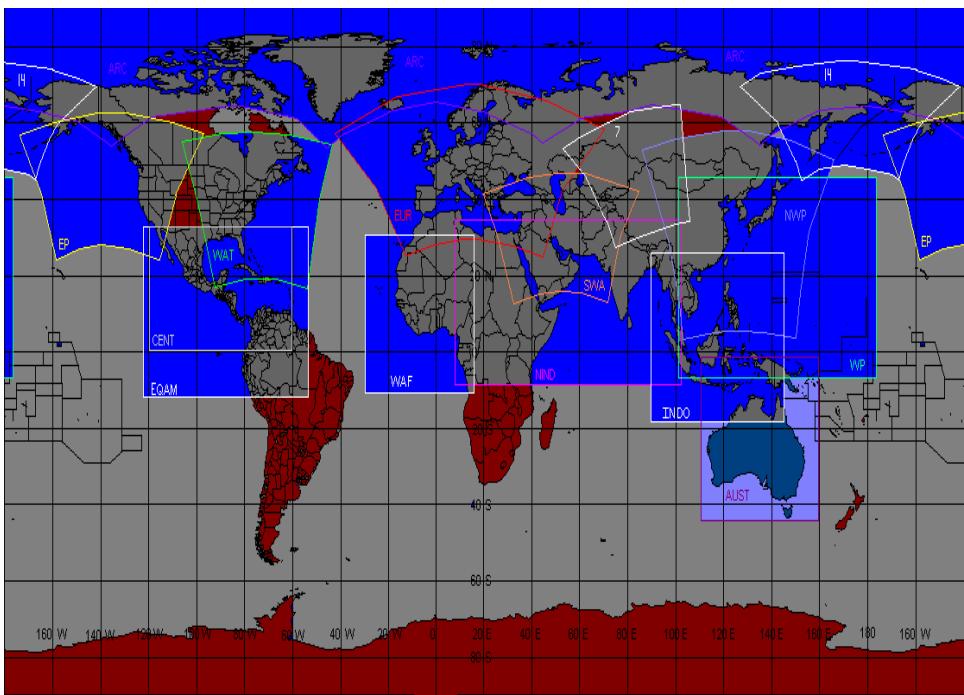


# NEPTUNE: Next Generation Atmospheric Modeling at the U.S. Naval Research Laboratory

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- 5: U.S. Naval Postgraduate School, Department of Meteorology;
- 6: U.S. Naval Postgraduate School, Department of Applied Mathematics
- Monterey, CA, USA

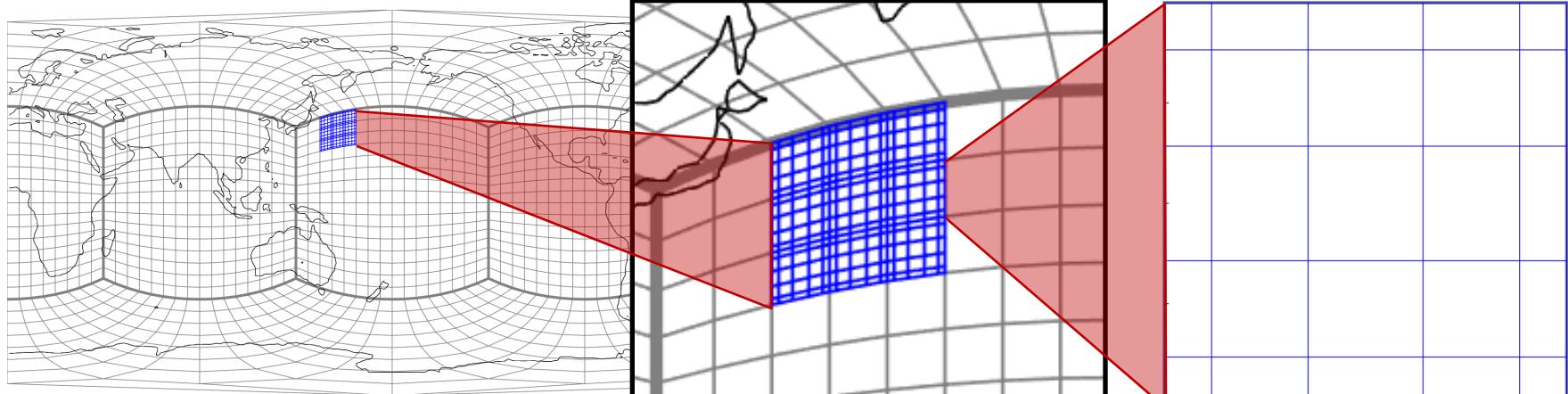
# NRL Marine Meteorology Division and Operational Partner FNMO

- Weather and seasonal climate
- Global Forecasting:
  - NAVGEM, SL-SI spectral transform
    - 4 times daily, currently 31km resolution
- Limited Area (Mesoscale) Forecasting:
  - COAMPS®, split-explicit FD
    - Over 70 unclassified COAMPS domains run daily down to 500m resolution
    - Domains are always in flux
- Why invest in a new system?
  - Neither system is positioned to exploit next generation architectures
  - Both systems are low order and non-conservative (though skillful nonetheless)
  - We are not a large laboratory, roughly 100 scientists, less than half working on model development
- consolidation to a unified system would be advantageous in many ways



# Next Generation Modeling

- Navy goal to develop next generation model, with capabilities:
  - Multi-scale non-hydrostatic dynamics (global-scale to mesoscale)
  - Highly scalable, flexible, accurate, and conservative numerical methods
  - Structured, unstructured, or adaptive grids; scale-aware parameterizations
- A spectral element (SE) technique is the selected numerical method
  - Solution is represented by a local polynomial expansion, good convergence
  - Very small communication footprint implies excellent computational scaling
- Use the **NUMA<sup>1</sup>** dynamical core as the foundation for our NWP system
  - Global and limited area capabilities.



<sup>1</sup>**NUMA:** Nonhydrostatic Unified Model of the Atmosphere (Giraldo et. al. 2013)

## Features

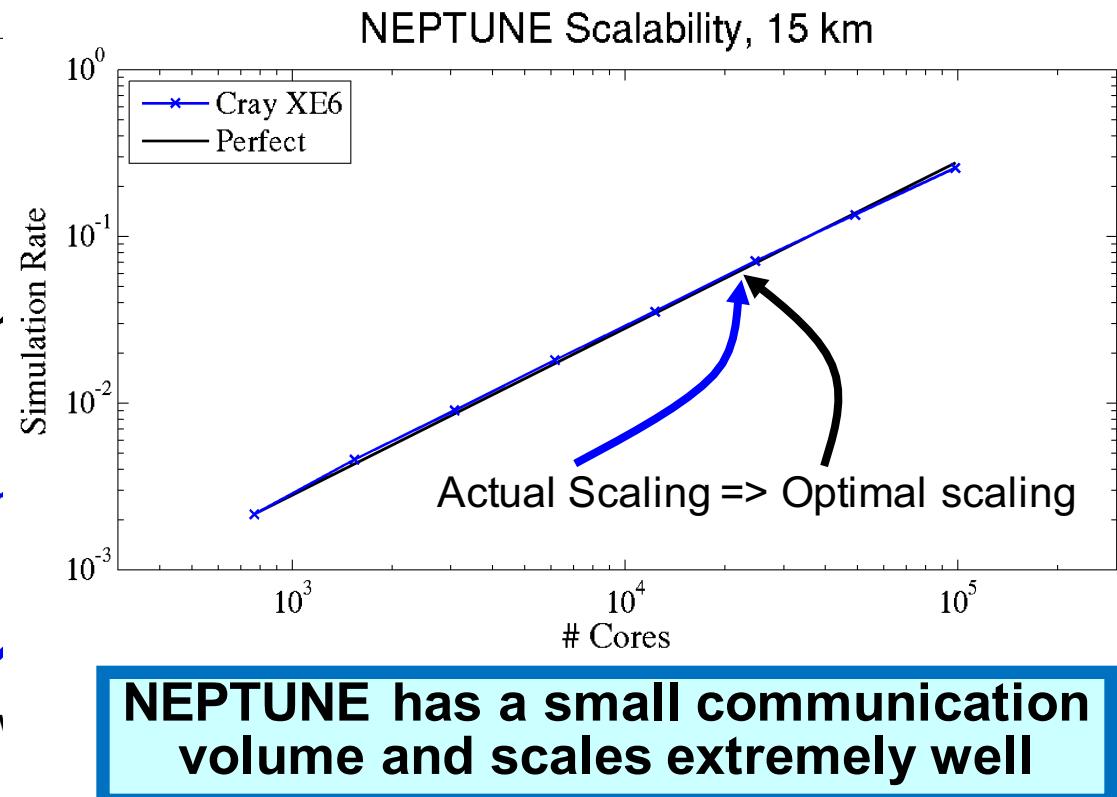
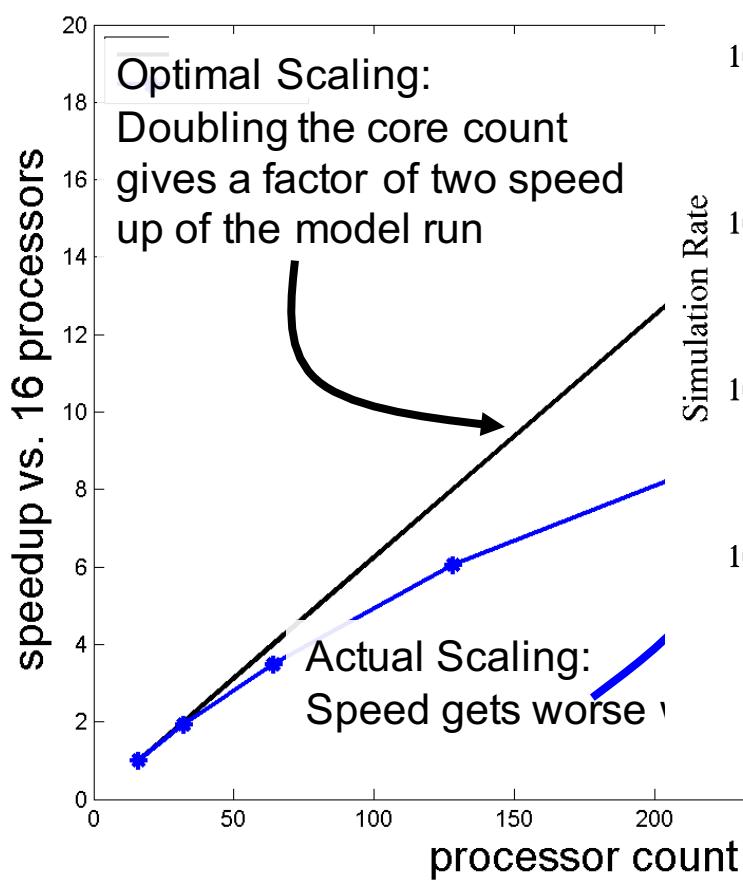


Non-hydrostatic Unified Model  
of the Atmosphere

- Deep atmosphere equations
- Non-hydrostatic
- Unified **3D** CG/DG dynamical core
- Cartesian coordinate system for limited area
- Sphere centered Cartesian coordinate system for global prediction
- Inexact integration (mass lumping)
- 1D/3D IMEX for efficiency
- Non-conforming AMR

Kelly and Giraldo 2012 JCP, Giraldo et. al J. Sci. Comput. 2013,  
Kopera and Giraldo 2014 JCP

## Computational Scaling



**NEPTUNE has a small communication volume and scales extremely well**

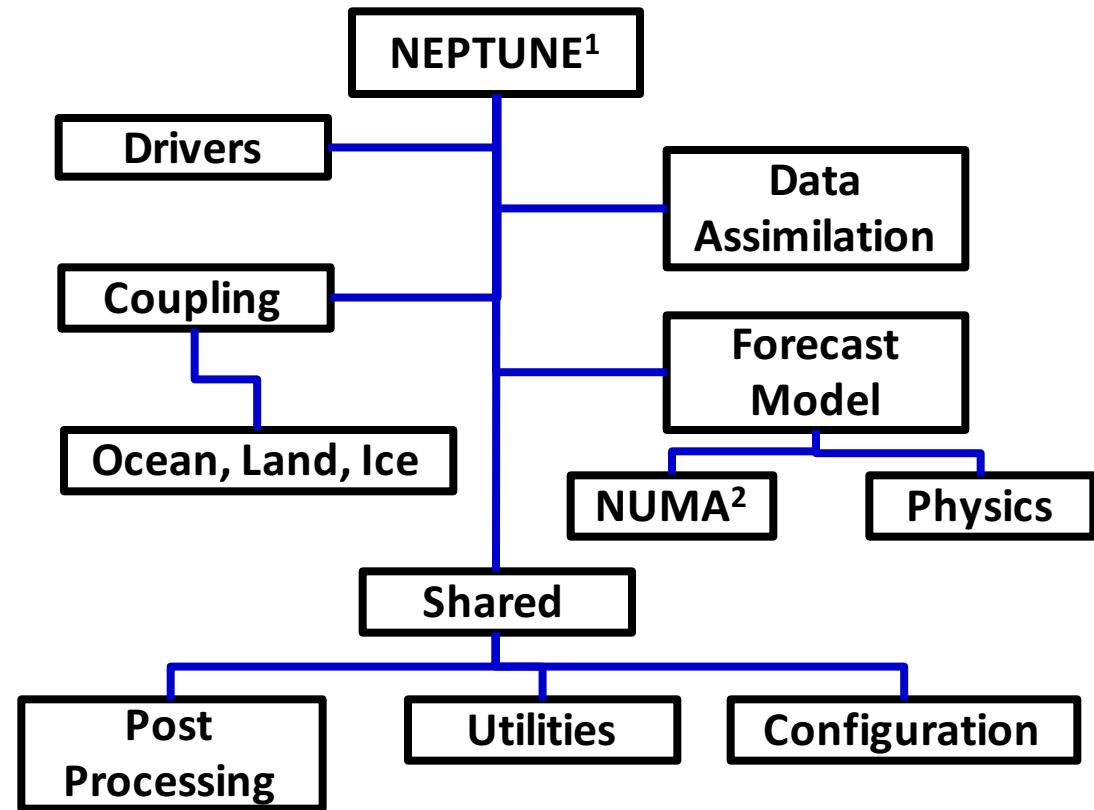
**Often with models that require large communication volumes, the cost of communication will dominate the cost of computation as the core count increases.**

