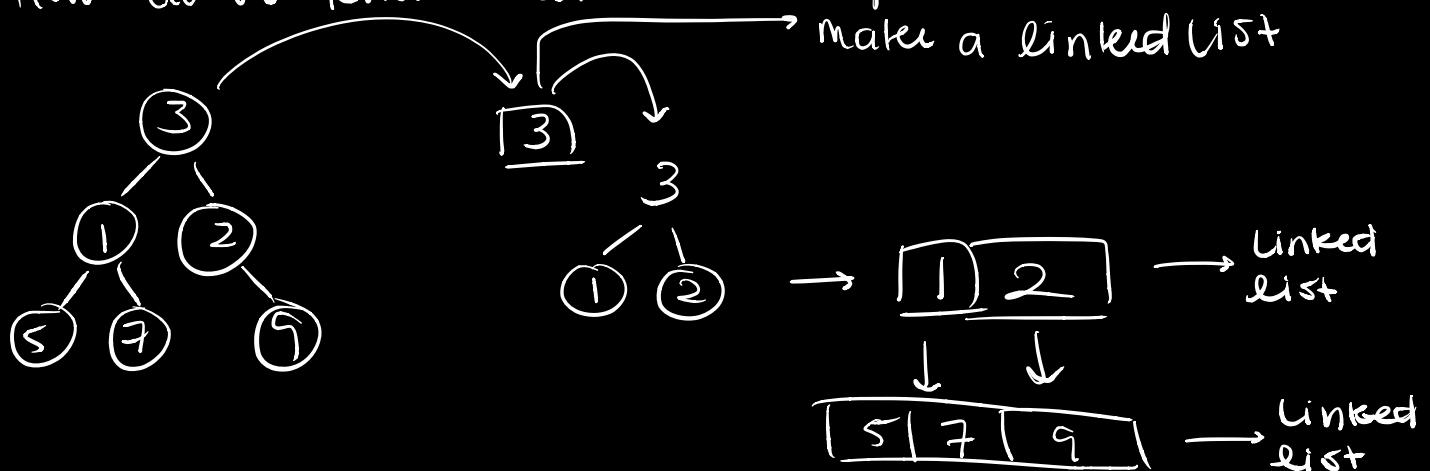
$D = 3$ ,  
3 linked lists

Fig 2.

Linked lists for  
each depth of  
fig 1.



How do we know these are the partitions?



make a linked list

- Have a list hold all linked lists
- At each level, create a linked list of all nodes in that level
- starting with the root, store its children
- reset linked list after visiting each level

## Breadth-First Search Solution (Iterative)

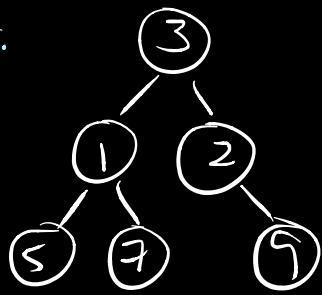
```
function createLinkedLists(root) {
    let results = [ ]; // Array for containing linked lists
    let currentLevel = new LinkedList();
    if (root !== null) {
        currentLevel.append(root);
    }
    while (currentLevel.size > 1) {
        results.push(currentLevel);
        let parents = currentLevel;
        currentLevel = new LinkedList();
        for (parent in parents) {
            if (parent.left !== null) {
                currentLevel.append(parent.left);
            }
            if (parent.right !== null) {
                currentLevel.append(parent.right);
            }
        }
    }
    return results;
}
```

### Complexity Analysis:

- Time:  $O(n)$ , we end up visiting each node in the tree once.
- Space:  $O(n)$ , for the creation of the linked lists that gets returned

## Illustrated Test:

given:



1. results = [ ]

currentLevel =  $\boxed{3} \rightarrow \emptyset$

↓

2. enter while loop

results =  $\left[ \boxed{3} \rightarrow \emptyset \right]$

parents =  $\boxed{3} \rightarrow \emptyset$

↓

3. enter for loop for parents

currentLevel =  $\boxed{1} \rightarrow \boxed{2} \rightarrow \emptyset$

4. back to the beginning of the while loop

results =  $\left[ \boxed{3} \rightarrow \emptyset, \boxed{1} \rightarrow \boxed{2} \rightarrow \emptyset \right]$

parents =  $\boxed{1} \rightarrow \boxed{2} \rightarrow \emptyset$

5. currentLevel =  $\boxed{5} \rightarrow \boxed{7} \rightarrow \boxed{9} \rightarrow \emptyset$

6. back to the beginning of the while loop, again

results =  $\left[ \boxed{3} \rightarrow \emptyset, \boxed{1} \rightarrow \boxed{2} \rightarrow \emptyset, \boxed{5} \rightarrow \boxed{7} \rightarrow \boxed{9} \rightarrow \emptyset \right]$

- end -

## Recursive Solution (depth-first search via preorder traversal)

```
function createlinkedlists(root) {
    let results = [];
    createLinkedList (root, results, 0);
    return results;
}

function createLinkedList (root, results, level) {
    if (root == null) {
        return;
    }

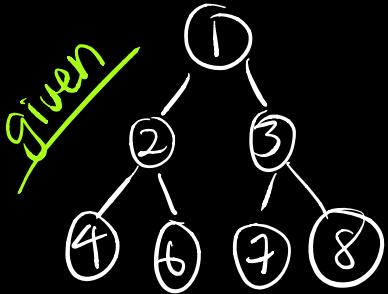
    let result = null;
    if (results.size == level) {
        result = new LinkedList();
        results.push(result);
    } else {
        result = results.get(level);
    }

    result.append(root);
    createLinkedList (root.left, results, level + 1);
    createLinkedList (root.right, results, level + 1);
}
```

## Complexity Analysis

Time:  $O(n)$ , we visit each node in the tree once  
Space:  $O(n)$ , although the recursive calls result in  $O(\log n)$  of the stack to be used, we are still returning linked lists of the same size as the tree that is given. Therefore, the larger complexity trumps the smaller one.

running  
through the  
function:



①  $\text{root} = 1$   
 $\text{results} = [] = \emptyset$   
 $\text{level} = 0$   
 $\text{results} = [\emptyset]$

②  $\text{root} = 2$   
 $\text{results} = [\underline{1} \rightarrow \emptyset] = 1$   
 $\text{level} = 1$   
 $\text{results} = [\underline{1} \rightarrow \emptyset, \emptyset]$   
 $\text{result} = \underline{2} \rightarrow \emptyset$

③  $\text{root} = 4$   
 $\text{results} = [\underline{1} \rightarrow \emptyset, \underline{2} \rightarrow \emptyset]$   
 $\text{level} = 2$   
 $\text{results} = [$   
 $\text{result} = \underline{4} \rightarrow \emptyset$

③  $\text{root} = 6$   
 $\text{results} = [\underline{1} \rightarrow \emptyset, \underline{2} \rightarrow \emptyset, \underline{4} \rightarrow \emptyset]$   
 $\text{level} = 2$   

go to else statement!

 $\text{result} = \underline{4} \rightarrow \underline{6} \rightarrow \emptyset$

②  $\text{root} = 3$   
 $\text{results} = [\underline{1} \rightarrow \emptyset, \underline{2} \rightarrow \emptyset, \underline{4} \rightarrow \underline{6} \rightarrow \emptyset]$   
 $\text{level} = 1$   
 $\text{result} = \underline{2} \rightarrow \underline{3} \rightarrow \emptyset$