7/1/2019 01_worksheet

Worksheet 01~05

In [1]: %config IPCompleter.greedy=True

```
In [2]: from sympy import *
    from sympy.geometry.line import Line
    from sympy.plotting import plot, plot3d
    import matplotlib.pyplot as plt
    %matplotlib inline

    plt.rcParams['figure.figsize'] = 10, 10
    init_printing(use_unicode=True)
    x, y, a, b, k, K, A, B = symbols('x y a b k K A B')
```

1. If
$$a(x + 2) + b(x - 1) = 3$$
 for all x , then $a =$
(A) -1 (B) 0 (C) 1 (D) 2 (E) 3

Solution

My work

$$a(x + 2) + b(x - 1) = 3$$

 $ax + 2a + bx - b = 3$
 $(a + b)x + (2a - b) = 3$
 $a + b = 0$ or $2a - b = 3$

$$\begin{array}{rcl}
+ \left\{ \begin{array}{rcl}
a+b & = & 0 \\
2a-b & = & 3 \\
\hline
3a & = & 3
\end{array} \right.$$

$$a = \frac{3}{3} = 1$$

$$b = -a = -1$$

$$\begin{cases} a = 1 \\ b = -1 \end{cases}$$

Using SymPy

Method 1

```
In [3]: eq = Eq((a*(x+2))+b*(x-1), 3)
eq
```

Out[3]: a(x+2) + b(x-1) = 3

```
In [4]: solve(eq, a, b)
```

Out[4]: $\{a:1, b:-1\}$

Method 2

```
In [5]: solve(((a*(x+2))+b*(x-1)-3), a, b)
```

Out[5]: $\{a:1, b:-1\}$

Answer: (C)

2. If
$$a + b = 2$$
 and $ab = -1$, then $a^2 + b^2 =$
(A) 4 (B) 5 (C) 6 (D) 8 (E) 10

Solution

My Work

$$a^{2} + b^{2} = a^{2} + b^{2} + 2ab - 2ab$$

$$= (a + b)^{2} - 2ab$$

$$= 2^{2} - 2(-1)$$

$$= 6$$

Using SymPy

Out[6]: 6

Answer: (C)

3. C. If the graphs of 3x + 4y = 5 and kx + 2y = 5 are perpendicular, then k = 3

Solution

My Work

• Set $slop_1$ for ℓ_1 : 3x + 4y = 5

$$3x + 4y = 5$$

$$y = \frac{-3x + 5}{4} = -\frac{3}{4}x + \frac{5}{4}$$

$$slop_1 = -\frac{3}{4}$$

• Set $Slop_2$ for ℓ_2 : kx + 2y = 5

$$kx + 2y = 5$$

$$y = \frac{-kx + 5}{2} = -\frac{k}{2}x + \frac{5}{2}$$

$$slop_2 = -\frac{k}{2}$$

• ℓ_1 and ℓ_2 are perpendicular, it means $slop_1*slop_2=-1$

$$(-\frac{3}{4})*(-\frac{k}{2}) = -1$$

 $k = -\frac{2*4}{3} = -\frac{8}{3} \approx -2.67$

Using SymPy

Out[7]: -2.67

Answer: (B)

4. If
$$K = \frac{AB}{A+B}$$
, then $B =$

- $(A) \frac{A}{1 A}$
- $(B) \; \frac{AK}{A-K}$
- $(C) \; \frac{AK}{K-A}$
- $(D) \, \frac{A+K}{A}$
- $(E) \; \frac{A-K}{AK}$

Solution

My Work

$$K = \frac{AB}{A+B}$$

$$K(A+B) = AB$$

$$KA + KB = AB$$

$$KA = (A - K)B$$

$$(A - K)B = KA$$

$$B = \frac{KA}{A - K}$$

By SymPy

Out[8]:
$$\left[\frac{AK}{A-K}\right]$$

Answer: (B)

5. If
$$\log 3 = a$$
, then $\log 90 =$

- $(A) \ 1 + 2a$
- (B) $10a^2$
- (C) 10 + 2a
- (D) 30a
- (E) 10 + 3a

Solution

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My Work

```
\log 90 = \log (9 * 10)
= \log (9) + \log (10)
= \log 3^{2} + 1
= 2 \log 3 + 1
= 2a + 1
```

By SymPy

```
In [9]: expr = 2*log(3)+1
  expr.subs(log(3), a)
```

Out[9]: 2a + 1

Answer: (A)

In []: