

HOFEM-AIRBUS 2D Emulation

**Group of Radiofrequency, Electromagnetism, Microwaves
and Antennas (GREMA)**

<http://grema.webs.tsc.uc3m.es/>

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uc3m | Universidad Carlos III de Madrid

Outline

- 1 Green3D vs Green2D for FE-IIIE
 - Green's Function for 2D Emulation
 - Near Field (FE-IIIE loop)
 - Far Field (postprocess)
 - Further Rethinking on Possible Use of Green3D
 - A note on Field Representation on Surfaces
 - Further Numerical Results (using Green2D)
 - TE Polarization
 - Dielectric Coated Cylinder (TM and TE)
- 2 Ewald Acceleration (1D periodicity)
 - Differences with Respect to 2D Periodicity
 - Fortran Module
- 3 EMULATION_2D Fortran Module
- 4 Far Field Numerical Results
- 5 Oblique Incidence
 - Green's Function
 - Far Field
 - Integration of EMULATION_2D and PBCs
 - A note on ABC_PERIODIC boundary condition

Outline (cont.)

- Numerical Results (oblique incidence)

6 Modifications on Near Field Postprocessing

7 MPI related issues

We start considering the use of Green3D or Green2D for the scattering of infinite cylinders using a 3D simulator on a section (“slice”) of the cylinder

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- Fortran Module

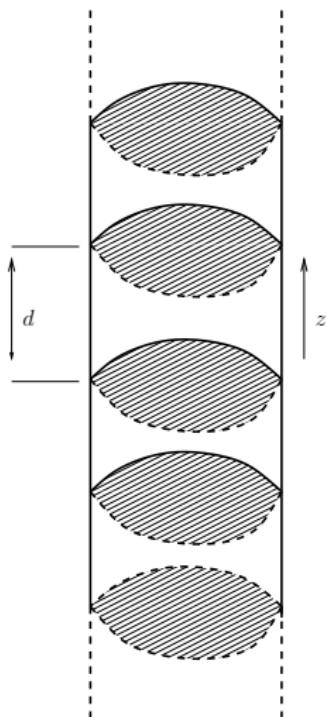
3 EMULATION_2D Fortran Module

4 Far Field Numerical Results

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6 Modifications on Near Field Postprocessing



3D Green's Function

- Sum of infinite contributions (from each repeated cell)
- Ewald acceleration needed

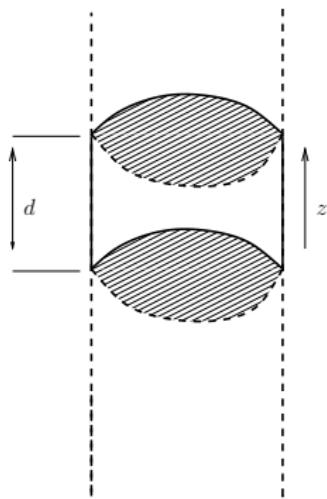
$$\text{Green}(R) = \frac{1}{4\pi} \sum_{n=-\infty}^{\infty} \frac{e^{-jkR_n}}{R_n}$$

with

$$R_n = |\mathbf{r} - \mathbf{r}'_n|, \mathbf{r}'_n = \mathbf{r}'_0 + n\mathbf{d}$$

- ▶ New implementation (for 1D periodicity) required
- ▶ 1D periodicity case is different (and much more involved) than 2D periodicity already present in the code for the infinite array.
- ▶ See details later in Section 50

HOFEM 2D Emulation (cont.)



2D Green's Function

- No summation needed

$$\text{Green}(\rho) = \frac{1}{4j} H_0^{(2)}(k|\rho|)$$

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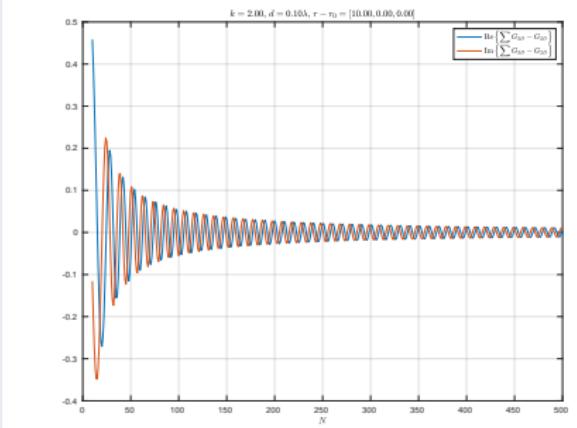
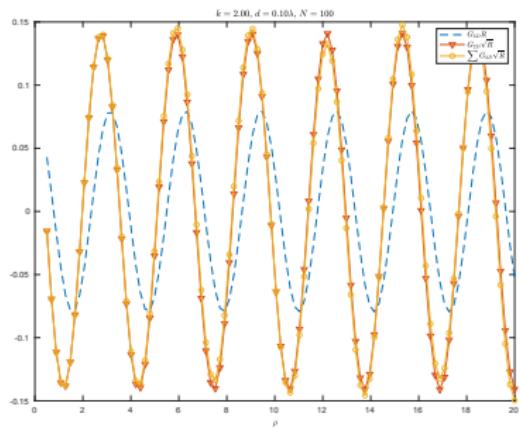
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Near Field (FE-IIEE loop)

Sanity Checks (MATLAB)

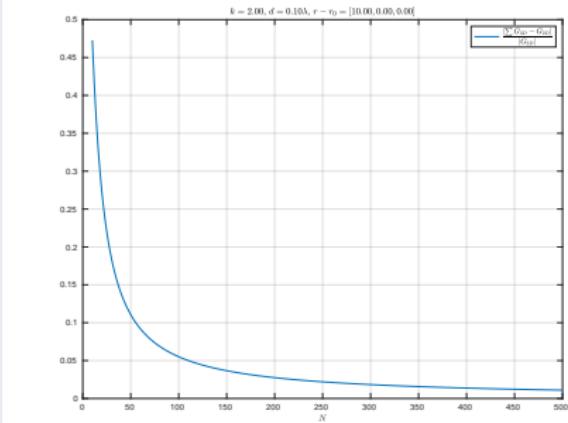
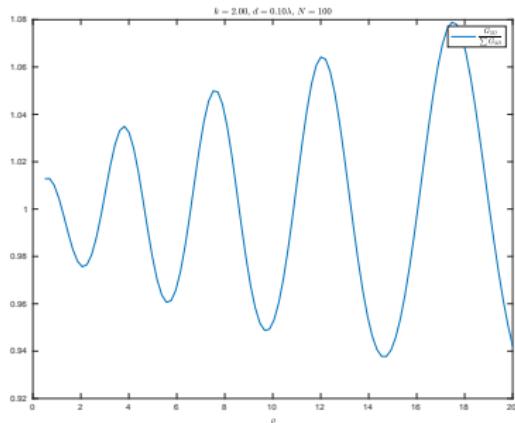
- Equivalence of infinite sum of 3D Green's function with 2D Green's function on the unit cell



Near Field (FE-IIEE loop) (cont.)

Sanity Checks (MATLAB)

Equivalence of infinite sum of 3D Green's function with 2D Green's function on the unit cell



Near Field (FE-IIEE loop) (cont.)

HOFEM Implementation

- Coded
- Tested

```
[#] EXECUTING IIEE TRUNCATION METHOD...
```

```
[#] CALCULATING SCATTERING FIELD...
```

```
[#] SCATTERING FIELD CALCULATED IN  
0.190 [sec]
```

```
[#] CALCULATING SCATTERING RHS...
```

```
[#] SCATTERING RHS CALCULATED IN  
0.014 [sec]
```

```
Iteration:  
1. (err 1.19E-02) 0.235 [sec]
```

```
[#] CALCULATING SCATTERING FIELD...
```

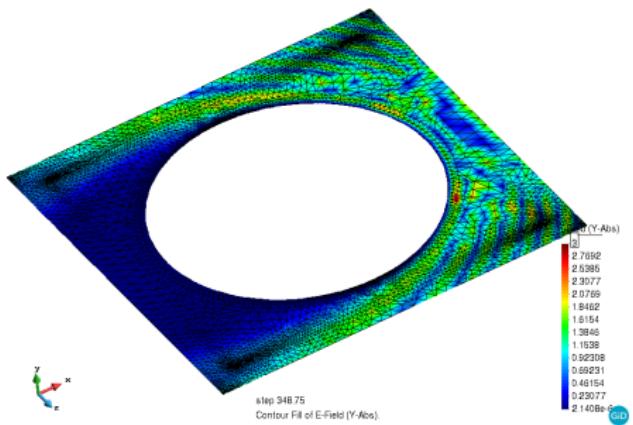
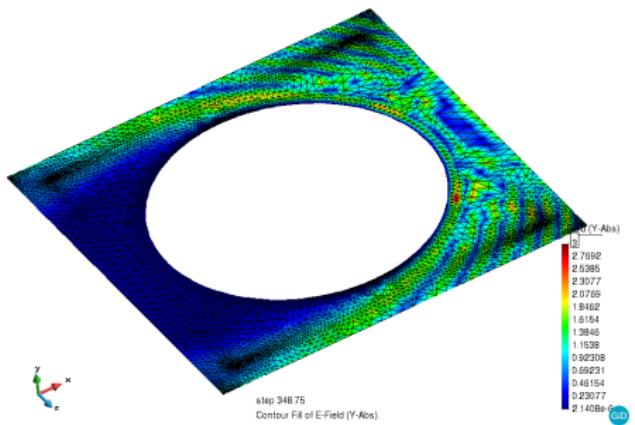
Near Field (FE-IIEE loop) (cont.)

Code output (terminal):

```
Iteration : 1. (err 1.19E-02)
Iteration : 2. (err 8.31E-05)
Iteration : 3. (err 7.23E-07)
Iteration : 4. (err 6.10E-09)
```

```
Iteration : 1. (err 1.50E-02)
Iteration : 2. (err 1.02E-04)
Iteration : 3. (err 8.28E-07)
Iteration : 4. (err 7.00E-09)
```

Near Field (FE-IIEE loop) (cont.)



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6 Modifications on Near Field Postprocessing

Far Field (postprocess)

Equivalence of Green's Functions for Far Field

- Can we use an infinite sum of 3D Green's far-field functions to model the 2D Green's far-field?
 - ▶ NO
 - ▶ and it makes sense!

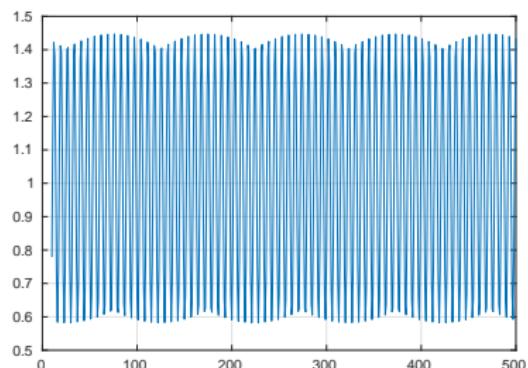
Far Field as Fourier Transform

The Fourier Transform of a constant current contribution along z is a delta function in the spatial frequency domain, i.e., variable θ :

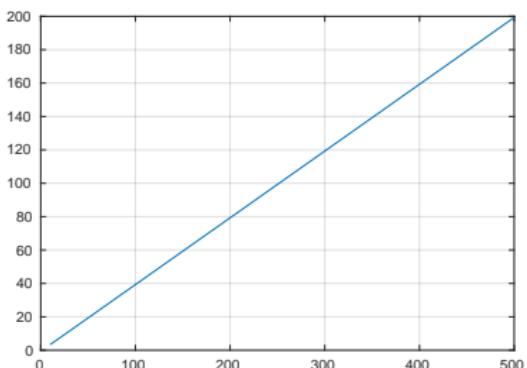
$$\text{Far Field}(\theta, \phi) = \delta(\theta - \pi/2) F(\phi) \quad (1)$$

Far Field (postprocess) (cont.)

$\theta \neq 90^\circ$: Oscillations



$\theta = 90^\circ$: Divergence



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 - Related issues

Rethinking . . .

AIRBUS: *hay un chico con nosotros que resuelve problemas de scattering de cilindros y no usa función de Hankel. Usa Green3D para calcular el campo (lejano) de scattering de una rodaja y le funciona.*

- Further study of differences between Green2D and Green3D
 - ▶ Obvious (after a maturation process) for far field
 - ▶ Not so obvious for near field (i.e., in its impact in FE-IIEE loop)

Far Field (postprocess)

Equivalence of Green's Functions for Far Field

- Can we use an infinite sum of 3D Green's far-field functions to model the 2D Green's far-field?
 - ▶ NO
 - ▶ and it makes sense!
 - ▶ No need of infinite sum (**far field Green3D/Green2D is enough**)
 - ★ Note that far field versions of Green3D (with $r = \rho$) and Green2D are equal up to a constant

Far Field as Fourier Transform

The Fourier Transform of a constant current contribution along z is a delta function in the spatial frequency domain, i.e., variable θ :

$$\text{Far Field}(\theta, \phi) = \delta(\theta - \pi/2) F(\phi) \quad (2)$$

Far Field (postprocess) (cont.)

Green2D vs Green3D

$F(\phi)$ is the same (after normalization) considering asymptotic expressions of Green3D and Green3D

$$H_0^{(2)}(k\rho) \underset{\rho \rightarrow \infty}{\approx} \sqrt{\frac{2j}{\pi k\rho}} e^{-jk\rho} \quad \frac{e^{-jkR}}{4\pi R} \underset{r \rightarrow \infty}{\approx} \frac{e^{-jkr}}{4\pi r} e^{jkr' \cos \psi}$$

Near Field (FE-IIEE loop)

Code output (terminal):

- From previous meeting

Green2D

```
Iteration : 1. (err 1.50E-02)
Iteration : 2. (err 1.02E-04)
Iteration : 3. (err 8.28E-07)
Iteration : 4. (err 7.00E-09)
```

Green3D

```
Iteration : 1. (err 1.19E-02)
Iteration : 2. (err 8.31E-05)
Iteration : 3. (err 7.23E-07)
Iteration : 4. (err 6.10E-09)
```

How can it work? Note we used Green3D itself (only one slide was considered)

Near Field (FE-IIEE loop) (cont.)

Code output (terminal):

- Large $S' - S$

Green2D

```
Iteration : 1. (err 1.50E-02)
Iteration : 2. (err 1.02E-04)
Iteration : 3. (err 8.28E-07)
Iteration : 4. (err 7.00E-09)
```

Green3D

```
Iteration : 1. (err 1.19E-02)
Iteration : 2. (err 8.31E-05)
Iteration : 3. (err 7.23E-07)
Iteration : 4. (err 6.10E-09)
```

- Small $S' - S$

Green2D

```
Iteration : 1. (err 5.16E-01)
Iteration : 2. (err 1.22E-01)
Iteration : 3. (err 2.53E-02)
Iteration : 4. (err 4.34E-03)
Iteration : 5. (err 6.86E-04)
Iteration : 6. (err 1.21E-04)
Iteration : 7. (err 2.46E-05)
Iteration : 8. (err 5.06E-06)
```

Green3D

```
Iteration : 1. (err 7.65E-02)
Iteration : 2. (err 6.08E-03)
Iteration : 3. (err 5.46E-04)
Iteration : 4. (err 5.05E-05)
Iteration : 5. (err 4.59E-06)
Iteration : 6. (err 4.24E-07)
Iteration : 7. (err 4.14E-08)
Iteration : 8. (err 4.13E-09)
```

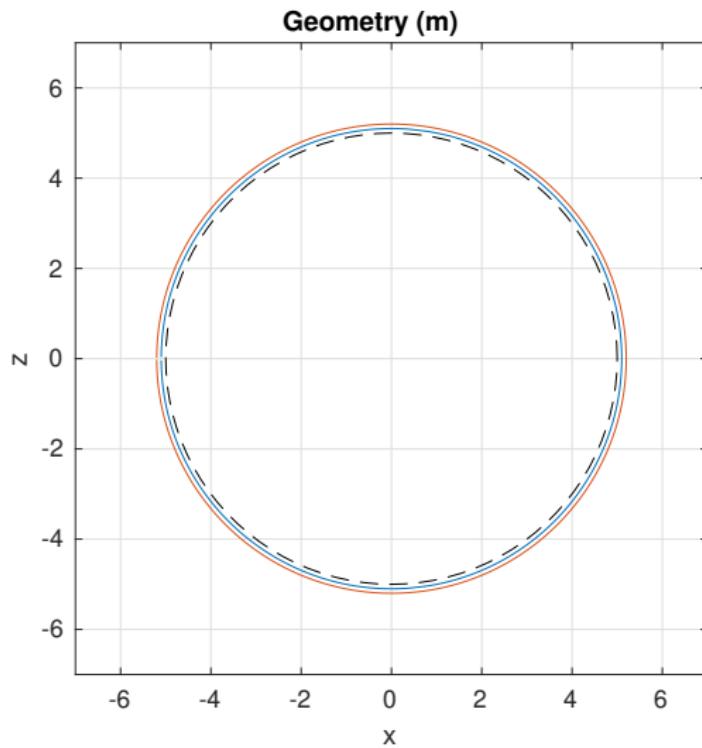
Green2D vs Green3D

Comparison with analytical solution

- Most results displayed correspond to TM and E field
- H field (i.e., RotE) identical conclusions
- By duality (satisfied by HOFEM) TE results “should” be identical (tested).
- Most results shown here correspond to both S' and S conformal to the cylinder (circular boundary). Analogous results/conclusions are obtained with rectangular boundaries for S' and S (and combinations of them).

Green2D vs Green3D (cont.)

Comparison with analytical solution



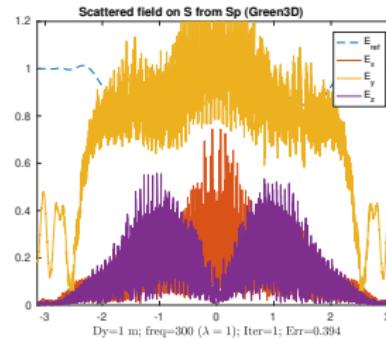
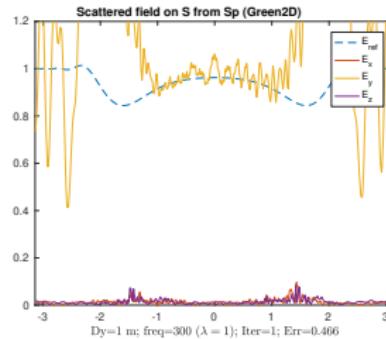
- 300 MHz
- Small $S - S'$
- Thick slice

Green2D vs Green3D (cont.)

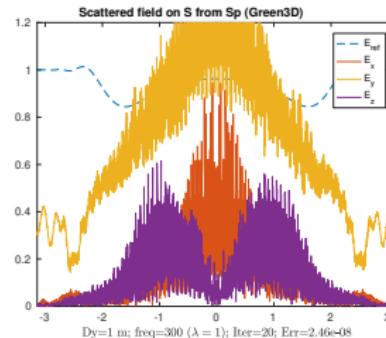
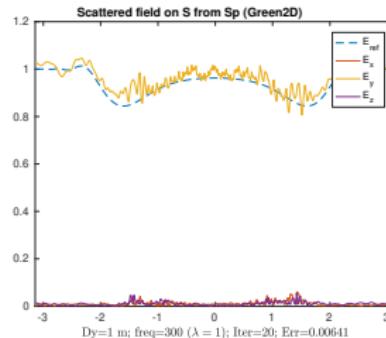
Comparison with analytical solution

Evolution scattered electric field (S' over S)

Iteration 1:



Iteration 20:

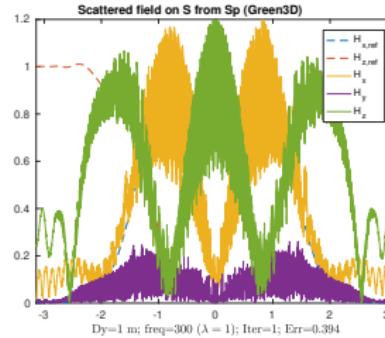
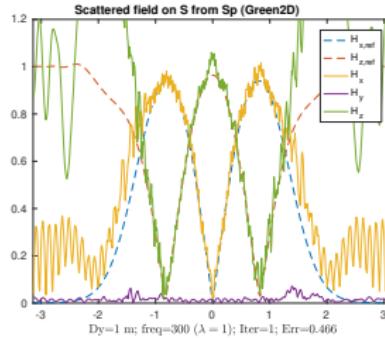


Green2D vs Green3D (cont.)

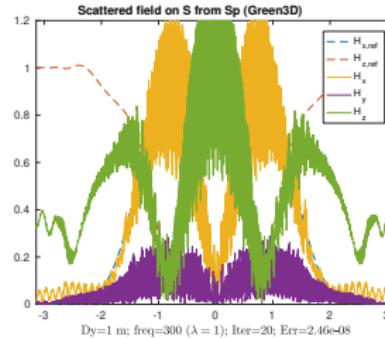
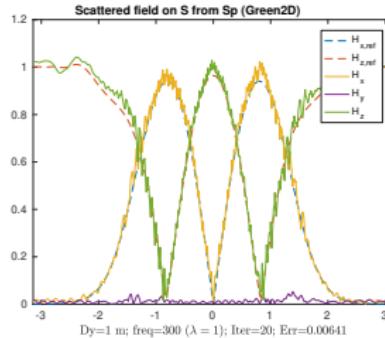
Comparison with analytical solution

Evolution scattered magnetic field (S' over S)

Iteration 1:



Iteration 20:

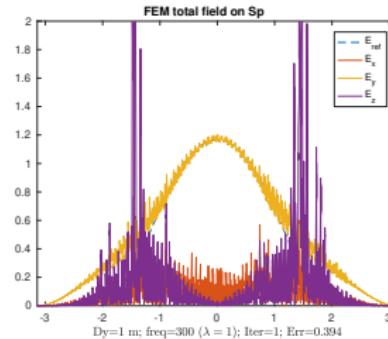
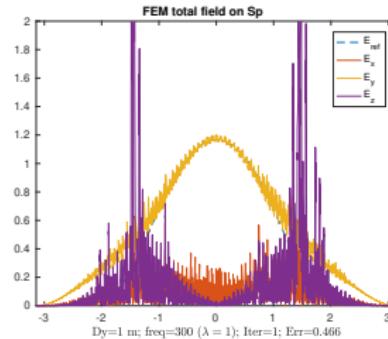


Green2D vs Green3D (cont.)

