# Gap

There are N non-negative integers  $a_1, a_2, \ldots, a_N$  satisfying the following inequality  $0 \le a_1 < a_2 < \cdots < a_N \le 10^{18}$ . Jeehak wants to know the *largest possible* value of  $a_{i+1} - a_i$  where i ranges from 1 to N-1. The input integers will not be given directly to Jeehak's program but will be accessible through a special funtion. See sections Implementation of your selected programming language for details.

#### **Task**

Help Jeehak to implement a function to return the largest possible value of  $a_{i+1} - a_i$  where i ranges from 1 to N-1.

## Implementation for C and C++

You need to implement one function findGap(T, N) that takes the following parameter and returns an integer of type long long:

- T the subtask number (1 or 2)
- N the number of given integers

Your function findGap can call function MinMax(s, t, &mn, &mx) where the first two parameters s and t are integers of type long long and the last two parameters &mn and &mx are pointers to integer variables of type long long, i.e., mn and mx are integer variables of type long long. When MinMax(s, t, &mn, &mx) returns, the variable mn will have the value of smallest  $a_i$  larger than or equal to the value of s and the variable mx will have the value of largest  $a_j$  smaller than or equal to the value of t. In case there are no input integers between s and t (inclusive), then both mn and mx will have the value -1. The value of s should be no larger than the value of t when MinMax is called. If this condition is not met, program will be terminated with a non-zero exit code.

#### **Implementation for Pascal**

You need to implement one function findGap(T, N) that takes the following parameter and returns an integer of type Int64:

- T the subtask number (1 or 2) (Integer type)
- N the number of given integers (LongInt type)

Your function findGap can call procedure MinMax(s, t, mn, mx) where the first two parameters s and t are integers of type Int64 and the last two parameters mn and mx are variables called by reference of type Int64, i.e., mn and mx are integer variables of type Int64. When MinMax(s, t, mn, mx) exits, the variable mn will have the value of smallest  $a_i$  larger than or equal to the value of s and the variable mx will have the value of largest  $a_j$  smaller than or equal to the value of t. In case there are no input integers between s and t (inclusive), then both mn and mx will have the value -1. The value of s should be no larger than the value of t when MinMax is called.

If this condition is not met, the program will be terminated.

#### Implementation for all

In addition to the standard requirements (time and memory limits, no runtime errors, etc), your submission has to achieve the following in order to solve a testcase:

- your function findGap must return the correct answer,
- the cost M associated with calls to function MinMax must not exceed the allowed limit (see section Scoring).

#### Example for C, C++

Consider the case where N=4 and  $a_1=2, a_2=3, a_3=6$ , and  $a_4=8$ .

The answer, which is **3**, can be calculated and thus returned by **findGap** if the following calls to **MinMax** are made:

- MinMax(1, 2, &mn, &mx) is called and mn and mx both have the value 2.
- MinMax(3, 7, &mn, &mx) is called and mn have the value  $\mathbf{3}$  and mx has the value  $\mathbf{6}$ .
- MinMax(8, 9, &mn, &mx) is called and mn and mx both have the value 8.

#### **Example for Pascal**

Consider the case where N=4 and  $a_1=2, a_2=3, a_3=6$ , and  $a_4=8$ .

The answer, which is **3**, can be calculated and thus returned by **findGap** if the following calls to **MinMax** are made:

- MinMax(1, 2, mn, mx) is called and mn and mx both have the value 2.
- MinMax(3, 7, mn, mx) is called and mn have the value 3 and mx has the value 6.
- MinMax(8, 9, mn, mx) is called and mn and mx both have the value 8.

# **Scoring**

In all subtasks the constraint  $2 \le N \le 100,000$  holds.

**Subtask 1 (30 points):** Each call to MinMax will add **1** to M. You will receive the full score for the subtask if  $M \leq \frac{N+1}{2}$  for all test cases.

**Subtask 2 (70 points):** Let k be the number of input integers larger than or equal to s and smaller than or equal to t in a call to MinMax. Each call to MinMax will add k+1 to m. The final score will be calculated by the following rule: Final score for the subtask is the minimum score you received among all test cases. For a test case, the score is m and m

otherwise.

## **Experimentation**

The sample grader which can be downloaded from the scoring system will read data from standard input. The first line of input should contain two integers, subtask number T, and N. The next line should contain N integers in ascending order. The sample grader will write to standard output the value returned by findGap in the first line and the value of M appropriate for the subtask the input test case belongs to.

The following input describes the above example:

2 4

2 3 6 8