Group Work Project - Econometrics - Group 6 - D

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1. Basic Statistics

This section was contributed by Leila Tugarayeva.

In this section we performed basic analysis of daily JP Morgan historical stock prices. Period under review is February 1, 2018 – December 30, 2018.

All calculations are shown on the pictures below.

Calculations in R:

- 1.1. Average stock value is equal to 106.3496 USD (picture 1).
- 1.2. Daily stock volatility 0.0144 (picture 1).

Annualized stock volatility - 0.2289 (picture 1).

1.3. Daily stock returns (first several values are shown on picture 2).

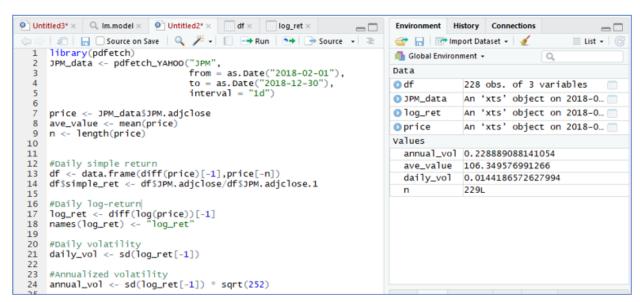
Calculations in Excel

- 1.4. Average stock value 106.3496 USD (picture 3).
- 1.5. Daily stock volatility 0.0144 (picture 4).

Annualized stock volatility – 0.2289 (picture 5).

- 1.6. Daily stock returns (first several values are shown on picture 6).
- 1.7. JP Morgan stock price evolution using a scatter plot (picture 7).
- 1.8. Trendline on the graph in p. 1.7 (picture 7).

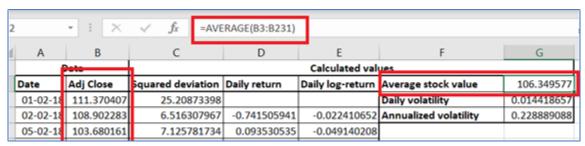
We obtained same results using R and Excel for the average stock value, stock volatility and daily returns. Scatterplot and the trendline exhibit general downwards slope of the closing adjusted prices.



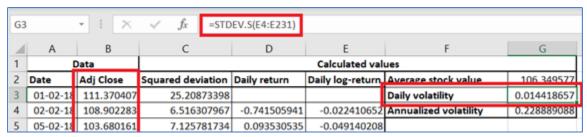
Picture 1 – R code and results of calculations for subsections 1.1, 1.2 and 1.3

•	JPM.adjclose [‡]	JPM.adjclose.1 [‡]	simple_ret	_	log_ret [‡]
2018-02-02	-2.468124	111.37041	-2.216140e-02	2018-02-02	-2.241065e-02
2018-02-05	-5.222122	108.90228	-4.795236e-02	2018-02-05	-4.914021e-02
2018-02-06	3.154243	103.68016	3.042282e-02	2018-02-06	2.996922e-02
2018-02-07	0.724236	106.83440	6.779052e-03	2018-02-07	6.756178e-03
2018-02-08	-4.755188	107.55864	-4.421019e-02	2018-02-08	-4.521725e-02
2018-02-09	2.058357	102.80345	2.002226e-02	2018-02-09	1.982445e-02
2018-02-12	1.619995	104.86181	1.544886e-02	2018-02-12	1.533074e-02
2018-02-13	0.657539	106.48180	6.175130e-03	2018-02-13	6.156142e-03
2018-02-14	2.477654	107.13934	2.312553e-02	2018-02-14	2.286219e-02
2018-02-15	0.457405	109.61700	4.172756e-03	2018-02-15	4.164074e-03
2018-02-16	-0.790932	110.07440	-7.185431e-03	2018-02-16	-7.211370e-03
2018-02-20	0.028580	109.28347	2.615217e-04	2018-02-20	2.614875e-04
2018-02-21	0.457413	109.31205	4.184470e-03	2018-02-21	4.175740e-03
2018-02-22	-0.200112	109.76946	-1.823021e-03	2018-02-22	-1.824684e-03
2018-02-23	2.220352	109.56935	2.026435e-02	2018-02-23	2.006176e-02