# NEPTUNE

**NEPTUNE** is the US NAVY's next generation NWP system

**NUMA** is the dynamical core of NEPTUNE

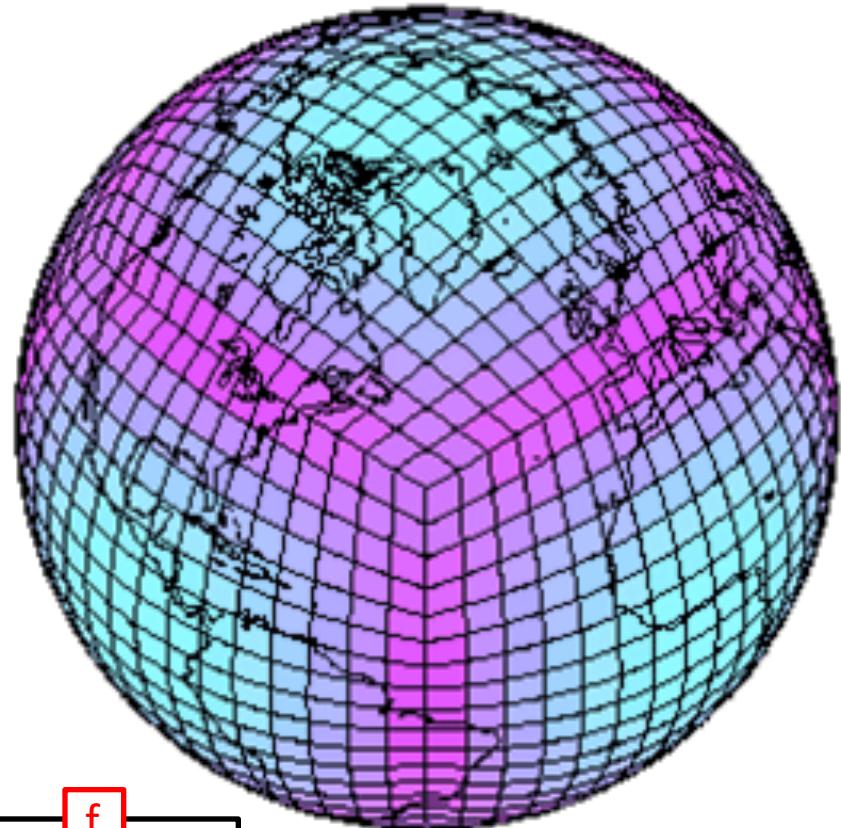
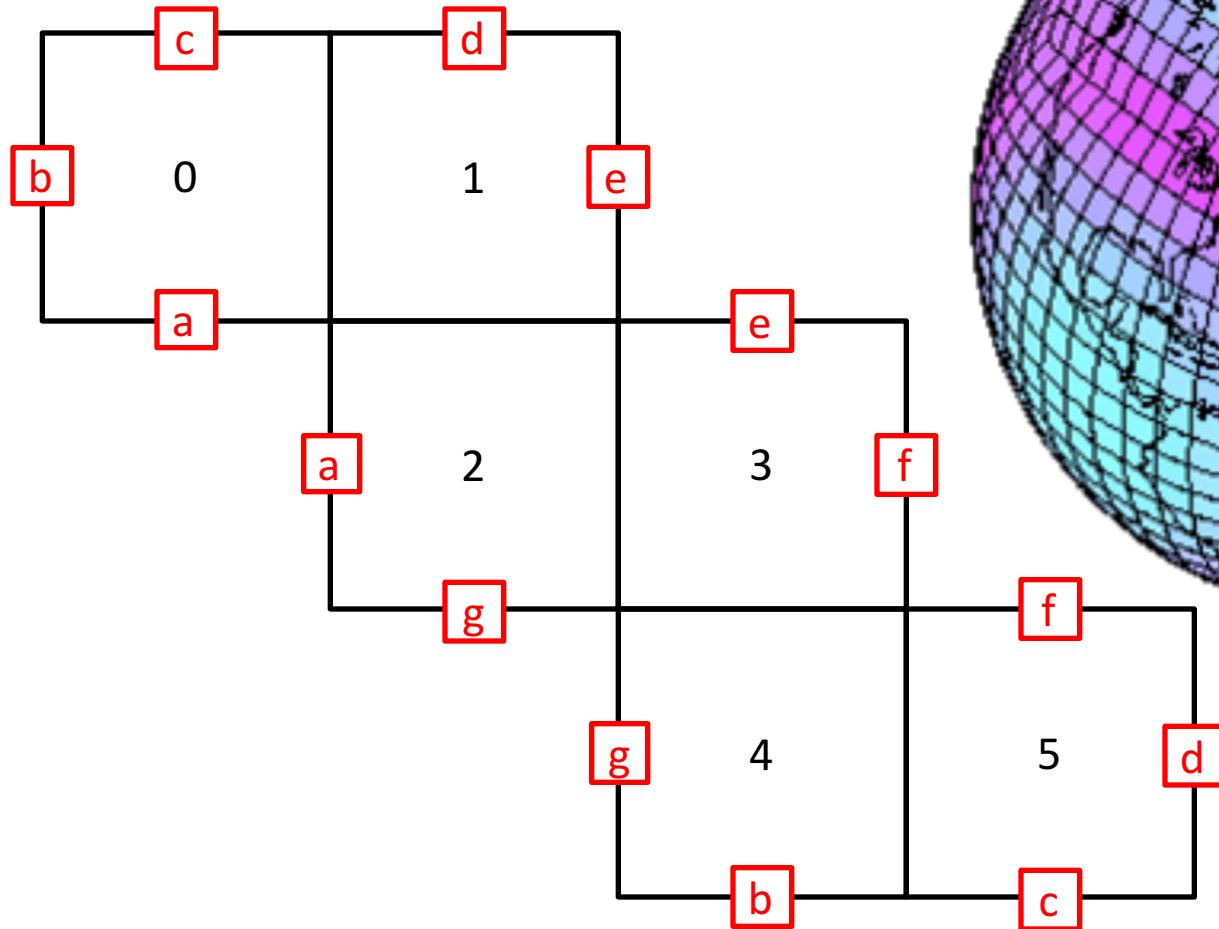
**NUMA** uses a **three-dimensional** spectral element technique with a sphere centered Cartesian coordinate system on the cubed sphere



<sup>1</sup>**NEPTUNE**: **Navy Environmental Prediction sysTem Utilizing the **NUMA**<sup>2</sup> corE**

<sup>2</sup>**NUMA**: **Nonhydrostatic Unified Model of the Atmosphere (Giraldo et. al. 2013)**

# NUMA Grid on the Sphere (Cubed Sphere)



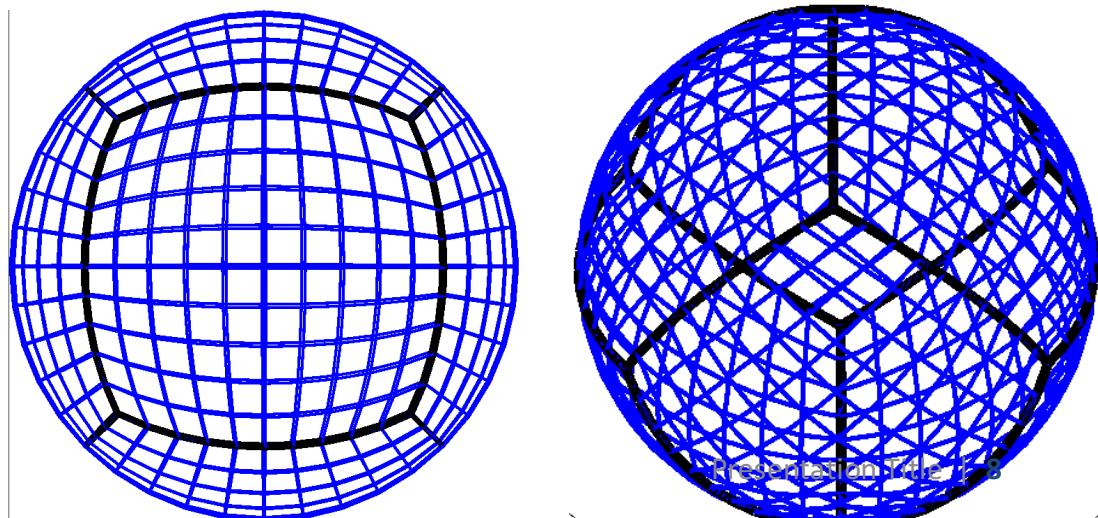
# NUMA Grid on the Sphere (Cubed Sphere)

- Equi-angular gnomonic plane
- Equi-distant gnomonic transform
- Local spherical transform (template face)
- Rotate to respective faces to build cubed sphere
  - expand radially
  - Cartesian transform

$$\hat{\lambda}^f \begin{cases} \lambda^{fc} + \tan^{-1} \left( \frac{\cos \phi^1 \sin \lambda^1}{\cos \phi^1 \cos \lambda^1 \cos \phi^{fc} - \sin \phi^1 \sin \phi^{fc}} \right) \\ \sin^{-1} (\sin \phi^1 \cos \phi^{fc} + \cos \phi^1 \cos \lambda^1 \sin \phi^{fc}) \end{cases}$$

– *Superscripts: f for face number, fc for face center, 1 for template face at (0,0)*

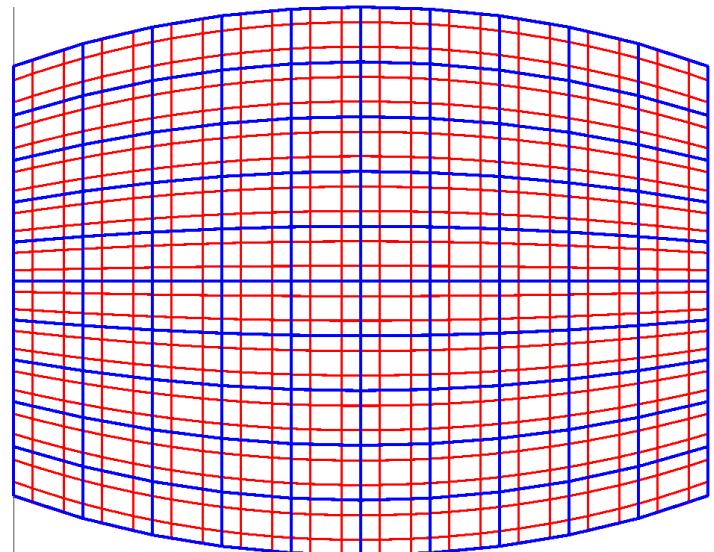
$$\begin{aligned} \{\lambda, \phi\} &\rightarrow \{\lambda, \phi, r\} \\ \vec{x} = \{x, y, z\} \in [-r, r] & \quad \vec{x} = \begin{cases} r \cos \phi \cos \lambda \\ r \cos \phi \sin \lambda \\ r \sin \phi \end{cases} \end{aligned}$$



## Original Metric Terms

- Metric terms for transforming between physical ( $\vec{x} = \{x, y, z\}$ ) and canonical ( $\vec{\xi} = \{\xi, \eta, \zeta\}$ ) spaces use the SE machinery (basis functions) and are built ***discretely***
- Attempts to resolve the result of several trigonometric transforms using a low-order basis*
- Results in significant error in representing the sphere for polynomial degrees less than 8*

$$\nabla_{\vec{\xi}} \vec{x} = \begin{pmatrix} x_\xi & x_\eta & x_\zeta \\ y_\xi & y_\eta & y_\zeta \\ z_\xi & z_\eta & z_\zeta \end{pmatrix}$$

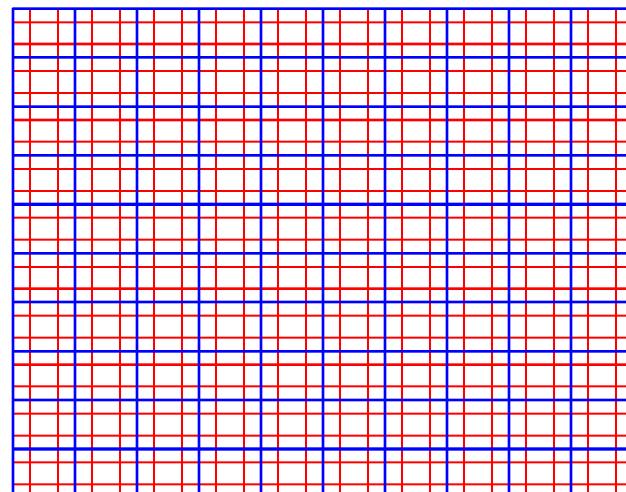


## Semi-Analytic Metric Terms (Current)

- Replace discrete metric terms with analytic terms wherever possible using the chain rule and the steps used to create the cubed sphere
- Uses analytic representations of Jacobians from the:
  - Equidistant gnomonic transform
  - Local spherical transform
  - Cartesian coordinate transform
- Discrete derivatives in canonical space are performed on the equiangular plane
  - This is linear and representable by a low order basis in the absence of terrain

$$\nabla_{\vec{\xi}} \vec{x} = (\nabla_{\vec{\xi}} \vec{x}_\alpha) [(\nabla_{\vec{x}_\alpha} \vec{x}_e) (\nabla_{\vec{x}_e} \vec{\lambda}) \mathbf{R}^{-1} (\nabla_{\vec{\lambda}} (\mathbf{R} \vec{x}))]_A$$

- Subscript *A* is for *analytic*
- **R** is a rotation matrix back to face 1 (0,0) of the cubed sphere to avoid pole problems and apply metrics consistently across each face



# Shallow Atmosphere Approximation

- Applying the shallow atmosphere approximation is trivial using the semi-analytic metric terms

$$\vec{x} = \begin{pmatrix} r \cos \phi \cos \lambda \\ r \cos \phi \sin \lambda \\ r \sin \phi \end{pmatrix}$$

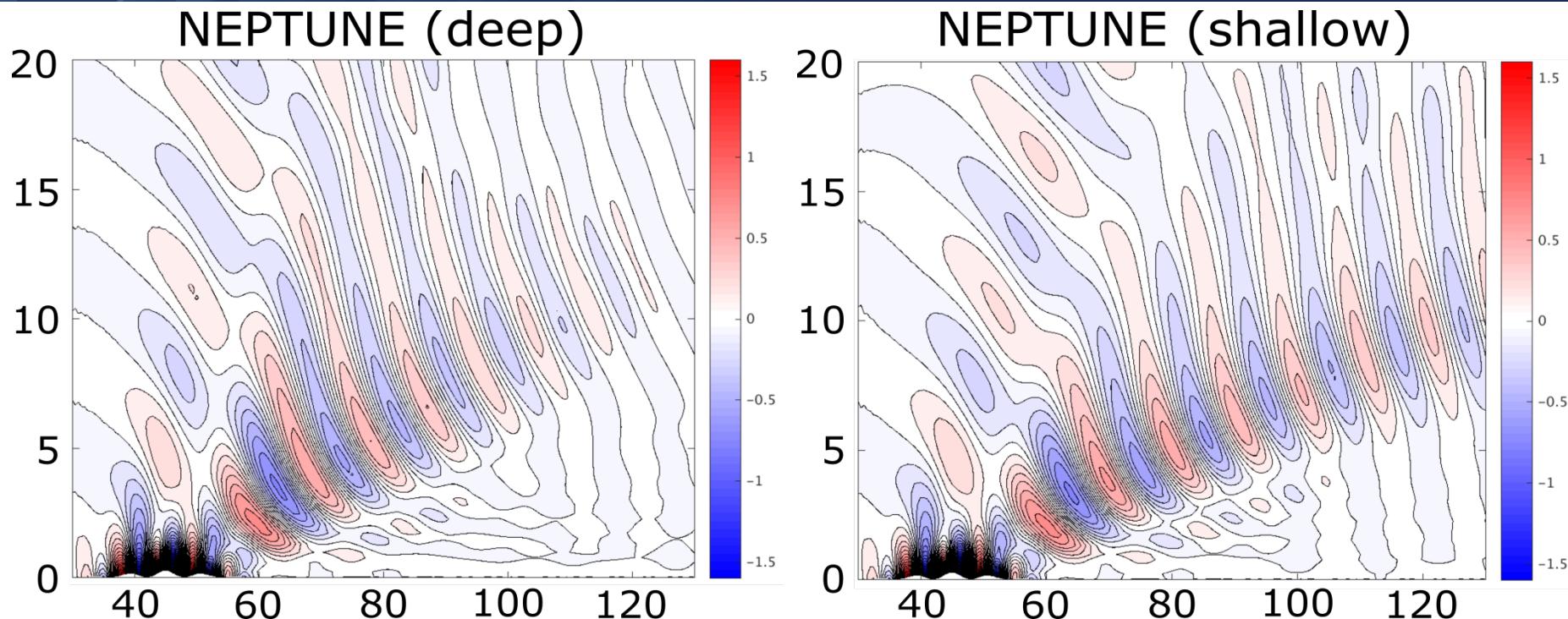
- In the Jacobian of the mapping from spherical to Cartesian space, replace all instances of  $r$  with  $a$

- $a$  is the radius of the earth and  $r = (a+z)$

$$\nabla_{\vec{\lambda}} \vec{x} = \begin{pmatrix} -r \cos \phi \sin \lambda & -r \sin \phi \sin \lambda & \cos \phi \cos \lambda \\ r \cos \phi \cos \lambda & -r \sin \phi \cos \lambda & \cos \phi \sin \lambda \\ 0 & r \cos \phi & \sin \phi \end{pmatrix}$$

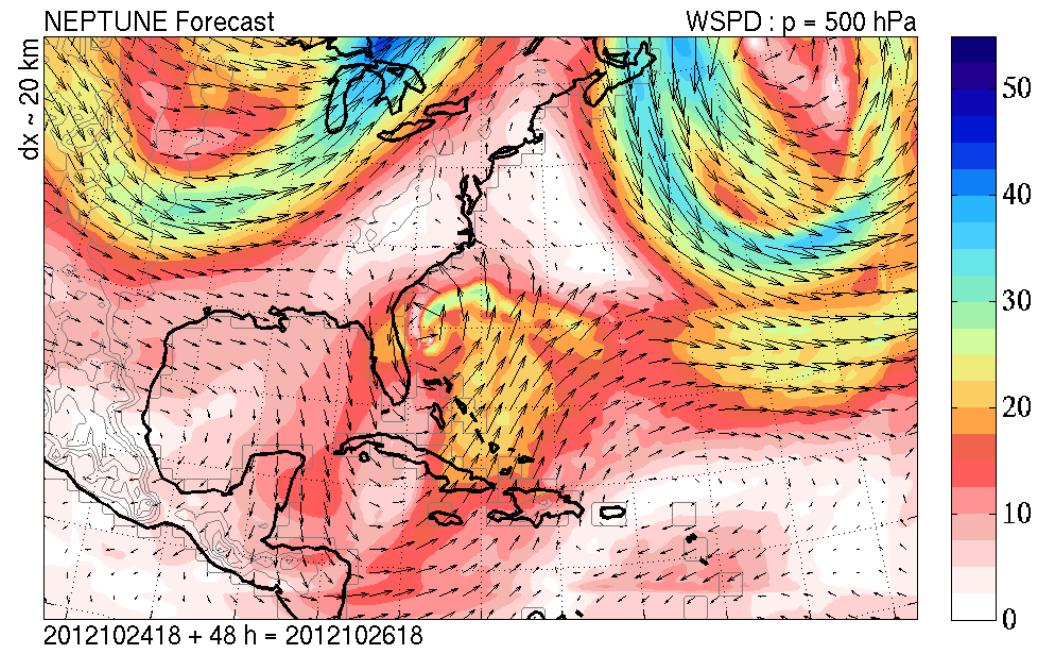
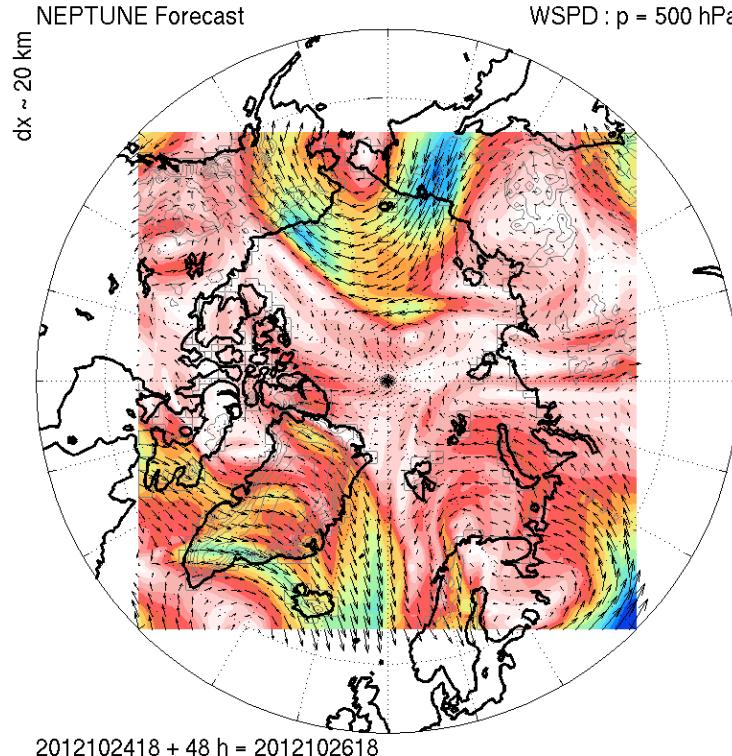
$$\{\nabla_{\vec{\lambda}} \vec{x}\}_{SA} = \begin{pmatrix} -a \cos \phi \sin \lambda & -a \sin \phi \sin \lambda & \cos \phi \cos \lambda \\ a \cos \phi \cos \lambda & -a \sin \phi \cos \lambda & \cos \phi \sin \lambda \\ 0 & a \cos \phi & \sin \phi \end{pmatrix}$$

# Sheared Flow over Schär Mountain



- Horizontal grid stretching with increasing  $z$  which attenuates the vertically propagating wave energy using the deep atmosphere equations
- The shallow equations eliminate the attenuation resulting in increased wave amplitude both aloft and downstream

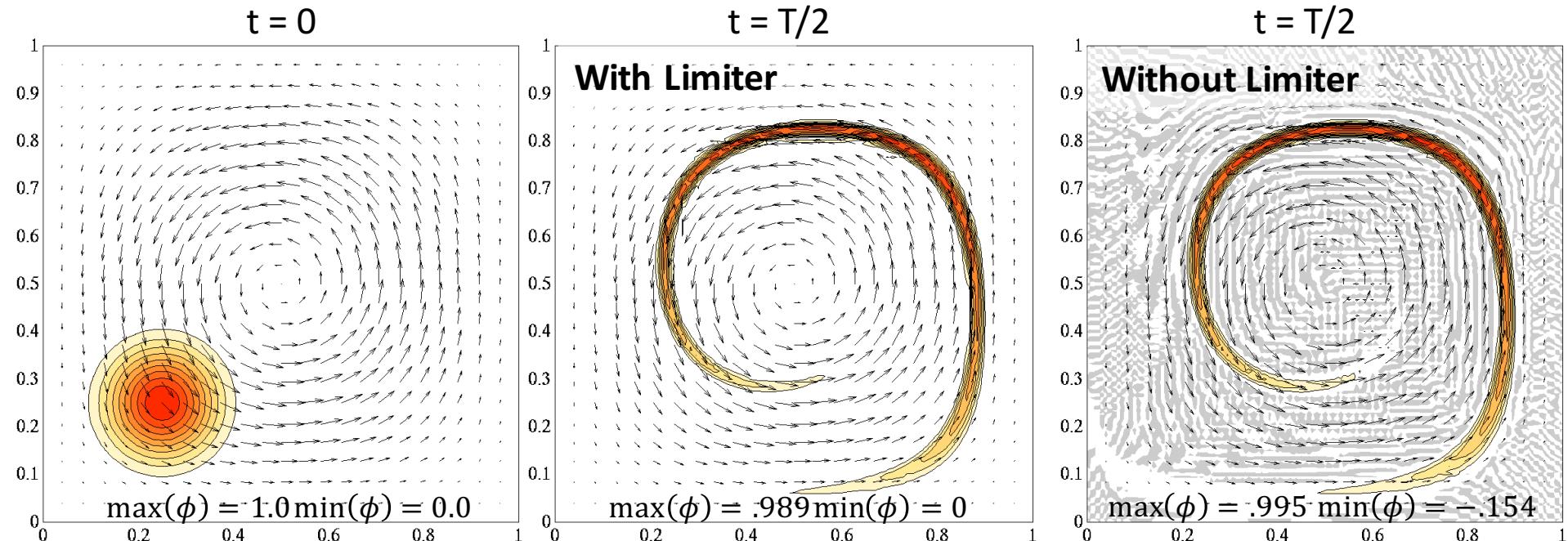
# Limited Area Model Application



- Developed a limited area version of NEPTUNE with set of projections
  - Lambert Conformal, Mercator, Stereographic
  - Solution prescribed at lateral boundaries using Davies BC's
- Used to test high-resolution physics without needing to run a high-resolution version of the global configuration

# Positive Definite Tracer Transport

Implement a high-order, global conservative, positive definite limiter (TMAR) into NEPTUNE based on Light and Durran, 2016



Stream function defines the non-divergent velocity field

$$\Psi(x, y, t) = \frac{1}{\pi} \sin(\pi x)^2 \sin(\pi y)^2 \cos\left(\frac{\pi t}{T}\right)$$

## Time Integration

A wide range of high-order IMEX (1D and 3D) time integrators available in NUMA

### Problem

- Horizontal sound waves limit  $\Delta t$  for 1D-IMEX (e.g.  $\Delta t = 30$  s for 60 km horizontal resolution)
- Convergence rates for 3D-IMEX are too slow for real-data

