Package 'SEMsens'

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An analysis based on structural equation modeling may suffer from the impact of a potential missing confounder that may change its conclusions (Harring, McNeish, & Hancock, 2017). This package is a tool to evaluate the sensitivity of structural equation models to potential missing confounders using the Ant Colony Optimization (ACO; Colorni, Dorigo, & Maniezzo, 1992; Dorigo & Stützle, 2004; Socha & Dorigo, 2008) algorithm. The reference for the current package is: Leite, W., Shen, Z., Marcoulides, K., Fish, C., & Harring, J. (in press). Using ant colony optimization for sensitivity analysis in structural equation modeling. Structural Equation Modeling: A Multidisciplinary Journal.

The current version includes three main functions and they are

- gen.sens.pars function: This function generates a set of required sensitivity parameters according to the rank of object function, with which the method has been developed by Socha & Dorigo (2008).
- sa.aco function: This function automatically performs the search for an omitted confounder in structural equation modeling using the ACO algorithm
- sens.table function: This function provides five summary tables of results produced in the sa.aco function.

Next, we use an example to illustrate how to perform sensitivity analysis in structural equation modeling.

1. Function sa.aco

Given a data set (or variance covariance matrix) and an analytic model, this function searches an omitted confounder to optimize the objective function. *sa.aco* function calls *gen.sens.pars* function to perform the algorithm together.

We need the following information/arguments to perform the search

- data: The data set used for an analysis. If there is no data available, use covariance matrix instead.
- sample.cov: Covariance matrix.
- sample.nobs: Number of observations for covariance matrix.
- model: The analytic model of interest.
- sens.model: Sensitivity analysis model template for structural equation modeling with a phantom variable. This is the model of interest with a phantom variable and sensitivity parameters added. See the example provided.
- opt.fun: Customized or preset object function for optimization.
-

To see more arguments, please run ?sa.aco in R or RStudio.

An exmaple

Load lavaan and SEMsens packages

Sentence_copying~Working_memory

Discourse=~TNL+Expository
Writing=~One day+Castle

Writing~Spelling+Sentence_copying+Discourse

Discourse~Inference+ToM+Vocabulary+Grammar+Working_memory

The example is from: Kim, Y. S. G., & Schatschneider, C. (2017). Expanding the developmental models of writing: A direct and indirect effects model of developmental writing (DIEW). Journal of Educational psychology, 109(1), 35-50.

```
require(lavaan)
require(SEMsens)
set.seed(1)
# STEP 1: Prepare data:
# Lower diagonal correlation matrix in the study by Kim & Schatschneider (2017)
lower = '
1.00
.40 1.00
.40 .64 1.00
.41 .66 .61 1.00
.42 .52 .53 .61 1.00
.34 .50 .46 .53 .48 1.00
.42 .47 .41 .43 .47 .55 1.00
.39 .46 .39 .30 .21 .30 .37 1.00
.24 .31 .30 .31 .26 .32 .27 .56 1.00
.33 .35 .35 .40 .31 .25 .35 .51 .42 1.00
.30 .42 .36 .32 .24 .37 .43 .44 .37 .49 1.00'
# Convert to full covariance matrix
sample.cov = getCov(lower, sds = c(5.64, 14.68, 6.57, 6.07, 3.39, 10.16, 6.11, 4.91, 15.59, 0.96, 0.99),
              names = c("Working_memory",
                         "Vocabulary",
                         "Grammar",
                         "Inference",
                         "ToM",
                         "TNL",
                         "Expository",
                         "Spelling",
                         "Sentence_copying",
                         "One_day",
                         "Castle"))
# STEP 2: Set up analytic model and sensitivity anaysis model
  # The original analytic model
model <-'Vocabulary~Working_memory</pre>
  Grammar~Working_memory
  Inference~Vocabulary+Grammar+Working_memory
  ToM~Vocabulary+Grammar+Working_memory
  Spelling~Working_memory
```

```
Vocabulary~~Grammar
 Grammar~~Sentence_copying
 Vocabulary~~Sentence copying
 Grammar~~Spelling
 Vocabulary~~Spelling
 Inference~~ToM
 Discourse~~Sentence_copying
 Discourse~~Spelling
 Spelling~~Sentence_copying'
 # A sensitivity analysis model template, which additionally includes paths
 # from a phantom variable to a set of variables (= number of sensitivity parameters)
 # in the analytic model.
sens.model <- 'Vocabulary~Working_memory</pre>
 Grammar~Working_memory
 Inference~Vocabulary+Grammar+Working_memory
 ToM~Vocabulary+Grammar+Working_memory
 Spelling~Working_memory
 Sentence_copying~Working_memory
 Discourse~Inference+ToM+Vocabulary+Grammar+Working_memory
 Writing~Spelling+Sentence_copying+Discourse
 Discourse=~TNL+Expository
 Writing=~One_day+Castle
 Vocabulary~~Grammar
 Grammar~~Sentence_copying
 Vocabulary~~Sentence_copying
 Grammar~~Spelling
 Vocabulary~~Spelling
 Inference~~ToM
 Discourse~~Sentence_copying
 Discourse~~Spelling
 Spelling~~Sentence_copying
 Working_memory ~ phantom1*phantom
 Grammar ~ phantom2*phantom
 Vocabulary ~ phantom3*phantom
 ToM ~ phantom4*phantom
 Inference ~ phantom5*phantom
 Spelling ~ phantom6*phantom
 Sentence_copying ~ phantom7*phantom
 Discourse ~ phantom8*phantom
 Writing ~ phantom9*phantom
 phantom =~ 0 # added for mean of zero
 phantom ~~ 1*phantom'
# STEP 3: Set up the paths of interest to be evaluated in sensitivity analysis.
 paths <- 'Vocabulary~Working_memory</pre>
 Grammar~Working memory
 Inference~Vocabulary+Grammar+Working_memory
 ToM~Vocabulary+Grammar+Working memory
 Spelling~Working_memory
```