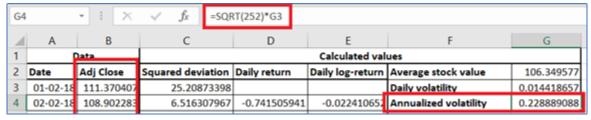
Picture 2 – First several results of subsection 1.3 – simple daily return and log-return



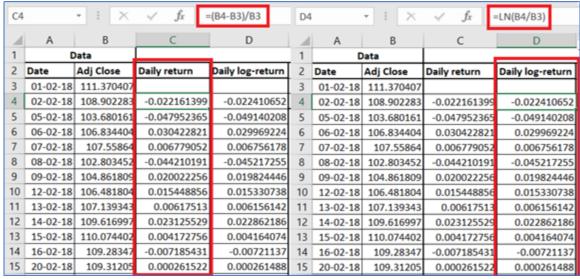
Picture 3 – Average stock value calculations in Excel



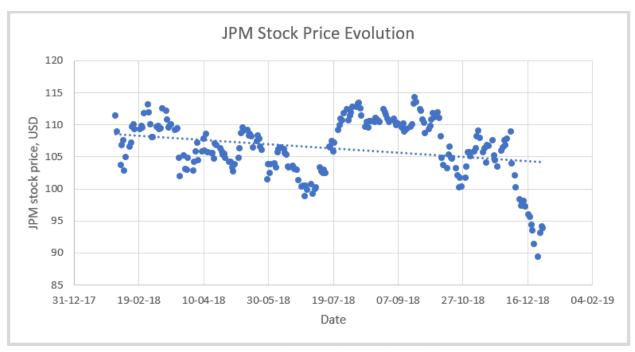
Picture 4 – Daily volatility calculations in Excel



Picture 5 – Annualized volatility calculations in Excel



Picture 6 – First several results of subsection 1.6 – simple daily return (left) and log-return (right)



Picture 7 – JPM stock price evolution and its trend line.

2. Linear Regression

This section was contributed by Leila Tugarayeva.

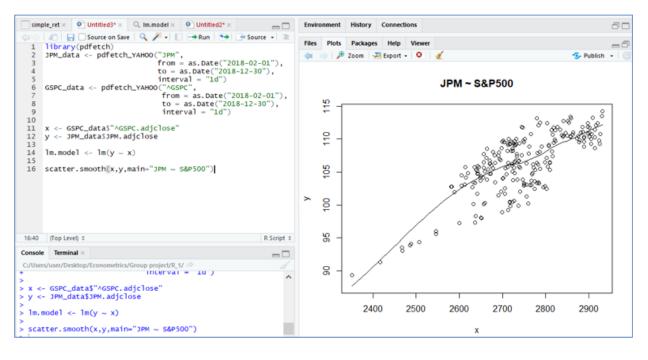
In this section, we implement a two-variable regression in R and Excel.

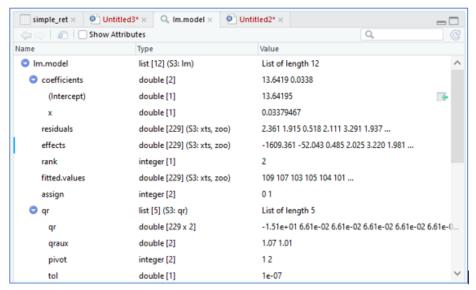
Explained variable: Daily JP Morgan adjusted close prices. **Explanatory variable:** Daily S&P500 adjusted close prices **Period under review:** February 1, 2018 – December 30, 2018

Calculations performed both in R (picture 8) and Excel (picture 9) yielded the following results:

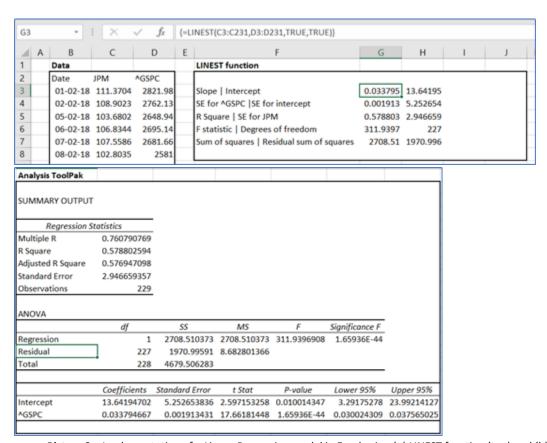
Intercept	13.6419
SE for intercept	5.2527
Slope	0.0338
SE for slope	0.0019
Multiple R	0.760790769
R Square	0.578802594
F-statistic	311.9397
P-value of F-statistic	1.6594E-44

Correlation coefficient of 0.76 indicates that there is relatively strong positive relationship between the two variables. The goodness-of-fit of 0.5788 indicates that around 58% of the dependent variable variance is explained by the model.





Picture 8 – Implementation of a Linear Regression model in R (top) and the resulting model (bottom).



Picture 9 – Implementation of a Linear Regression model in Excel using (a) LINEST function (top) and (b) the Analysis Tool Pak (bottom).

3. Univariate Time Series Analysis

In this section, we develop an ARIMA model for the S&P/Case-Shiller U.S. National Home Price Index.

3.1 Augmented Dickey-Fuller (ADF) Test

This sub-section was contributed by Shiqi Zhang.

Below are the steps taken to use Augmented Dickey-Fuller Test for checking the existence of a unit root in Case-Shiller Index series, using the R language.

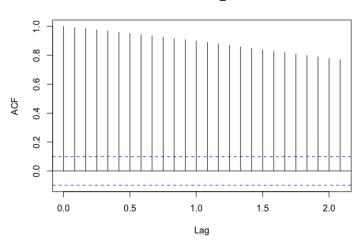
```
library(tidyverse)
library(stats)
library(readxl)
library(tseries)
library(forecast)
library(ggplot2)
CSUSHPINSA <- read_excel("Desktop/CSUSHPINSA.xls",</pre>
                          sheet = "FRED Graph", col_types = c("date",
                                                                "numeric"),
skip = 10)
# view time plots
ggplot(data = CSUSHPINSA, mapping = aes(x = observation_date, y =
CSUSHPINSA)) +
  geom_line(color = "darkblue") +
 labs(x = "month", y = "Home Price")
# convert to Time Series data
Home_Price <- ts(CSUSHPINSA$CSUSHPINSA, start = 1987, frequency = 12)</pre>
# ADF & ACF tests
adf.test(Home Price)
acf(Home_Price)
```

```
> adf.test(Home_Price)

Augmented Dickey-Fuller Test

data: Home_Price
Dickey-Fuller = -2.2758, Lag order = 7, p-value = 0.4607
alternative hypothesis: stationary
```

Series Home_Price



Picture 10 – ACF plot of Home-Shiller Index

The null hypothesis of ADF test is that unit root exists, and the time series is non-stationary. The ADF test on the original Price index time series shows a result of -2.2758 with p-value = 0.4607 which is >0.05 significant level. This suggest that we cannot reject the null hypothesis, hence there exists a unit root in Case-Shiller Index series.

Furthermore, by running ACF test we confirmed the existence of unit root and non-stationarity because autocorrelations are very close to 1 and fading very slowly across many lags.

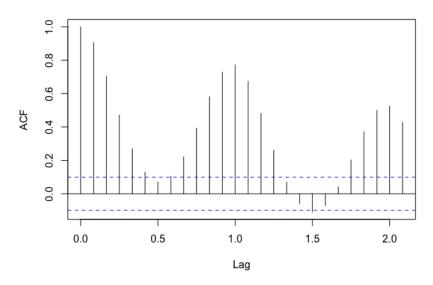
```
# get the first difference of the Home Price Index
Home_Price_Diff <- diff(Home_Price, lag = 1, differences = 1)

# ADF & ACF tests on 1st diff Home_Price
acf(Home_Price_Diff)
adf.test(Home_Price_Diff)</pre>
```

```
> adf.test(Home_Price_Diff)
        Augmented Dickey-Fuller Test

data: Home_Price_Diff
Dickey-Fuller = -2.8115, Lag order = 7, p-value = 0.2345
alternative hypothesis: stationary
```

Series Home_Price_Diff



Picture 11 – ACF plot of differenced Home-Shiller Index

We then proceed to determine the degree of differencing required to transform the original time series to achieve stationarity. The ADF test on the first difference of Price Index shows a result of -2.8115 and p-value = 0.2345, which is still >0.05 significant level. Therefore, we are still unable to reject the null hypothesis and unit root and non-stationarity remain. The ACF test on first difference time series confirms this result. A shock in some months will still have an impact on the current level more than two months into the future.

```
# get the second difference of the Home Price Index
Home_Price_Diff2 <- diff(Home_Price, lag = 1, differences = 2)

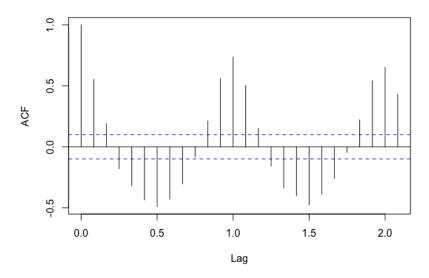
# ADF & ACF tests on 2nd diff Home_Price
acf(Home_Price_Diff2)
adf.test(Home_Price_Diff2)</pre>
```

```
> adf.test(Home_Price_Diff2)
        Augmented Dickey-Fuller Test

data: Home_Price_Diff2
Dickey-Fuller = -16.102, Lag order = 7, p-value = 0.01
alternative hypothesis: stationary

Warning message:
In adf.test(Home_Price_Diff2) : p-value smaller than printed p-value
```

Series Home_Price_Diff2



Picture 12 – ACF plot of twice-differenced Home-Shiller Index

The ADF test on the second difference Price Index yield positive results. DF = -16.102 and p-value < 0.01, which is less than the significant level of 0.05. Hence, we reject the null hypothesis and the transformation was successful in achieving stationarity. ACF results also confirms this.

We will continue to implement an ARIMA model on the Home Price Index in the next section.

3.2 Auto Regressive Integrated Moving Average (ARIMA) model

This sub-section was contributed by Mateusz Iwo Dubaniowski. _____

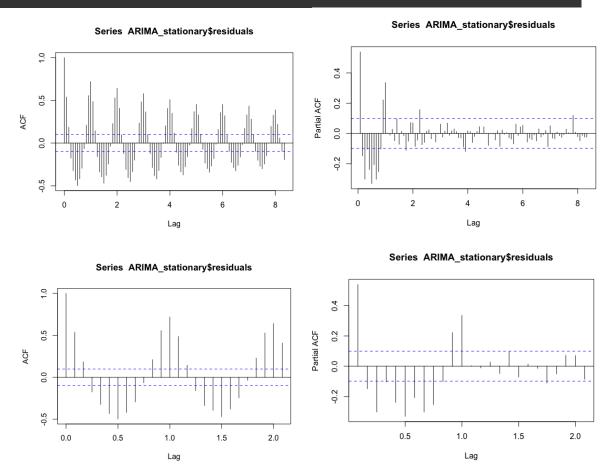
The task was completed in R.

