

Suppose I have the function $y=3x+4$.

We may identify the format of the function as the Slop-Intercept Form.

- $y = mx + b$

Find points to Plot on the graph

- The point at which the line crosses the y axis of the graph is known as the **y-intercept**
- At the **y intercept** $x = 0$
 - o $y = 3x+4$
 - o **y intercept** $= 3(0) + 4$
 - o **y intercept** $= 4$
 - o **y intercept** $= (0,4)$
- The point at which the line crosses the x axis of the graph is known as the x-intercept
- At the **x intercept** $y = 0$
 - o $y = 3x+4$
 - o $0 = 3(x \text{ intercept}) + 4$
 - o $-4 = 3(x \text{ intercept})$
 - o $\frac{-4}{3} = x \text{ intercept}$
 - o $x \text{ intercept} = \frac{-4}{3}$
 - o $x \text{ intercept} = (-\frac{4}{3}, 0)$ OR $(-1.333, 0)$
- Plot the points $(0,4)$ and $(-1.333,0)$ and connect the dots forming a line (image on next page)
- Notice that in the formula $y = mx + b$, that when x is 0,
- **b is the y intercept.**
- Now what does m represent. We can solve for m by picking any point on the line and solving. Lets pick the points $(-1, 1)$.
 - o $y = mx + b$
 - o $1 = m(-1) + 4$
 - o $1-4 = m(-1)$
 - o $-3 = m(-1)$
 - o $-3/-1 = m$
 - o $m = 3$, yes it does the original formula was in-fact $y=3x+b$!!!, this math works at any point along the straight line.

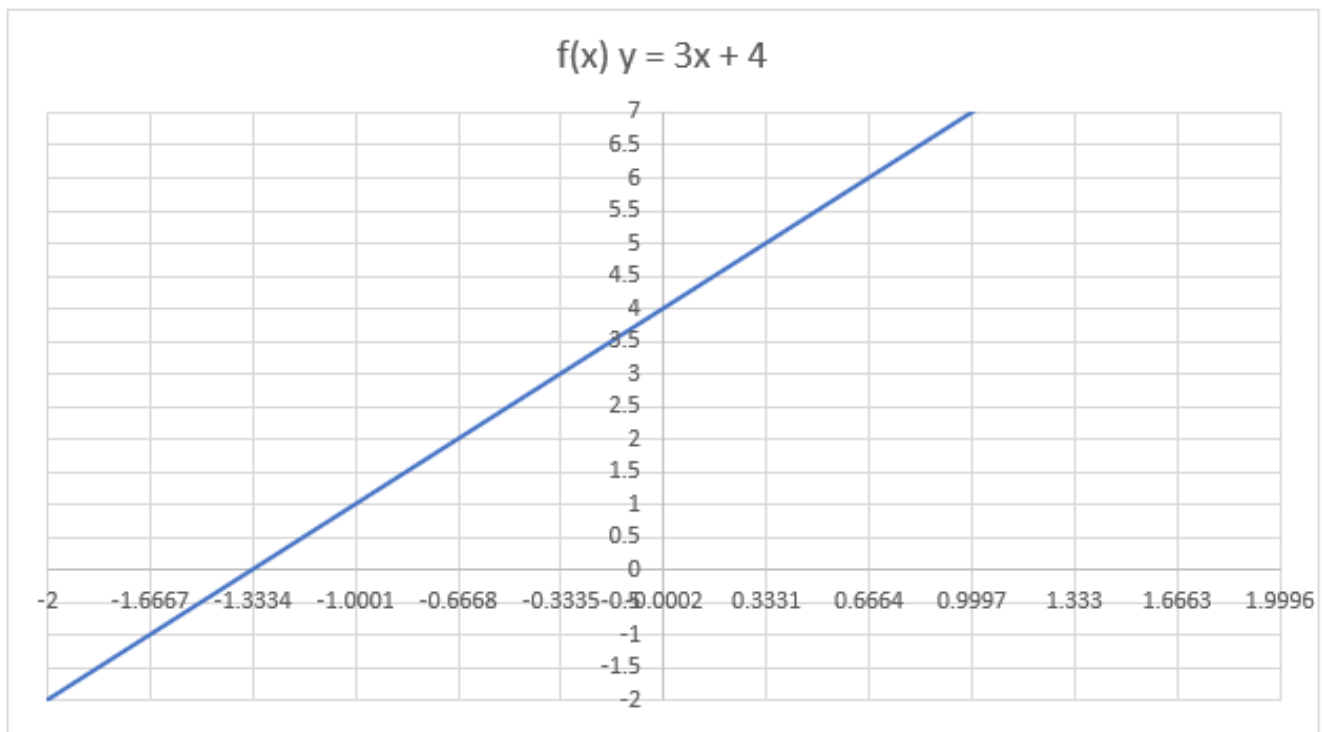
- **m is the slope of the line:**

$$o \quad m = \frac{\text{The Change in } y}{\text{The change in } x} \quad \text{OR} \quad \frac{y_1 - y_2}{x_1 - x_2} \quad \text{OR} \quad \frac{\Delta y}{\Delta x}$$

- o If we compare points (-1, 1) to (0,4)

- We get $m = \frac{1-4}{-1-0} = \frac{-3}{-1} =$
- **m = 3, yes it does!**

- And that is the beauty of the Slope-Intercept form



Imagine yourself questioning, “What does all this, (Analytical Geometry), have to do with intro to calculus”?

I'm glad you asked!

First let's review our original function. $y = 3x + 4$

In calculus we can take the derivative of the function to find $\frac{dy}{dx}$ of the function

- If $y = ax^n$ then $\frac{dy}{dx} = anx^{n-1}$
 - y is y & x is x
 - a is the number in front of x
 - n is the exponent of x
- Now we can rewrite the formula for clarification
 - $y = 3x^1 + 4x^0$ then $\frac{dy}{dx} = 3(1)x^{1-1} + 4(0)(NA)$
 - $\frac{dy}{dx} = 3x^0 + 0$
 - $\frac{dy}{dx} = 3(1) + 0$
 - $\frac{dy}{dx} = 3$
- Now we can see that the derivative $\frac{dy}{dx}$ is equal the slope $\frac{\Delta y}{\Delta x}$
 - $\frac{dy}{dx} = \frac{\Delta y}{\Delta x}$
- Therefore, the Derivative of a function is equal to the slope (instantaneous slope).