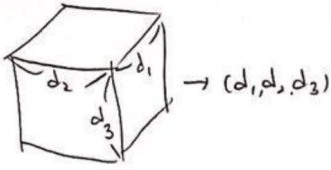
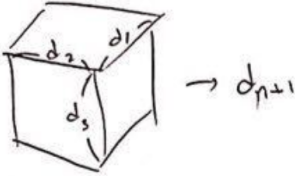


torch.Tensor.size

a.size()	
	Require
	<ul style="list-style-type: none"> $a = (d_1, d_2, \dots, d_k)$
	Guarantees
	<ul style="list-style-type: none"> (d_1, d_2, \dots, d_k)를 튜플로 반환

$$\frac{\sigma \vdash E \Rightarrow e, c}{\sigma \vdash E.size() \Rightarrow shapeToTuple(e), c}$$

a.size(n)	
	Require
	<ul style="list-style-type: none"> $a = (d_1, d_2, \dots, d_k)$ $0 \leq n < k$
	Guarantees
	<ul style="list-style-type: none"> d_{n+1}을 숫자(int)로 반환

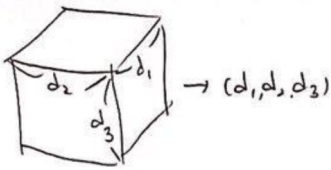
$$\frac{\sigma \vdash E \Rightarrow e, c \quad k = \text{rank}(e) \quad c' = \{(k \geq 1) \wedge (0 \leq n < k)\}}{\sigma \vdash E.size(n) \Rightarrow e[n+1], c \cup c'}$$

torch.tensor

torch.tensor(x)	
	Comment
	numpy나 파이썬 리스트로 선언된 객체를 torch에서 호환가능한 형태로 바꾸는 함수.

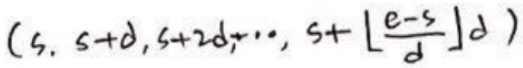
$$\frac{\sigma \vdash E \Rightarrow e, c}{\sigma \vdash \text{tensor}(E) \Rightarrow e, c}$$

torch.Tensor.shape

a.shape	
	Require
	<ul style="list-style-type: none"> $a = (d_1, d_2, \dots, d_k)$
	Guarantees
	<ul style="list-style-type: none"> (d_1, d_2, \dots, d_k)를 튜플로 반환

$$\frac{\sigma \vdash E \Rightarrow e, c}{\sigma \vdash E.shape \Rightarrow shapeToTuple(e), c}$$

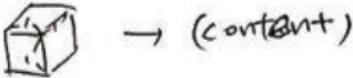
torch.range

torch.range(s, e, d)	
	Require
	<ul style="list-style-type: none">• $d \neq 0$• $(e - s)/d > 0$
	Guarantees
	<ul style="list-style-type: none">• $y = (1 + (e - s)/d)$
	Comment
	<ul style="list-style-type: none">• $(s, s + d, s + 2d, \dots)$를 반환• 기본값은 $s = 0, d = 1$

$$c = \{(d \neq 0) \wedge ((e - s)/d > 0)\}$$
$$\sigma \vdash \text{range}(s, e, d) \Rightarrow (1 + \lfloor (e - s)/d \rfloor), c$$

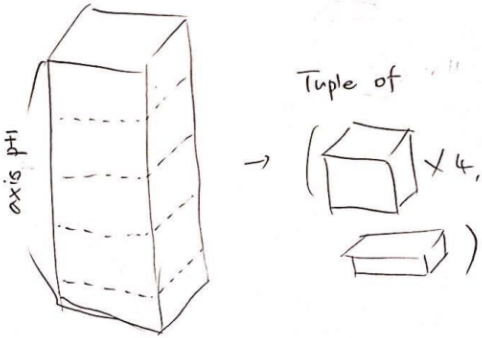
Default: $s = 0, d = 1$

torch.Tensor.item

a.item()	
	Require
	<ul style="list-style-type: none">• $a = ()$ or $a = (1, 1, 1, \dots, 1)$
	Guarantees
	<ul style="list-style-type: none">• $y = e_n$
	Comment
	<ul style="list-style-type: none">• Singular element tensor의 원소(스칼라 타입으로 반환)