Extensively commented R code can be found below. Respective graphs are placed below the code with short explanations. The graphs are also referred to in the code. Running the code will produce the graphs.

```
#From Part 3.1.3.1, we know that degree of differencing to achieve
stationarity is 2.
#Hence, we analyze residuals at differencing degree of 2, d=2:
ARIMA_stationary <- arima(Data$log, order=c(∅, 2, ∅), method="ML")
#We look at ACF and PACF graphs:
#With 100 lags considered:
acf(ARIMA stationary$residuals, lag.max=100)
pacf(ARIMA_stationary$residuals, lag.max=100)
#Zoom in with default no. of lags:
acf(ARIMA stationary$residuals)
pacf(ARIMA_stationary$residuals)
#From the graph, we see: ACF is a damped sine wave, PACF cuts of at lag-12.
#This suggests AR signature.
q=0
#ARIMA(12, 2, 0)
ARIMA_model <- arima(Data$log, order=c(12, 2, 0), method="ML")
summary(ARIMA_model)
#By looking at summary, we can see that most parameters are significant.
#Errors on average are also small. This is good too.
#We use Box-Pierce test to check if residuals are independently
distributed:
print(Box.test(ARIMA_model$residuals, lag=12))
print(Box.test(ARIMA model$residuals, lag=20))
print(Box.test(ARIMA model$residuals, lag=30))
#They are independently distributed, as we get high p-values and do not
reject the null hypothesis of Box-Pierce test.
#p-values: lag=12: 0.9929, lag=20: 0.7966, lag=30: 0.5233, lag=40: 0.5513,
lag=50: 0.7285
#Finally just to double check, we also look at the graphs of ACF and PACF
of the residuals of the model.
acf(ARIMA model$residuals, lag.max = 100)
pacf(ARIMA_model$residuals, lag.max =100)
#The graphs show that residuals are majorly within significance bands.
#The residuals seem to be randomly independently distributed, and are
negligible. This is good.
grow with increasing order of lag.
```

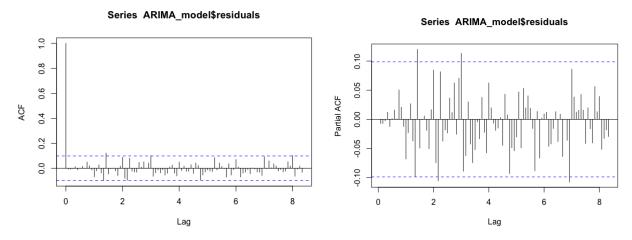
#Overall, this presents a good characteristic of the model.

#The model should perform well with a forecast, and it will be tested with an in-sample forecast to confirm this.



Picture 13 – ACF and PACF plots of ARIMA(0, 2, 0) residuals

Above are plots for ACF and PACF of stationary data i.e. raw data differenced to second degree, i.e. ARIMA(0,2,0).



Picture 14 - ACF and PACF plots of ARIMA(12, 2, 0) residuals

Above are ACF and PACF graphs for residuals of the model. We can see that these are small, and randomly, independently distributed. This is desired, and we confirmed this observation with Box-Pierce test. The residuals also do not seem to increase with increasing lag, which is another desired feature that we can infer from the ACF and PACF graphs of the residuals.

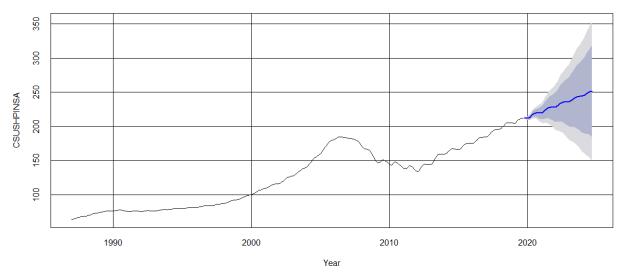
This model also minimizes AIC in the region. It has lower AIC than: ARIMA(13, 2, 0), ARIMA(11, 2, 0), ARIMA(12, 2, 1), ARIMA(12, 2, 2), ARIMA(13, 2, 1), ARIMA(13, 2, 2), ARIMA(11, 2, 1), ARIMA(11, 2, 2). The minimization of AIC shows further that the model is good.

The model should perform reasonably well with a forecast, and it will be tested with an in-sample forecast to confirm this.

3.3 Forecasting

This sub-section was contributed by Nguyen Long Son.