2. Function sens.tables

sens.tables function can help summarize the sensitivity analysis results. Beyond this function, investigators always can summarize the results by accessing to the results in sa.aco function.

```
my.table <- sens.tables(my.sa)
# Table 1: Summary of the sensitivity analysis for each path
my.table[[1]]</pre>
```

```
##
                                   model.est model.pvalue mean.est.sens
## Discourse~Grammar
                                   0.1003703 2.544519e-01
                                                               0.1052304
                                   0.1245455 2.598216e-02
## Inference~Working memory
                                                               0.1232723
## Writing~Sentence_copying
                                   0.1719948 4.222710e-02
                                                               0.1633071
## Discourse~Working_memory
                                   0.1888038 7.941219e-03
                                                               0.1910799
## Discourse~Inference
                                   0.1943264 3.608645e-02
                                                               0.1920310
## ToM~Working_memory
                                   0.2036364 1.096483e-03
                                                               0.2030261
## Sentence_copying~Working_memory 0.2399999 3.306180e-04
                                                               0.2401460
## ToM~Vocabulary
                                   0.2565656 6.016058e-04
                                                               0.2540932
## Discourse~ToM
                                   0.2610613 1.360093e-03
                                                               0.2545997
## Discourse~Vocabulary
                                   0.2589070 4.345386e-03
                                                               0.2615377
## ToM~Grammar
                                   0.2843434 1.345400e-04
                                                               0.2878169
                                                               0.2894558
## Inference~Grammar
                                   0.2873737 1.336915e-05
## Spelling~Working memory
                                   0.3899999 2.976197e-11
                                                               0.3883753
                                   0.3759830 3.442786e-05
## Writing~Spelling
                                                               0.3886019
## Grammar~Working memory
                                   0.3999999 5.308198e-12
                                                               0.3979180
## Vocabulary~Working_memory
                                   0.3999999 5.308198e-12
                                                               0.3996722
## Inference~Vocabulary
                                   0.4262626 3.005818e-11
                                                               0.4261592
## Writing~Discourse
                                   0.4504663 3.396553e-07
                                                               0.4355599
                                   min.est.sens max.est.sens
## Discourse~Grammar
                                     0.04912704
                                                   0.1774544
                                                    0.1485761
## Inference~Working_memory
                                     0.10477421
## Writing~Sentence_copying
                                     0.05199882
                                                    0.2657367
## Discourse~Working_memory
                                     0.14529692
                                                    0.2331204
## Discourse~Inference
                                     0.15029004
                                                    0.2484007
## ToM~Working_memory
                                     0.17420102
                                                   0.2505132
## Sentence_copying~Working_memory
                                     0.23129571
                                                    0.2588857
## ToM~Vocabulary
                                     0.22454770
                                                    0.3059992
## Discourse~ToM
                                     0.15889535
                                                    0.3087243
## Discourse~Vocabulary
                                     0.23408924
                                                   0.3120485
```

```
## ToM~Grammar
                                   0.21758721
                                                0.3477721
                                   0.23936198
## Inference~Grammar
                                                0.3261455
## Spelling~Working memory
                                  0.36602307
                                                0.4141131
## Writing~Spelling
                                  0.19253896
                                                0.6603765
## Grammar~Working_memory
                                   0.36081953
                                                0.4178667
## Vocabulary~Working memory
                                                0.4096268
                                  0.38836436
## Inference~Vocabulary
                                  0.40745780
                                                0.4641450
## Writing~Discourse
                                   0.16872738
                                                0.5776849
```