$$\sigma \vdash E \Rightarrow e, c$$
$$k = \text{rank}(e)$$
$$c' = \{(\forall i = 1, 2, \dots, k, e[i] = 1)\}$$
$$\frac{}{\sigma \vdash E.\text{item}() \Rightarrow e_n, c \cup c'}$$

torch.split

torch.split(x, n, p=0)	
	Require
	<ul style="list-style-type: none">• $x = (d_1, d_2, \dots, d_k)$• $k \geq 1$• $0 \leq p < k$
	Guarantees
	<ul style="list-style-type: none">• 아래 proof tree와 같이 $p+1$번째 axis가 최대 n개의 원소를 가지도록 $\lceil d_{p+1}/n \rceil$개 튜플 형태로 반환
	Comment
	<ul style="list-style-type: none">• Concat의 반대 역할 함수• Divisible 여부 assert하지 않음• 학습 및 테스트 데이터를 배치단위로 쪼개는 용도로 쓰일 것으로 추측

$$\sigma \vdash E \Rightarrow e, c$$

$$k = \text{rank}(e)$$

$$e_1 = e[1:p]@ (n) @ e[p+2:k]$$

$$e_2 = e[1:p]@ (n) @ e[p+2:k]$$

...

$$e_{l-1} = e[1:p]@ (n) @ e[p+2:k]$$

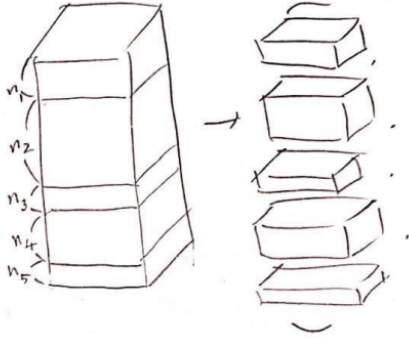
$$e_l = e[1:p]@ (n') @ e[p+2:k] \quad \text{where } e[p+1] = n(l-1) + n', 0 < n' \leq n$$

$$c' = \{(k \geq 1) \wedge (0 \leq p < k)\}$$

$$\sigma \vdash \text{split}(E, n, p=0) \Rightarrow (e_1, e_2, \dots, e_l), c \cup c'$$

l -원소 tuple 형태로 반환

`torch.split(x, [n1, n2, ..., nl], p=0)`



Require

- $|x| = (d_1, d_2, \dots, d_k)$
- $k \geq 1$
- $0 \leq p < k$
- $d_{p+1} = n_1 + n_2 + \dots + n_l$

Guarantees

- 아래 proof tree와 같이 $p+1$ 번째 axis의 크기가 n_1, n_2, \dots, n_l 인 l 개의 텐서 튜플을 반환
- n_i 의 합과 d_{p+1} 이 같은지 assert

$$\sigma \vdash E \Rightarrow e, c$$

$$k = \text{rank}(e)$$

$$e_1 = e[1:p]@ (n_1) @ e[p+2:k]$$

$$e_2 = e[1:p]@ (n_2) @ e[p+2:k]$$

...

$$e_l = e[1:p]@ (n_l) @ e[p+2:k]$$

$$c' = \{(k \geq 1) \wedge (0 \leq p < k) \wedge (e[p+1] = n_1 + n_2 + \dots + n_l)\}$$

$$\sigma \vdash \text{split}(E, [n_1, n_2, \dots, n_l], p=0) \Rightarrow (e_1, e_2, \dots, e_l), c \cup c'$$

