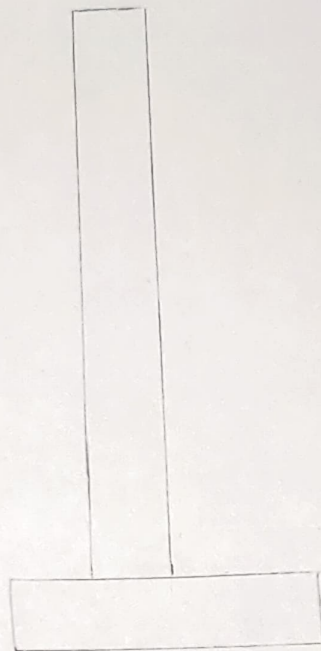
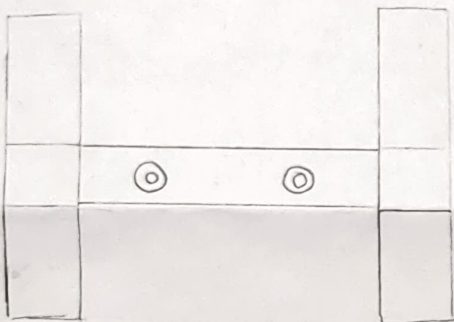


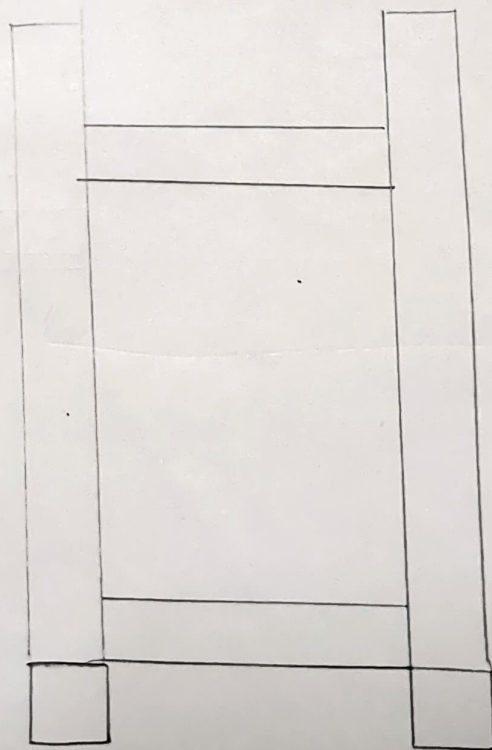
B.V



S.V



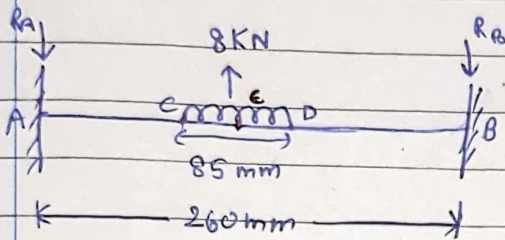
T.V



FV

Design and Development of Portable Universal Testing Machine for Miniature Testing ...

→ Lower Crosshead



$$R_A + R_B = 8000 \text{ N} \quad \text{--- (i)}$$

$$\sum M_A = 0 \quad \text{--- (ii)}$$

From (ii), $-R_B \times (0.26) + 8 \times 10^3 \times (0.13) = 0$
 $\Rightarrow R_B = 4 \times 10^3 \text{ N} \quad \text{--- (iii)}$

From (i) & (iii), $R_A + 4 \times 10^3 \text{ N} = 8 \times 10^3 \text{ N}$
 $\Rightarrow R_A = 4 \times 10^3 \text{ N}$

BM at B = 0

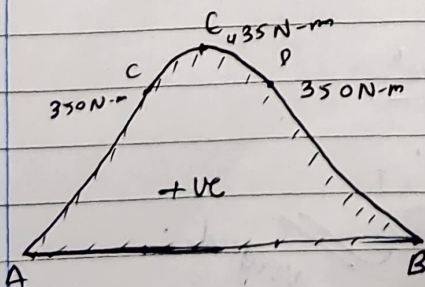
BM at D = $R_B \times (0.0875) = 4000 \times 0.0875$
 $= 350 \text{ Nm}$

BM at C = $R_B \times (0.1725) - 8 \times 10^3 \times (0.0425)$
 $= 350 \text{ Nm}$

BM at A = $R_B \times (0.260) - 8 \times 10^3 \times (0.130)$
 $= 0$

BM at mid point of UDL (say E):
 $= R_B \times (0.130) - \frac{8 \times 10^3 \times (0.02125)}{2}$
 $= 435 \text{ Nm}$