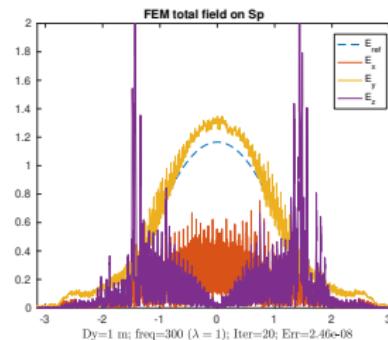
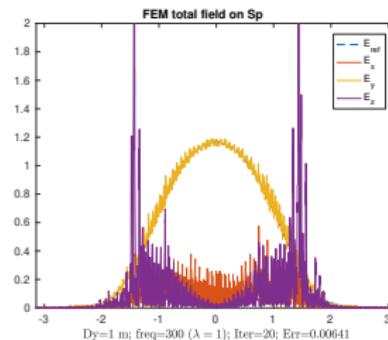
Comparison with analytical solution

Evolution electric field on S'

Iteration 1:



Iteration 20:



Green2D vs Green3D (cont.)

Comparison with analytical solution

- Higher error with Green3D
 - ▶ This is a case with small distance $S - S'$ and large thickness
 - ▶ Nevertheless, the error is always significantly higher than Green2D
- Green3D does not converge to right solution
- Components E_x, E_z, H_y are not null
 - (issue of (*) certainly added confusion on the debugging/verification of the code)
 - ▶ Much higher levels with Green3D
 - ▶ Green3D (the Green's function itself) generates non null E_x, E_z, H_y from E_z on S'
 - ▶ Green2D (the Green's function itself) does not generate any E_x, E_z, H_y
 - ★ Numerically, non-zero levels of E_x, E_z, H_y are generated because numerical FEM solution has non zero levels of E_x, E_z, H_y (tested!)
- Numerical noise always present due to discretization
 - ▶ Clearly visible in this case
 - ▶ Decreases with finer discretization —FEM mesh— (tested!)

(*) Issue of GiD/HOFEM-GUI representation of fields on surface

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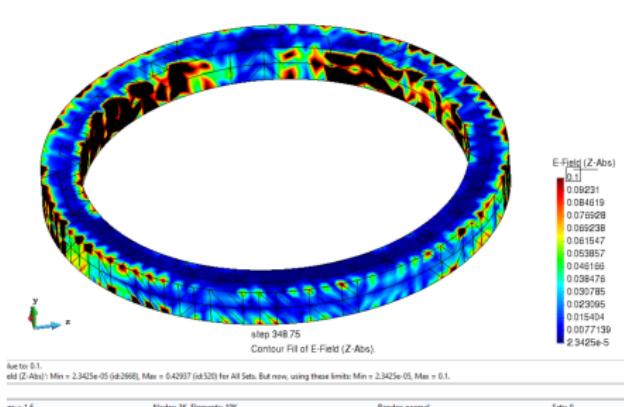
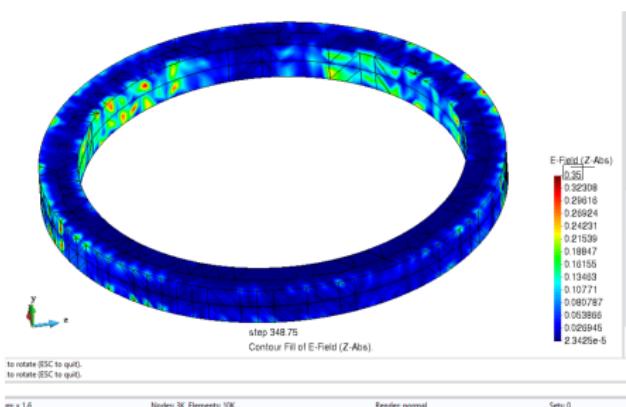
Rethinking . . .

(*) Issue of GiD/HOFEM-GUI representation of fields on surface

GiD/HOFEM-GUI Field Representation on Surfaces

Examples with PEC surfaces

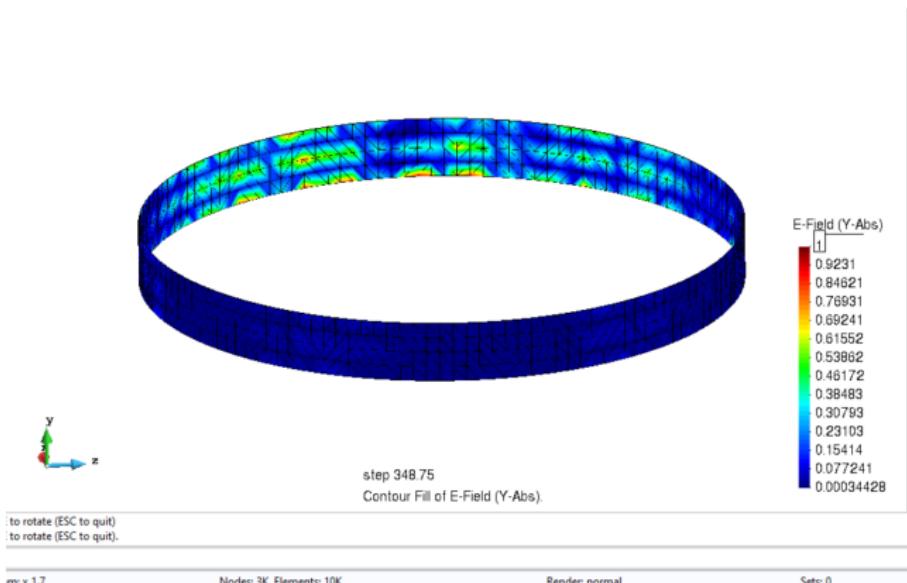
- E_z should be null on the caps (top and bottom $y = \text{cte}$)



GiD/HOFEM-GUI Field Representation on Surfaces (cont.)

Examples with PEC surfaces

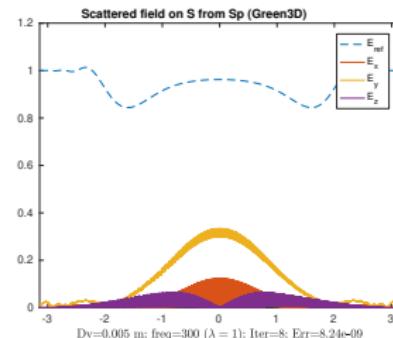
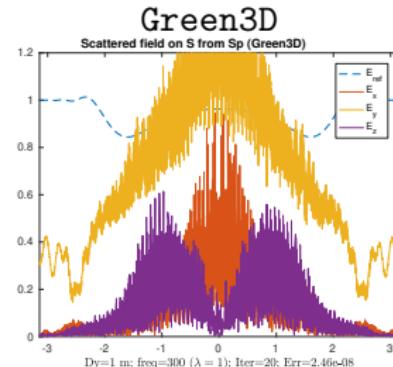
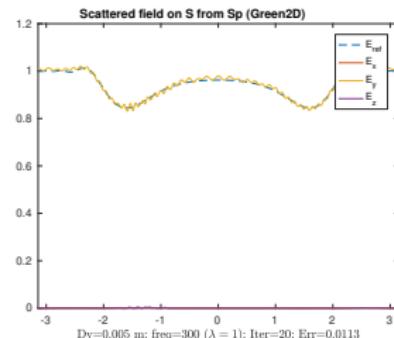
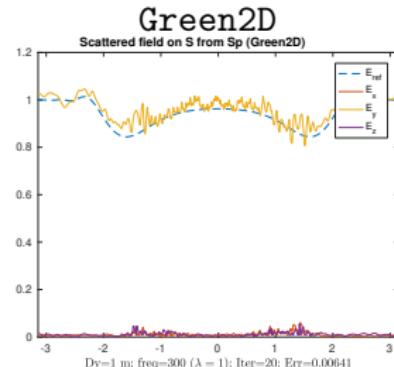
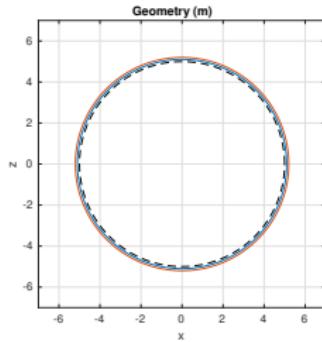
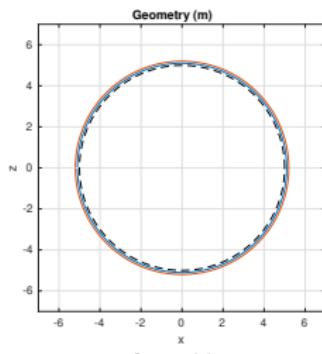
- E_y should be null on the cylinder “sides” (i.e., on the PEC cylinder)



$|E_y|$ (only PEC cylinder surface shown)

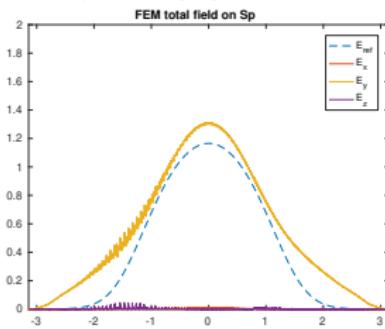
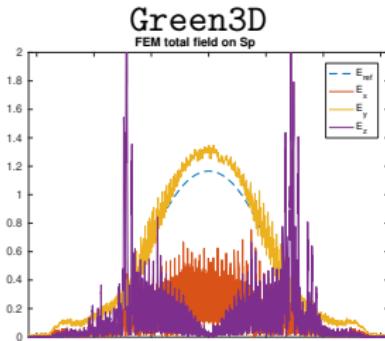
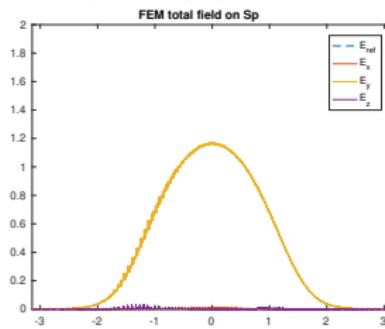
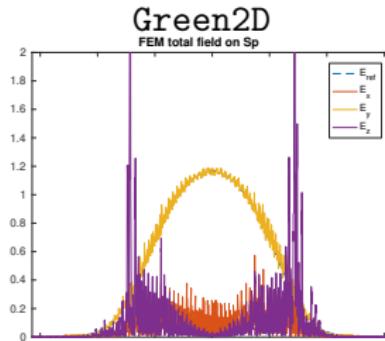
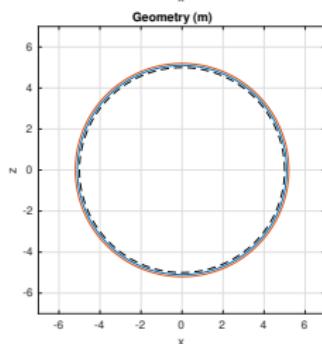
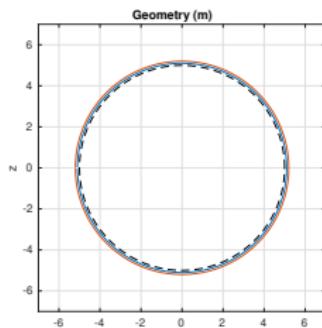
Effect of “Thickness”

Scattered near field —Note error in figure captions: thickness is 0.05λ for the thin slice—



Effect of “Thickness”

FEM solution —Note error in figure captions: thickness is 0.05λ for the thin slice—



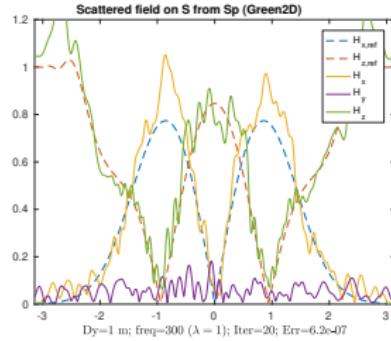
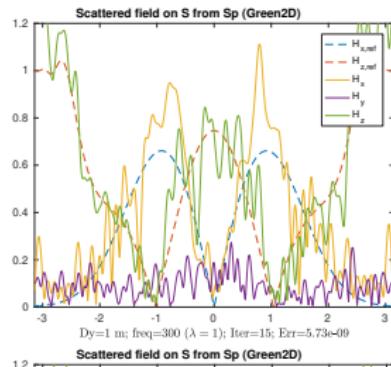
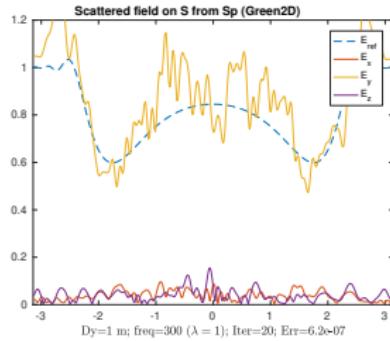
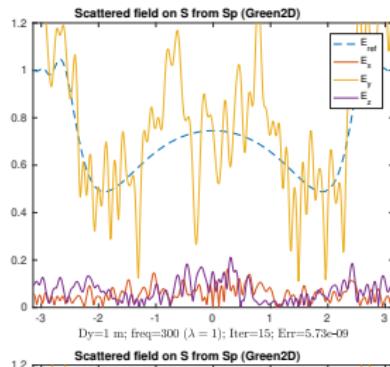
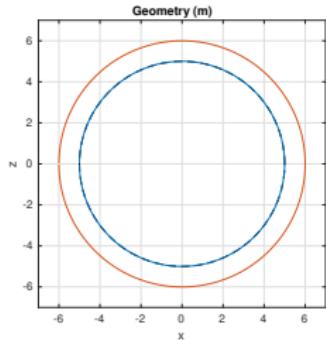
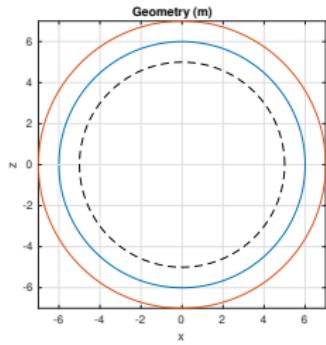
Effect of “Thickness” (cont.)

FEM solution —Note error in figure captions: thickness is 0.05λ for the thin slice—

- The thickness is the main factor for error with Green3D
- Green2D behaves great!
- Always lower error with thin slices

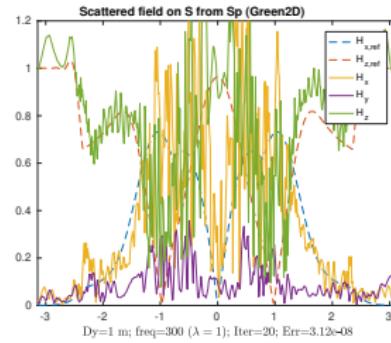
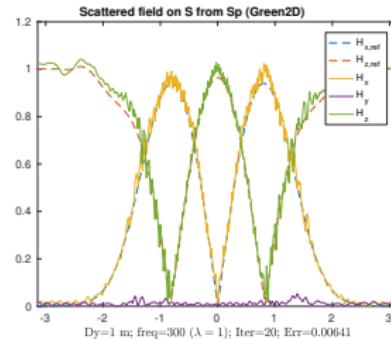
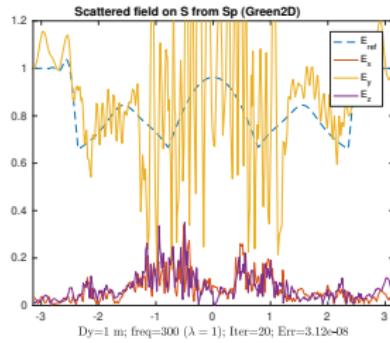
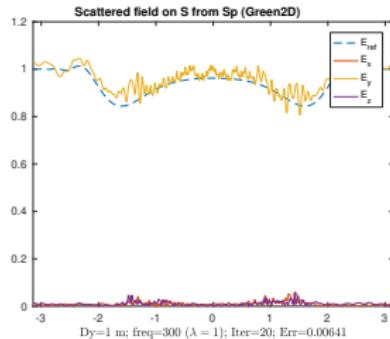
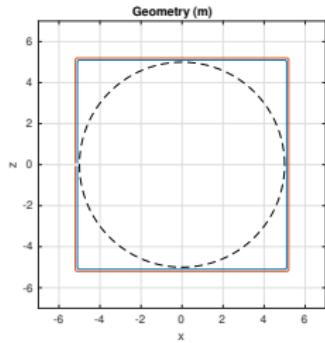
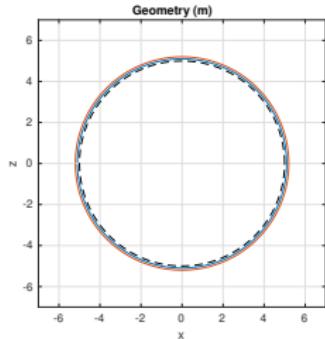
Other Effects (paranoic mode)

Effect of S' on PEC cylinder



Other Effects (paranoic mode)

Effect of S' , S Curved



Green3D vs Green2D

Conclusions

Conclusions

- Green3D itself not valid for 2D Emulation
 - ▶ FE-IIEE converges but
 - ★ Quality of solution far from great
 - ★ It may guide you to wrong solution
- Need to activate contributions of slice replicas along direction of cylinder (translation symmetry) **Green3D_Ewald1D**, Section 50

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4 Far Field Numerical Results

5 Oblique Incidence

- Green's Function
- Far Field
- Integration of EMULATION_2D and PBCs
- A note on ABC_PERIODIC boundary condition
- Numerical Results (oblique incidence)

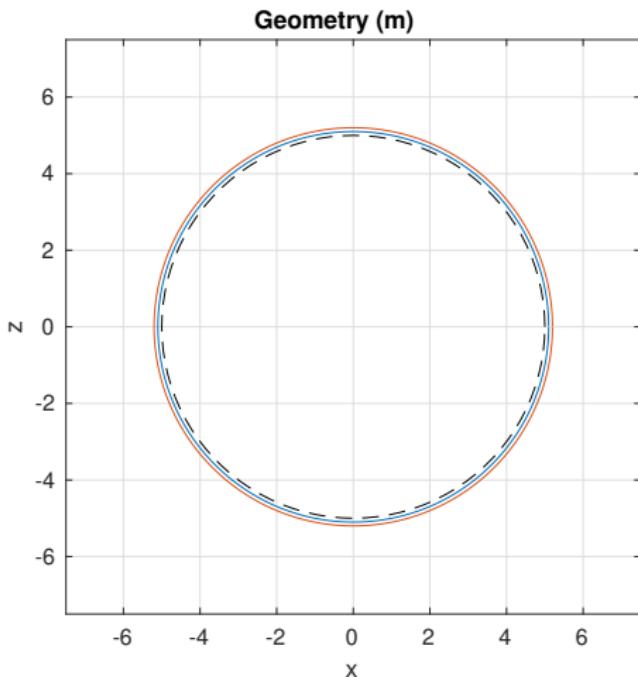
6 Modifications on Near Field Postprocessing

From now on we only use Green2D

- We check TE polarization for PEC cylinder
- We check for the dielectric coated cylinder

Check TE polarization

Comparison with TM results

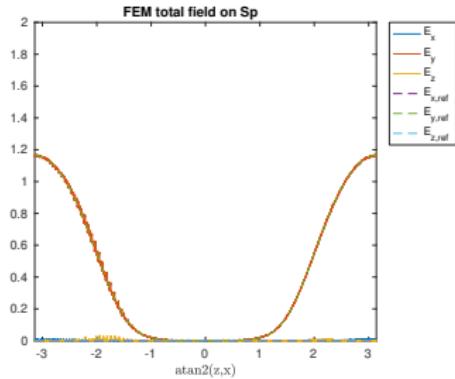


- Freq: 300 MHz. ($\lambda = 1 \text{ m}$)
- Thickness: 0.05 m

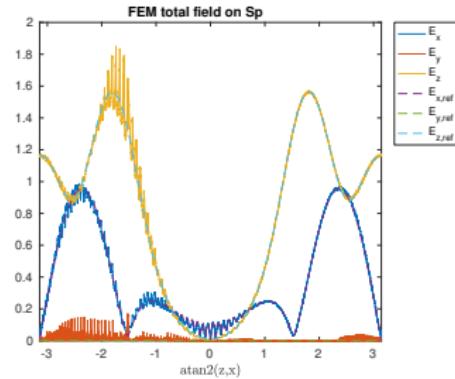
Check TE polarization (cont.)

Comparison with TM results

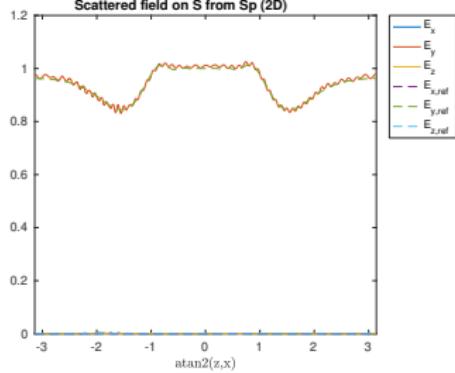
TM incident field



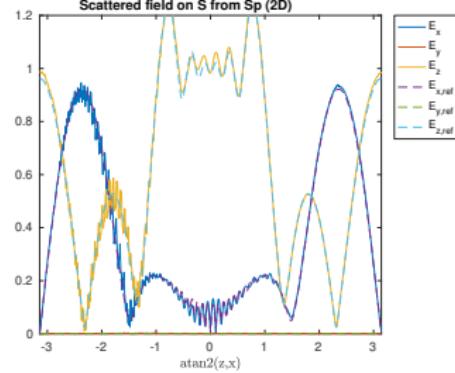
TE incident field



Scattered field on S from Sp (2D)



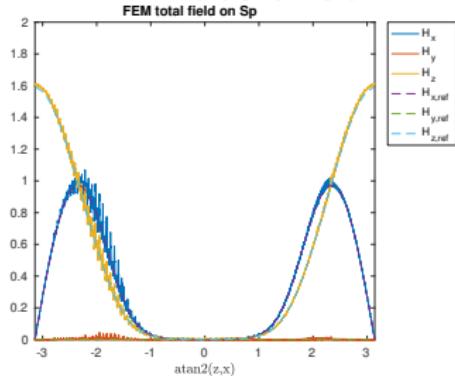
Scattered field on S from Sp (2D)



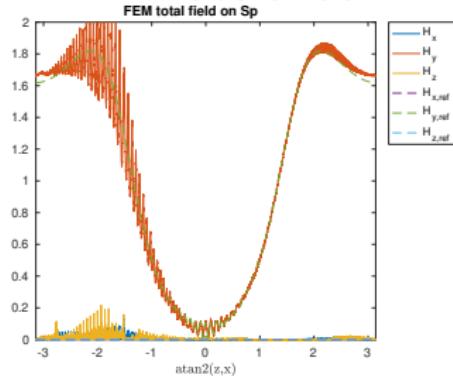
Check TE polarization (cont.)

