7/1/2019 01\_worksheet

#### Worksheet 01~05

In [1]: %config IPCompleter.greedy=True

```
In [2]: from sympy import *
    from sympy.geometry.line import Line
    from sympy.plotting import plot, plot3d
    import matplotlib.pyplot as plt
    %matplotlib inline

    plt.rcParams['figure.figsize'] = 10, 10
    init_printing(use_unicode=True)
    x, y, a, b, k, K, A, B = symbols('x y a b k K A B')
```

1. If 
$$a(x + 2) + b(x - 1) = 3$$
 for all  $x$ , then  $a =$ 
(A) -1 (B) 0 (C) 1 (D) 2 (E) 3

#### **Solution**

#### My work

$$a(x + 2) + b(x - 1) = 3$$
  
 $ax + 2a + bx - b = 3$   
 $(a + b)x + (2a - b) = 3$   
 $a + b = 0$  or  $2a - b = 3$ 

$$\begin{array}{rcl}
+ \left\{ \begin{array}{rcl}
a+b & = & 0 \\
2a-b & = & 3 \\
\hline
3a & = & 3 
\end{array} \right.$$

$$a = \frac{3}{3} = 1$$

$$b = -a = -1$$

$$\begin{cases} a = 1 \\ b = -1 \end{cases}$$

#### **Using SymPy**

#### Method 1

```
In [3]: eq = Eq((a*(x+2))+b*(x-1), 3)
eq
```

Out[3]: a(x+2) + b(x-1) = 3

```
In [4]: solve(eq, a, b)
```

Out[4]:  $\{a:1, b:-1\}$ 

#### Method 2

```
In [5]: solve(((a*(x+2))+b*(x-1)-3), a, b)
```

Out[5]:  $\{a:1, b:-1\}$ 

# Answer: (C)

2. If 
$$a + b = 2$$
 and  $ab = -1$ , then  $a^2 + b^2 =$ 
(A) 4 (B) 5 (C) 6 (D) 8 (E) 10

#### **Solution**

#### My Work

$$a^{2} + b^{2} = a^{2} + b^{2} + 2ab - 2ab$$

$$= (a + b)^{2} - 2ab$$

$$= 2^{2} - 2(-1)$$

$$= 6$$

#### **Using SymPy**

Out[6]: 6

# Answer: (C)

3. C. If the graphs of 3x + 4y = 5 and kx + 2y = 5 are perpendicular, then k =

# Solution

#### My Work

• Set  $slop_1$  for  $_1: 3x + 4y = 5$ 

$$3x + 4y = 5$$

$$y = \frac{-3x + 5}{4} = -\frac{3}{4}x + \frac{5}{4}$$

$$slop_1 = -\frac{3}{4}$$

• Set  $Slop_2$  for  $_2: kx + 2y = 5$ 

$$kx + 2y = 5$$

$$y = \frac{-kx + 5}{2} = -\frac{k}{2}x + \frac{5}{2}$$

$$slop_2 = -\frac{k}{2}$$

•  $_1$  and  $_2$  are perpendicular, it means  $slop_1*slop_2=-1$ 

$$(-\frac{3}{4})*(-\frac{k}{2}) = -1$$
  
 $k = -\frac{2*4}{3} = -\frac{8}{3} \approx -2.67$ 

Out[7]: -2.67

# Answer: (B)

4. If 
$$K = \frac{AB}{A+B}$$
, then  $B =$ 

- $(A) \frac{A}{1 A}$
- $(B) \; \frac{AK}{A-K}$
- $(C) \; \frac{AK}{K-A}$
- $(D) \, \frac{A+K}{A}$
- $(E) \; \frac{A-K}{AK}$

## **Solution**

#### **My Work**

$$K = \frac{AB}{A+B}$$

$$K(A+B) = AB$$

$$KA + KB = AB$$

$$KA = (A - K)B$$

$$(A - K)B = KA$$

$$B = \frac{KA}{A - K}$$

## By SymPy

Out[8]: 
$$\left[\frac{AK}{A-K}\right]$$

# Answer: (B)

5. If 
$$\log 3 = a$$
, then  $\log 90 =$ 

- $(A) \ 1 + 2a$
- (B)  $10a^2$
- (C) 10 + 2a
- (D) 30a
- (E) 10 + 3a

#### **Solution**

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## My Work

```
\log 90 = \log (9 * 10)
= \log (9) + \log (10)
= \log 3^{2} + 1
= 2 \log 3 + 1
= 2a + 1
```

#### By SymPy

```
In [9]: expr = 2*log(3)+1
  expr.subs(log(3), a)
```

Out[9]: 2a + 1

# Answer: (A)

In [ ]: