

Ans. to the question no. 03:

function Dijkstra (Graph, source):

dist[source] \leftarrow 0

queue = Priority Queue()

visited = [None] * (length(Graph) + 1)

prev = [None] * (length(Graph) + 1)

for each vertex V in graph : $\longrightarrow O(V)$

if $V \neq \text{source}$:

dist[V] = ∞

prev[V] = null

queue.put((dist[source], source))

while queue not empty : $\longrightarrow O(E \log E)$

U = queue.extract_min() $\longrightarrow \log E$

if visited[U]:

continue

visited[U] \leftarrow True

for each neighbour v of U : $\longrightarrow O(E)$

alt = dist[U] + length(U, v)

if alt < dist[v]:

dist[v] = alt

prev[v] = U

queue.put((distance[v], U)) $\longrightarrow O(\log E)$

For task 1, if we use adjacency list then the time complexity will be $O((V+E)\log(V))$.
 If we use adjacency matrix then the time complexity will be $O(V^2 + E\log(V))$.

For task 2, same as task 1 pseudo code \neq just adding the path -

flag = end-point

temp = []

temp.append(flag)

~~temp.~~

while flag \neq source $\rightarrow O(V)$

as adding $O(V)$ with the time complexity of the Dijkstra's pseudo code will not add any significance to the time complexity, so we ignore it.

Time complexity for task 2.

For adjacency list = $O((V+E) \log(V))$

Matrix = $O(V^2 + E \log(V))$

PART 2

If the number of titans in each road is exactly 1 or weight of each edge is 1 we can use BFS Algorithm to solve the problem. The time complexity of BFS is $O(N+M)$.

for adjacency matrix it will be $O(N^2)$

Algo \rightarrow function BFS(visited, graph, node, endpoint):

visited[node] = 1

queue.put(node)

$O(N) \leftarrow$ while queue not empty:

m = queue.get()

if m = endpoint:

return

$O(M) \leftarrow$ for each neighbour of m in graph:

if visited[neighbour] = 0

visited[neighbour] = 1

queue.put(neighbour)

Ans. to the question no. 04:

We know BFS also gives shortest path between source and destination. But in this case each edge have weights of each route/path. We know we can't use BFS for weighted graph to find shortest path. So we used Dijkstra to find a path from Motijheel to Moghbazar.

