

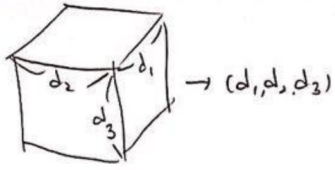
Matmul Layers

Activations

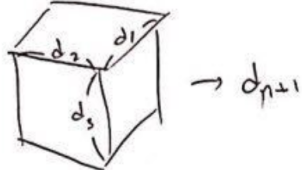
Technique

Wrapper

`torch.Tensor.size`

<code>a.size()</code>	
	Require
	<ul style="list-style-type: none"> $a = (d_1, d_2, \dots, d_k)$
	Guarantees
	<ul style="list-style-type: none"> (d_1, d_2, \dots, d_k)를 튜플로 반환

$$\frac{\sigma \vdash E \Rightarrow e, c}{\sigma \vdash E.size() \Rightarrow shapeToTuple(e), c}$$

<code>a.size(n)</code>	
	Require
	<ul style="list-style-type: none"> $a = (d_1, d_2, \dots, d_k)$ $0 \leq n < k$
	Guarantees
	<ul style="list-style-type: none"> d_{n+1}을 숫자(int)로 반환

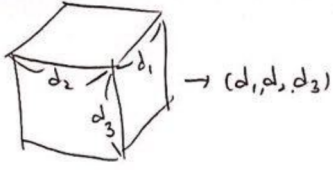
$$\frac{\begin{array}{l} \sigma \vdash E \Rightarrow e, c \\ k = \text{rank}(e) \\ c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \end{array}}{\sigma \vdash E.size(n) \Rightarrow e[n+1], c \cup c'}$$

`torch.tensor`

<code>torch.tensor(x)</code>	
	Comment
	numpy나 파이썬 리스트로 선언된 객체를 torch에서 호환가능한 형태로 바꾸는 함수.

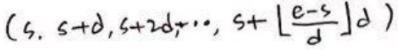
$$\frac{\sigma \vdash E \Rightarrow e, c}{\sigma \vdash \text{tensor}(E) \Rightarrow e, c}$$

torch.Tensor.shape

a.shape	
	Require
	<ul style="list-style-type: none"> $a = (d_1, d_2, \dots, d_k)$
	Guarantees
	<ul style="list-style-type: none"> (d_1, d_2, \dots, d_k)를 튜플로 반환

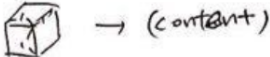
$$\frac{\sigma \vdash E \Rightarrow e, c}{\sigma \vdash E.\text{shape} \Rightarrow \text{shapeToTuple}(e), c}$$

torch.range

torch.range(s, e, d)	
	Require
	<ul style="list-style-type: none"> $d \neq 0$ $(e - s)/d > 0$
	Guarantees
	<ul style="list-style-type: none"> $y = (1 + (e - s)/d)$
	Comment
	<ul style="list-style-type: none"> $(s, s + d, s + 2d, \dots)$를 반환 기본값은 $s = 0, d = 1$

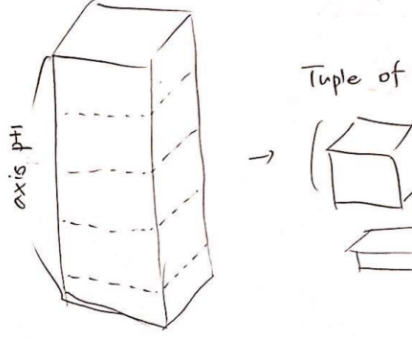
$$\frac{c = \{(d \neq 0) \wedge ((e - s)/d > 0)\}}{\sigma \vdash \text{range}(s, e, d) \Rightarrow (1 + \lfloor (e - s)/d \rfloor), c} \quad \text{Default: } s = 0, d = 1$$

torch.Tensor.item

a.item()	
	Require
	<ul style="list-style-type: none"> $a = ()$ or $a = (1, 1, 1, \dots, 1)$
	Guarantees
	<ul style="list-style-type: none"> $y = e_n$
	Comment
	<ul style="list-style-type: none"> Singular element tensor의 원소(스칼라 타입으로 반환)