Comparison with TM results

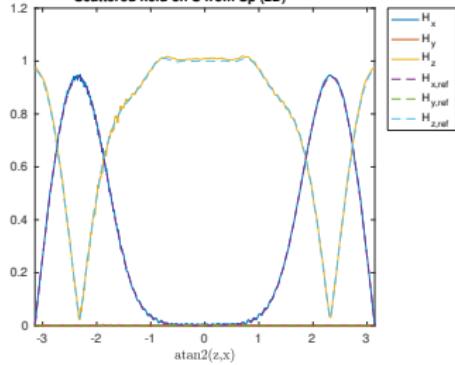
TM incident field



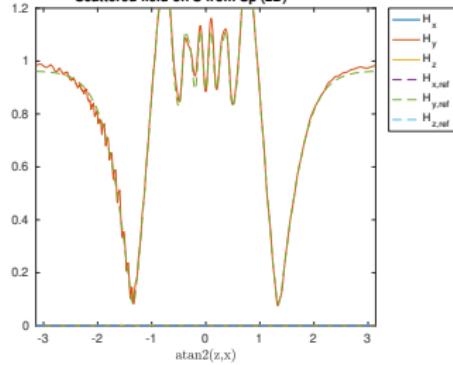
TE incident field



Scattered field on S from Sp (2D)

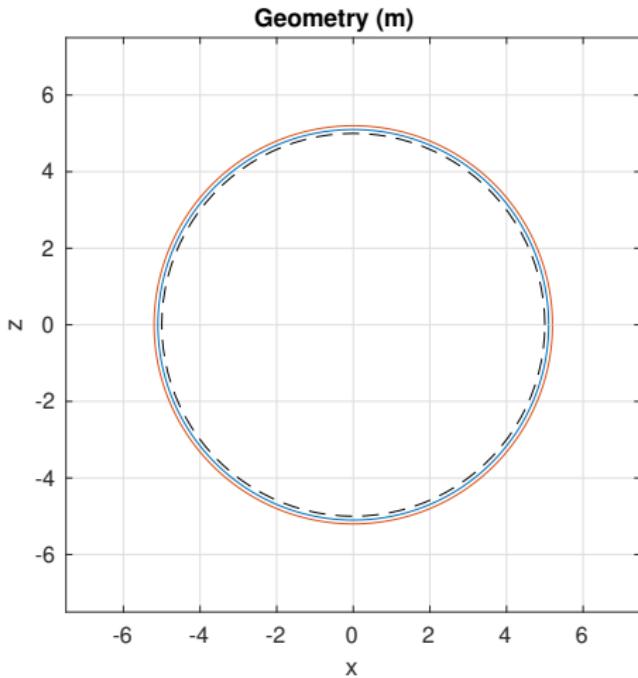


Scattered field on S from Sp (2D)



Dielectric Coated Cylinders

Comparison with the analytical solution

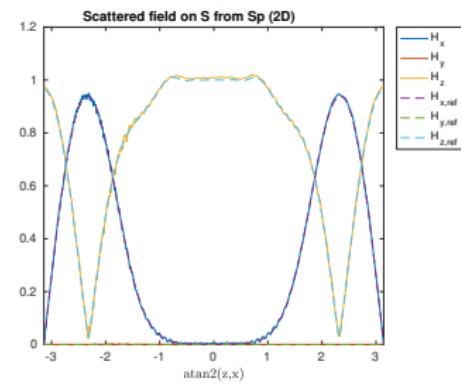
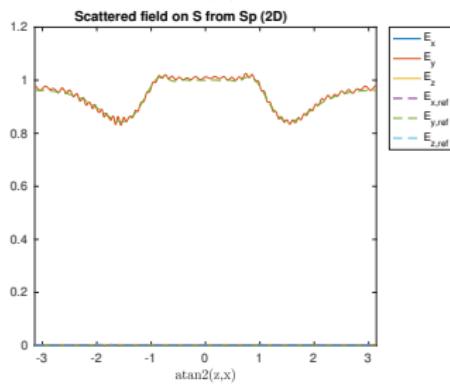
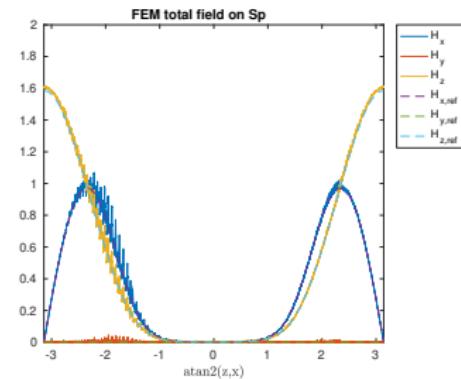
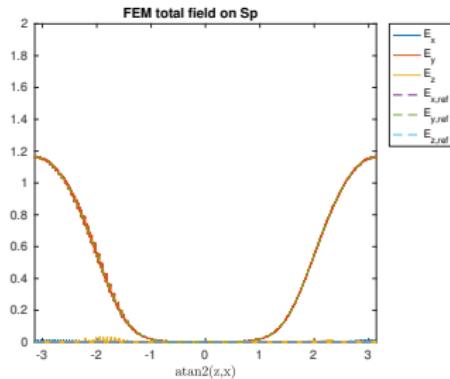


- Freq: 300 MHz. ($\lambda = 1 \text{ m}$)
- Thickness: 0.05 m
- Dielectric substrate between S and S' with relative permittivity ε_r .

Dielectric Coated Cylinders (cont.)

Comparison with the analytical solution

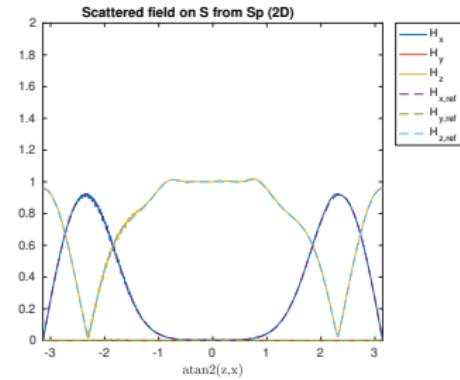
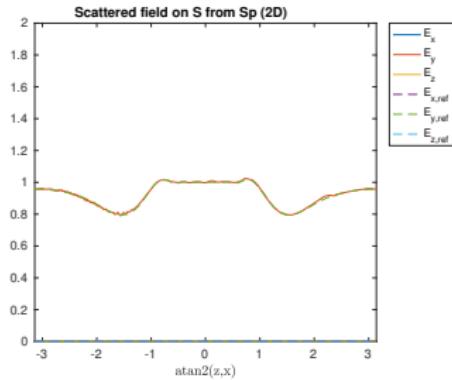
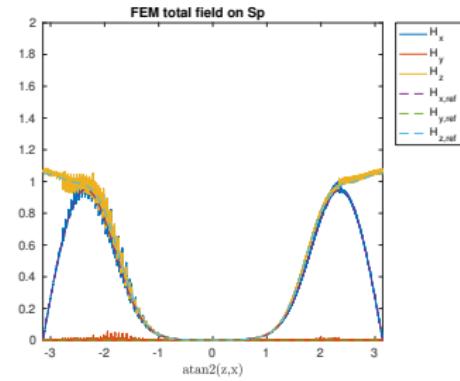
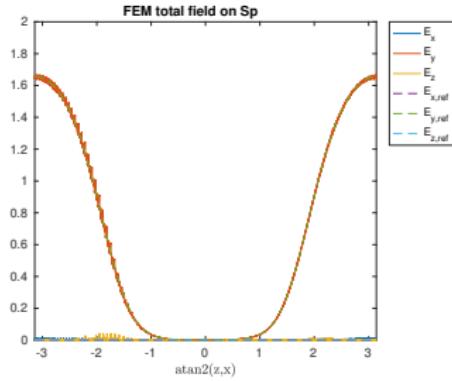
TM incident field $\varepsilon_r = 1$



Dielectric Coated Cylinders (cont.)

Comparison with the analytical solution

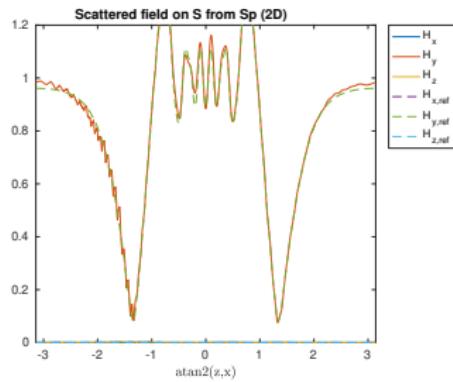
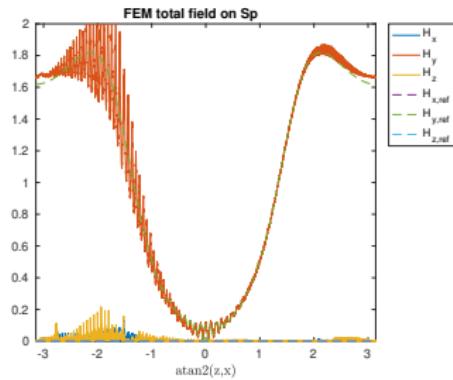
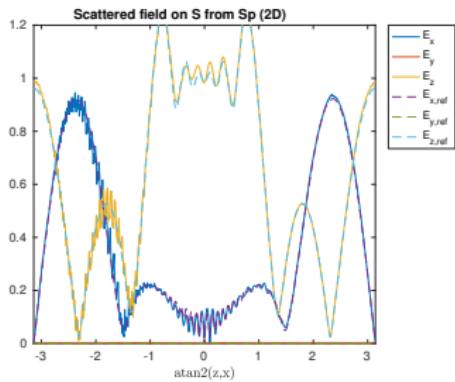
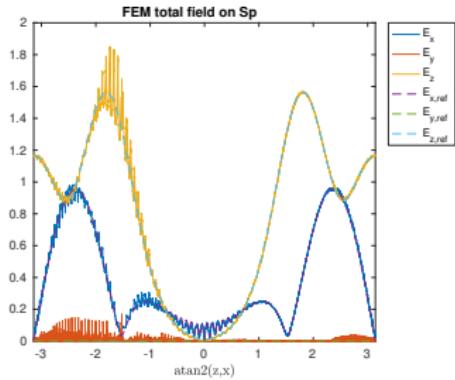
TM incident field $\epsilon_r = 4$



Dielectric Coated Cylinders (cont.)

Comparison with the analytical solution

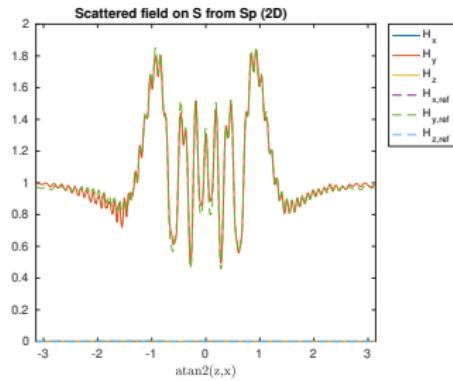
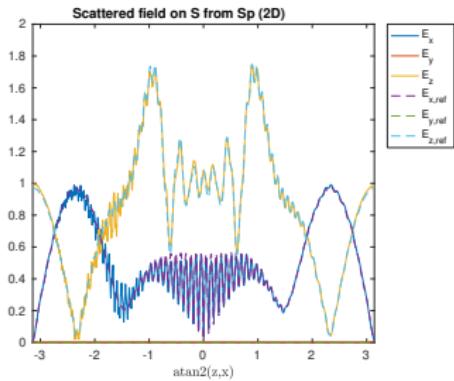
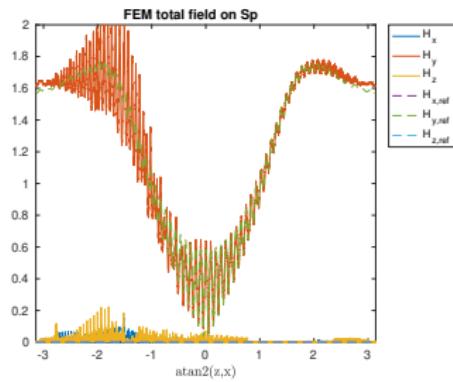
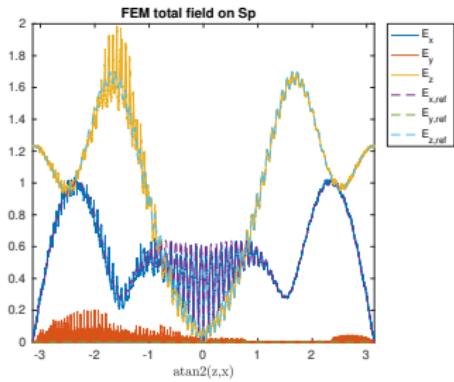
TE incident field $\varepsilon_r = 1$



Dielectric Coated Cylinders (cont.)

Comparison with the analytical solution

TE incident field $\epsilon_r = 1.5$



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Outline (cont.)

- Numerical Results (oblique incidence)

6 Modifications on Near Field Postprocessing

7 MPI related issues

Details on Ewald (1D periodicity)

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Green3D_Ewald1D

Ewald Method in HOFEM

where s is a complex variable. The periodic Green's function can be written in two parts by using the previous identity and splitting the path integration at the parameter \mathbf{E} as

$$G_p(\mathbf{r}, \mathbf{r}_s) = G_{p1}(\mathbf{r}, \mathbf{r}_s) + G_{p2}(\mathbf{r}, \mathbf{r}_s) \quad (5.41)$$

where $G_{p1}(\mathbf{r}, \mathbf{r}_s)$ is given by

$$\begin{aligned} G_{p1}(\mathbf{r}, \mathbf{r}_s) &= \frac{1}{4\pi} \sum_{m=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} e^{-j(k_x m D_x + k_y n D_y)} \\ &\quad \times \frac{2}{\sqrt{\pi}} \int_0^{\mathbf{E}} e^{\left(-R_{mn}^2 s^2 + \frac{k_0^2}{4s^2}\right)} ds \end{aligned} \quad (5.42)$$

and $G_{p2}(\mathbf{r}, \mathbf{r}_s)$ is given by

$$\begin{aligned} G_{p2}(\mathbf{r}, \mathbf{r}_s) &= \frac{1}{4\pi} \sum_{m=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} e^{-j(k_x m D_x + k_y n D_y)} \\ &\quad \times \frac{2}{\sqrt{\pi}} \int_{\mathbf{E}}^{\infty} e^{\left(-R_{mn}^2 s^2 + \frac{k_0^2}{4s^2}\right)} ds \end{aligned} \quad (5.43)$$

```
!Distancia de la celda unidad en X
Dx = &
      SQRT(DOT_PRODUCT(PBC_structure%offset_vector(1),
!Distancia de la celda unidad en Y
Dy = &
      SQRT(DOT_PRODUCT(PBC_structure%offset_vector(2),
E = SQRT(PI/Dx/Dy)

!Sum using Ewald transformation
DO m=-2,2
  DO n=-2,2
    !Calcular alpha_mn
    alpha_mn = SQRT(CMPLX((PI*m/Dx)**2 + &
                           (PI*n/Dy)**2 + (PI*m/Dx)*Kx + &
                           (PI*n/Dy)*Ky + &
                           (1.0_DBL/4.0_DBL)*(Kx**2+Ky**2-K**2),0.0_DBL))
```

Ewald 1D periodicity

- Naively we thought it was simply setting either $m = 0$ or $n = 0$
- **But it is NOT ... see next slide on Ewald 1D**

Ewald sum

- Technique for summing contribution from an infinite set of sources (in this case along z axis):

$$\sum_n G(R_n) = \frac{1}{4\pi} \sum_n e^{-j(k \cos \theta)nd} \frac{e^{-jkR_n}}{R_n}$$

where $R_n = \sqrt{(x - x')^2 + (y - y')^2 + (z - z' + nd)^2}$, θ is elevation angle.

- The Green function is decomposed in two terms:

$$\sum_n G(R_n) = \sum_n G_1(R_n) + \sum_n G_2(R_n)$$

- ▶ One of them decays quickly with R_n : $|G_2(R_{n+1})| \ll |G_2(R_n)|$
- ▶ For the other one the Poisson summation formula is applied:

$$\sum_n G_1(R_n) = \sum_n \hat{G}_1(k_n)$$

where $\hat{G}_1(k)$ is the Fourier transform of $G_1(R)$ ¹.

¹ $\hat{G}_1(k)$ is narrow in k because $G_1(R)$ is wide in R

1D from 2D periodicity Ewald sum

- No problem with *spatial* term:

$$\sum_m \sum_n G_2(R_{n,m}) \rightarrow \sum_n G_2(R_{n,0})$$

- But the *spectral* term...

$$\sum_m \sum_n \hat{G}_1(k_{n,m}) \rightarrow ??$$

The Fourier Transform of $G_1(n, 0)$ must be computed from scratch:

$$\hat{G}_{1,n} = \frac{e^{j(z-z')(k_z - 2\pi \frac{n}{d})}}{2\pi d} g\left(\frac{\alpha_n^2}{4E^2}, \rho^2 E^2\right)$$

$$\rho^2 = (x - x')^2 + (y - y')^2 \quad \alpha_n^2 = \left(k \cos \theta + \frac{2\pi n}{d}\right)^2 - k^2$$

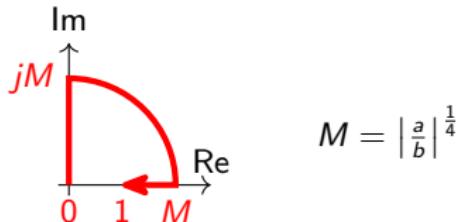
1D from 2D periodicity Ewald sum (cont.)

where we need the following numerical integration

$$g(a, b) = \int_0^1 \frac{e^{-\frac{a}{z^2} - bz^2}}{z} dz$$

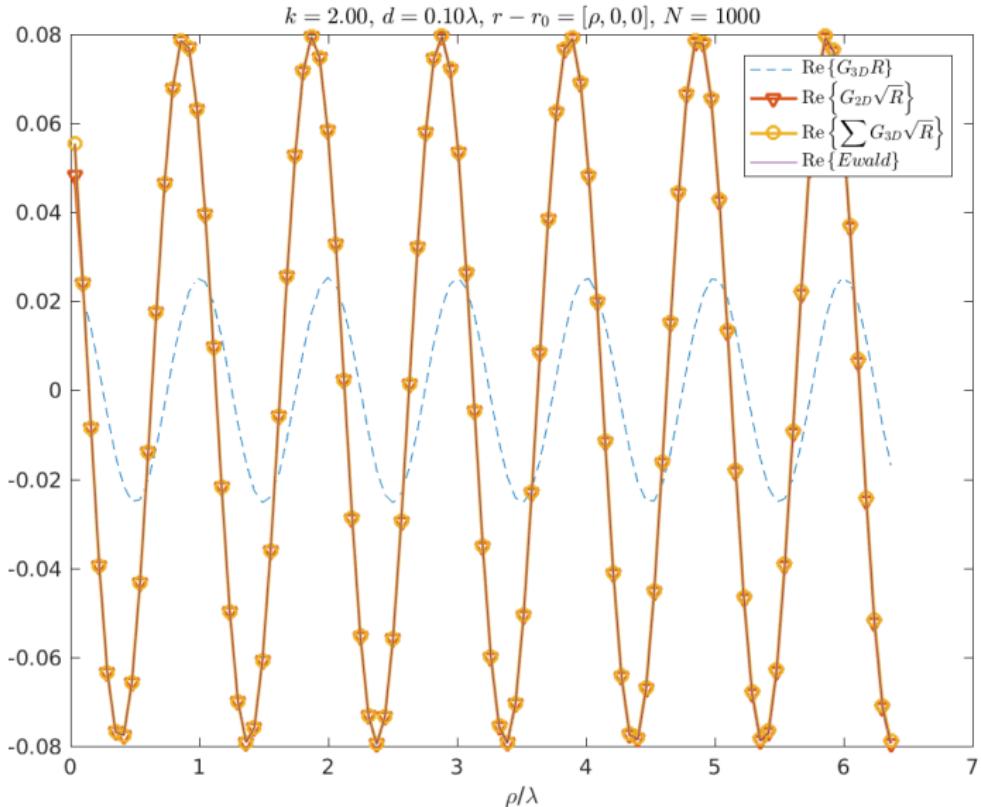
Notes about $g(a,b)$

- It is a complex integral whose value (and convergence) depends on the chosen path.
- For calculating $\hat{G}_{1,n}$:
 - ▶ $a, b \in \mathbb{R}$
 - ▶ $b > 0$,
 - ▶ but a is negative for the first n values (At each n term in the sum $a = \alpha_n^2/4E^2$).
- If $a > 0$, the integral can be done through real axis.
- If $a < 0$, the integral must be done through the following path:

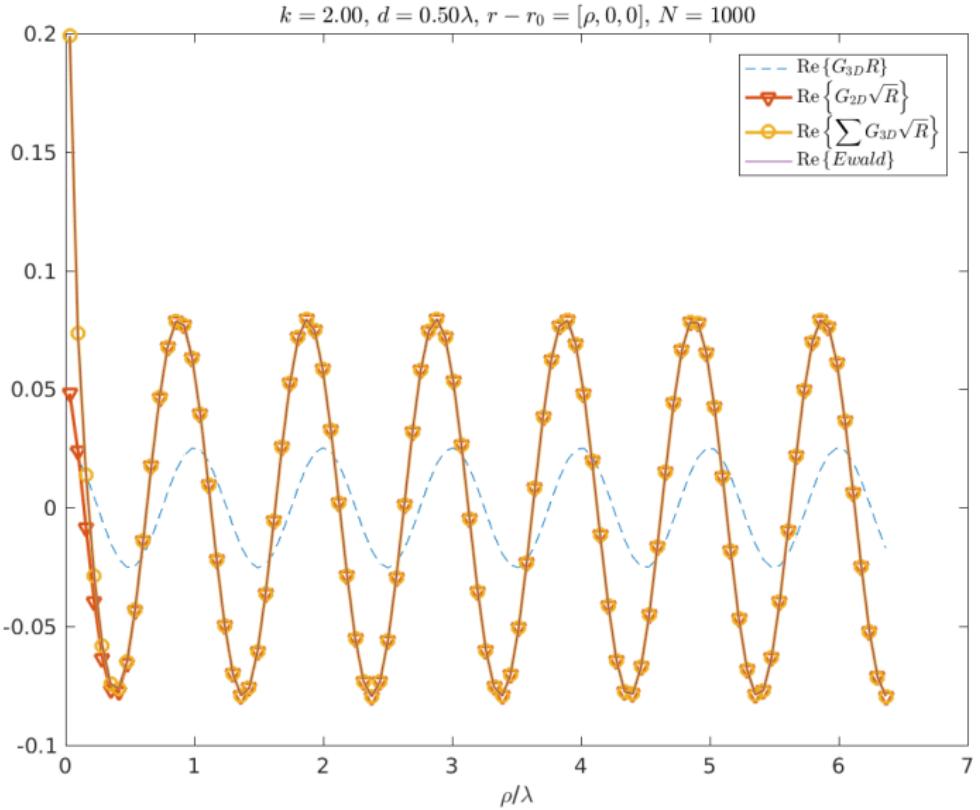


- If $a = 0$, integral does not converge. It happens for specific values of k and d (not a problem: Greens function is singular there).