Forecast 60 months ahead



Picture 15 – 5-year out-of-sample forecast

```
# Explore the standard error as a percentage of the predicted value
ARMA_predict <- predict(ARMA_model, n.ahead = 60, se.fit = TRUE)
100*ARMA_predict$se/ARMA_predict$pred</pre>
```

```
Jan
                      Feb
                                 Mar
                                                       May
                                                                  Jun
                                                                             Jul
2019
2020 0.6522653 0.8537091 1.0552280 1.2527889 1.4464249 1.6361502
                                                                      1.8247538
                3.6386046
                           3.9495943
                                     4.2536354
                                                4.5542090
                                                            4.8545999
2021
     3.3211443
                                                                       5.1568204
2022
     7.2640333
                7.6481385
                           8.0176925 8.3769535
                                                 8.7344607
                                                            9.0967029
                                                                      9.4661744
2023 11.9694788 12.3943473 12.7990456 13.1916105 13.5842816 13.9859364 14.4000253
2024 17.1769113 17.6275832 18.0547194 18.4692178 18.8856686 19.3145968 19.7604331
                      Sep
                                 0ct
                                            Nov
2019
                           0.1118006 0.2655155
                                                 0.4553626
2020 2.0120514 2.2086335 2.4370438 2.7046415 3.0054082
2021 5.4623030 5.7789678 6.1180938 6.4843698 6.8714432
2022 9.8445210 10.2368508 10.6492517 11.0824627 11.5277164
2023 14.8281167 15.2731556 15.7375003 16.2179580 16.7030871
2024 20.2246563 20.7083778
```

As we can see from the result, starting from 2020 Sep (i.e., 12 months from the last available value) the standard error starts to exceed 10% of the predicted value. Therefore, the model is suitable for predicting up to 1 year ahead

```
# Now we will test the model using in-sample forecast. We will use a subset
of the available data
# from year 1987 until year Y (1990 < Y < 2010) and forecast H year ahead
(Y + H < 2019)
# after that we compare the predicted value with the available data of the
same period

Y <- 2000 # Year
H <- 5 # Year ahead

tData <- ts(Data$CSUSHPINSA, start = c(1987, 1), frequency = 12)

tData_isp <- window(tData, start = c(1987,1), end = c(Y,12))
# tData_isp is the in-sample data we use to build the model

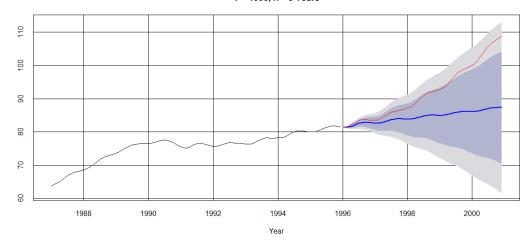
tData_pred <- window(tData, start = c(Y+1,1), end = c(Y+H,12))
# tData_pred is the known data we use to compare with the predicted value
built using tData_isp

ARMA_model <- arima(tData_isp, order = c(12,2,0), method = "ML")

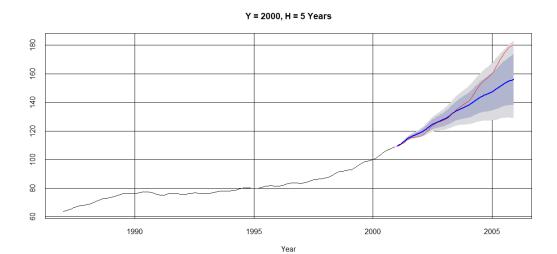
plot(forecast(ARMA_model, h = 12*H), main = "")
lines(tData_pred, col = "red")
#plotting predicted value against known value on the same plot</pre>
```

Below are some results with different Y and H. On the plots below, the red line is the known value while the blue line is the predicted value

