

# *Optical force and its applications based on heterosexual phosphorene waveguide*

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**Abstract**—We study the optical properties of face-to-face phosphorene pairs, including propagation length, optical constraint, and gradient force. The symmetric and anti-symmetric plasmonic modes occur on account of the strong anisotropic dispersion of phosphorene. Compared with the anti-symmetric mode, the symmetric mode owns stronger optical constraint and much larger gradient force. Based on the large gradient force and high optical constraint, we also propose a scheme of ultra-small phase shifter. Our results may suggest an opportunity for optical manipulation and development of photonic phosphorene-based devices.

**Keywords**—phosphorene pairs; propagation length; light confinement; gradient force

## I. INTRODUCTION

When light spreads in two parallel waveguides, the optical gradient force will be generated [1]. This force can be either attraction or repulsion. It depends on the relative phase difference of corresponding guided modes in the two waveguides, which is 0 or  $\pi$  [2]. This furnishes a new manner for manipulation of the light in photonic molecule [3-10]. To manipulate the light better, larger optical force is required [11-14]. People can enhance the optical force by employing slow light in photonic crystals [15], the cavity resonance of a high-Q (quality factor) optical resonator, metamaterials and surface plasmon polaritons (SPPs). As a result of the strong optical energy constraint of metallic surface plasmons (MSPs), the optical force can be enhanced substantially.

Lately, it is discovered that the graphene can support the formation and propagation of SPPs in infrared and terahertz ranges [16-24]. Furthermore, as a newly found 2D material, single-layer black phosphorus (BP), the so-called phosphorene, has attracted more and more research interest in recent years owing to its natural semi-conductor properties. In 2014, phosphorene was first synthesized from the bulk BP using a scotch-tape-based microcleavage [25]. Nevertheless, researches on the basic properties and potential applications of phosphorene are in the infancy. In phosphorene, the covalent bonds of the phosphorus atoms make a hexagonal lattice of a folded cellular structure with other three atoms [26]. This

special atomic structure causes extremely anisotropic electronic dispersion and direction-dependent conductivity [27-29]. As a 2D material, a lot of researches have been done on graphene, and compared to graphene, phosphorene may be more suitable for series of applications, such as nano-resonators [30], flexible electronics [31], charge trap memories [32], Terahertz photodetection [33], and amplitude modulation (AM) demodulators [31].

In this paper, we set the two phosphorene layers in three different relative orientations, and the symmetric mode and of the anti-symmetric mode are found in all three configurations. Results show that the symmetric modes exhibit larger optical constraint and gradient force compared to the anti-symmetric modes in BP pairs. More interestingly, we find that the armchair-armchair configuration has the largest propagation length, the zigzag-zigzag configuration has the largest gradient force, while the armchair-zigzag has the largest optical constraint ratio. Compared with the relevant parallel silicon nanobeams, the anisotropy and the optical parameter of the black phosphorus which is related to the thickness provide more tenability to us. Our results may be of benefit to the implementation of nanoscale optical manipulation and facilities based on BP. Finally, we propose an application example of our results as an ultra-small phase shifter.

## II. RESULTS AND DISCUSSIONS

We study the optical properties of separated and face-to-face phosphorene pairs. The gap  $d$  is sandwiched between the separated phosphorene pair. The width and the thickness of the phosphorene are respectively defined as  $w$  and  $t$ . Figure 1(a) shows the electric field y-components of the symmetric mode and of the anti-symmetric mode with  $d = 50$  nm for the armchair direction. From Fig. 1(b), we can see the effective refractive index of the symmetric mode is larger than that of the anti-symmetric mode. Meanwhile, with the gap  $d$  increasing, the inclination of the former becomes larger, which indicates a larger optical field gradient. The propagation lengths ( $1/[2\text{Im}(\beta)]$ ) of the two modes are shown in Fig. 1(c).

Besides, we discuss the optical constraint ratio in the BP pair, which is specified as the ratio of the integrated Poynting

vector  $P_z$  in the regions between and outside the phosphorene layers,

$$\xi = \int_{-d/2}^{d/2} P_z ds / \int_{-\infty}^{\infty} P_z ds \quad (1)$$

The distributions of  $P_z$  in the BP structures can be obtained by using the FEM simulations, and the optical constraint ratio  $\xi$  can be obtained by integrating  $P_z$  vertical to the phosphorene layers.