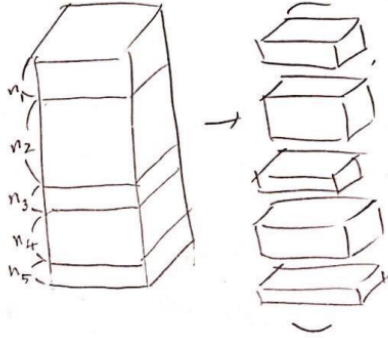
$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
c' = \{(\forall i = 1, 2, \dots, k, e[i] = 1)\} \\
\hline
\sigma \vdash E.\text{item}() \Rightarrow e_n, c \cup c'
\end{array}$$

torch.split

torch.split(x, n, p=0)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1$ • $0 \leq p < k$
	Guarantees
	<ul style="list-style-type: none"> • 아래 proof tree와 같이 $p+1$번째 axis가 최대 n개의 원소를 가지도록 $\lceil d_{p+1}/n \rceil$개 튜플 형태로 반환
	Comment
	<ul style="list-style-type: none"> • Concat의 반대 역할 함수 • Divisible 여부 assert하지 않음 • 학습 및 테스트 데이터를 배치단위로 쪼개는 용도로 쓰일 것으로 추측

$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
e_1 = e[1:p] @ (n) @ e[p+2:k] \\
e_2 = e[1:p] @ (n) @ e[p+2:k] \\
\vdots \\
e_{l-1} = e[1:p] @ (n) @ e[p+2:k] \\
e_l = e[1:p] @ (n') @ e[p+2:k] \quad \text{where } e[p+1] = n(l-1) + n', 0 < n' \leq n \\
c' = \{(k \geq 1) \wedge (0 \leq p < k)\} \\
\hline
\sigma \vdash \text{split}(E, n, p=0) \Rightarrow (e_1, e_2, \dots, e_l), c \cup c'
\end{array}$$

l -원소 tuple 형태로 반환

torch.split(x, [n1, n2, ..., nl], p=0)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1$ • $0 \leq p < k$ • $d_{p+1} = n_1 + n_2 + \dots + n_l$
	Guarantees
	<ul style="list-style-type: none"> • 아래 proof tree와 같이 $p + 1$번째 axis의 크기가 n_1, n_2, \dots, n_l인 l개의 텐서 튜플을 반환 • n_i의 합과 d_{p+1}이 같은지 assert

$\sigma \vdash E \Rightarrow e, c$

$k = \text{rank}(e)$

$e_1 = e[1:p]@(n_1)@e[p+2:k]$

$e_2 = e[1:p]@(n_2)@e[p+2:k]$

...

$e_l = e[1:p]@(n_l)@e[p+2:k]$

$c' = \{(k \geq 1) \wedge (0 \leq x < k) \wedge (e[p+1] = n_1 + n_2 + \dots + n_l)\}$

$\sigma \vdash \text{split}(E, [n_1, n_2, \dots, n_l], p=0) \Rightarrow (e_1, e_2, \dots, e_l), c \cup c'$ l -원소 tuple 형태로 반환

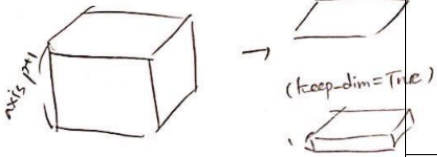
torch.zeros, torch.rand, torch.randn

torch.zeros(t1, t2, ..., tl) or .rand, .randn	
	Require
	Guarantees
	<ul style="list-style-type: none"> • $y = (t_1, t_2, \dots, t_l)$
	Comment
	<ul style="list-style-type: none"> • 입력받은 형태대로 0, uniformly random, gaussian random 텐서를 반환

$\forall ft \in \{\text{zeros}, \text{rand}, \text{randn}\},$

$\overline{\sigma \vdash ft(t_1, t_2, \dots, t_l) \Rightarrow (t_1, t_2, \dots, t_l), \emptyset}$

torch.mode

torch.mode(x, n=0, keep_dim=False)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1$ • $0 \leq n < k$
	Guarantees
	<ul style="list-style-type: none"> • $y = z = (d_1, d_2, \dots, d_n, d_{n+2}, \dots, d_k)$인 (y, z) 튜플 반환 • 세 번째 인자 $keep_dim$이 $True$이면 $y = z = (d_1, d_2, \dots, d_n, 1, d_{n+2}, \dots, d_k)$
	Comment
	<ul style="list-style-type: none"> • 입력받은 축을 기준으로한 통계적 최빈값 계산 함수

$$\begin{array}{l}
 \sigma \vdash E \Rightarrow e, c \\
 k = \text{rank}(e) \\
 e' = e[1:n]@e[n+2:k] \\
 c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
 \hline
 \sigma \vdash \text{mode}(E, n=0) \Rightarrow (e', e'), c \cup c'
 \end{array}
 \quad \text{tuple 형태로 반환}$$

$$\begin{array}{l}
 \sigma \vdash E \Rightarrow e, c \\
 k = \text{rank}(e) \\
 e' = e[1:n]@(1)@e[n+2:k] \\
 c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
 \hline
 \sigma \vdash \text{mode}(E, n=0, True) \Rightarrow (e', e'), c \cup c'
 \end{array}
 \quad \text{tuple 형태로 반환}$$

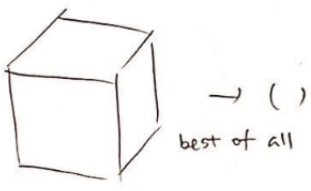
$$\begin{array}{l}
 \sigma \vdash \text{mode}(E, n) \Rightarrow (e, e), c \\
 \hline
 \sigma \vdash \text{mode}(E, n=0, False) \Rightarrow (e, e), c
 \end{array}
 \quad \text{tuple 형태로 반환}$$

torch.randint

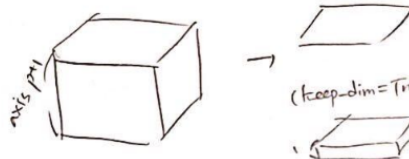
torch.randint(low=0, high, shape)	
	Require
	<ul style="list-style-type: none"> • $low < high$ • $shape$이 well-defined인 텐서 shape. (스칼라 타입은 X)
	Guarantees
	<ul style="list-style-type: none"> • $y = shape$

$$\frac{low < high}{\sigma \vdash \text{randint}(low = 0, high, s) \Rightarrow \text{tupleToShape}(s), \emptyset}$$

torch.max, torch.min

torch.max(x) or .min	
	Require
	Guarantees
	<ul style="list-style-type: none"> • $y = ()$
	Comment <ul style="list-style-type: none"> • 주어진 텐서에서 최대/최소 값을 ()-shape 텐서로 반환(스칼라 X)

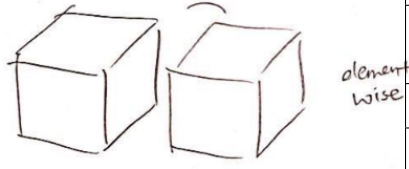
$$\forall ft \in \{\min, \max\}, \quad \frac{\sigma \vdash E \Rightarrow _, c}{\sigma \vdash ft(E) \Rightarrow (), c}$$