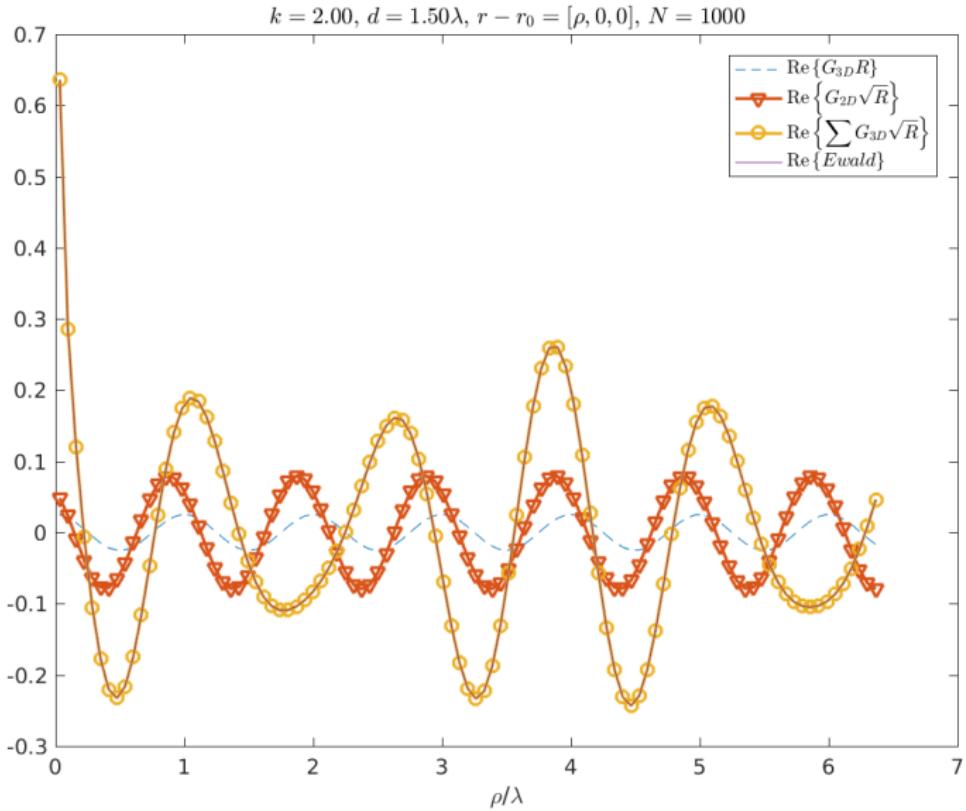
Checking results (thin slice)



Checking results (medium slice)

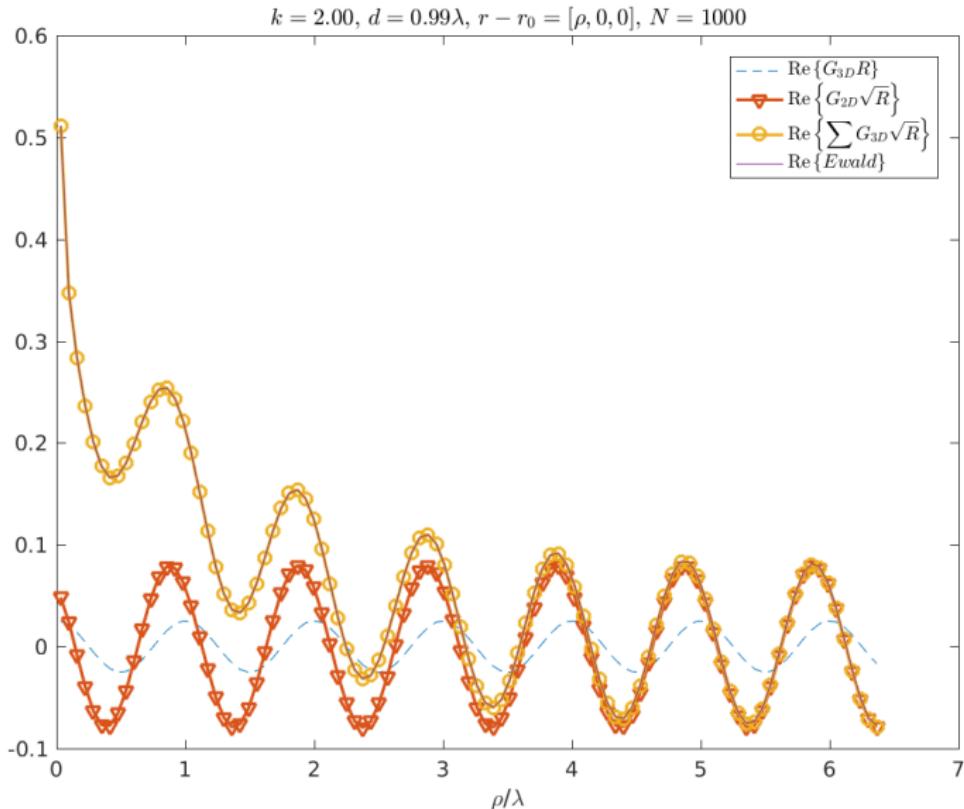


Checking results (thick slice)



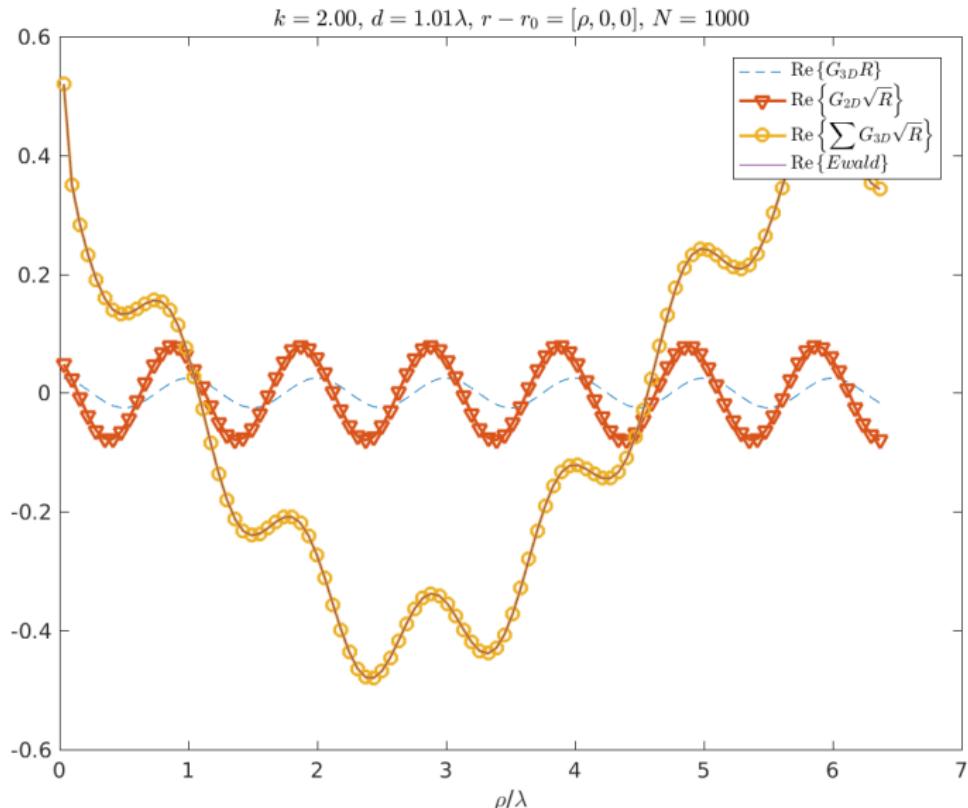
Checking results (close to transverse Floquet resonance)

$$\alpha_0^2 \simeq 0$$

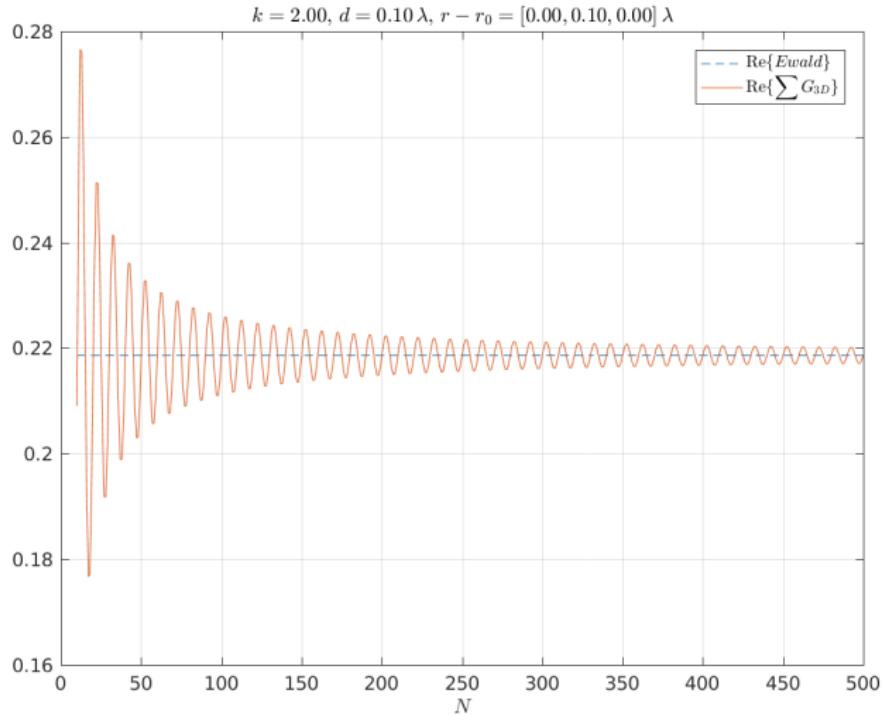


Checking results (close to transverse Floquet resonance)

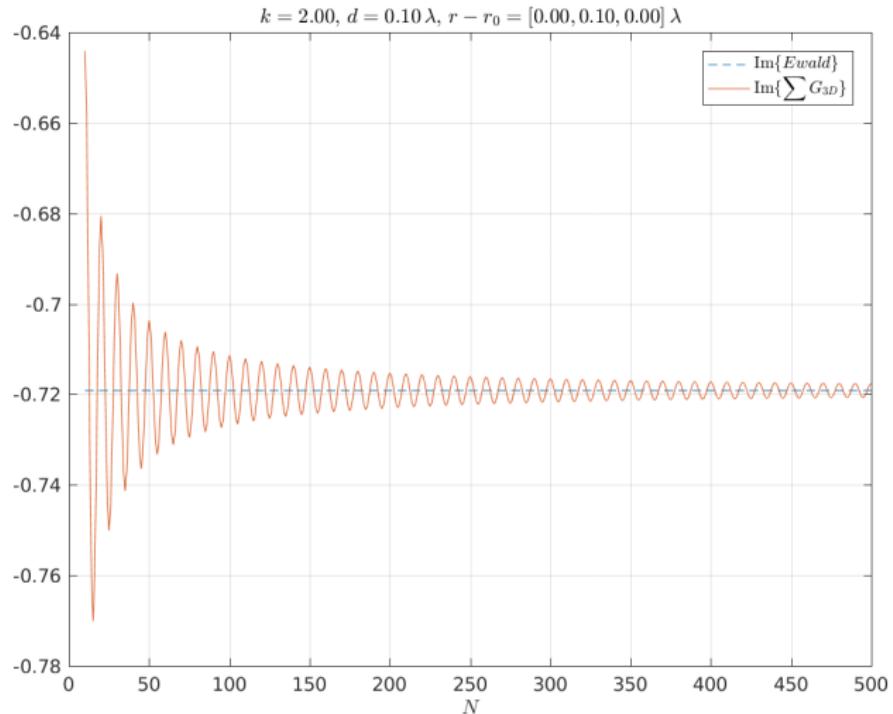
$$\alpha_0^2 \simeq 0$$



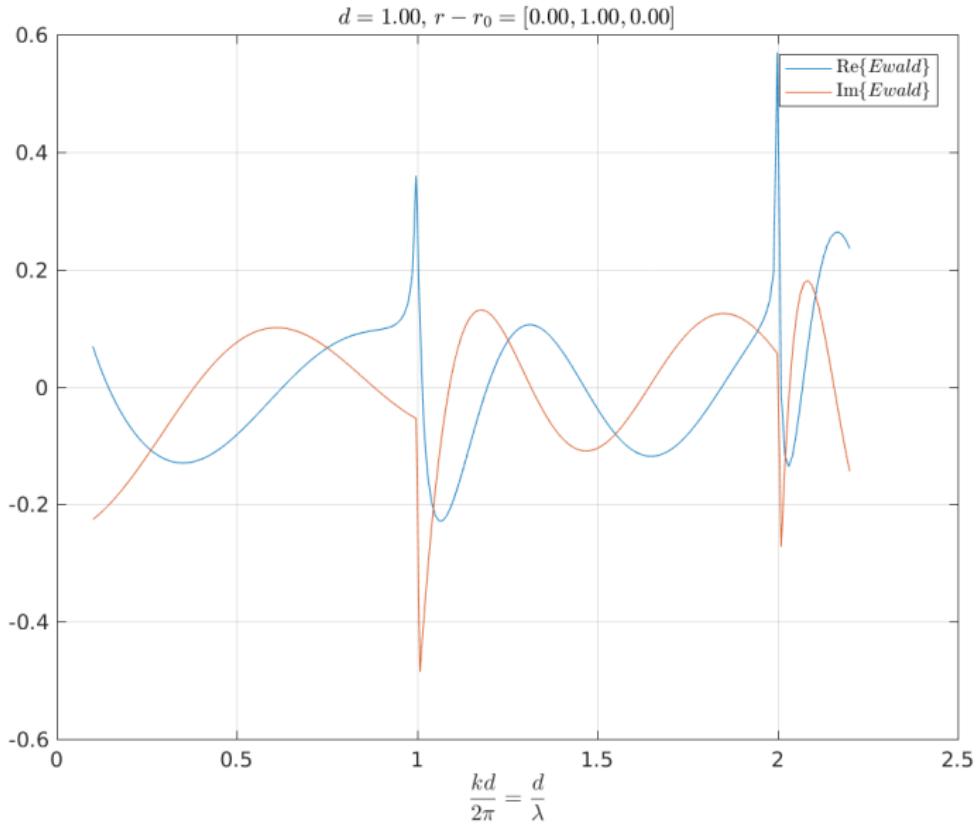
Convergence of the direct sum



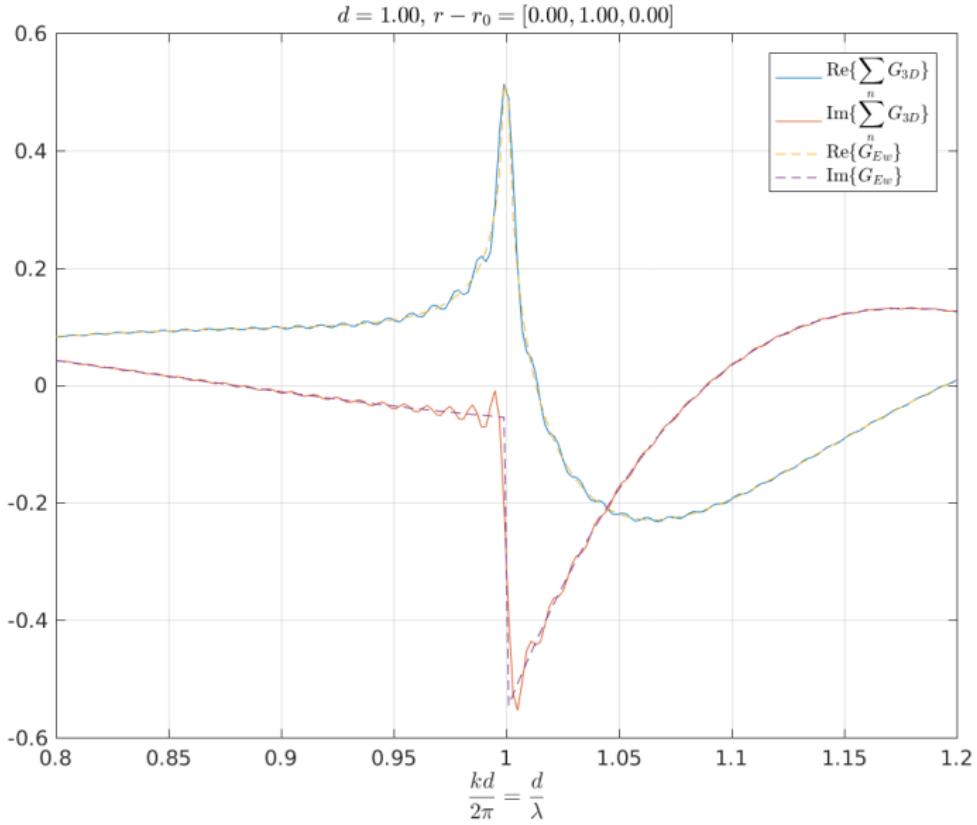
Convergence of the direct sum (cont.)



Dependence with frequency



Singularities when $\alpha_n^2 \rightarrow 0$



Additional notes

- CPU time cost similar to sum 100 terms of G_{3D} .
- Matlab prototype.
- Numerical integral may be improved using classic algorithms for calculate exponential integrals (see ² and ³) **Done!**: Calculation 10 times faster, but inestable for large values of ρ ($\rho > d$)
- Checked:

$$\int_{-\frac{d}{2}}^{\frac{d}{2}} G_{3D}(\rho, z) dz = G_{2D}(\rho)$$

where G_{3D} is numerically evaluated with Ewald, and G_{2D} is the Hankel function: $\frac{1}{4j} H_0^{(2)}(k|\rho|)$.

²F. Capolino *et al.*, "Efficient Computation of the 2-D Green's Function for 1-D Periodic Structures Using the Ewald Method", *IEEE-TAP*, 2005. Equation (23).

³F. Capolino *et al.*, "Efficient Computation of the 3D Green's Function with One Dimensional Periodicity Using the Ewald Method", *IEEE-APS*, 2006.

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Fortran Module

Ewald1D_Green_module.F90

```
MODULE Ewald1D_Green_module

!> This module contains functions for evaluation different versions
!> of the Green function.

USE program_global_variables, ONLY : DBL, PI, ZERO, ONE
USE program_global_variables, ONLY : HOFEM_LENGTH => LENGTH
USE program_global_variables, ONLY : MYEPS, MYEPS1, MYEPS2, MYEPS3, MYEPS6
USE iso_fortran_env, ONLY : UNIT_OUT => OUTPUT_UNIT
USE iso_fortran_env, ONLY : UNIT_ERROR => error_unit
USE quadpack_double, ONLY : dqag, dqags, dqng, dlobatto
USE specfun_module, ONLY : vdExpIntP, dExpIntP, faddeeva_erfc
USE specfun_module, ONLY : StruveH0 => STRVH0, StruveH1 => STRVH1

!> IMPORTANT: Numerical stability concerns.

PRIVATE
PUBLIC :: g_integral_Ep, g_integral_IN, g_integral
PUBLIC :: G1k_ewald, G2k_ewald
PUBLIC :: Ewald1D_Green_function
```

Ewald1D_Green_function

```
SUBROUTINE Ewald1D_Green_function &
    (K, Kz, rrp, slice_thickness, cylinder_axis, &
     G, dG, ddG)

    ! PARAMETERS
    REAL(KIND=DBL), PARAMETER :: RTOL = MYEPS2
    REAL(KIND=DBL), PARAMETER :: TOL = MYEPS

    ! INPUT:
    ! K: wavenumber
    ! Kz: transversal wavenumber to cylinder axis.
    !      Kz=cos(theta). Kz=0 for normal incidence
    ! rrp: vector r-r' in global coordinates
    REAL(KIND=DBL), INTENT(IN) :: rrp(3), K, Kz
    REAL(KIND=DBL), INTENT(IN) :: slice_thickness
    REAL(KIND=DBL), DIMENSION(3), INTENT(IN) :: cylinder_axis

    ! OUTPUT: complex green function value and derivatives
    COMPLEX(KIND=DBL), INTENT(OUT) :: G
    COMPLEX(KIND=DBL), INTENT(OUT) :: dG(3)
    COMPLEX(KIND=DBL), INTENT(OUT) :: ddG(3,3)
```

Ewald1D_Green_function (cont.)

Calculate:

$$G_{p1D}(x_1, x_2, x_3) = \sum_n G(R_n) = \sum_n \hat{G}_1(k_n) + \sum_n G_2(R_n)$$

where $(x_1, x_2, x_3) = \mathbf{r} - \mathbf{r}'$, and their derivatives:

$$\frac{\partial G_{p1D}}{\partial x_i} \quad \frac{\partial^2 G_{p1D}}{\partial x_i \partial x_j}$$

- Arbitrary periodicity axis (cylinder_axis)
- Sum convergence criteria defined by parameters:
 - ▶ Relative: RTOL=MYEPS2
 - ▶ Absolute: TOL=MYEPS2, tolabs=TOL*abs(G)
- where G is the value of the 2D Green function (Hankel function)
- Ewald separation constant: E=sqrt(PI)/slice_thickness
 - ▶ It is the recommended value by different authors (may not be the optimum)

G2k_ewald

Spatial sum element

```
SUBROUTINE G2k_ewald(rrp, K, E, &
    G2, dG2xyz, ddG2xyz)

    ! INPUT
    ! rrp: vector r - (r' + n*slice_thickness*cylinder_axis)
    ! E: Separation constant in Ewald sum
    real(DBL), intent(in) :: rrp(3), K, E

    ! OUTPUT
    real(DBL), intent(out) :: G2, dG2xyz(3), ddG2xyz(3,3)
```

Calculate a term of the spatial sum: $G_2(R_n)$

- Complex erfc function calculated from Faddeeva function
 - ▶ Algorithm ACM TOMS 680 (module specfun_module.F90)
 - ▶ Same algorithm that is used in Ewald 2D
 - ▶ faddeeva_erfc defined in specfun_module.F90

G1k_ewald

```
SUBROUTINE G1k_ewald(rho2, Az, vrho, K, Kz, floquet, &
    E, cylinder_axis, tolrel, tolabs, &
    G1, dG1xyz, ddG1xyz)

! INPUT
! Az: dot_product(r - r', cylinder_axis)
! vrho: r - r' - Az*cylinder_axis
! rho2: dot_product(vrho, vrho)
! floquet: floquet wavenumber (2*Pi/slice_thickness*n)
! E: Separation constant in Ewald sum
real(DBL), intent(in) :: rho2, Az, vrho(3)
real(DBL), intent(in) :: K, Kz, floquet
real(DBL), intent(in) :: E, cyl_axis(3)
real(DBL), intent(in) :: tolrel, tolabs
! OUTPUT
complex(DBL), intent(out) :: G1, dG1xyz(3), ddG1xyz(3,3)

[...]
flokz = floquet + kz
alpha2 = (flokz**2 - k**2)/4.0_db1
a = alpha2/E**2
b = rho2*E**2
call g_integral(a, b, 1, P, tolrel, tolabs, err)
call g_integral(a, b, -1, dP, tolrel, tolabs, derr)
call g_integral(a, b, -3, ddP, tolrel, tolabs, dderr)
```

G1k_ewald (cont.)