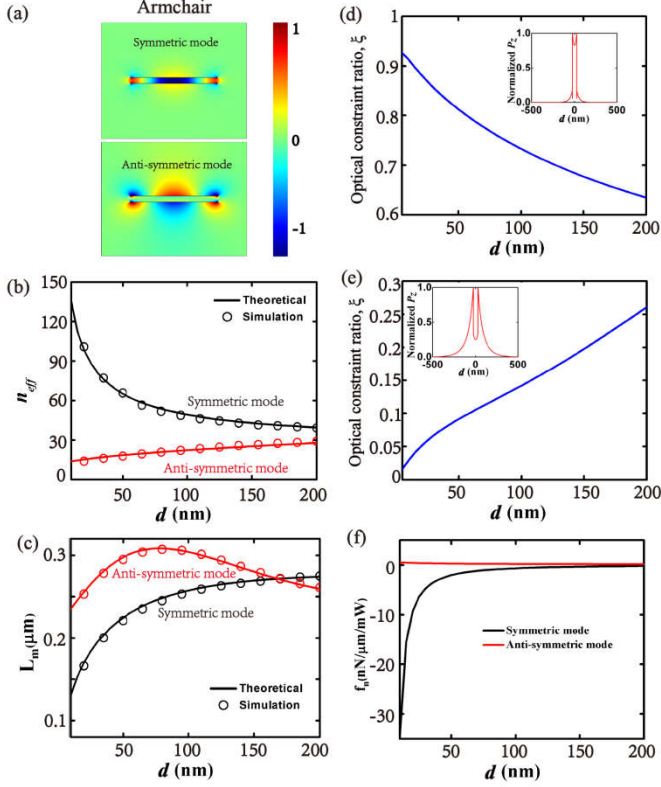


Fig. 1 (a-c) The electric field, effective refractive index, propagation length of the symmetric and anti-symmetric modes for the armchair direction. (d,e) Optical constraint ratio ( $\xi$ ) of the two modes in the BP pair. The inset shows the intensity of normalized  $P_z$ . (f) The gradient force of the two modes.

Through integrating the Maxwell Stress Tensor (MST) around a discretional surface containing the phosphorene pairs, and the gradient force  $f_n$  can be calculated [1]. By defining [26]

$$T_{ij} = \epsilon_0 (E_i E_j - \delta_{ij} E^2 / 2) + \mu_0 (H_i H_j - \delta_{ij} H^2 / 2), \quad (2)$$

where  $\delta$  is the Kronecker delta function, the normalized gradient force along  $y$  direction is defined as

$$f_n = \oint_S T ds \cdot n_y, \quad (3)$$

where  $S$  is the surface of the volume containing the phosphorene pairs and  $n_y$  is the unit vector along the  $y$  direction.

Figures 1(d, e) respectively show the optical constraint ratio of the two modes. Just as the inset of Fig. 1(d), for the

symmetric mode, most light power can be concentrated between the phosphorene pair, while the majority of the light power spreads outside of the BP pair for the anti-symmetric mode as the inset of Fig. 1(e) shows. The strong constraint of light in the waveguides makes the contribution to the formation of giant force [29]. Figure 1(f) shows the gradient force  $f_n$  as functions of the gap  $d$  for the two modes. It can be learnt that in comparison with the symmetric mode, the gradient force  $f_n$  under the anti-symmetric mode can even be ignored.

### III. THE OPTOMECHANICAL APPLICATIONS

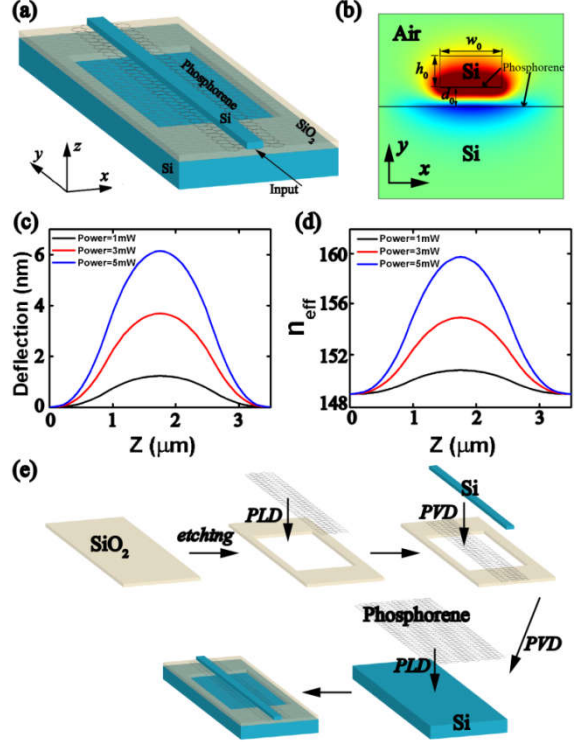


Fig. 2 (a) The 3D schematic illustration of the optomechanical phase shifter. (b) The electric field  $x$ -component at wavelength  $\lambda_0 = 10 \mu\text{m}$ . (c,d) Deflection and the effective refractive index along the free-standing waveguide under the circumstance of different incident power. (e) Schematic illustration of the fabrication procedures of the device.

In virtue of the strong gradient force between the phosphorene sheets, we propose a realization of ultra-small phase shifter working in mid-infrared region. The 3D schematic illustration is shown in Fig. 2(a). Figure 2(b) shows the electric field. Both the phosphorene sheet and nanoribbon are set along the armchair direction. The deflection of the double-clamped beam is shown in Fig. 2(c). The separation of the phosphorene sheet and nanoribbon becomes narrower owing to the change of deflection, and causes the change of the effective refractive index as Fig. 2(d) shows. Figure 2(e) simply shows the fabrication procedures of the device.

Finally, we can obtain the phase shift resulting from different incident power with the following formula:

$$\Delta\phi = \int \beta_1(z) dz - \int \beta_2(z) dz, \quad (4)$$

where  $\Delta\varphi = k_0 \cdot S$  and  $S$  is the region sandwiched by two curves with propagation constants  $\beta_1(z)$  and  $\beta_2(z)$ .

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