torch.max(x, n, keep_dim=False) or .min	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1, 0 \leq n < k$
	Guarantees
	<ul style="list-style-type: none"> • $y = z = (d_1, d_2, \dots, d_n, d_{n+2}, \dots, d_k)$인 (y, z) 튜플 반환 • 세 번째 인자 <code>keep_dim</code>이 <code>True</code>이면 $y = z = (d_1, d_2, \dots, d_n, 1, d_{n+2}, \dots, d_k)$
	Comment <ul style="list-style-type: none"> • 주어진 텐서에서 축 상의 최대/최소값과, 그에 해당하는 인덱스 번호를 쌍으로 묶어 튜플로 반환

$$\forall ft \in \{\min, \max\}, \quad \frac{\begin{array}{l} \sigma \vdash E \Rightarrow e, c \\ k = \text{rank}(e) \\ e' = e[1:n] @ e[n+2:k] \\ c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \end{array}}{\sigma \vdash ft(E, n) \Rightarrow (e', e'), c \cup c'} \quad \text{tuple 형태로 반환}$$

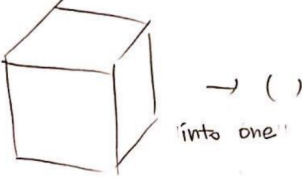
$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
e' = e[1:n]@ (1) @ e[n+2:k] \\
c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{}{\sigma \vdash \text{ft}(E, n, \text{True}) \Rightarrow (e', e'), c \cup c'} \quad \text{tuple 형태로 반환}
\end{array}$$

$$\begin{array}{l}
\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{\sigma \vdash \text{ft}(E, n) \Rightarrow (e, e), c}{\sigma \vdash \text{ft}(E, n, \text{False}) \Rightarrow (e, e), c} \quad \text{tuple 형태로 반환}
\end{array}$$

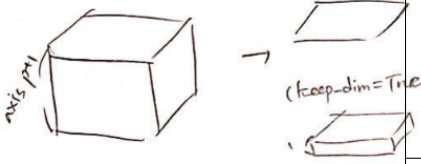
torch.max(x, y) or .min	
	Require
	<ul style="list-style-type: none"> • $\text{broadcastable}(x , y)$
	Guarantees
	<ul style="list-style-type: none"> • $\text{broadcast}(x , y)$
Comment	
<ul style="list-style-type: none"> • 두 텐서의 elementwise 최대/최소 	

$$\begin{array}{l}
\sigma \vdash E_1 \Rightarrow e_1, c_1 \\
\sigma \vdash E_2 \Rightarrow e_2, c_2 \\
\forall \text{ft} \in \{\text{min}, \text{max}\}, \quad \frac{}{\sigma \vdash \text{ft}(E_1, E_2) \Rightarrow \text{broadcast}(e_1, e_2), c_1 \cup c_2 \cup \text{broadcastable}(e_1, e_2)}
\end{array}$$

torch.sum, torch.mean

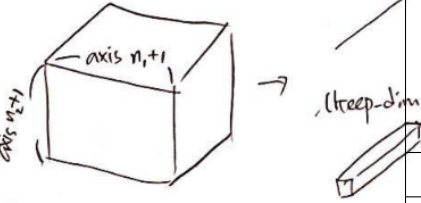
torch.sum(x) or .mean	
	Require
	<ul style="list-style-type: none"> • .mean에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • $y = ()$
Comment	
<ul style="list-style-type: none"> • 주어진 텐서의 합계/평균값을 ()-shape 텐서로 반환(스칼라 X) 	

$$\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{\sigma \vdash E \Rightarrow _, c}{\sigma \vdash \text{ft}(E) \Rightarrow (), c}$$

torch.sum(x, n, keep_dim=False) or .mean	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1, 0 \leq n < k$ • .mean에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • $y = (d_1, d_2, \dots, d_n, d_{n+2}, \dots, d_k)$ • 세 번째 인자 <code>keep_dim</code>이 <code>True</code>이면 $y = (d_1, d_2, \dots, d_n, 1, d_{n+2}, \dots, d_k)$
	Comment
	<ul style="list-style-type: none"> • 주어진 텐서에서 축 상의 합/평균을 반환