Calculate a term of the spatial sum: $\hat{G}_1(k_n)$

- It needs the following complex integral:

$$g(a, b, m) = \int_0^1 \frac{e^{-\frac{a}{z^2} - bz^2}}{z^m} dz$$

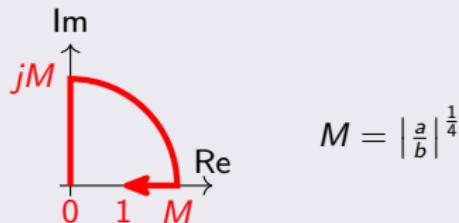
where

- $a \in \mathbb{R}$, $b \in \mathbb{R}^+$
- $m \in \{1, -1, -3\}$

$$a > 0$$



$$a < 0$$



$$M = \left| \frac{a}{b} \right|^{\frac{1}{4}}$$

NOTE: If m is even, the integral can be evaluated with the erfc function (Ewald2D case)

g_integral

```
SUBROUTINE g_integral(a, b, m, g, tolrel, tolabs, outerr, used_routine)

REAL(kind=DBL), PARAMETER :: EPS=MYEPS

! INPUT
REAL(kind=DBL), INTENT(in) :: a, b
INTEGER, INTENT(in) :: m
REAL(kind=DBL), INTENT(IN) :: tolrel, tolabs
! OUTPUT
COMPLEX(kind=DBL), INTENT(OUT) :: g
REAL(kind=DBL), INTENT(OUT), OPTIONAL :: outerr
INTEGER, INTENT(OUT), OPTIONAL :: used_routine
```

Matlab implementation

```
fun = @(x) exp(-( a./x.^2 + b*x.^2 ))./x.^m;
if a>0
    g = integral(fun, 0, 1)
else
    g = integral(fun, 0, 1, 'Waypoints', [Mmax*j, Mmax])
end
```

g_integral_Ep

Alternative to numeric integration

```
SUBROUTINE g_integral_Ep(a, b, m, g, err, tolrel, abserr)
! Parameters
INTEGER, PARAMETER :: MAXITER = 10000
```

- Based on *exponential integral*
- Faster than numerical integration
- Calculated by MKL function vdExpInt1
- Details:

F. Capolino *et al.*, "Efficient Computation of the 2-D Green's Function for 1-D Periodic Structures Using the Ewald Method", *IEEE-TAP*, 2005.

- Numerical problems when $b \gg 1$ or $a \ll -1$ or $|ab| \gg 1$ or ...

g_integral_IN

Numeric integration

```
SUBROUTINE g_integral_IN(a, b, m, gI, err, tolrel, tolabsd)
! Parameters
REAL(KIND=DBL), PARAMETER :: EPS = MYEPS1
REAL(KIND=DBL), PARAMETER :: LOGEPS = log(1/EPS)
! INPUT
real(kind=DBL), intent(in) :: a, b
integer, intent(in) :: m
real(kind=DBL), intent(in) :: tolrel
real(kind=DBL), OPTIONAL :: tolabsd
! OUTPUT
COMPLEX(kind=DBL), INTENT(OUT) :: gI
REAL(kind=DBL), INTENT(OUT) :: err
```

- Complex integration on liner paths:
 - ▶ The result is real. It is a real integration.
 - ▶ The integrand is smooth.
 - ▶ The simple real integration function dqng from library *quadpack2* is used.
- Integration on circular path:
 - ▶ Integrand oscilate (more when $b \gg 1$)
 - ▶ Imaginary part: is a Bessel function
 - ▶ Real part: is a Struve function.

g_integral_IN

Integration on circular part

```
! Integral from j*Mmin to Mmin (circular path)
if (m==1) then
    gIaux = -PI/2.0_dbl*StruveH0(ab)
elseif (m==-1) then
    gIaux = Mmin2*(1.0_dbl - PI/2.0_dbl*StruveH1(ab))
elseif (m==-3) then
    gIaux = Mmin4*PI/2.0_dbl*(StruveH0(ab) - &
        2.0_dbl*StruveH1(ab)/ab)
else
    call dqng(g_integrand_circle_real, PI/2.0_dbl, 0.0_dbl,  &
        tolabs, tolrel, gIaux, erraux, neval, ier)
    err = err + erraux
end if
gI_real = gI_real + gIaux
[...]

! Imaginary part
gI_imag = - PI/2*(-a)**(p-1)* &
    BESSEL_JN(p-1, 2*sqrt(abs(a*b))) &
    /sqrt(abs(a*b))**(p-1)
```

specfun_module

Integration on circular part

```
MODULE specfun_module

    !> This module contains tools for evaluate special functions

#define CHKERRQ(n,x) IF (n /= 0) THEN; WRITE(UNIT_OUT,*) 'ERROR:' ,x;STOP;  &
    ENDIF

    USE program_global_variables, ONLY : DBL, PI, ZERO, ONE
    USE program_global_variables, ONLY : MYEPS, MYEPS1, MYEPS2, MYEPS3, MYEPS6
    USE iso_fortran_env, ONLY : UNIT_OUT => OUTPUT_UNIT

    IMPLICIT NONE

    PRIVATE
    PUBLIC :: vdExpIntP, dExpIntP
    PUBLIC :: faddeeva_erfc
    PUBLIC :: STRVHO, STRVH1
    PUBLIC :: STVHO, STVH1

    include "mkl_vml"
```

specfun_module (cont.)

Integration on circular part

```
!-----  
!> @author  
!> Sergio Llorente Romano, Luis E. Garcia Castillo, Adrian Amor  
!  
! DESCRIPTION:  
!> Struve function H0 and H1  
!>  
!> Adaption from https://netlib.org/toms/757  
!>  
!-----  
  
FUNCTION STRVHO(XVALUE)  
[...]  
FUNCTION STRVH1(XVALUE)
```

Outline

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Outline (cont.)

- Numerical Results (oblique incidence)

6 Modifications on Near Field Postprocessing

7 MPI related issues

Implementation of Fortran Module:
EMULATION_2D_scattering_module.F90

Fortran Module

EMULATION_2D_scattering_module.F90

```
TYPE :: EMULATION_2D_scattering_type
PRIVATE
LOGICAL :: enabled_EMULATION_2D_scattering = &
    DEFAULT_ENABLED_EMULATION_2D_SCATTERING
CHARACTER(len=2) :: green_function_type = DEFAULT_GREEN_FUNCTION_TYPE
LOGICAL :: enabled_normal_incidence = DEFAULT_ENABLED_NORMAL_INCIDENCE
! Thickness (height) of 3D slice used to emulate 2D
REAL(KIND=DBL) :: slice_thickness = DEFAULT_SLICE_THICKNESS
END TYPE EMULATION_2D_scattering_type

PUBLIC :: &
    is_EMULATION_2D_scattering_enabled, &
    enable_EMULATION_2D_scattering, &
    disable_EMULATION_2D_scattering, &
    get_EMULATION_2D_scattering_green_function_type, &
    set_EMULATION_2D_scattering_green_function_type, &
    is_EMULATION_2D_scattering_normal_incidence, &
    enable_EMULATION_2D_scattering_normal_incidence, &
    disable_EMULATION_2D_scattering_normal_incidence, &
    get_EMULATION_2D_scattering_slice_thickness, &
    set_EMULATION_2D_scattering_slice_thickness, &
    EMULATION_2D_scattering_print, &
    EMULATION_2D_scattering_sanitycheck
```

Fortran Module (cont.)

EMULATION_2D_scattering_module.F90

Input file .em

```
-----  
--      EMULATION 2D properties      --  
-----  
-- EMULATION 2D activation flag  
EMULATION_2D = true  
-- Set the type of green function used  
EMULATION_2D_green_function_type = "2D"
```

- Once EMULATION_2D mode is activated FE-IIEE and farfield calculations are specialized
- By default, the Green's function used is the one for 2D problems, i.e., H_0^2 (selected as above):
$$\text{EMULATION_2D_green_function_type} = \text{"2D"}$$
- If “3D” is selected, the Green’s function of 3D is used and Ewald acceleration (“Ewald 1D”) is automatically activated.

Fortran Module (cont.)

EMULATION_2D_scattering_module.F90

Input file .em

```
-- EMULATION 2D properties      --
-----
-- Activation flag for normal incidence
EMULATION_2D_normal_incidence = true
-- Thickness of the slice used as pseudo2D problem
EMULATION_2D_slice_thickness = 1.0
```

- The case of “normal incidence” is kept as a separate case
 - ▶ It does not require periodic meshes
- Value of “slice thickness” set up manually (desirable to be set automatically, e.g., GUI or HOFEM mesh preprocessing)

Fortran Module

EMULATION_2D_scattering_module.F90

Input file .em

```
-----  
--      EMULATION 2D properties      --  
-----  
-- Orientation of the cylinder (axis unit vector)  
EMULATION_2D_cylinder_axis = {0.0,1.0,0.0}
```

- Cylinder axis in arbitrary direction
 - ▶ Cylinder axis is set up manually (desirable to be set automatically, e.g., GUI or HOFEM mesh preprocessing)

Fortran Module (cont.)

EMULATION_2D_scattering_module.F90

Input file .em

```
-----  
--      EMULATION 2D properties      --  
-----  
-- Number of incidence angles to be analized  
EMULATION_2D_num_exterior_excitations = 1  
-- Type of plane wave ("Single", "Multiple")  
EMULATION_2D_exterior_type_1 = "Single"  
-- Angle of incidence (with respect to local spherical coordinate  
-- system with z axis along the cylinder axis)  
--   * First number is 'theta' (angle with respect to cylinder axis;  
--     90 corresponds to normal incidence)  
--   * Second number is 'phi' (angle of associated local cylindrical  
--     coordinate system)  
EMULATION_2D_exterior_angle_1 = {90,45}  
-- Polarization (TM or TE)  
EMULATION_2D_polarization_type_1 = "TM"
```

Fortran Module (cont.)

EMULATION_2D_scattering_module.F90

- Definition of angles for excitations with respect to local spherical coordinate system with z axis along the cylinder axis
 - ▶ Angles are transformed back and forth between local and global axis.
- Definition of polarization as either “TM” or “TE”
 - ▶ Vector components (polarization) are transformed back and forth between local and global axis.

Fortran Module (cont.)

EMULATION_2D_scattering_module.F90

Input file farfield_EMULATION_2D.conf

```
!- Farfield mode (bistatic,monostatic)
Bistatic
!- Farfield component (|rE-longitudinal|, rE-longitudinal-real, rE-longitudinal-imag, rE-transverse-real, rE-transverse-imag, rE-transverse-imag, RCS-dB, RCS-longitudinal-dB, RCS-transverse-dB, Monostatic-RCS, RCS
!- Frequency index and number of rhs
1 1
!- Rhs index
1
!- Rhs phase
0
!- Rhs amplitude
1
```

Fortran Module (cont.)

EMULATION_2D_scattering_module.F90

Input file farfield_EMULATION_2D.conf

```
!- Monitor number
1
!- Phi_cyl sampling points (num init stop)
37 0 360
!- RCS units
sigma-lambda
!- Array analysis (flag ,num_elem_u ,num_elem_v)
0 1 1
```

Fortran Module (cont.)

EMULATION_2D_scattering_module.F90

- Specialization to EMULATION 2D mode
 - ▶ Farfield-mode: only scattering
 - ▶ Farfield-component: “longitudinal” and “transverse” components with respect to cylinder
 - ▶ ...
- Only the angles “phi” need to be defined for the plot (plot associated to the transversal plane to the cylinder (perpendicular to its axis))
- Array analysis: we keep it as it might be of interest to consider finite 1D/2D periodic structures based on pseudo2D cylinders

Fortran Module

EMULATION_2D_scattering_module.F90

- Near field: GreenD derivatives are rewritten in a compact way supporting computation of the scattering near field (within FE-IIEE loop) for arbitrarily oriented cylinders
- Far field: Also works with arbitrarily oriented cylinders in terms of local θ , ϕ components (local in the sense of spherical coordinate system with axis z along the cylinder axis)
 - ▶ Note that for normal incidence
 - ★ θ -component is longitudinal component ($-z$ -component)
 - ★ ϕ -component is transverse component
 - ▶ Perfect agreement between numerical and analytical solutions for both TE/TM polarizations and normal incidence ...
 - ★ However, we have identified a case for oblique incidence which there is no agreement neither with TM or TE polarization (See file FarField_bug.pdf for details)

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Outline (cont.)

- Numerical Results (oblique incidence)

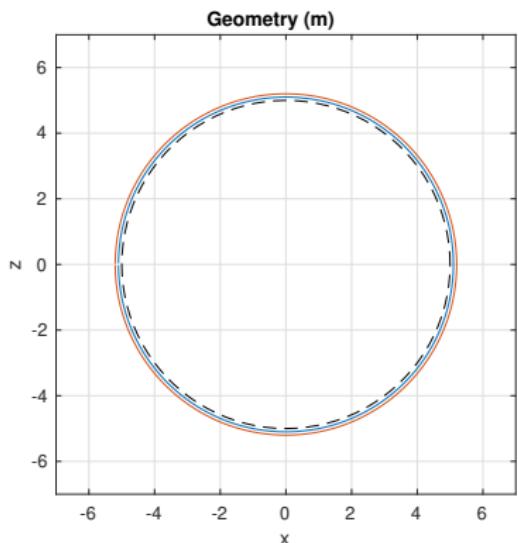
6 Modifications on Near Field Postprocessing

7 MPI related issues

Far-field Bistatic RCS calculation

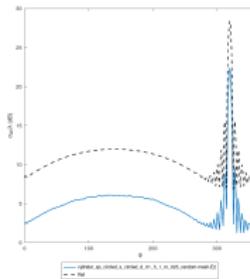
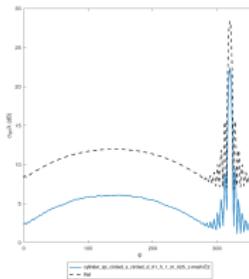
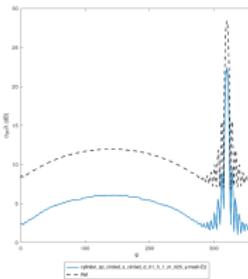
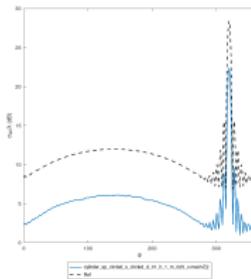
Reference cases

The same geometry is analyzed with different orientations of the longitudinal axis:



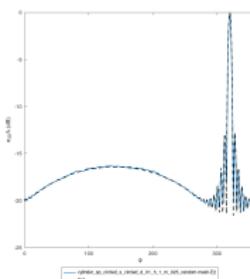
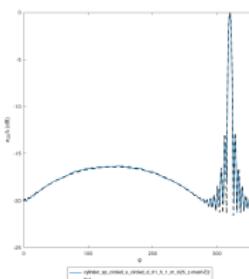
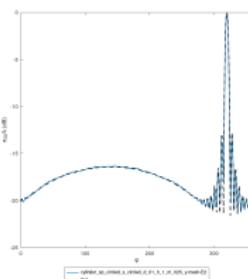
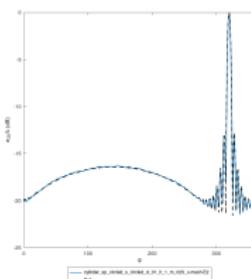
- Normal incidence
- Dashed black line:
- Blue line: S'
- Red line: S
- Different values of permittivity between PEC and S' : ϵ_r
- $f = 300 \text{ MHz}$ ($\lambda = 1 \text{ m}$, cylinder radius is 5λ).

TM polarization, $\varepsilon_r = 1$ (reference case)

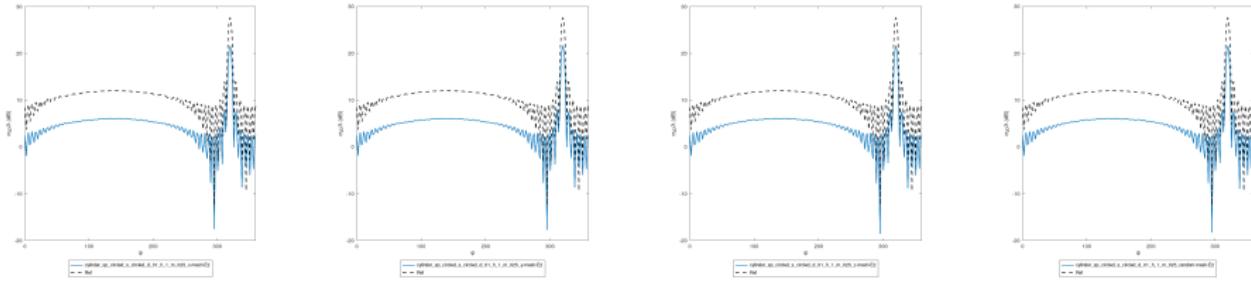


Analytical curves and FEM curves agree except for a constant factor. **DEBO
ACTUALIZAR ESTO QUE YA ESTA SUPERADO**

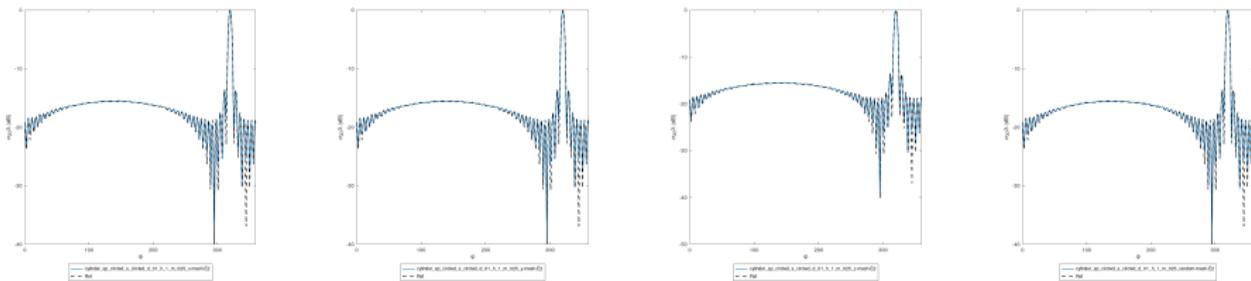
Normalized bistatic-RCS:



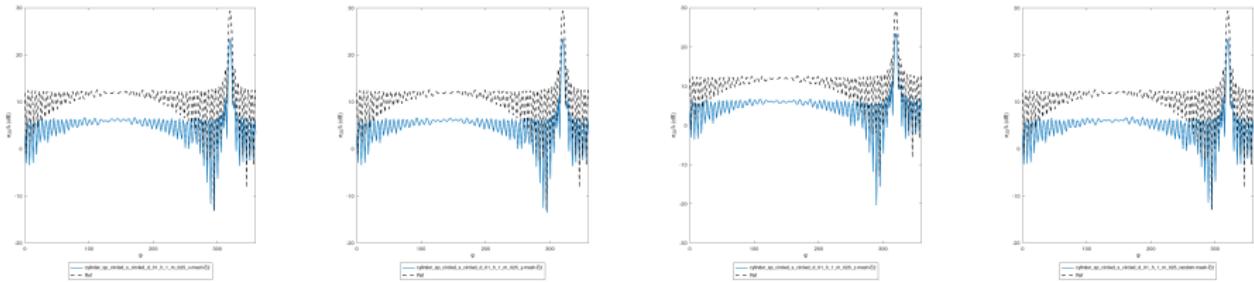
TE polarization, $\varepsilon_r = 1$



Analytical curves and FEM curves agree except for a constant factor.
Normalized bistatic-RCS:

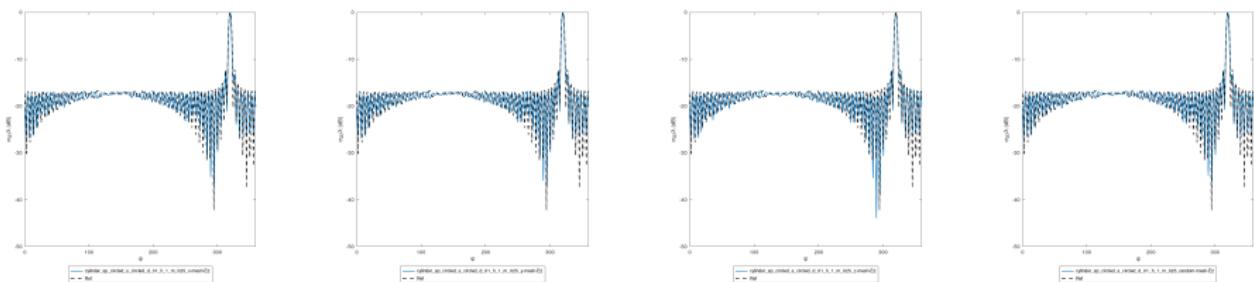


TM polarization, $\varepsilon_r = 8$

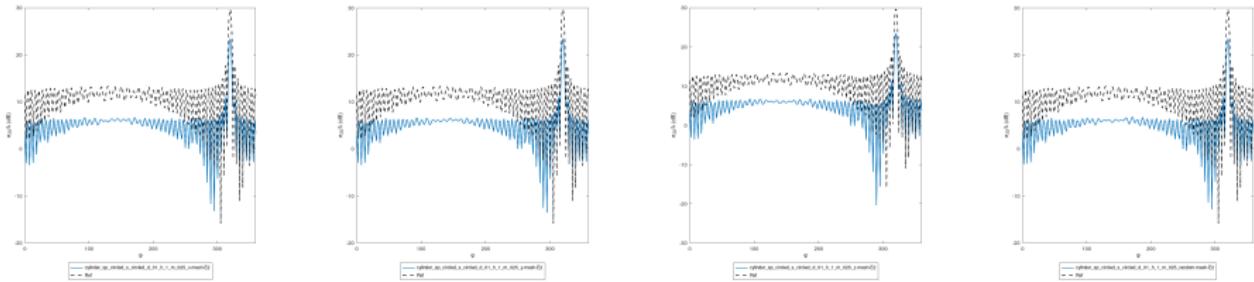


Analytical curves and FEM curves agree (minor discrepancies) except for a constant factor.