### Solution

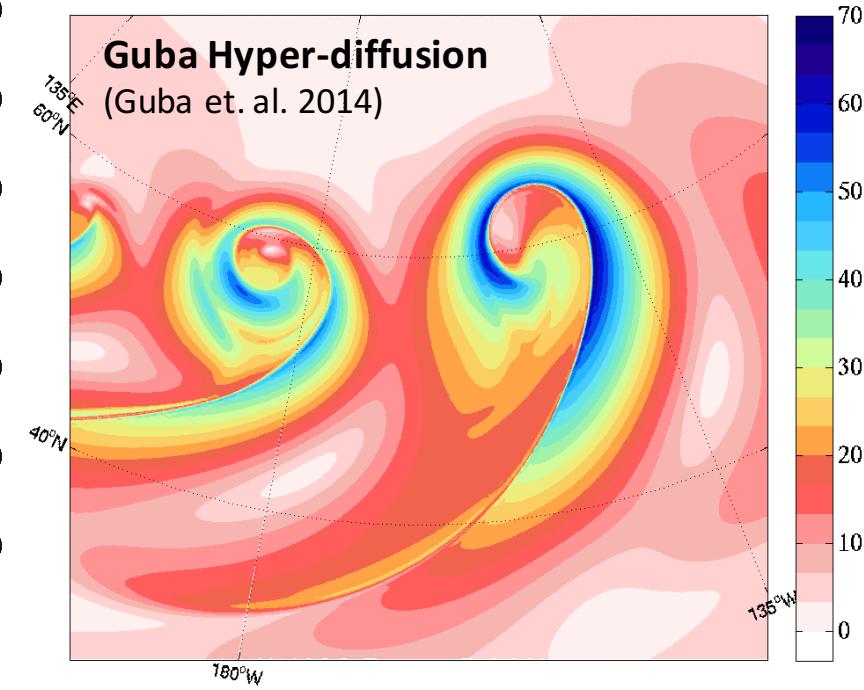
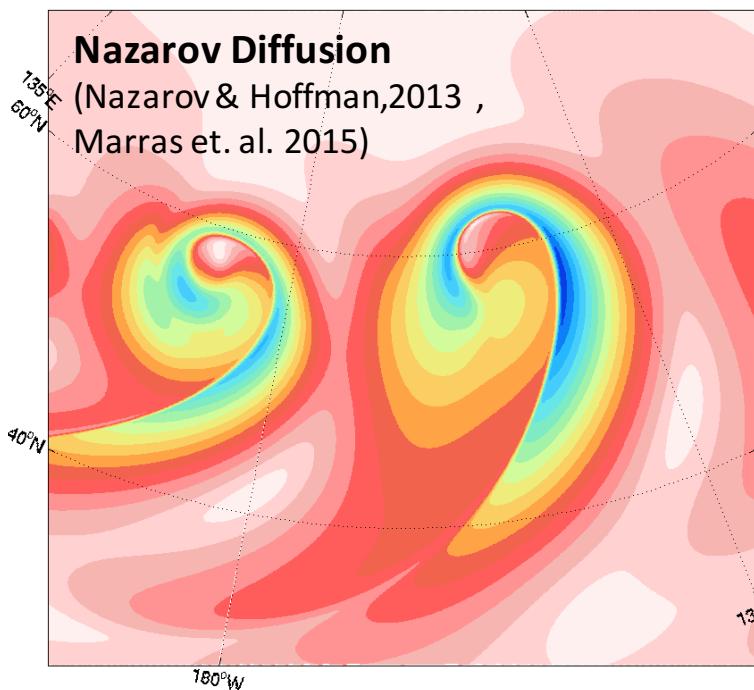
- Implement a split-explicit scheme Runge-Kutta scheme
- Sound waves integrated on a small time step
- Not necessarily a long term solution

### Result

- Up to 8x larger  $\Delta t$  over 1D-IMEX
- More applicable to NWP

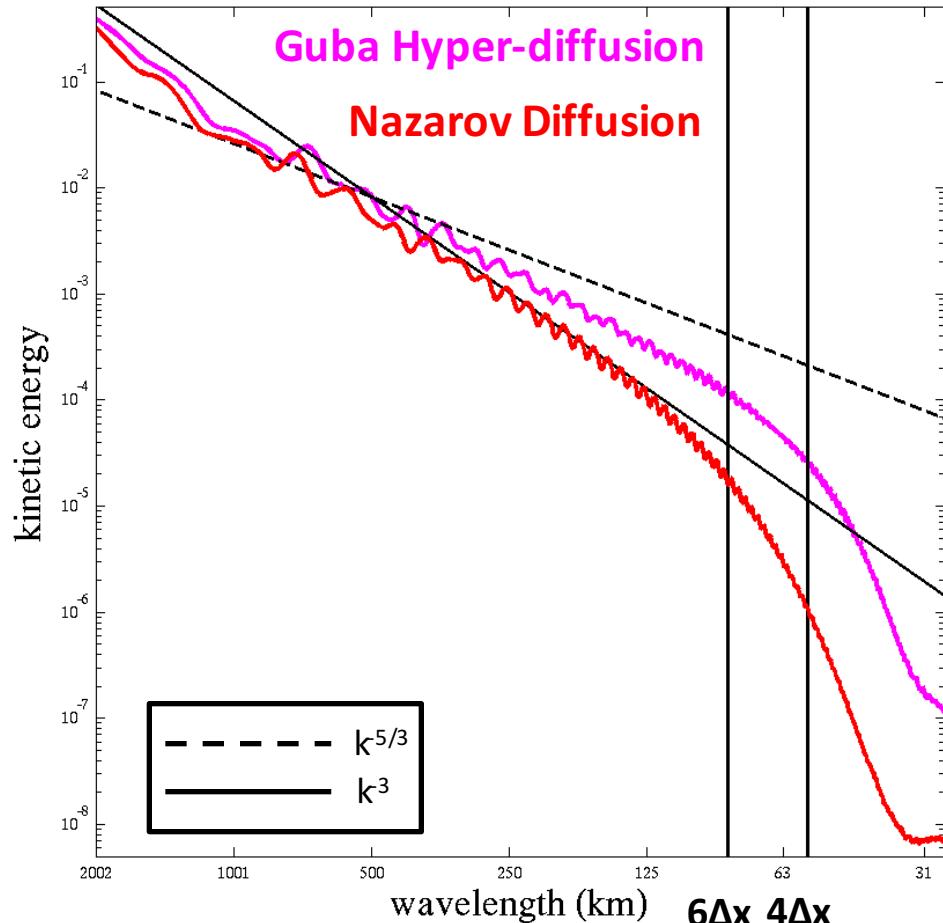
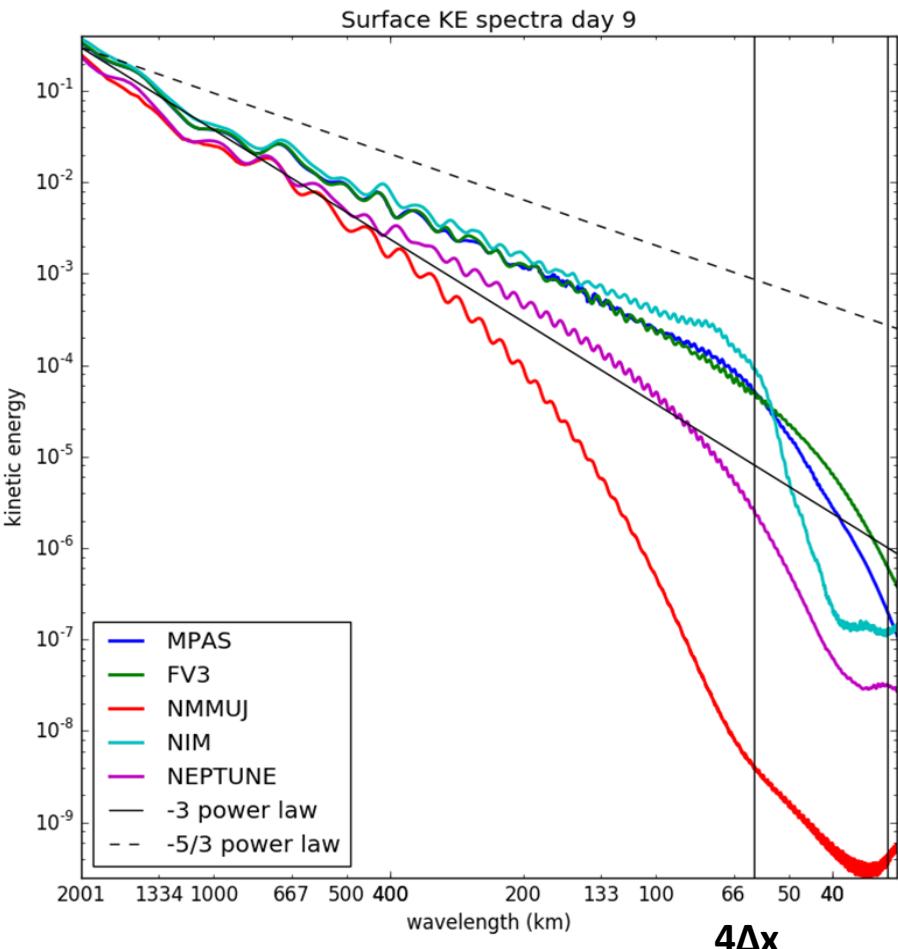
# Dry Baroclinic Wave Test