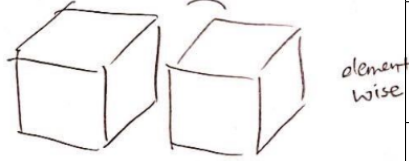
$$\begin{array}{l}
 \sigma \vdash E \Rightarrow e, c \\
 k = \text{rank}(e) \\
 e' = e[1:n] @ e[n+2:k] \\
 c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
 \forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{}{\sigma \vdash \text{ft}(E, n) \Rightarrow e', c \cup c'}
 \end{array}$$

$$\begin{array}{l}
 \sigma \vdash E \Rightarrow e, c \\
 k = \text{rank}(e) \\
 e' = e[1:n] @ (1) @ e[n+2:k] \\
 c' = \{(k \geq 1) \wedge (0 \leq n < k)\} \\
 \forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{}{\sigma \vdash \text{ft}(E, n, \text{True}) \Rightarrow e', c \cup c'}
 \end{array}$$

torch.sum(x, [n1, n2, ..., nl], keep_dim=False) or .mean	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, \dots, d_k)$ • $k \geq 1, 0 \leq n < k$ • .mean에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • $y = (d_{i_1}, d_{i_2}, \dots, d_{i_{k-l}})$ - 1, 2, ..., k에서 $n_1 + 1, n_2 + 1, \dots, n_l + 1$번째 항이 지워진 shape • 세 번째 인자 <code>keep_dim</code>이 <code>True</code>이면 $n_1 + 1, n_2 + 1, \dots, n_l + 1$번째 항은 삭제되지 않고 1로 남음
	Comment
	<ul style="list-style-type: none"> • 주어진 텐서에서 여러 축을 통합한 합/평균을 반환

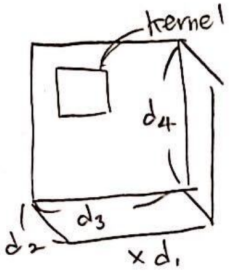
$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
e_1 = \text{if } 0 \in \{n_1, n_2, \dots, n_r\} \text{ then } () \text{ else } (e[1]) \\
e_2 = \text{if } 1 \in \{n_1, n_2, \dots, n_r\} \text{ then } () \text{ else } (e[2]) \\
\dots \\
e_k = \text{if } k-1 \in \{n_1, n_2, \dots, n_r\} \text{ then } () \text{ else } (e[k]) \\
e' = e_1 @ e_2 @ \dots @ e_k \\
c' = \{(k \geq 1) \wedge (\forall i = 1, 2, \dots, r, 0 \leq n_i < k)\} \\
\hline
\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \sigma \vdash \text{ft}(E, (n_1, n_2, \dots, n_r)) \Rightarrow e', c \cup c'
\end{array}$$

$$\begin{array}{l}
\sigma \vdash E \Rightarrow e, c \\
k = \text{rank}(e) \\
e_1 = \text{if } 0 \in \{n_1, n_2, \dots, n_r\} \text{ then } (1) \text{ else } (e[1]) \\
e_2 = \text{if } 1 \in \{n_1, n_2, \dots, n_r\} \text{ then } (1) \text{ else } (e[2]) \\
\dots \\
e_k = \text{if } k-1 \in \{n_1, n_2, \dots, n_r\} \text{ then } (1) \text{ else } (e[k]) \\
e' = e_1 @ e_2 @ \dots @ e_k \\
c' = \{(k \geq 1) \wedge (\forall i = 1, 2, \dots, r, 0 \leq n_i < k)\} \\
\hline
\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \sigma \vdash \text{ft}(E, (n_1, n_2, \dots, n_r), \text{True}) \Rightarrow e', c \cup c'
\end{array}$$