l -원소 tuple 형태로 반환

`torch.zeros, torch.rand, torch.randn`

`torch.zeros(t1, t2, ..., tl) or .rand, .randn`

Require

Guarantees

- $|y| = (t_1, t_2, \dots, t_l)$

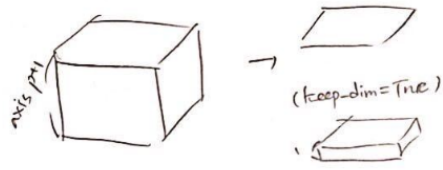
Comment

- 입력받은 형태대로 0, uniformly random, gaussian random 텐서를 반환

$$\forall \text{ft} \in \{\text{zeros}, \text{rand}, \text{randn}\},$$

$$\sigma \vdash \text{ft}(t_1, t_2, \dots, t_l) \Rightarrow (t_1, t_2, \dots, t_l), \emptyset$$

torch.mode

torch.mode(x, n=0, keep_dim=False)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1$ • $0 \leq n < k$
	Guarantees
	<ul style="list-style-type: none"> • $y = z = (d_1, d_2, \dots, d_n, d_{n+2}, \dots, d_k)$인 (y, z) 튜플 반환 • 세 번째 인자 <code>keep_dim</code>이 <code>True</code>이면 $y = z = (d_1, d_2, \dots, d_n, 1, d_{n+2}, \dots, d_k)$
	Comment
	<ul style="list-style-type: none"> • 입력받은 축을 기준으로한 통계적 최빈값 계산 함수

$$\begin{array}{l}
 \sigma \vdash E \Rightarrow e, c \\
 k = \text{rank}(e) \\
 e' = e[1:n] @ e[n+2:k] \\
 c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
 \hline
 \sigma \vdash \text{mode}(E, n = 0) \Rightarrow (e', e'), c \cup c'
 \end{array}$$

tuple 형태로 반환

$$\begin{array}{l}
 \sigma \vdash E \Rightarrow e, c \\
 k = \text{rank}(e) \\
 e' = e[1:n] @ (1) @ e[n+2:k] \\
 c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
 \hline
 \sigma \vdash \text{mode}(E, n = 0, \text{True}) \Rightarrow (e', e'), c \cup c'
 \end{array}$$

tuple 형태로 반환

$$\begin{array}{l}
 \sigma \vdash \text{mode}(E, n) \Rightarrow (e, e), c \\
 \hline
 \sigma \vdash \text{mode}(E, n = 0, \text{False}) \Rightarrow (e, e), c
 \end{array}$$

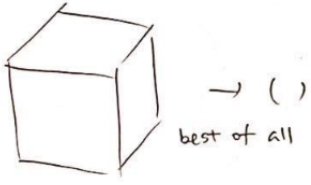
tuple 형태로 반환

torch.randint

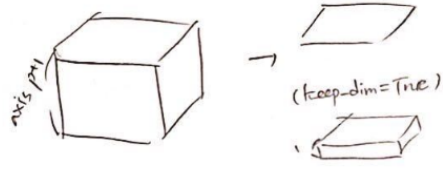
torch.randint(low=0, high, shape)	
	Require
	<ul style="list-style-type: none"> • $low < high$ • <code>shape</code>이 well-defined인 텐서 shape. (스칼라 타입은 X)
	Guarantees
	<ul style="list-style-type: none"> • $y = shape$

$$\begin{array}{l}
 low < high \\
 \hline
 \sigma \vdash \text{randint}(low = 0, high, s) \Rightarrow \text{tupleToShape}(s), \emptyset
 \end{array}$$

torch.max, torch.min

torch.max(x) or .min	
	Require
	Guarantees
	<ul style="list-style-type: none"> • $y = ()$
	Comment
	<ul style="list-style-type: none"> • 주어진 텐서에서 최대/최소 값을 ()-shape 텐서로 반환(스칼라 X)