Normalized bistatic-RCS:

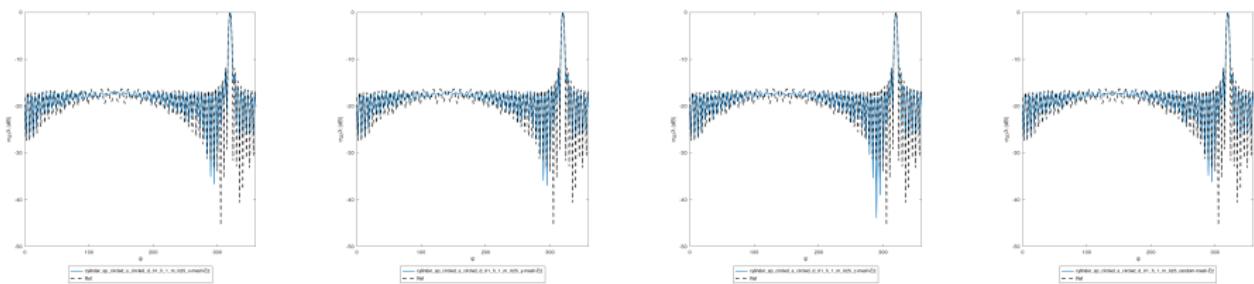


TE polarization, $\varepsilon_r = 2$

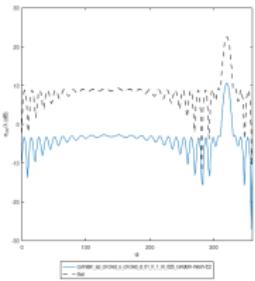
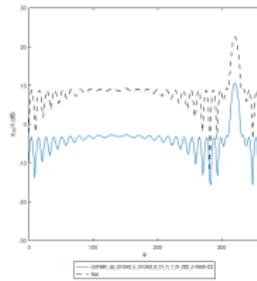
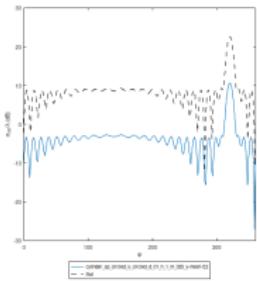
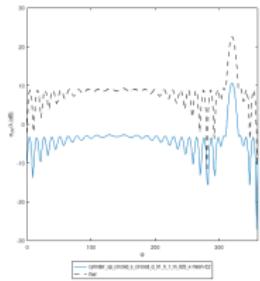


Analytical curves and FEM curves agree (some discrepancies) except for a constant factor.

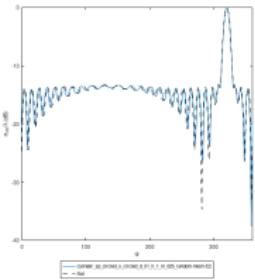
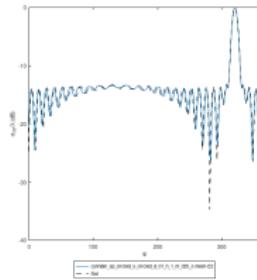
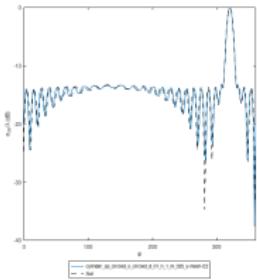
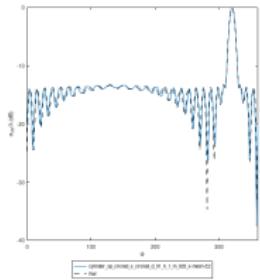
Normalized bistatic-RCS:



TE polarization, $\epsilon_r = 2$, $f = 150$ MHz



For a smaller problem (same mesh, double wavelength), almost full agree.
Normalized bistatic-RCS:

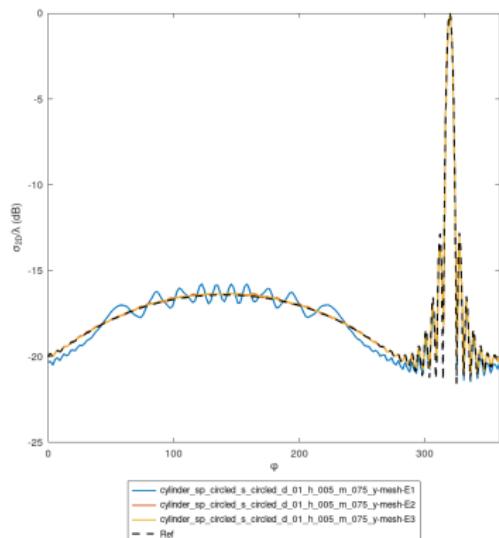
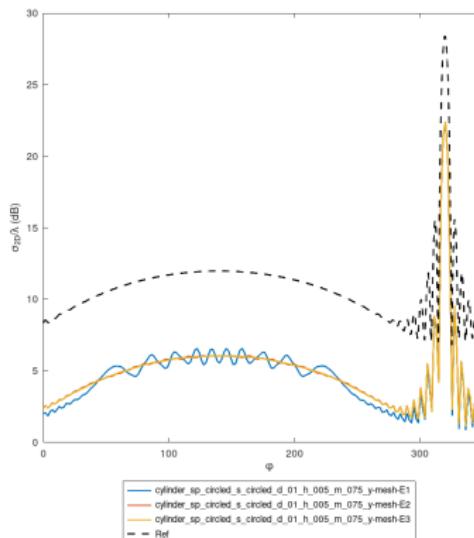


Effect of IIEE iterative method in Far Field

TM polarization, $\varepsilon_r = 1$, (reference case)

Results for the following residual errors:

- M1: 10^{-1} (blue)
- M2: 10^{-2} (red)
- M3: 10^{-3} (orange)



Note: Orange and red lines overlap.

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Outline (cont.)

- Numerical Results (oblique incidence)

6 Modifications on Near Field Postprocessing

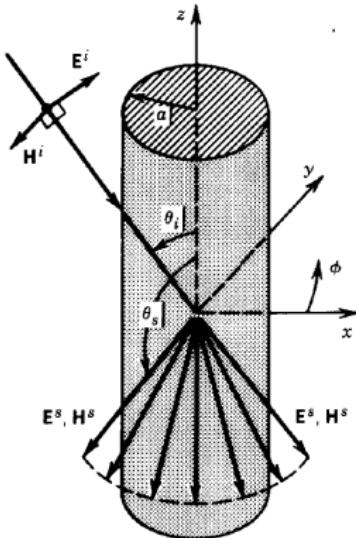
7 MPI related issues

Until now we were considering normal incidence to the cylinder
Now we consider the extension to case of "Oblique Incidence"

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Oblique Incidence



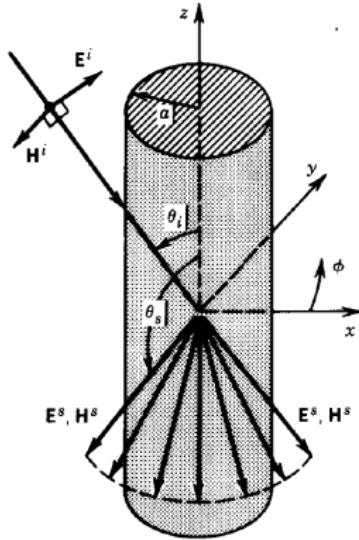
Green's Function

$$G = \int_{-\infty}^{\infty} \frac{e^{-jk\sqrt{\rho^2+z^2}}}{4\pi\sqrt{\rho^2+z^2}} e^{\pm j\beta_z z} dz$$
$$= \begin{cases} \frac{1}{4j} H_0^{(2)} \left(\rho \sqrt{k^2 - \beta_z^2} \right) & k^2 > \beta_z^2 \\ \frac{1}{2\pi} K_0^{(2)} \left(\rho \sqrt{k^2 - \beta_z^2} \right) & \beta_z^2 > k^2 \end{cases}$$

$$\text{where } \beta_z^2 = k^2 \cos^2 \theta_i < k^2$$

IMPORTANT: The symbol θ_s in the figure (and in the following slides) has nothing to do with the θ_s of Fig. 5.1 of Ph.D Thesis of Daniel Garcia Doñoro

Oblique Incidence (cont.)



Green's Function

- For any θ_i we have

$$G = \frac{1}{4j} H_0^{(2)} \left(\rho \sqrt{k^2 - \beta_z^2} \right) = \frac{1}{4j} H_0^{(2)} (k_\rho |\rho|)$$

where $k_\rho = k \sin \theta_i$

- The particularization to $\theta_i = 90^\circ$ (normal incidence) yields to the well known result

$$G = \frac{1}{4j} H_0^{(2)} (k |\rho|)$$

Oblique Incidence (cont.)

FE-IIEE loop

- As in the case of normal incidence

- We use Green2D^a on the whole 3D slice and we divide the scattered field at each target point by the “slice thickness”
- We work with ρ instead of r , i.e.,

$$|\rho - \rho'| = |(\mathbf{r} - \mathbf{r}') - ((\mathbf{r} - \mathbf{r}') \cdot \hat{\mathbf{z}})\hat{\mathbf{z}}|$$

where $\hat{\mathbf{z}}$ stands for the direction along the cylinder axis^b

- The z -dependence of the solution (including the scattering field) must be as

$$\mathbf{E}, \mathbf{H} \propto e^{jk \cos \theta_i z}$$

Note that $\beta_z \equiv k \cos \theta_i > 0$

^aWe may also use Green3D_Ewald1D

^bThe code supports arbitrary orientations for the cylinder

Oblique Incidence (cont.)

FE-IIEE loop (cont.)

- Thus, for oblique incidence we need to take into account the relative “height” between \mathbf{r} and \mathbf{r}'
- That is, we need to add a factor to the 2D Green function when summing up the contributions on given integration target points of “height” $\mathbf{r} \cdot \hat{\mathbf{z}}$ from different integration point sources of “height” $\mathbf{r}' \cdot \hat{\mathbf{z}}$.

The factor is

$$e^{+jk \cos \theta_i (\mathbf{r} - \mathbf{r}') \cdot \hat{\mathbf{z}}}$$

or equivalently

$$e^{-jk \cos \theta_i (\mathbf{r}' - \mathbf{r}) \cdot \hat{\mathbf{z}}}$$

Oblique Incidence (cont.)

In other words,

$$G(|\mathbf{r} - \mathbf{r}'|) = \frac{1}{4j} H_0^{(2)}(k_\rho |\boldsymbol{\rho} - \boldsymbol{\rho}'|) e^{+j\beta_z(z - z')}$$

where $k_\rho = k \sin \theta_i$ and $\beta_z = k \cos \theta_i$

Remarks:

- Symbol $\hat{\mathbf{z}}$ stands for the direction along the cylinder axis
- The code supports arbitrary orientations for the cylinder
- Implementation status:
 - ▶ Coded
 - ▶ Tested (using PBCs)
 - ★ Bug/error correction affecting with arbitrary orientations of the cylinder

Oblique Incidence (cont.)

- ★ Note that the non-null variation with z on the Green's function makes computation of derivatives (needed up to second order for FE-IIEE) cumbersome, specially if coded for arbitrary orientations of the cylinder

Oblique Incidence (cont.)

A remark on dielectric (and dielectric coated PEC) cylinders...

Dielectric cylinders (also dielectric coated PEC)

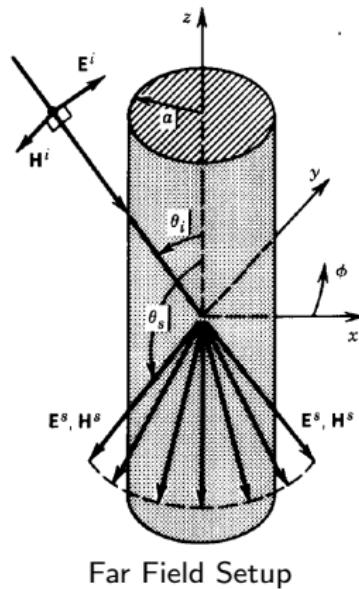
- TM and TE are not longer solutions (**polarizations are coupled**) for oblique incidence
- In the limit, with angle tending to normal incidence, the polarizations are effectively decoupled
- Analogously, TM and TE coupling appears also when using IBC (even isotropic case) for oblique incidence

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Oblique Incidence

Far Field



Far Field

- Green's function

$$G_{\text{far}} \propto e^{+jk\rho \sin \theta_i} \underbrace{e^{-jk \cos \theta_i z}}_{F_{1z}(z)}$$

- Potential, fields

$$\text{Potentials, fields} \propto F_{2\phi}(k, \phi, \sin \theta_i) F_{2\theta}(\theta)$$

where

$$F_{2\theta}(\theta) = \int_{-\infty}^{\infty} F_{1z}(z) e^{+jk \cos \theta z} = \delta(\theta - (\pi - \theta_i))$$

Using far field version of Green2D on a 3D slice can be used to calculate $F_{2\phi}$ (the variation with ϕ of the scattering field: RCS, scattering width)

Oblique Incidence (cont.)

Far Field

More precisely...

- Green's Function

$$G_{\text{far}} = \frac{1}{4j} H_0^{(2)}(k\rho \sin \theta_i) \Big|_{k\rho \rightarrow \infty} \approx \frac{1}{4j} \sqrt{\frac{2j}{\pi k\rho \sin \theta_i}} e^{-jk\rho \sin \theta_i}$$

Oblique Incidence (cont.)

Far Field

Far Field Computation using 3D Slice

- We use Green2D on the whole 3D slice and we divide the scattered field at each target point by the “slice thickness”
- We need to take into account the z -dependence of the 3D (FEM) solution, i.e.,

$$\mathbf{E}, \mathbf{H} \propto e^{ik \cos \theta_i z}$$

Oblique Incidence (cont.)

Far Field

Far Field Algorithm:

- ① We start from \mathbf{J} , \mathbf{M} on S'
- ② We “equalize” \mathbf{J} , \mathbf{M} on z -dependence⁴

$$\mathbf{J} = \mathbf{J} e^{-jk \cos \theta_i z}$$

$$\mathbf{M} = \mathbf{M} e^{-jk \cos \theta_i z}$$

- ③ We transform \mathbf{J} , \mathbf{M} to spherical coordinates on local coordinate system attached to the cylinder

$$\mathbf{J} \rightarrow (J_\theta, J_\phi)$$

$$\mathbf{M} \rightarrow (M_\theta, M_\phi)$$

- ▶ Note that for normal incidence the local θ, ϕ components are longitudinal J_z , M_z and transverse J_ϕ , M_ϕ components, respectively

Oblique Incidence (cont.)

Far Field

- ④ We compute vector potentials $A_\theta, A_\phi, F_\theta, F_\phi$

$$J_\theta \rightarrow A_\theta \quad M_\theta \rightarrow F_\theta$$

$$J_\phi \rightarrow A_\phi \quad M_\phi \rightarrow F_\phi$$

- ⑤ and from vector potentials we compute the far field components

$$(A_\theta, A_\phi, F_\theta, F_\phi) \rightarrow (E_\theta, E_\phi, H_\theta, H_\phi)$$

- ⑥ We do not forget to divide by “slice thickness”

$$(E_\theta, E_\phi, H_\theta, H_\phi) \rightarrow (E_\theta, E_\phi, H_\theta, H_\phi) / \text{“slice thickness”}$$

- ⑦ Due to decomposition of currents in **local** θ and ϕ components, we can naturally obtain the TM and TE components, i.e.,

$$(E_\theta, H_\phi) \rightarrow \text{TM}$$

$$(E_\phi, H_\theta) \rightarrow \text{TE}$$

Oblique Incidence (cont.)

Far Field

Scattering Width σ

$$\boldsymbol{\sigma} = \begin{bmatrix} \sigma_{(TM,TM)} & \sigma_{(TM,TE)} \\ \sigma_{(TE,TM)} & \sigma_{(TE,TE)} \end{bmatrix}$$

- Note that for PEC cylinders we have $\sigma_{(TM,TE)} = \sigma_{(TE,TM)} = 0$
- Implementation status:
 - ▶ Coded
 - ▶ UPDATE: Tested (using PBCs)
 - ★ Level correct (constant captured)
 - ★ TM working
 - ★ TE (minor bug yet to be captured)

⁴The “equalization” can alternatively be applied on the Greens’s Function

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Integration EMULATION_2D and PBCs

Logic for Oblique Incidence

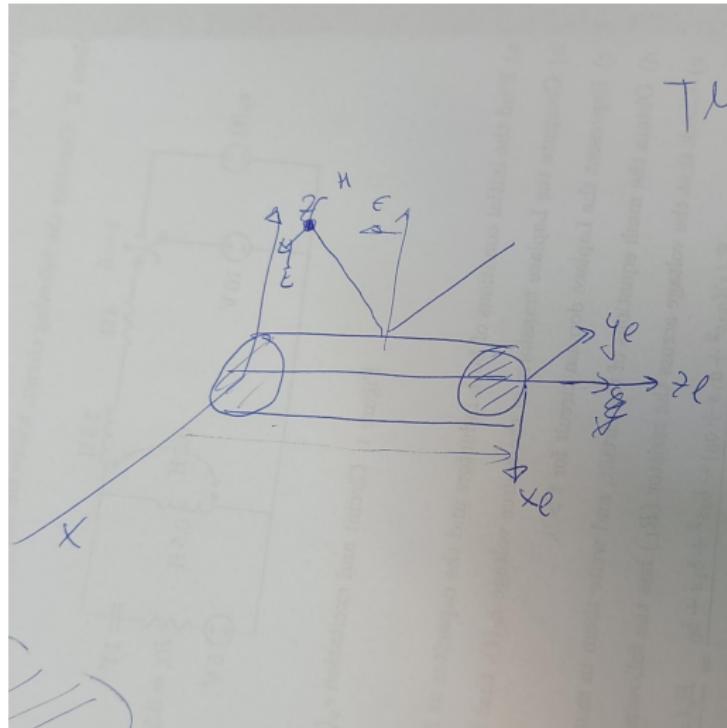
Angle of Incidence

- Angle of incidence set up in file .em
- Discard PBC info (scan theta and phi angles) in file .em:
`periodic_phi_angle, periodic_theta_angle`
- PBC \leftarrow EMULATION_2D info from file
 - ▶ Example: `EMULATION_2D_exterior_angles_1 = {45,140}`
`EMULATION_2D_cylinder_axis = {0.0,1.0,0.0}`
 \Rightarrow `periodic_phi_angle=122.73, periodic_theta_angle=57.20`

NOTE: Note that the local x, y, z axis may be rotated with respect to global x, y, z axis when cylinder axis vector is not along global z -axis

Integration EMULATION_2D and PBCs (cont.)

Logic for Oblique Incidence



Integration EMULATION_2D and PBCs (cont.)

Logic for Oblique Incidence

offset_vector

- Coherence between matrix `offset_vector` (obtained from processing the mesh) and `cylinder_axis`, `slice_thickness` (from EMULATION_2D module)
 - ▶ It is checked
 - ▶ And even corrected under certain circumstances
- **NOTE:** The algorithm to compute matrix `offset_vector` is extremely sensible to coordinate precision and prone to error on concluding about the types and number of periodicities (1D, 2D, etc) present in the mesh

Integration EMULATION_2D and PBCs (cont.)

Logic for Oblique Incidence

Logic for Normal Incidence

- The case with normal incidence can be run as a particular case of oblique incidence, i.e, using PBCs
 - Obviously, it can be run with `enabled_normal_incidence`
 - ▶ There is no PBC interaction
 - ▶ `cylinder_axis` and `slice_thickness` read from file `.ema`
 - ▶ Angle of incidence set up in file `.em`:
 - ★ Example: `EMULATION_2D_exterior_angles_1 = {90,140}`
- Actually, the θ angle of incidence is checked (and forced) to be 90 degrees

^aNevertheless, that information could be obtained by preprocessing the mesh within HOFEM code (extra task, not considered at present)

Integration EMULATION_2D and PBCs (cont.)

Logic for Oblique Incidence

Tons of checks...

• ...