torch.sum(x, y) or .mean	
	Require
	<ul style="list-style-type: none"> • <i>broadcastable</i>(x , y) • .mean에 대해서는 텐서 타입이 floating이어야 함
	Guarantees
	<ul style="list-style-type: none"> • <i>broadcast</i>(x , y)
	Comment
	<ul style="list-style-type: none"> • 두 텐서의 elementwise 합/평균

$$\forall \text{ft} \in \{\text{sum}, \text{mean}\}, \quad \frac{\sigma \vdash \text{ft}(E, X) \Rightarrow e, c}{\sigma \vdash \text{ft}(E, X, \text{False}) \Rightarrow e, c}$$

torch.nn.Conv2d

torch.nn.Conv2d(in, out, kernel_size, stride=1, padding=0, dilation=1, groups=1)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, d_3, d_4) \quad (rank = 4)$ • $d_2 = in$ • $kernel_size[0] \leq d_3 + 2 \times padding[0]$ • $kernel_size[1] \leq d_4 + 2 \times padding[1]$ • $groups in$ and $groups out$
	Guarantees
	<ul style="list-style-type: none"> • (d_1, out, h, w) where.. refers to the proof tree.
	Comment
	<ul style="list-style-type: none"> • Convolution layer입니다. 선배님의 자료를 pytorch의 사용에 맞게 풀어 쓴 것입니다.

$$\sigma \vdash E \Rightarrow e, c$$

$$k = \mathbf{rank}(e)$$

$$h = \left\lfloor \frac{e[3] + 2 \times padding[0] - dilation[0] \times (kernel_size[0] - 1) - 1}{stride[0]} \right\rfloor + 1$$

$$w = \left\lfloor \frac{e[4] + 2 \times padding[1] - dilation[1] \times (kernel_size[1] - 1) - 1}{stride[1]} \right\rfloor + 1$$

$$e' = (e[1], out, h, w)$$

$$c_{dim} = \{(k = 4) \wedge (e[2] = in)\}$$

$$c_w = \{(kernel_size[0] \leq e[3] + 2 \times padding[0])\}$$

$$c_h = \{(kernel_size[1] \leq e[4] + 2 \times padding[1])\}$$

$$c_{group} = \{(in \% groups = 0) \wedge (out \% groups = 0)\}$$

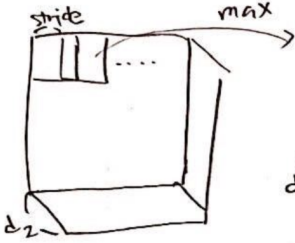
$$\sigma \vdash \mathbf{Conv2d}(in, out, kernel_size, stride = 1, padding = 0, dilation = 1, groups = 1)(E) \Rightarrow e', c \cup c_{dim} \cup c_w \cup c_h \cup c_{gro}$$

$kernel_size, stride, padding, dilation$ 는 가로-세로별 2-tuple로도 들어갈 수 있

이 경우를 위해 $stride[0], stride[1]$ 으로 표기

만일 $stride$ 가 튜플이 아닌 스칼라라면 $stride[0]$ 또는 $[1]$ 은 $stride$ 값 자체를 의

torch.nn.MaxPool2d

torch.nn.MaxPool2d(kernel_size, stride=kernel_size, padding=0, dilation=1)	
	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, d_3, d_4)$ or (d_2, d_3, d_4) • $kernel_size[0] \leq d_3 + 2 \times padding[0]$ • $kernel_size[1] \leq d_4 + 2 \times padding[1]$
	Guarantees
	<ul style="list-style-type: none"> • (d_1, d_2, h, w) or (d_2, h, w) where.. proof tree.
	Comment
	<ul style="list-style-type: none"> • Convolution 다음 activation으로 자주 쓰이는 MaxPool 레이어 입니다.