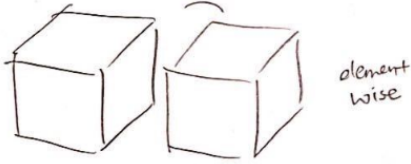
$$\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{\sigma \vdash E \Rightarrow \neg, c}{\sigma \vdash \text{ft}(E) \Rightarrow (), c}$$

torch.max(x, n, keep_dim=False) or .min	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1, 0 \leq n < k$
	Guarantees
	<ul style="list-style-type: none"> • $y = z = (d_1, d_2, \dots, d_n, d_{n+2}, \dots, d_k)$인 (y, z) 튜플 반환 • 세 번째 인자 keep_dim이 True이면 $y = z = (d_1, d_2, \dots, d_n, 1, d_{n+2}, \dots, d_k)$
	Comment
	<ul style="list-style-type: none"> • 주어진 텐서에서 축 상의 최대/최소값과, 그에 해당하는 인덱스 번호를 쌍으로 묶어 튜플로 반환

$$\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{\begin{array}{l} \sigma \vdash E \Rightarrow e, c \\ k = \text{rank}(e) \\ e' = e[1:n]@e[n+2:k] \\ c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \end{array}}{\sigma \vdash \text{ft}(E, n) \Rightarrow (e', e'), c \cup c'} \quad \text{tuple 형태로 반환}$$

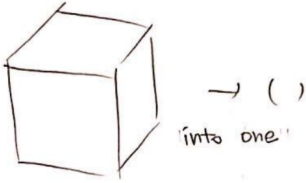
$$\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{\begin{array}{l} \sigma \vdash E \Rightarrow e, c \\ k = \text{rank}(e) \\ e' = e[1:n]@(1)@e[n+2:k] \\ c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \end{array}}{\sigma \vdash \text{ft}(E, n, \text{True}) \Rightarrow (e', e'), c \cup c'} \quad \text{tuple 형태로 반환}$$

$$\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{\sigma \vdash \text{ft}(E, n) \Rightarrow (e, e), c}{\sigma \vdash \text{ft}(E, n, \text{False}) \Rightarrow (e, e), c} \quad \text{tuple 형태로 반환}$$

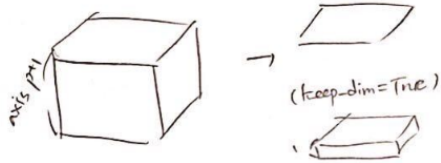
torch.max(x, y) or .min	
	Require
	<ul style="list-style-type: none"> • $\text{broadcastable}(x , y)$
	Guarantees
	<ul style="list-style-type: none"> • $\text{broadcast}(x , y)$
	Comment
	<ul style="list-style-type: none"> • 두 텐서의 elementwise 최대/최소

$$\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{\sigma \vdash E_1 \Rightarrow e_1, c_1 \quad \sigma \vdash E_2 \Rightarrow e_2, c_2}{\sigma \vdash \text{ft}(E_1, E_2) \Rightarrow \text{broadcast}(e_1, e_2), c_1 \cup c_2 \cup \text{broadcastable}(e_1, e_2)}$$

torch.sum, torch.mean

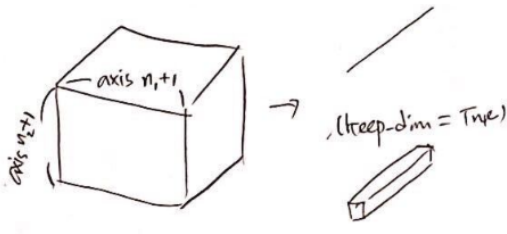
torch.sum(x) or .mean	
	Require
	<ul style="list-style-type: none"> • .mean에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • $y = ()$
	Comment
	<ul style="list-style-type: none"> • 주어진 텐서의 합계/평균값을 ()-shape 텐서로 반환(스칼라 X)

$$\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{\sigma \vdash E \Rightarrow -, c}{\sigma \vdash \text{ft}(E) \Rightarrow (), c}$$

torch.sum(x, n, keep_dim=False) or .mean	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1, 0 \leq n < k$ • .mean에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • $y = (d_1, d_2, \dots, d_n, d_{n+2}, \dots, d_k)$ • 세 번째 인자 keep_dim이 True이면 $y = (d_1, d_2, \dots, d_n, 1, d_{n+2}, \dots, d_k)$
	Comment
	<ul style="list-style-type: none"> • 주어진 텐서에서 축 상의 합/평균을 반환