## Surface Winds – Day 9



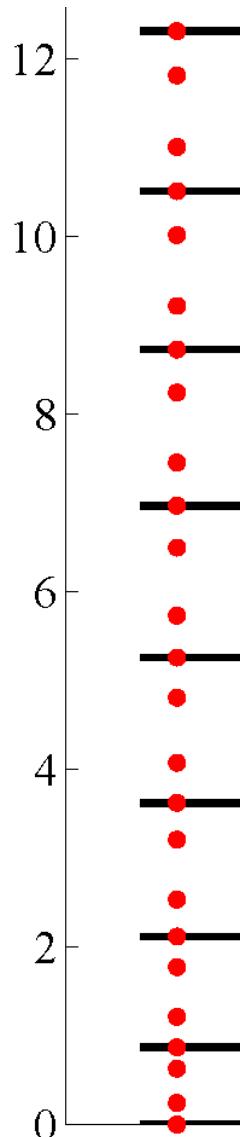
- Initially not able to maintain stability → 3-D diffusion operator
- Implemented Nazarov based diffusion for stabilization
- Change to Guba hyper-diffusion (4<sup>th</sup>-order) → horizontal and vertical

# Baroclinic Wave Spectra



- Original KE spectra of NEPTUNE falls off too rapidly with wavenumber
- Improved performance with updated diffusion options

## Physics Grid



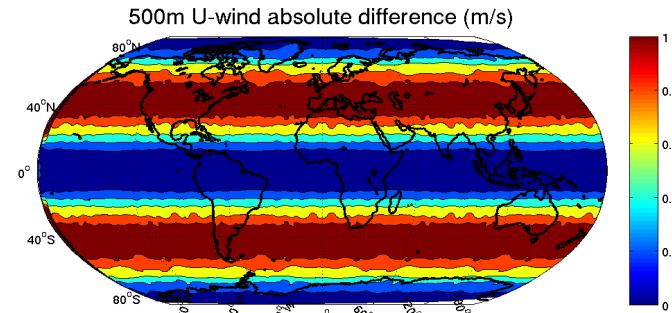
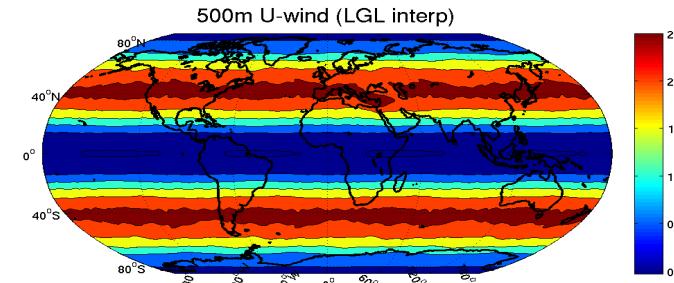
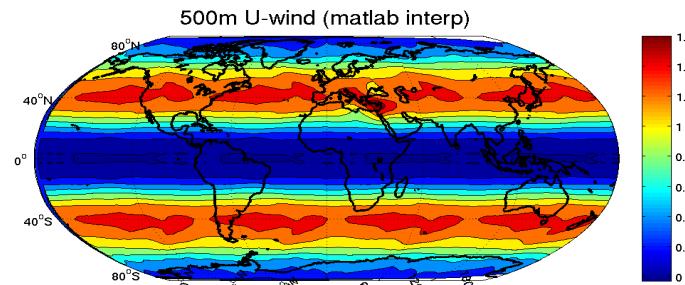
Three Dimension Spectral Element implies vertical grid spacing is non-uniform

Unknown how this will impact physical parameterizations

1. Do nothing. Apply physics on GLL grid
2. Linear remap of fields to a regularly spaced grid within each element. Linear map tendencies back to GLL grid.
3. Use basis functions to perform a high-order remap to a regularly spaced grid. High-order map tendencies back to GLL grid (invert the remap operator).

## Post-Processing: Remapping

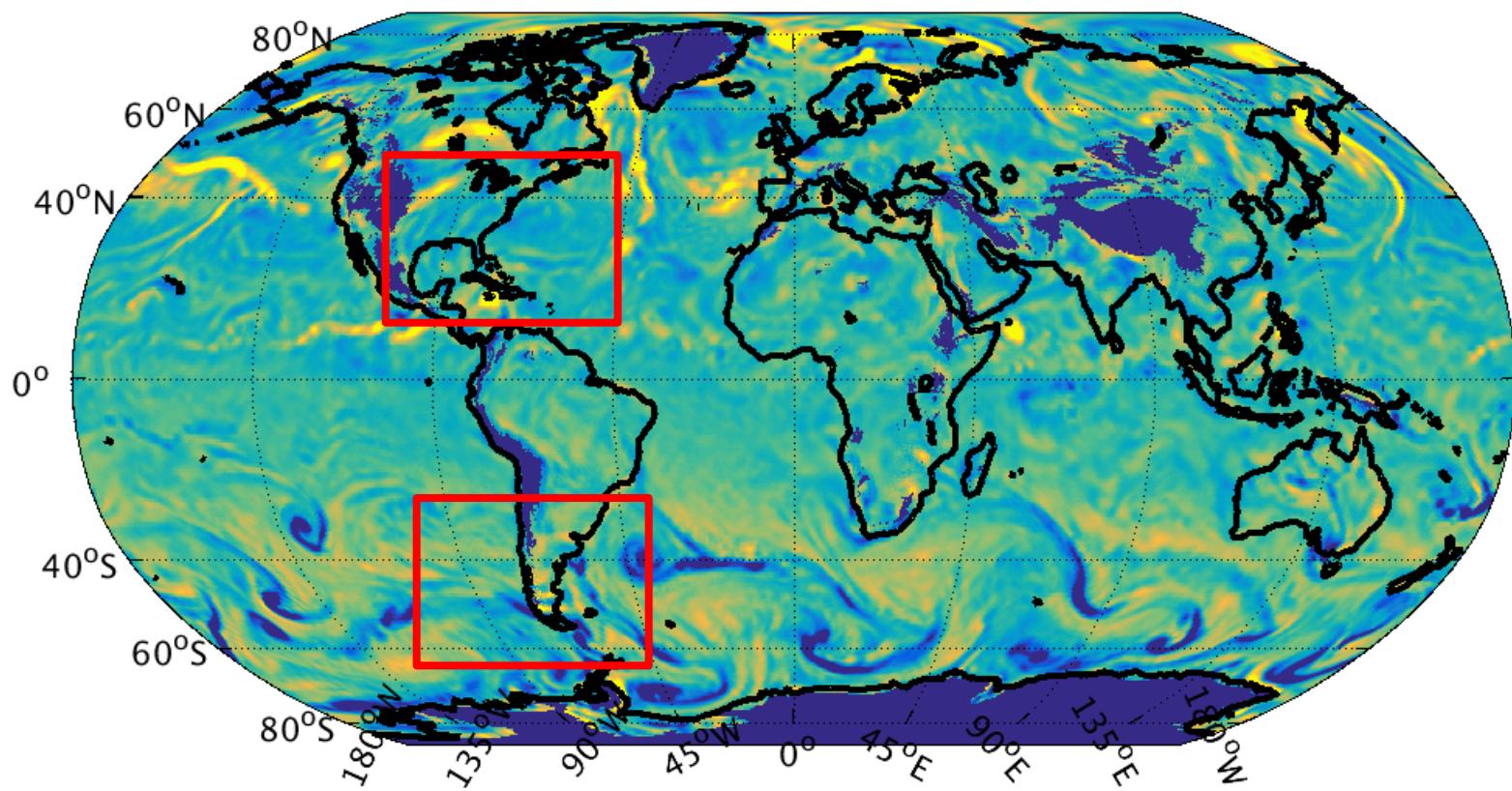
- We can use the basis functions to remap the solutions from the LGL grid to any output grid we choose in a conservative manner
- Involves iterative quasi-Newton method to find:
  - 1) the element in which the new point lies
  - 2) its canonical coordinate so we can build the 3D interpolating function