$$\sigma \vdash E \Rightarrow e, c$$

$$k = \text{rank}(e)$$

$$h_{orig} = e[k-1]$$

$$w_{orig} = e[k]$$

$$h = \left\lfloor \frac{h_{orig} + 2 \times padding[0] - dilation[0] \times (kernel_size[0] - 1) - 1}{stride[0]} \right\rfloor + 1$$

$$w = \left\lfloor \frac{w_{orig} + 2 \times padding[1] - dilation[1] \times (kernel_size[1] - 1) - 1}{stride[1]} \right\rfloor + 1$$

$$e' = e[1:k-2] @ (h, w)$$

$$c_{dim} = \{(k = 3 \vee k = 4)\}$$

$$c_w = \{(kernel_size[0] \leq h_{orig} + 2 \times padding[0])\}$$

$$c_h = \{(kernel_size[1] \leq w_{orig} + 2 \times padding[1])\}$$

$$\sigma \vdash \text{MaxPool2d}(kernel_size, stride = kernel_size, padding = 0, dilation = 1)(E) \Rightarrow e', c \cup c_{dim} \cup c_w \cup c_h$$

$kernel_size, stride, padding, dilation$ 는 가로-세로별 2-tuple로도 들어갈 수 있음

이 경우를 위해 $stride[0], stride[1]$ 으로 표기함

만일 $stride$ 가 튜플이 아닌 스칼라라면 $stride[0]$ 또는 $[1]$ 은 $stride$ 값 자체를 의미

`torch.nn.MaxPool2d(kernel_size, stride=..., dilation=1, return_indices=False, ceil_mode=False)`

<p><i>return_indices가 True이면, 이런 인덱스로부터 값들을 튜플로 반환 (같은 shape 등 ?)</i></p>	Require
	<ul style="list-style-type: none"> • $x = (d_1, d_2, d_3, d_4)$ or (d_2, d_3, d_4) • $kernel_size[0] \leq d_3 + 2 \times padding[0]$ • $kernel_size[1] \leq d_4 + 2 \times padding[1]$
	Guarantees

- (d_1, d_2, h, w) or (d_2, h, w) where.. proof tree.
- *return_indices*가 *True*이면 인덱스 번호까지 튜플로 반환
- *ceil_mode*가 *True*이면 *floor*대신 *ceil*로 shape 계산

$\sigma \vdash E \Rightarrow e, c$

$k = \text{rank}(e)$

$h_{orig} = e[k-1]$

$w_{orig} = e[k]$

$h = \left\lfloor \frac{h_{orig} + 2 \times padding[0] - dilation[0] \times (kernel_size[0] - 1) - 1}{stride[0]} \right\rfloor + 1$

$w = \left\lfloor \frac{w_{orig} + 2 \times padding[1] - dilation[1] \times (kernel_size[1] - 1) - 1}{stride[1]} \right\rfloor + 1$

$h_{ceil} = \left\lceil \frac{h_{orig} + 2 \times padding[0] - dilation[0] \times (kernel_size[0] - 1) - 1}{stride[0]} \right\rceil + 1$

$w_{ceil} = \left\lceil \frac{w_{orig} + 2 \times padding[1] - dilation[1] \times (kernel_size[1] - 1) - 1}{stride[1]} \right\rceil + 1$

$e' = \text{if } ceil_mode \text{ then } e[1:k-2] @ (h_{ceil}, w_{ceil}) \text{ else } e[1:k-2] @ (h, w)$

$e_{out} = \text{if } return_indices \text{ then } (e', e') \text{ else } e'$

$c_{dim} = \{(k = 3 \vee k = 4)\}$

$c_w = \{(kernel_size[0] \leq e[3] + 2 \times padding[0])\}$

$c_h = \{(kernel_size[1] \leq e[4] + 2 \times padding[1])\}$

$\sigma \vdash \text{MaxPool2d}(kernel_size, stride, padding, dilation, return_indices, ceil_mode)(E)$

$\Rightarrow e', c \cup c_{dim} \cup c_w \cup c_h$

*return_indices*가 *True*이면 (결과, 인덱스) 튜플 형태로 반환

*ceil_mode*가 *True*이면 *floor*대신 *ceil*함수로 계산