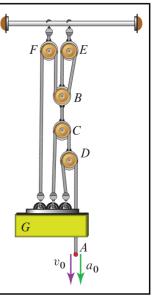
Problem 1

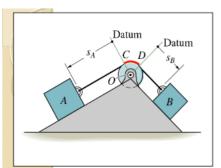
Dynamics 1e 259

Example 2-21

Assuming that all ropes are vertically aligned, determine the velocity and acceleration of the load G if $v_0 = 3$ ft/s and $a_0 = 1$ ft/s².



Recall & Analysis



In this example, think the cable length I_{AB} as subdivided in three:

- the length in contact with the pulley, CD
- the length CA
- the length DB

In this geometry, no matter how A and B move, the *quantity* in contact with the pulley is constant. We could write:

$$s_A + l_{CD} + s_B = l_{AB} = \text{constant}$$

Differentiating with respect to time,



$$\frac{ds_A}{dt} + \frac{ds_B}{dt} = 0 \qquad \dots \text{or} \dots \qquad v_B = -v_A$$

The length of all ropes are constant, so we can set up the equations with them.

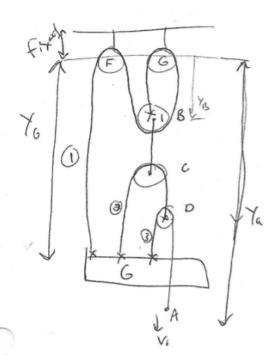
Here, we have three ropes: L_1, L_2, L_3 , L_1 is G - F - B - E - B, L_2 is G - C - D, L_3 is G - D - A. And their lengths are constant, so we can set up the equations with them.

Solution

In case to find v_G and a_G , we should first determine the expression of y_G . But we don't need the explicit form of it, since our final goal is velocity and acceleration.

First we need to set up our coordinates system, where y axis points downwards.

As the lengths of all ropes (L_1,L_2,L_3) don't change over time, we can set up the equations with them and coordinates of all pulleys.



$$egin{cases} L_1 = y_G + 3y_B \ L_2 = (y_G - y_C) + (y_D - y_C) \ L_3 = (y_G - y_D) + (y_A - y_D) \ L_4 = y_C - y_B \end{cases}$$
 $egin{cases} L_1 = y_G + 3y_B \ L_2 = y_G + y_D - 2y_C \ L_3 = y_A + y_G - 2y_D \ L_4 = y_C - y_B \end{cases}$

Do derivative w.r.t. time, we have:

$$\begin{cases} 0 = \dot{y_G} + 3\dot{y}_B \\ 0 = \dot{y_G} + \dot{y_D} - 2\dot{y}_C \\ 0 = \dot{y_G} + \dot{y_A} - 2\dot{y}_D \\ 0 = \dot{y_C} - \dot{y_B} \end{cases}$$

So, $\dot{y_B}=\dot{y_C}$, and plug it into the first and second equation, we have: $\dot{y_D}=-\frac{5}{3}\dot{y_G}$, then plug it into the third equation, we have:

$$\dot{y_G} = -rac{3}{13}\dot{y_A}$$

Placing $\dot{y_a}=v_0=3ft/s$ inside, we have $\dot{y_G}=-0.692ft/s$

As for acceleration, do time derivative, We have

$$\ddot{y_G} = -rac{3}{13}\ddot{y_A}$$

Where $\ddot{y_A}=a_0=aft/s$, and $\ddot{y_G}=0.231ft/s^2$

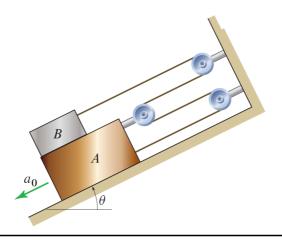
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Problem2

326 Solutions Manual

Example 2-22

Block A is released from rest and starts sliding down the incline with an acceleration $a_0 = 3.7 \,\text{m/s}^2$. Determine the acceleration of block B relative to the incline. Also, determine the time needed for B to move a distance $d = 0.2 \,\text{m}$ relative to A.



Recall & Analysis

$$ec{r}_B = ec{r}_A + ec{r}_{B/A}$$

Same as the previous problem, we can set up the equations with the lengths of all ropes.

Solution

make \vec{x} pointing downwards the slope.

$$L = 3x_A + x_B$$

 $0 = 3\ddot{x}_A + \ddot{x}_B$
 $0 = 3\ddot{x}_A + \ddot{x}_A$

using the fact $\ddot{x}_A=a_0$, we have

$$\vec{a}_B = -3\vec{a}_A = -3a_0 = -11.10m/s^2$$

where the positive direction is pointing downwards the incline.

$$ec{x}_{B/A}(t) = ec{x}_{B/A}(0) + \dot{ec{x}}_{B/A}(0)t + rac{1}{2}ec{a}_{B/A}t^2 \ ec{x}_{B/A}(t) = ec{x}_{B/A}(0) + \dot{ec{x}}_{B/A}(0)t + rac{1}{2}(ec{a}_B - ec{a}_A)t^2 \ ec{x}_{B/A}(t) = ec{x}_{B/A}(0) + \dot{ec{x}}_{B/A}(0)t + rac{1}{2}(-3a_0 - a_0)t^2$$

Since the block is released from rest, we have $\dot{ec{x}}_{B/A}(0)=0$, and $ec{x}_{B/A}(0)=0$, so we have:

$$ec{x}_{B/A}(t) = rac{1}{2}(-4a_0)t^2 \ ec{x}_{B/A}(t) = -2a_0t^2$$

When the distance d=0.2m, we have:

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 $-0.2 = -2a_0t^2$ t = 0.1644s

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