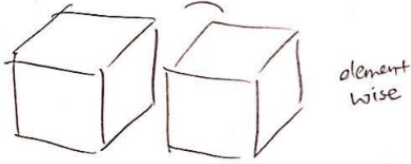
$$\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{\sigma \vdash E \Rightarrow e, c \quad k = \text{rank}(e) \quad e' = e[1:n] @ e[n+2:k] \quad c' = \{(k \geq 1) \wedge (0 \leq n < k)\}}{\sigma \vdash \text{ft}(E, n) \Rightarrow e', c \cup c'}$$

$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
e' = e[1:n] @ (1) @ e[n+2:k] \\
c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{}{\sigma \vdash \text{ft}(E, n, \text{True}) \Rightarrow e', c \cup c'}
\end{array}$$

torch.sum(x, [n1, n2, ..., nl], keep_dim=False) or .mean	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1, 0 \leq n < k$ • .mean에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • $y = (d_{i_1}, d_{i_2}, \dots, d_{i_{k-l}})$ $- 1, 2, \dots, k$에서 $n_1+1, n_2+1, \dots, n_l+1$번째 항이 지워진 shape • 세 번째 인자 <code>keep_dim</code>이 <code>True</code>이면 $n_1+1, n_2+1, \dots, n_l+1$번째 항은 삭제되지 않고 1로 남음
	Comment
	<ul style="list-style-type: none"> • 주어진 텐서에서 여러 축을 통합한 합/평균을 반환

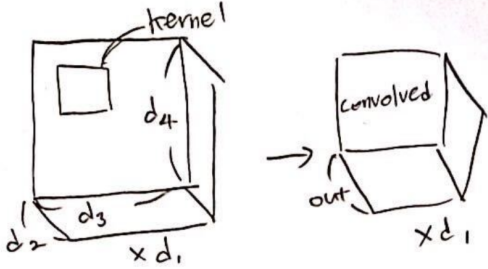
$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
e_1 = \text{if } 0 \in \{n_1, n_2, \dots, n_r\} \text{ then } () \text{ else } (e[1]) \\
e_2 = \text{if } 1 \in \{n_1, n_2, \dots, n_r\} \text{ then } () \text{ else } (e[2]) \\
\vdots \\
e_k = \text{if } k-1 \in \{n_1, n_2, \dots, n_r\} \text{ then } () \text{ else } (e[k]) \\
e' = e_1 @ e_2 @ \dots @ e_k \\
c' = \{(k \geq 1) \wedge (\forall i = 1, 2, \dots, r, 0 \leq n_i < k)\} \\
\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{}{\sigma \vdash \text{ft}(E, (n_1, n_2, \dots, n_r)) \Rightarrow e', c \cup c'}
\end{array}$$

$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
e_1 = \text{if } 0 \in \{n_1, n_2, \dots, n_r\} \text{ then } (1) \text{ else } (e[1]) \\
e_2 = \text{if } 1 \in \{n_1, n_2, \dots, n_r\} \text{ then } (1) \text{ else } (e[2]) \\
\vdots \\
e_k = \text{if } k-1 \in \{n_1, n_2, \dots, n_r\} \text{ then } (1) \text{ else } (e[k]) \\
e' = e_1 @ e_2 @ \dots @ e_k \\
c' = \{(k \geq 1) \wedge (\forall i = 1, 2, \dots, r, 0 \leq n_i < k)\} \\
\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{}{\sigma \vdash \text{ft}(E, (n_1, n_2, \dots, n_r), \text{True}) \Rightarrow e', c \cup c'}
\end{array}$$

torch.sum(x, y) or .mean	
	Require
	<ul style="list-style-type: none"> • $broadcastable(x , y)$ • <code>.mean</code>에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • $broadcast(x , y)$
	Comment
	<ul style="list-style-type: none"> • 두 텐서의 elementwise 합/평균