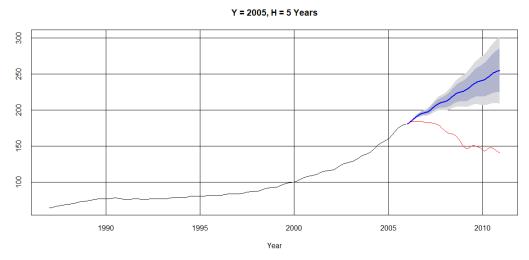
Y = 1995, H = 5 Years



Picture 16 – 5-year in-sample forecast, beginning 1995

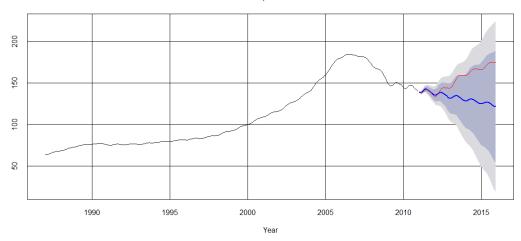


Picture 17 – 5-year in-sample forecast, beginning 2000

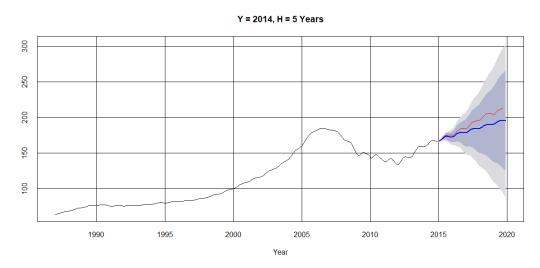


Picture 18 – 5-year in-sample forecast, beginning 2005





Picture 19 – 5-year in-sample forecast, beginning 2010



Picture 20 - 5-year in-sample forecast, beginning 2014

We can see that, if we choose Y from 1990 to 2000, or Y from 2010 to 2014, the predicted value is well in line with the known value within 1 year. However, if choosing Y from 2004 - 2007, the predicted value significantly differs from the real value. The predicted value of housing index continues to rise while the real index drops largely. The reason for that is the housing bubble during 2007 - 2009, the period of large volatility in house prices.

3.4 Suggested improvement exogenous variables

This sub-section was contributed by Matthew Ang. ______

The Case-Shiller Index is a monthly housing price index that measures the value of single-family home price indices using the repeat sales methodology. The index is constructed using a three-month moving average, and attempts to capture robust valuations by e.g. excluding homes with significant physical change, statistical anomalies and high-turnover houses (S&P Global, 2019).

As the housing price index is on an aggregate level, exogenous variables should be on a national level. Indeed, macroeconomic factors like the **job market**, **mortgage market**, and **economic outlook** could be useful in improving our forecast. We dive into each variable in turn:

- **Job market:** Analysis from Zimmermann (2017) suggests *household income growth* leads to higher housing prices. We can also consider *unemployment rate*, a leading indicator to wage growth.
- Mortgage market: While mortgage rates from Freddie Mac could be indicative of housing prices, structural variables such as *percentage of banks tightening mortgage lending* and *mortgage originations growth* are better indicators of the trends underlying the mortgage market.
- **Economic outlook:** Producer and consumer outlook indicators (such as the *Purchasing Managers' Index* and the *Consumer Confidence Index*) illustrate citizens' expectations of the future economy, and in turn affect their willingness to purchase houses.

Other housing indices can also be incorporated. While we expect other housing indices to be coincident, Moody's Case-Shiller Index methodology (2018) illustrated that the *FHFA Price Index* Granger-causes the Case-Shiller Index.

While not exogenous, **seasonal terms** can also be included in the model. This reuslts in a seasonal ARIMA. The ACF plot of the second-differenced Case-Shiller Index exhibits a cyclical pattern in the residuals. Thus, the data exhibits a seasonal structure, where *seasonal dummies* and/or *seasonal autoregressors* can be useful.

Series Home_Price_Diff2

Picture 21 – ACF plot of twice-differenced Home-Shiller Index

Inclusion of such terms changes our implicit assumptions of the data-generating process. It is therefore important that we reexamine ARIMA's p, q parameters when including these seasonal terms.

References

- Carbacho-Burgos, A., & Campbell, B. (2018, September). *Moody's Analytics Case-Shiller Home Price Index Forecast Methodology*. From Moody's Analytics: https://www.economy.com/home/products/samples/case-shiller-methodology.pdf
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