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What about CASE ('ABC_PERIODIC')

There is a PROBLEM with the ABC_PERIODIC boundary condition with
EMULATION_2D; actually, with 1D periodicity in general

- Not a plane wave
- But plane waves around/along a cone
- The scan angle θ_s depends on position

Conclusion/Decision

- We decide not to modify the ABC periodic to adapt it to the 1D periodicity case
- We leave/trust FE-IIEE loop take into account that effect and compensate

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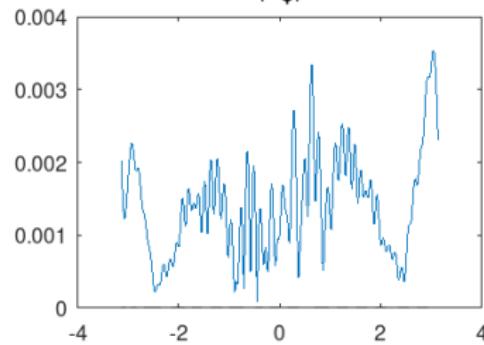
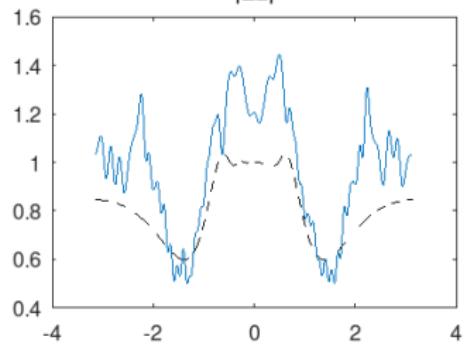


Oblique incidence tests

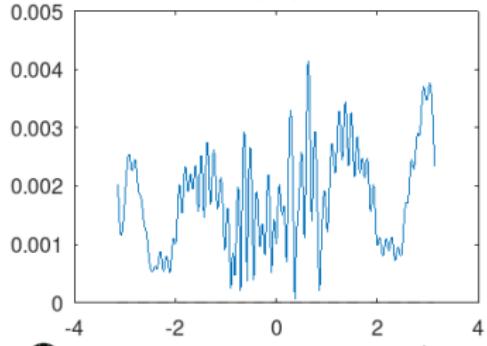
Near field

Mesh 1, TM, normal incidence

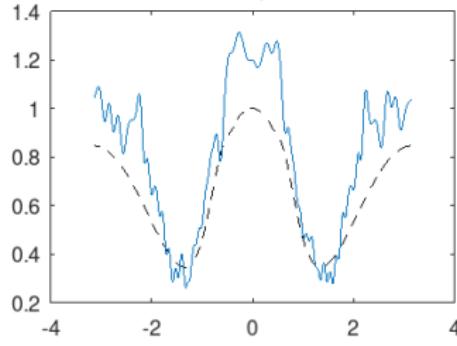
Scattered Field, TM incident plane wave, $\psi=90^\circ$



$|\mathbf{H}|$



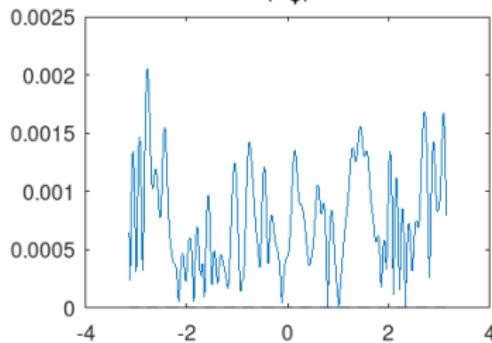
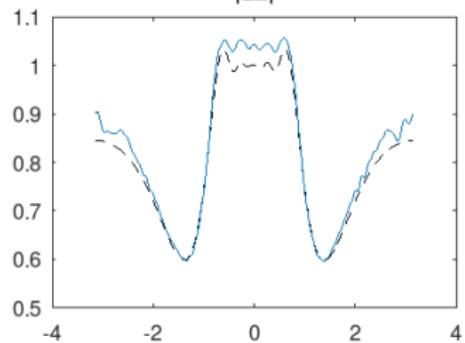
$|\mathbf{H}_\phi|$



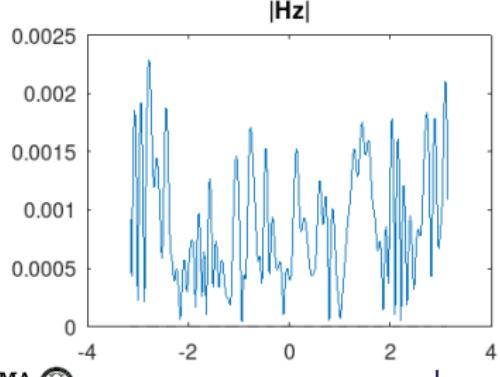
Near field

Mesh 2, TM, normal incidence

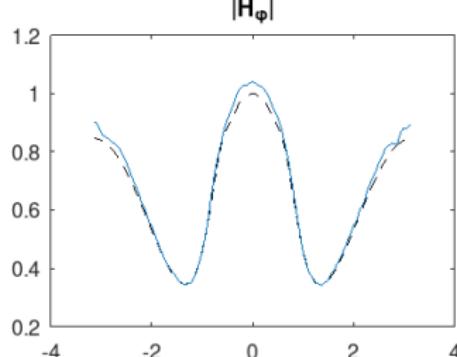
Scattered Field, TM incident plane wave, $\psi=90^\circ$



$|\mathbf{H}|$



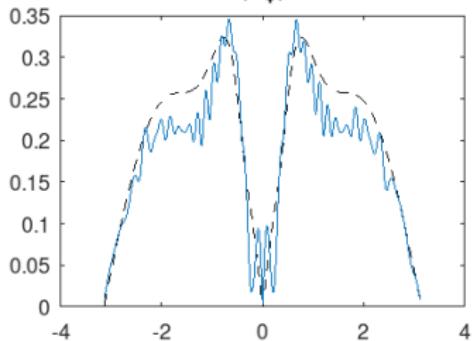
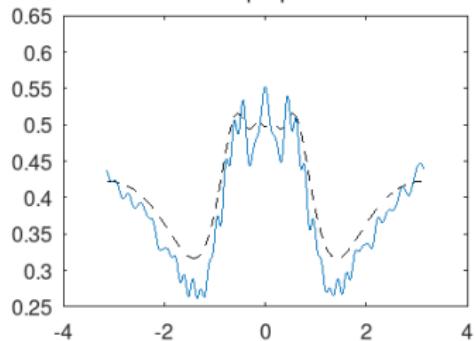
$|\mathbf{H}_\phi|$



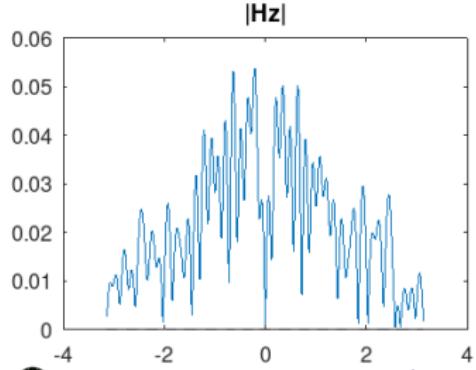
Near field

Mesh 1, TM, oblique incidence

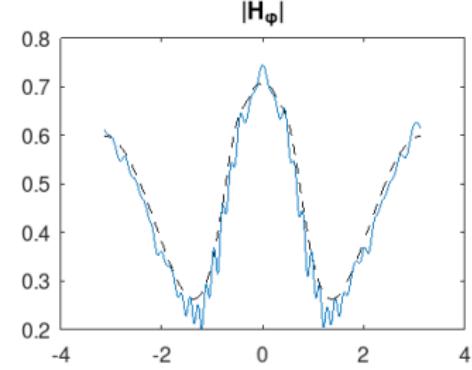
Scattered Field, TM incident plane wave, $\psi=45^\circ$



$|H_z|$



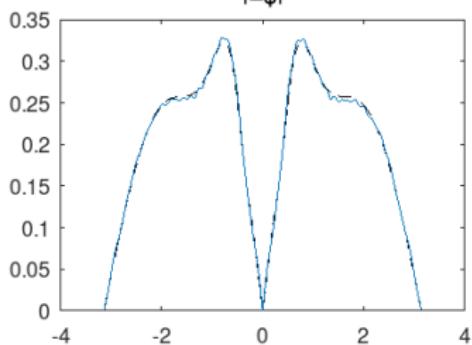
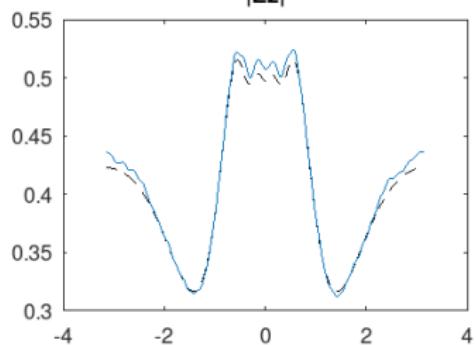
$|H_\phi|$



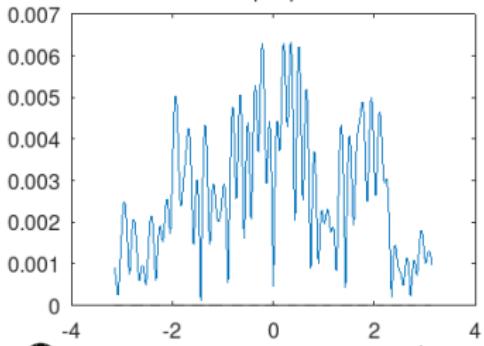
Near field

Mesh 2, TM, oblique incidence

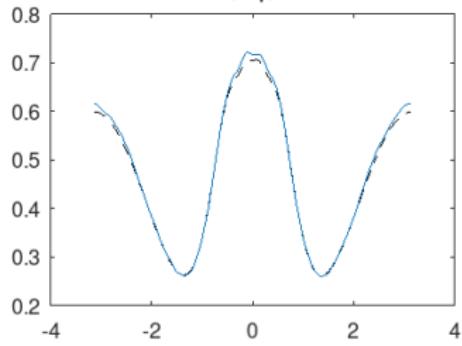
Scattered Field, TM incident plane wave, $\psi=45^\circ$



$|H_z|$



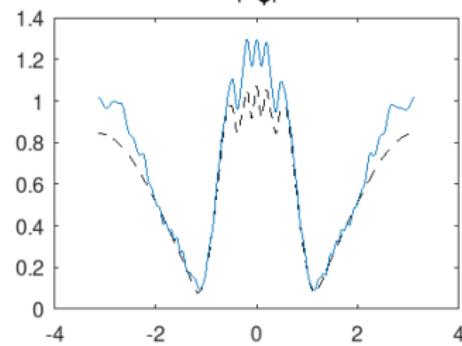
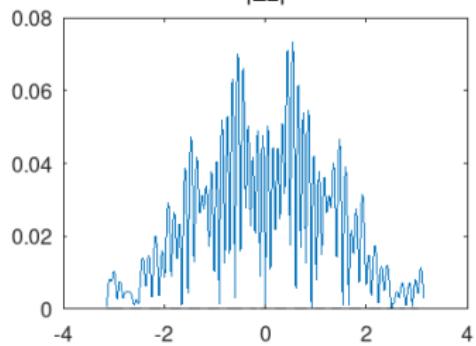
$|H_\phi|$



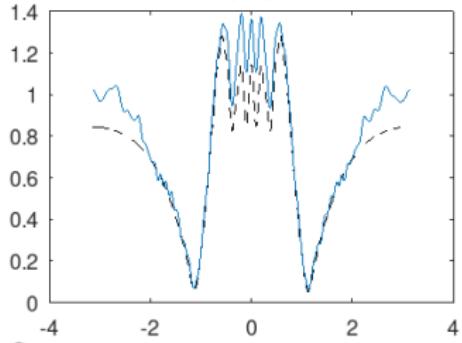
Near field

Mesh 1, TE, normal incidence

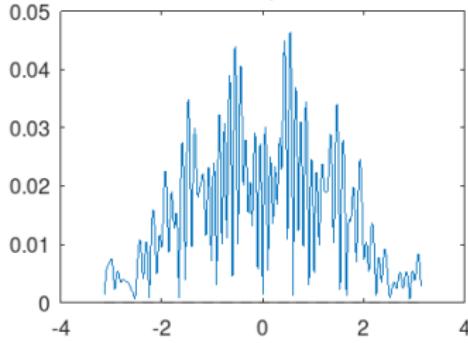
Scattered Field, TE incident plane wave, $\psi=90^\circ$



$|H_z|$



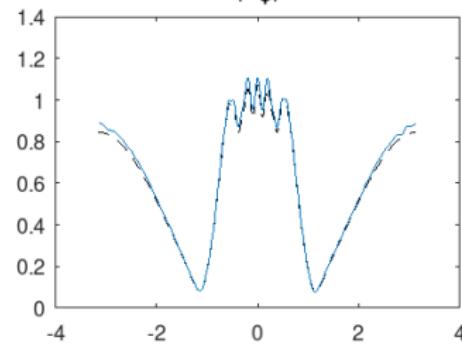
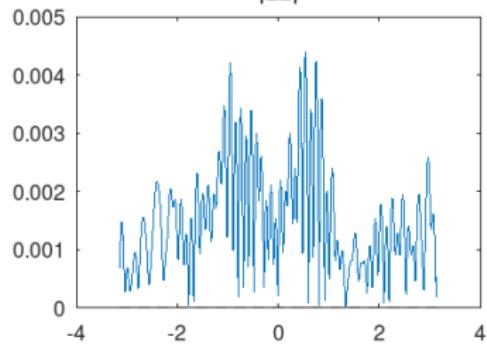
$|H_\phi|$



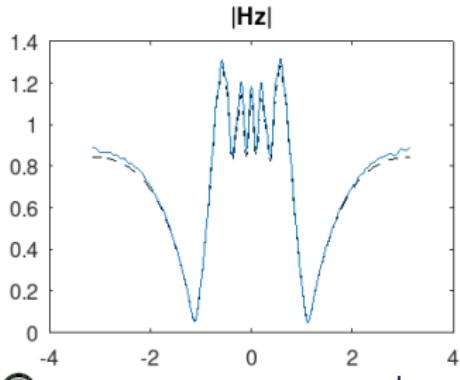
Near field

Mesh 2, TE, normal incidence

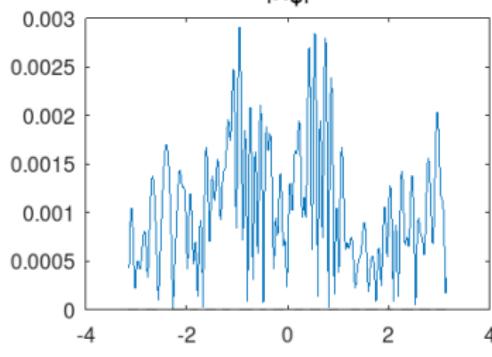
Scattered Field, TE incident plane wave, $\psi=90^\circ$



$|\mathbf{H}|$



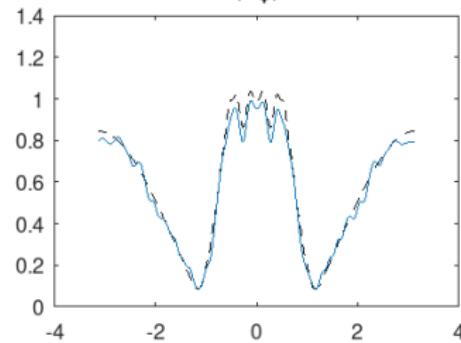
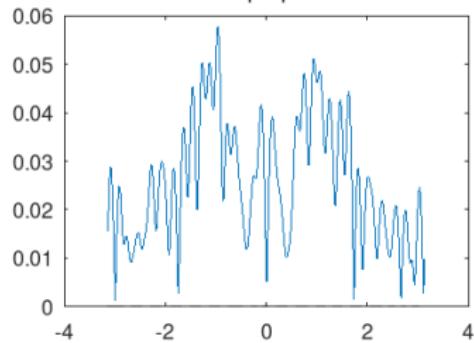
$|\mathbf{H}_\phi|$



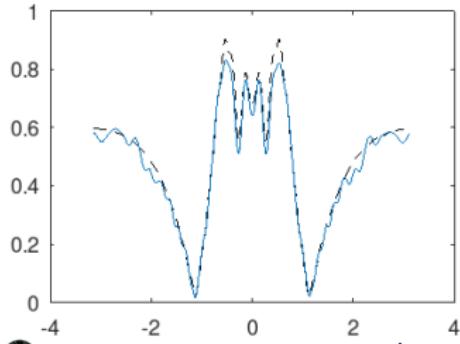
Near field

Mesh 1, TE, oblique incidence

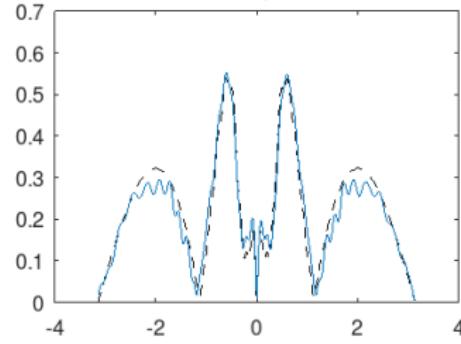
Scattered Field, TE incident plane wave, $\psi=45^\circ$



$|\mathbf{H}_z|$



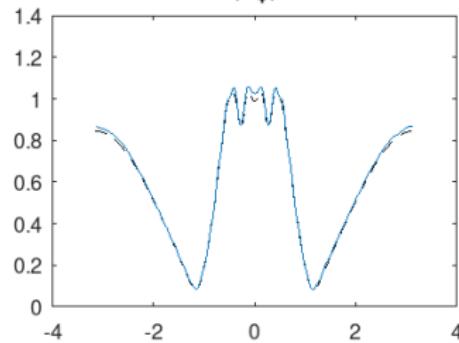
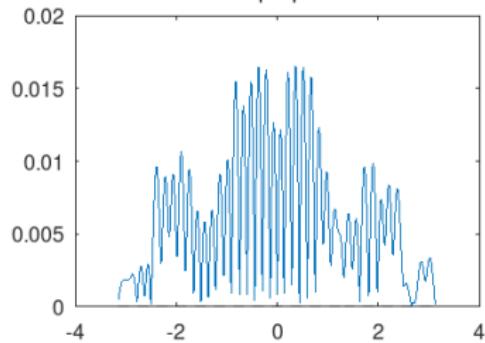
$|\mathbf{H}_\phi|$



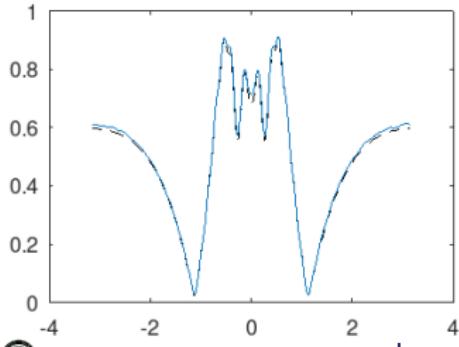
Near field

Mesh 2, TE, oblique incidence

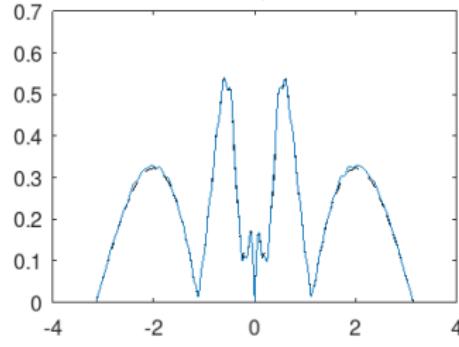
Scattered Field, TE incident plane wave, $\psi=45^\circ$