$$\forall ft \in \{\text{sum}, \text{mean}\}, \quad \frac{\sigma \vdash \text{ft}(E, X) \Rightarrow e, c}{\sigma \vdash \text{ft}(E, X, \text{False}) \Rightarrow e, c}$$

torch.nn.Conv2d

torch.nn.Conv2d(in, out, kernel_size, stride=1, padding=0, dilation=1, groups=1)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, d_3, d_4) \quad (\text{rank} = 4)$ • $d_2 = \text{in}$ • $\text{kernel_size}[0] \leq d_3 + 2 \times \text{padding}[0]$ • $\text{kernel_size}[1] \leq d_4 + 2 \times \text{padding}[1]$ • $\text{groups} \text{in}$ and $\text{groups} \text{out}$
	Guarantees
	<ul style="list-style-type: none"> • (d_1, out, h, w) where.. refers to the proof tree.
	Comment
	<ul style="list-style-type: none"> • Convolution layer입니다. 선배님의 자료를 pytorch의 사용에 맞게 풀어 쓴 것입니다.

$$\sigma \vdash E \Rightarrow e, c$$

$$k = \text{rank}(e)$$

$$h = \left\lfloor \frac{e[3] + 2 \times \text{padding}[0] - \text{dilation}[0] \times (\text{kernel_size}[0] - 1) - 1}{\text{stride}[0]} \right\rfloor + 1$$

$$w = \left\lfloor \frac{e[4] + 2 \times \text{padding}[1] - \text{dilation}[1] \times (\text{kernel_size}[1] - 1) - 1}{\text{stride}[1]} \right\rfloor + 1$$

$$e' = (e[1], \text{out}, h, w)$$

$$c_{dim} = \{(k = 4) \wedge (e[2] = \text{in})\}$$

$$c_w = \{(\text{kernel_size}[0] \leq e[3] + 2 \times \text{padding}[0])\}$$

$$c_h = \{(\text{kernel_size}[1] \leq e[4] + 2 \times \text{padding}[1])\}$$

$$c_{group} = \{(\text{in} \% \text{groups} = 0) \wedge (\text{out} \% \text{groups} = 0)\}$$

$$\sigma \vdash \text{Conv2d}(\text{in}, \text{out}, \text{kernel_size}, \text{stride} = 1, \text{padding} = 0, \text{dilation} = 1, \text{groups} = 1)(E) \Rightarrow e', c \cup c_{dim} \cup c_w \cup c_h \cup c_{group}$$

$\text{kernel_size}, \text{stride}, \text{padding}, \text{dilation}$ 는 가로-세로별 2-tuple로도 들어갈 수 있음

이 경우를 위해 $\text{stride}[0], \text{stride}[1]$ 으로 표기함

만일 stride 가 튜플이 아닌 스칼라라면 $\text{stride}[0]$ 또는 $[1]$ 은 stride 값 자체를 의미

torch.nn.MaxPool2d

torch.nn.MaxPool2d(kernel_size, stride=kernel_size, padding=0, dilation=1)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, d_3, d_4)$ or (d_2, d_3, d_4) • $kernel_size[0] \leq d_3 + 2 \times padding[0]$ • $kernel_size[1] \leq d_4 + 2 \times padding[1]$
	Guarantees
	<ul style="list-style-type: none"> • (d_1, d_2, h, w) or (d_2, h, w) where.. proof tree.
	Comment
	<ul style="list-style-type: none"> • Convolution 다음 activation으로 자주 쓰이는 MaxPool 레이어 입니다.