BMD

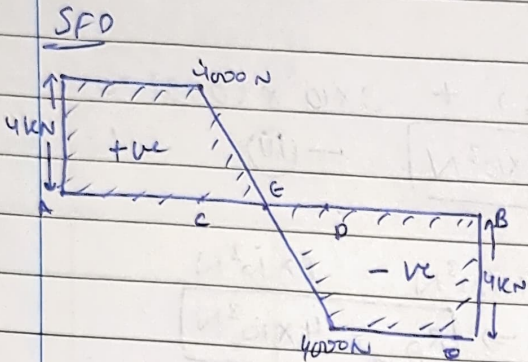


Shear Force at B = -4 kN

at D = -4 kN

at C = -4 + 8 kN
= +4 kN

at A = +4 kN



$$SF_{max} = 4000 \text{ N}$$

at E, BM is extreme

$$(BM)_E = 435 \text{ N-m}$$

So,

$$BM_{max} = 435 \text{ N-m}$$

Assumptions

① $b = d$

② $FOS = 3$

Data

$\sigma_{ys} = 800 \text{ MPa}$

Using Tresca's Theory / Max^m Shear Stress Theory of failure

$$\sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2} = \frac{\sigma_{ys}}{2 \times FOS}$$

$$\begin{cases} \sigma_x = 0 \\ \tau = \frac{SF_{max}}{bcl} = \frac{4 \times 10^3 \text{ N}}{b^2} \end{cases}$$

$$\text{So, } \frac{\sigma_y^2}{4} + \left(\frac{4000}{b^2}\right)^2 = \left(\frac{\sigma_{ys}}{2 \times 3}\right)^2$$

$$\Rightarrow \frac{\sigma_b^2}{4} = \frac{(800 \times 10^6)^2}{36} - \frac{(4000)^2}{b^4}$$

$$\sigma_b^2 = \frac{64 \times 4 \times 10^{16}}{36} - \frac{4 \times 16 \times 10^6}{b^4}$$

$$\sigma_b^2 = \frac{64 \times 10^{16}}{9 b^4} - 64 \times 10^6 \times \frac{4}{b^4}$$

✓ Verified.

$$\frac{-8000}{12(0.26)^2} \left[0.1725^3 (1.04 - 0.5175) - 0.0875^3 (1.04 - \cancel{0.26} 0.2625) \right]$$

$$\begin{array}{r} 0.00268 \\ 0.00216 \\ \hline 0.00052 \end{array}$$

$$M_{FAB} = -21.313 \text{ Nm} = M_A$$

$$M_C = M_A + \text{SFD area from A to C}$$

$$= -21.313 + (4000 \times 0.0875) =$$

$$M_C = 328.687$$

$$(center of beam) \rightarrow M_C + \text{Area from C to E}$$

$$= 328.687 + (0.0425 \times 4000)$$

$$= \boxed{498.687 \text{ Nm}}$$

$$9 \times (498.687)^2 \times 144 = 256 \times 10^{16} \times b^6 - 2304 \times 10^6 b^2$$

$$322.3 \times 10^6 = 256 \times 10^{16} b^6 - 2304 \times 10^6 b^2$$

$$\text{Let } b^2 = x$$

$$322.3 \times 10^6 = 256 \times 10^{16} x^3 - 2304 \times 10^6 x$$

$$256 \times 10^{16} x^3 - 2304 \times 10^6 x - 322.3 \times 10^6 = 0$$

$$x_1 = 5.0179 \times 10^{-4} \text{ m}$$

$$b = 0.0224 \text{ m}$$

$$\boxed{b = 2.24 \text{ cm}} = \boxed{22.4 \text{ mm}}$$

$$V = b^2 \times 320$$

$$\cancel{V = 160457.6 \text{ mm}^3}$$

$$V = 160563.2 \text{ mm}^3$$

$$= 160.5632 \text{ cm}^3$$

$$\rho = 7.75 \text{ g/cm}^3$$

$$= 7.8 \text{ g/cm}^3$$

$$\text{mass weight} = 1.252 \text{ kg}$$

II Lead Screw Design

$$\sigma_x = \frac{4000}{\frac{\pi}{4}d^2} + \frac{(wt/2)}{\frac{\pi}{4}d^2}$$

$$\frac{4}{\pi d^2} \left(4000 + \frac{49.354}{2} \right) = \sigma_n$$

$$\frac{1.27}{d^2} (4024.67) = \sigma_n$$

$$\left[\sigma_n = \frac{5124.37}{d^2} \right]$$

$$\sqrt{\left(\frac{\sigma_n}{2} \right)^2} = \frac{\sigma_{ys}}{2 \times FOS}$$

$$\frac{2562.185}{d^2} = \frac{800 \times 10^6}{2 \times 3}$$

$$d^2 = 19.21 \times 10^{-6} \text{ m}$$

$$d = 4.38 \times 10^{-3} \text{ m}$$

$$d = 4.38 \text{ mm}$$

$$d = 0.438 \text{ cm}$$

Weight of cross head?

$$V = (5)^2 \times 25.8 = 645 \text{ cm}^3$$

$$\rho = 7.8 \text{ g/cm}^3$$

$$m = V \times \rho = 5031 \text{ gm} \\ = 5.031 \text{ Kg}$$

$$Wt = mg = 5.031 \times 9.81$$

$$Wt = 49.354 \text{ N}$$

$$\sigma_1 = \frac{\sigma_x}{FOS}$$

$$\sigma_1 - \sigma_2 = \frac{\sigma_x}{FOS}$$

$$(\sigma_1, \sigma_2)$$

$$\sigma_1 = \frac{\sigma_x + \sigma_y}{2} + \sqrt{\left(\frac{\sigma_x - \sigma_y}{2} \right)^2 + \tau_{xy}^2}$$

$$\sigma_2 = \frac{\sigma_x + \sigma_y}{2} - \sqrt{\left(\frac{\sigma_x - \sigma_y}{2} \right)^2 + \tau_{xy}^2}$$