## Real Data Test Case

E256P3L43 :  $\langle \Delta x \rangle = 13 \text{ km}$ ; Full physics

850 hPa vertical vorticity

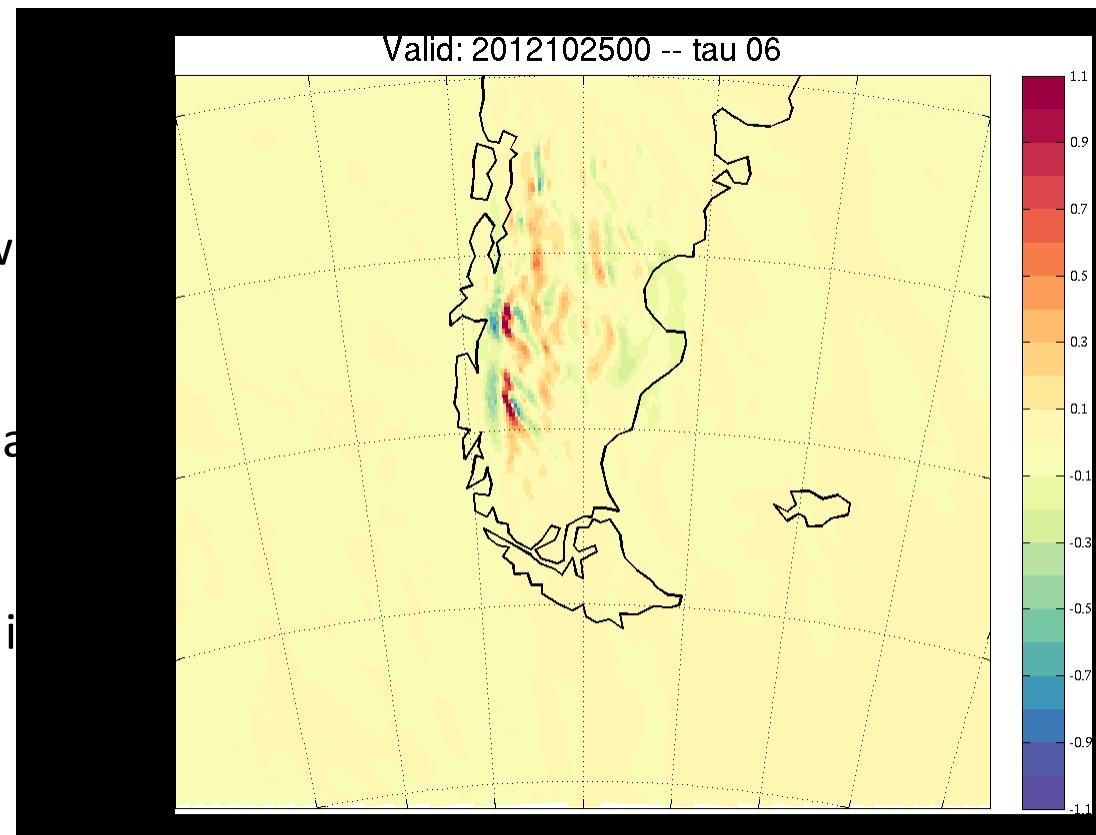


## Real Data Test Cases

- Southern Andes are hotspot for orographic gravity wave activity
- Play dominate role in the momentum budget of middle atmos.

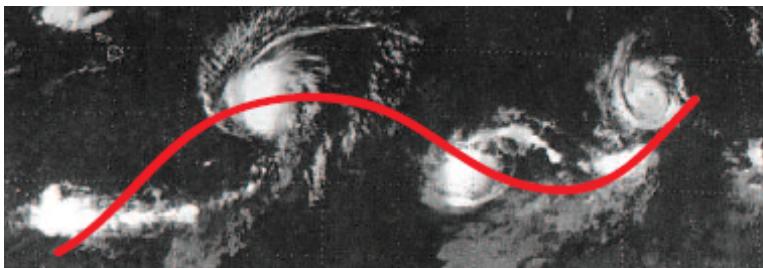
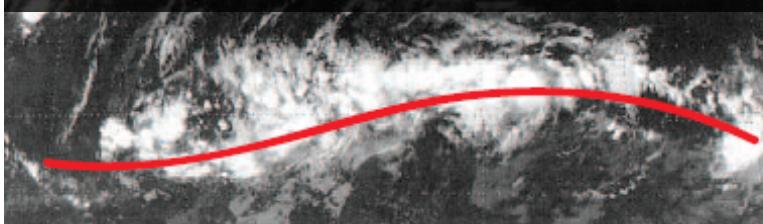
### 200 hPa Vertical Velocity

- Two frontal features interact w/ Andes during forecast period
- Vorticity streaks from individual peaks (maybe PV banners)
- Vertically propagating mountain wave at 200 hPa

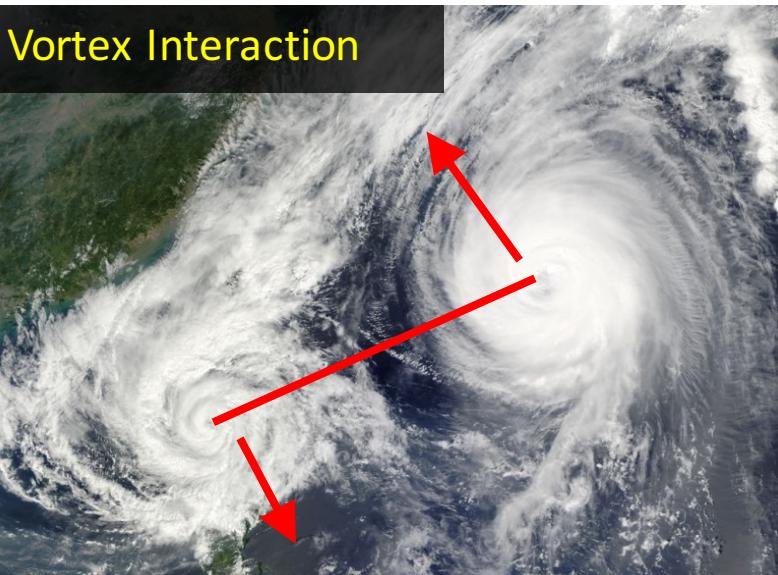


# NUMA AMR/Naval Interests

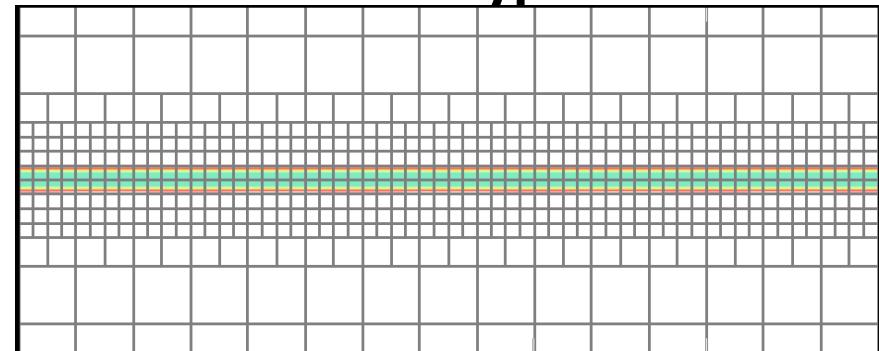
## Inter-Tropical Convergence Zone Instability



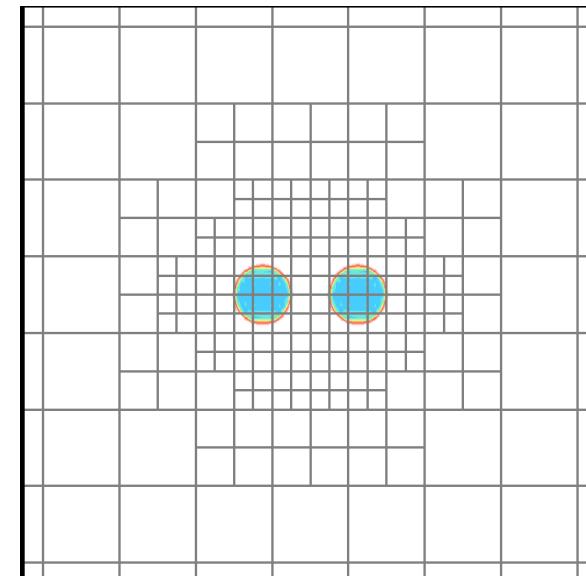
## Vortex Interaction



## Prototypes



3x fewer grid points



9x fewer grid points NEPTUNE | 22