$$\sigma \vdash E \Rightarrow e, c$$

$$k = \text{rank}(e)$$

$$h_{orig} = e[k - 1]$$

$$w_{orig} = e[k]$$

$$h = \left\lfloor \frac{h_{orig} + 2 \times padding[0] - dilation[0] \times (kernel_size[0] - 1) - 1}{stride[0]} \right\rfloor + 1$$

$$w = \left\lfloor \frac{w_{orig} + 2 \times padding[1] - dilation[1] \times (kernel_size[1] - 1) - 1}{stride[1]} \right\rfloor + 1$$

$$e' = e[1:k - 2] @ (h, w)$$

$$c_{dim} = \{(k = 3 \vee k = 4)\}$$

$$c_w = \{(kernel_size[0] \leq h_{orig} + 2 \times padding[0])\}$$

$$c_h = \{(kernel_size[1] \leq w_{orig} + 2 \times padding[1])\}$$

$$\sigma \vdash \text{MaxPool2d}(kernel_size, stride = kernel_size, padding = 0, dilation = 1)(E) \Rightarrow e', c \cup c_{dim} \cup c_w \cup c_h$$

$kernel_size, stride, padding, dilation$ 는 가로-세로별 2-tuple로도 들어갈 수 있음

이 경우를 위해 $stride[0], stride[1]$ 으로 표기함

만일 $stride$ 가 튜플이 아닌 스칼라라면 $stride[0]$ 또는 $[1]$ 은 $stride$ 값 자체를 의미

torch.nn.MaxPool2d(kernel_size, stride=..., dilation=1, return_indices=False, ceil_mode=False)	
<p><i>return_indices가 True이면, 이전 인덱스로부터 왔는지 튜플로 반환 (같은 shape 두 개)</i></p>	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, d_3, d_4)$ or (d_2, d_3, d_4) • $kernel_size[0] \leq d_3 + 2 \times padding[0]$ • $kernel_size[1] \leq d_4 + 2 \times padding[1]$
	Guarantees
	<ul style="list-style-type: none"> • (d_1, d_2, h, w) or (d_2, h, w) where.. proof tree. • $return_indices$가 <i>True</i>이면 인덱스 번호까지 튜플로 반환 • $ceil_mode$가 <i>True</i>이면 <i>floor</i>대신 <i>ceil</i>로 shape 계산

$$\begin{aligned}
& \sigma \vdash E \Rightarrow e, c \\
& k = \mathbf{rank}(e) \\
& h_{orig} = e[k-1] \\
& w_{orig} = e[k] \\
& h = \left\lfloor \frac{h_{orig} + 2 \times padding[0] - dilation[0] \times (kernel_size[0] - 1) - 1}{stride[0]} \right\rfloor + 1 \\
& w = \left\lfloor \frac{w_{orig} + 2 \times padding[1] - dilation[1] \times (kernel_size[1] - 1) - 1}{stride[1]} \right\rfloor + 1 \\
& h_{ceil} = \left\lceil \frac{h_{orig} + 2 \times padding[0] - dilation[0] \times (kernel_size[0] - 1) - 1}{stride[0]} \right\rceil + 1 \\
& w_{ceil} = \left\lceil \frac{w_{orig} + 2 \times padding[1] - dilation[1] \times (kernel_size[1] - 1) - 1}{stride[1]} \right\rceil + 1 \\
& e' = \mathbf{if } ceil_mode \mathbf{ then } e[1:k-2]@ (h_{ceil}, w_{ceil}) \mathbf{ else } e[1:k-2]@ (h, w) \\
& e_{out} = \mathbf{if } return_indices \mathbf{ then } (e', e') \mathbf{ else } e' \\
& c_{dim} = \{(k = 3 \vee k = 4)\} \\
& c_w = \{(kernel_size[0] \leq e[3] + 2 \times padding[0])\} \\
& c_h = \{(kernel_size[1] \leq e[4] + 2 \times padding[1])\} \\
\hline
& \sigma \vdash \mathbf{MaxPool2d}(kernel_size, stride, padding, dilation, return_indices, ceil_mode)(E) \\
& \Rightarrow e', c \cup c_{dim} \cup c_w \cup c_h
\end{aligned}$$

*return_indices*가 *True*이면 (결과, 인덱스) 튜플 형태로 반환

*ceil_mode*가 *True*이면 *floor*대신 *ceil*함수로 계산