$|H_z|$

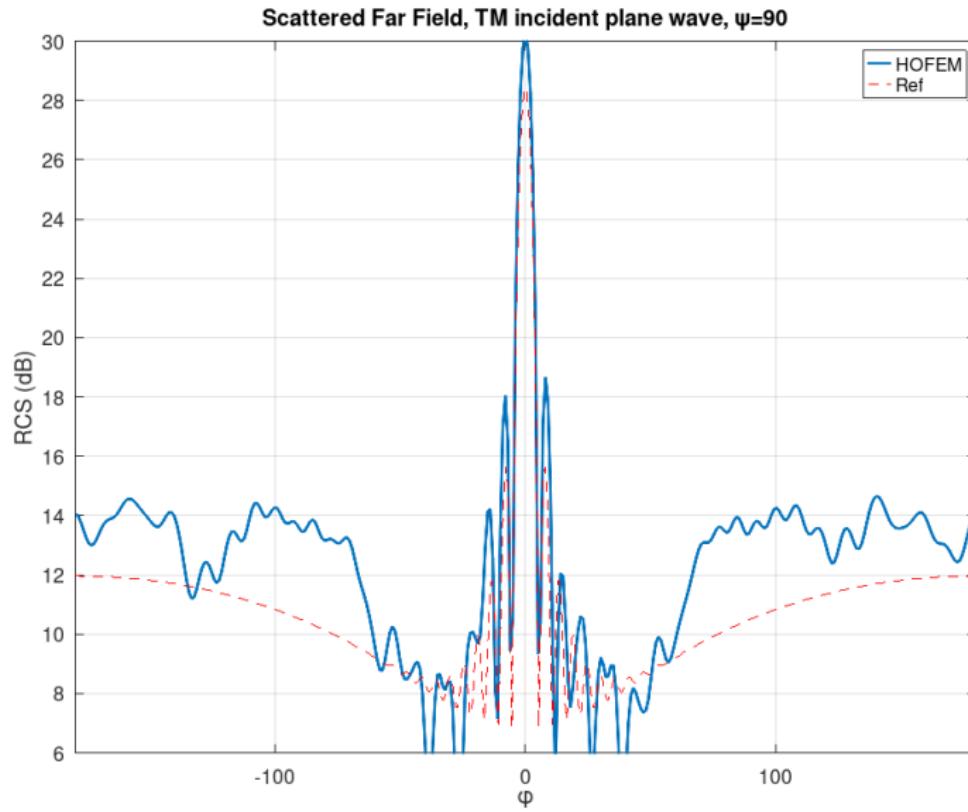


$|H_\phi|$



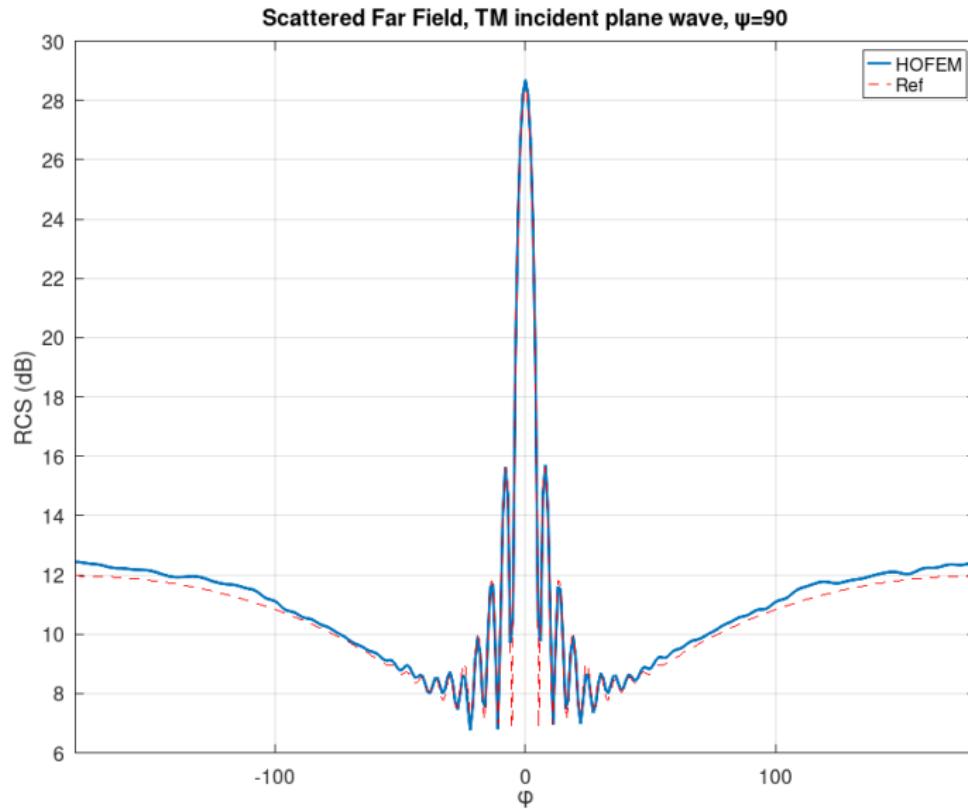
Far field

Mesh 1, TM, normal incidence



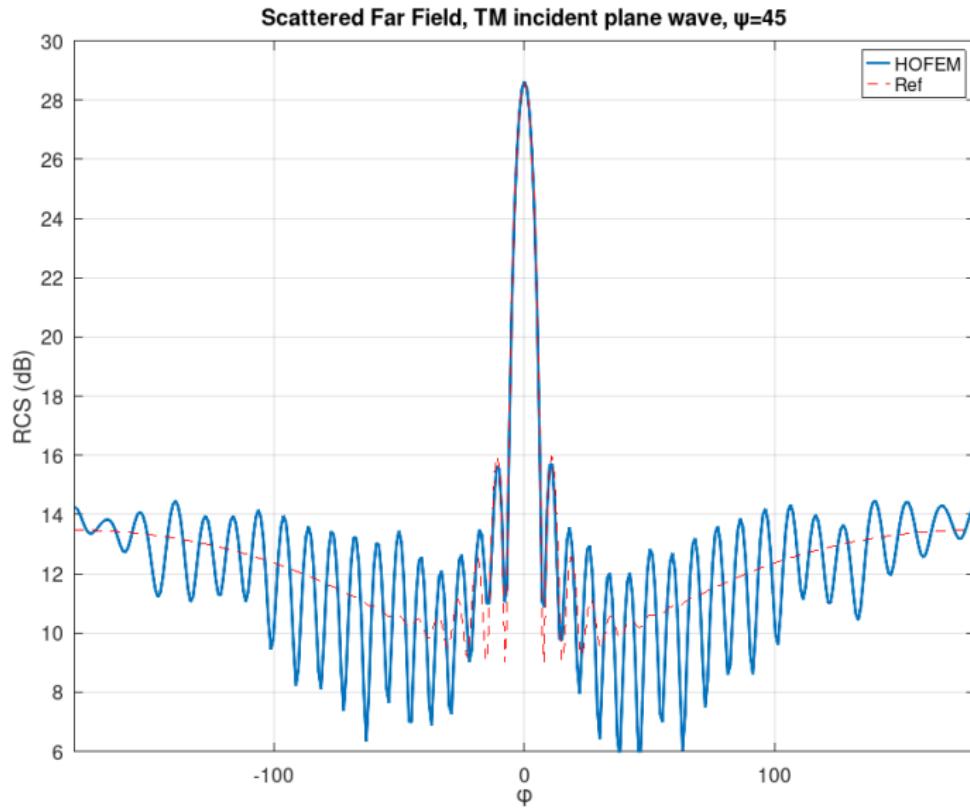
Far field

Mesh 2, TM, normal incidence



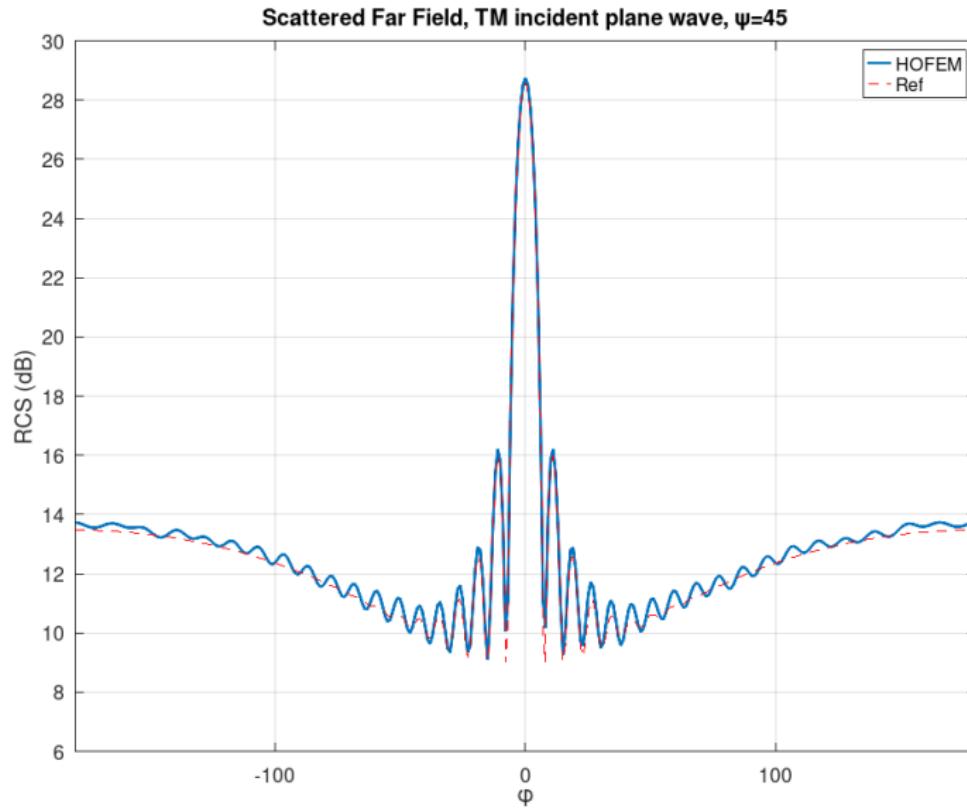
Far field

Mesh 1, TM, oblique incidence



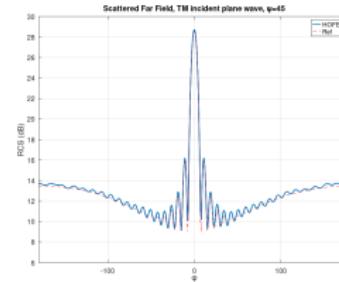
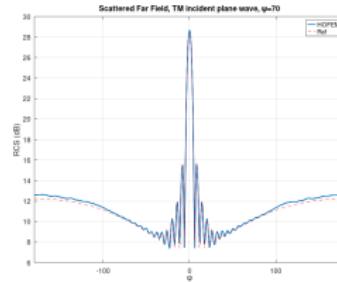
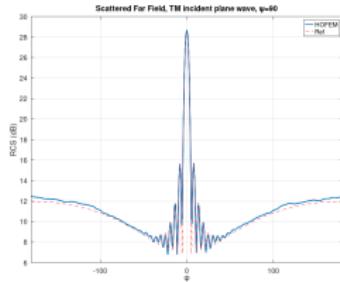
Far field

Mesh 2, TM, oblique incidence



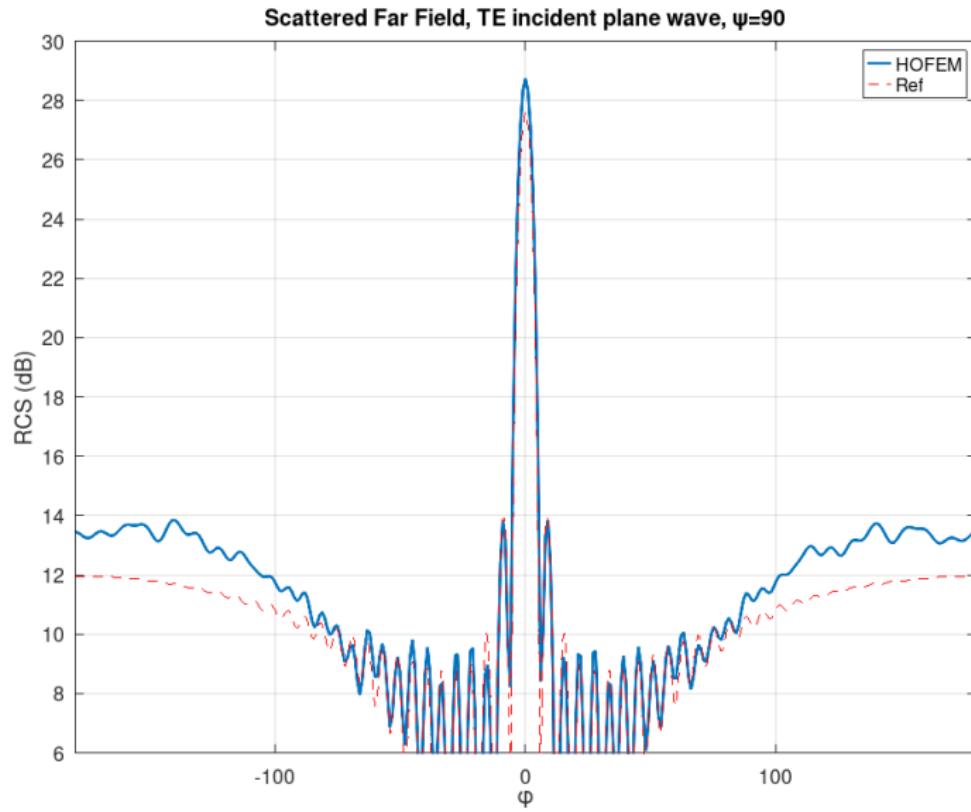
Far field

Mesh 2, TM, 90-70-45



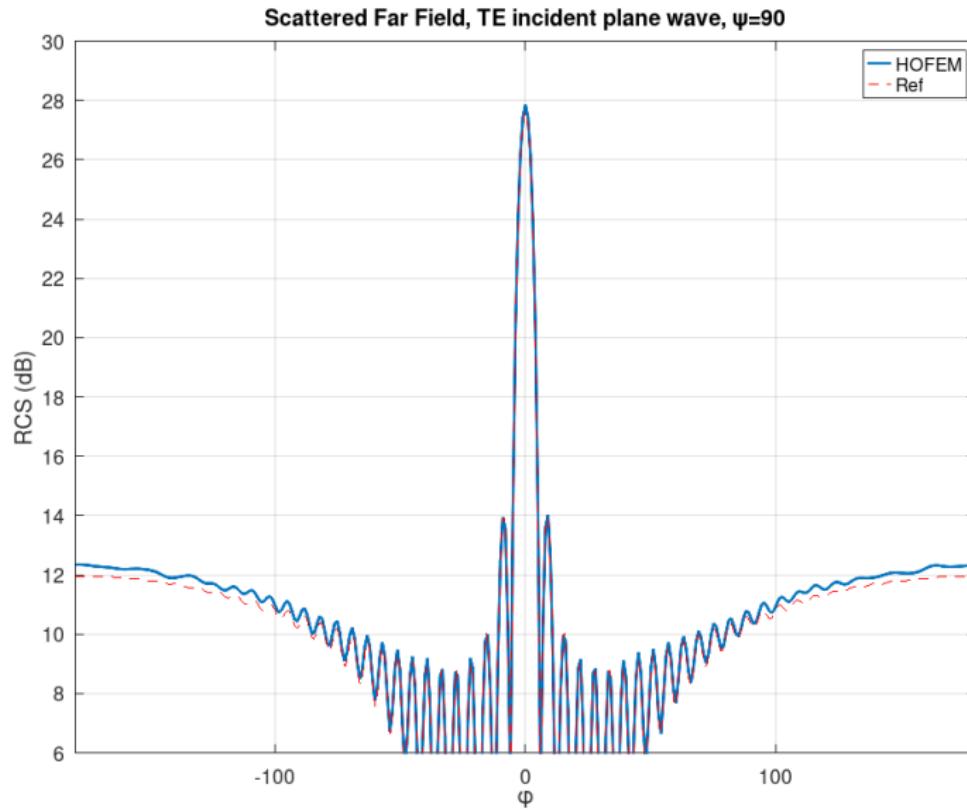
Far field

Mesh 1, TE, normal incidence



Far field

Mesh 2, TE, normal incidence



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Outline (cont.)

- Numerical Results (oblique incidence)

6 Modifications on Near Field Postprocessing

7 MPI related issues

Modifications relative to postprocessing (near field)

Postprocessing changes

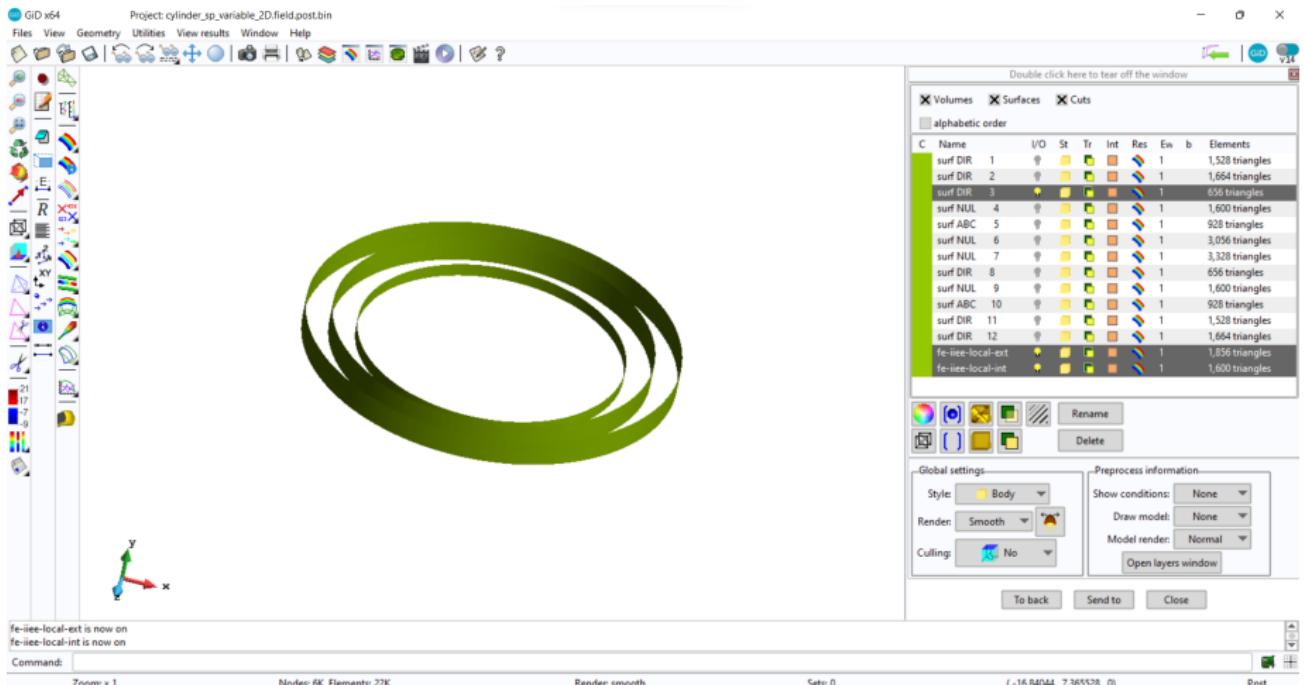
Extra information in nearfield

Changes in nearfield postprocessing

- Added a 3-character string after `surf` to denote the kind of boundary condition that surface is (DIR, NEU, NUL, ABC, ...)
- Added to the surface set the surfaces involved in FE-IIEE method, denoted as `fe-iiee-local-ext`, and `fe-iiee-local-int`, corresponding to S and S' surfaces respectively.

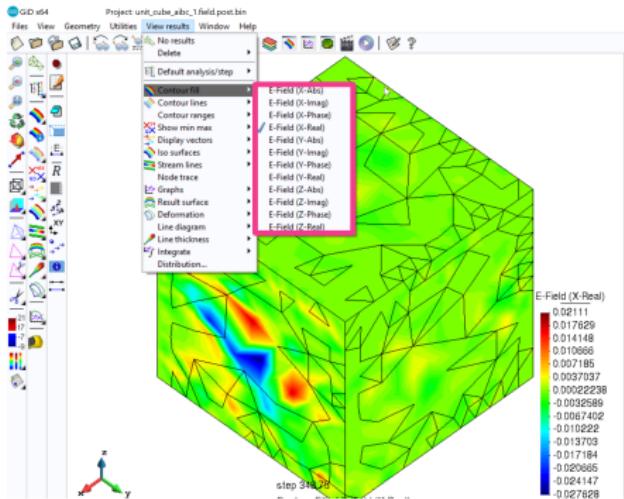
Postprocessing changes (cont.)

Extra information in nearfield



Postprocessing changes

Extra information in nearfield



- Included a new option to get all the available results for the near field.
- Implemented as a new option called **all-xyz**.

Outline

- 1 Green3D vs Green2D for FE-IIEE
 - Green's Function for 2D Emulation
 - Near Field (FE-IIEE loop)
 - Far Field (postprocess)
 - Further Rethinking on Possible Use of Green3D
 - A note on Field Representation on Surfaces
 - Further Numerical Results (using Green2D)
 - TE Polarization
 - Dielectric Coated Cylinder (TM and TE)
- 2 Ewald Acceleration (1D periodicity)
 - Differences with Respect to 2D Periodicity
 - Fortran Module
- 3 EMULATION_2D Fortran Module
- 4 Far Field Numerical Results
- 5 Oblique Incidence
 - Green's Function
 - Far Field
 - Integration of EMULATION_2D and PBCs
 - A note on ABC_PERIODIC boundary condition

Outline (cont.)

- Numerical Results (oblique incidence)

6 Modifications on Near Field Postprocessing

7 MPI related issues

MPI related issues

EMULATION_2D MPI Broadcast

- From FREQ-SWEEP to POST-MODE we write and read from disk

Write to Disk

```
SUBROUTINE write_EMULATION_2D_data_structure(filename)

CHARACTER(LEN=*) , INTENT(IN) :: filename
INTEGER:: ierror,fileunit

OPEN(NEWUNIT=fileunit , FILE=filename , STATUS="REPLACE" ,  &
      ACTION="WRITE" , FORM="UNFORMATTED" , IOSTAT=ierror)
IF (ierror /= 0) THEN
    CHKERRQ(ierror , 'write_EMULATION_2D_data_structure: &
                           Error opening file')
ENDIF
WRITE(fileunit , IOSTAT=ierror)   &
    EMULATION_2D_scattering_structure

CLOSE(fileunit)

END SUBROUTINE write_EMULATION_2D_data_structure
```

EMULATION_2D MPI Broadcast (cont.)

Read from Disk

```
SUBROUTINE read_EMULATION_2D_data_structure(filename)

CHARACTER(LEN=*) , INTENT(IN) :: filename
INTEGER:: ierror,fileunit

OPEN(NEWUNIT=fileunit, FILE=filename, STATUS="OLD", &
      ACTION="READ", FORM="UNFORMATTED", IOSTAT=ierror)
IF (ierror /= 0) THEN
    CHKERRQ(ierror, 'read_EMULATION_2D_data_structure: Error &
                      opening file')
ENDIF
READ(fileunit, IOSTAT=ierror)   &
    EMULATION_2D_scattering_structure

CLOSE(fileunit)

END SUBROUTINE read_EMULATION_2D_data_structure
```

EMULATION_2D MPI Broadcast (cont.)

- MPI communication between processes within POST-MODE
 - ▶ At present it is simply by all MPI processes reading the EMULATION_2D data structure from disk (and not only process 0)
 - ▶ A more attractive possibility for the future is the use of custom MPI datatypes (simple prototype under test at present)
 - ★ One MPI call: low latency, readability of the code
 - ★ Maintainability of the code: routines defined on each module to create MPI datatype associated to each derived datatype.

EMULATION_2D MPI Broadcast (cont.)

Fortran Derived DataType

```
! Derived type to test MPI_Type_create_struct
TYPE :: my_derived_type_def
  LOGICAL :: mylogical = .TRUE.
  CHARACTER(len=4) :: mystring = 'hola'
  REAL(KIND=DBL) :: myreal = 1.0_DBL
END TYPE my_derived_type_def

TYPE(my_derived_type_def) :: my_derived_type
```

EMULATION_2D MPI Broadcast (cont.)

MPI datatype creation (MPI_Type_create_struct) (cont.)

```
!! Creamos el MPI Datatype que se use para pasar el tipo &
derivado
!! entre procesos MPI

CALL MPI_GET_ADDRESS(my_derived_type,address(1), ierror)
CALL MPI_GET_ADDRESS(my_derived_type%mylogical,address(2), &
ierror)
CALL MPI_GET_ADDRESS(my_derived_type%mystring,address(3), &
ierror)
CALL MPI_GET_ADDRESS(my_derived_type%myreal,address(4), ierror)

DO i=1,COUNT
    ! MPI-3.0 & former: disp = iaddr(i+1)-iaddr(i)
    displacements(i) = MPI_Aint_diff(address(i+1),address(i))
ENDDO

typelist(1) = MPI_LOGICAL
typelist(2) = MPI_CHARACTER
typelist(3) = MPI_DOUBLE_PRECISION
```

EMULATION_2D MPI Broadcast (cont.)

MPI datatype creation (MPI_Type_create_struct) (cont.)

```
block_lengths(1)=1
block_lengths(2)=4
block_lengths(3)=1

! build the derived data type
call MPI_Type_create_struct(COUNT,block_lengths,displacements,&
    typelist, my_mpi_derived_type_def,ierr)
if (ierr /= 0 ) then
    print *, 'got an error in type create:', ierr
    call MPI_Abort(MPI_COMM_WORLD, ierr, ierr)
endif
```

EMULATION_2D MPI Broadcast (cont.)

Use of MPI datatype in MPI calls

```
! commit it to the system, so it knows we'll use it
! for communication
call MPI_TYPE_COMMIT(my_mpi_derived_type_def)
if (ierr /= 0) then
    print *, 'got an error in type commit:', ierr
    call MPI_Abort(MPI_COMM_WORLD, ierr, ierr)
endif

! use it
call &
MPI_BCAST(my_derived_type, 1, my_mpi_derived_type_def, 0, MPI_COMM_
```

Free MPI datatype created

```
! We free the MPI Datatype created
call MPI_TYPE_FREE(my_mpi_derived_type_def, ierr)
```

MPI Fortran interfaces

USE mpi_f08

```
USE mpi_f08
!! It requires compile-time argument checking with unique MPI
!! handle types and provides techniques to fully solve the
!! optimization problems with nonblocking calls. This is the &
!! only
!! Fortran support method that is consistent with the Fortran
!! standard (Fortran 2008 + TS 29113 and later). This method is
!! highly recommended for all MPI applications.
```

USE mpi

```
USE mpi
!! It requires compile-time argument checking. Handles are &
!! defined
!! as INTEGER. This Fortran support method is inconsistent &
!! with the
!! Fortran standard, and its use is therefore not recommended.
```

MPI Fortran interfaces (cont.)

INCLUDE 'mpif.h'

```
INCLUDE 'mpif.h'  
!! The use of the include file mpif.h is strongly discouraged  
!! starting with MPI-3.0, because this method neither &  
guarantees  
!! compile-time argument checking nor provides sufficient  
!! techniques to solve the optimization problems with &  
nonblocking  
!! calls, and is therefore inconsistent with the Fortran &  
standard.
```