Table 2: Summary of the sensitivity parameters my.table[[2]]

```
##
                              mean.phan
                                          min.phan
                                                    max.phan
## Grammar~phantom
                          -0.0255901298 -0.19855864 0.14923981
## Working_memory~phantom -0.0116100689 -0.21192127 0.16501694
## Inference~phantom
                          -0.0059654784 -0.15852757 0.19673890
## Vocabulary~phantom 0.0009162615 -0.07989683 0.06497973
## Sentence_copying~phantom 0.0040785197 -0.05962908 0.11357489
## Discourse~phantom 0.0302226186 -0.12647184 0.24583688
## Spelling~phantom
                         0.0366678782 -0.19658642 0.24672188
## ToM~phantom
                         0.0561965145 -0.23155307 0.49606813
## Writing~phantom
                           0.1132356278 -0.52889818 0.61827105
```

Table 3: The sensitivity parameters lead to the minimum coefficient for each my.table[[3]]

```
##
                                  Working_memory~phantom Grammar~phantom
## Vocabulary~Working_memory
                                            -0.211921268
                                                             -0.18415235
## Grammar~Working_memory
                                            -0.211921268
                                                             -0.18415235
## Inference~Vocabulary
                                            0.002184957
                                                            -0.19855864
## Inference~Grammar
                                            -0.110365605
                                                            -0.15220596
                                                            -0.04988583
## Inference~Working_memory
                                            -0.167003237
## ToM~Vocabulary
                                           -0.030085236
                                                            -0.12832087
## ToM~Grammar
                                           -0.110365605
                                                           -0.15220596
## ToM~Working memory
                                            -0.167003237
                                                             -0.04988583
## Spelling~Working memory
                                                           -0.01137375
                                            0.152931730
## Sentence_copying~Working_memory
                                           -0.155173551
                                                            0.08682558
## Discourse~Inference
                                            0.044223231
                                                            -0.06027779
## Discourse~ToM
                                            -0.034499544
                                                            -0.13024128
## Discourse~Vocabulary
                                             0.051240582
                                                           -0.06690173
## Discourse~Grammar
                                            -0.120907356
                                                            0.14923981
## Discourse~Working_memory
                                             0.165016936
                                                             -0.01754155
## Writing~Spelling
                                             0.048004382
                                                             -0.02181512
## Writing~Sentence_copying
                                             0.072626707
                                                              0.11784237
## Writing~Discourse
                                             0.072626707
                                                              0.11784237
                                  Vocabulary~phantom ToM~phantom
                                       -0.054220461 0.22938668
## Vocabulary~Working_memory
## Grammar~Working memory
                                        -0.054220461 0.22938668
## Inference~Vocabulary
                                      -0.030296701 0.20987620
## Inference~Grammar
                                        0.051535666 -0.21725287
## Inference~Working_memory
                                        -0.030364651 -0.22577041
## ToM~Vocabulary
                                        0.003831129 0.27028636
## ToM~Grammar
                                         0.051535666 -0.21725287
```

```
## ToM~Working_memory
                                         -0.030364651 -0.22577041
## Spelling~Working_memory
                                          0.049251697 -0.11155276
## Sentence copying~Working memory
                                         -0.011157983 0.28069048
## Discourse~Inference
                                         -0.035560127 -0.08384902
## Discourse~ToM
                                         -0.079896827 0.49606813
## Discourse~Vocabulary
                                          0.062516527 -0.20132409
## Discourse~Grammar
                                         -0.013843073 -0.18486429
                                         -0.017716484 -0.19524466
## Discourse~Working memory
## Writing~Spelling
                                         -0.064244453 0.14765876
## Writing~Sentence_copying
                                         -0.023845171 0.27678824
## Writing~Discourse
                                         -0.023845171 0.27678824
                                   Inference~phantom Spelling~phantom
                                          0.11169709
## Vocabulary~Working_memory
                                                            0.11546808
## Grammar~Working_memory
                                          0.11169709
                                                            0.11546808
## Inference~Vocabulary
                                          0.12562746
                                                            0.15355763
## Inference~Grammar
                                         -0.15852757
                                                            0.18009840
## Inference~Working_memory
                                                           -0.05282820
                                         -0.15021823
## ToM~Vocabulary
                                          0.06902098
                                                            0.02181626
## ToM~Grammar
                                         -0.15852757
                                                            0.18009840
## ToM~Working memory
                                         -0.15021823
                                                           -0.05282820
## Spelling~Working_memory
                                         -0.09672352
                                                            0.17233148
## Sentence copying~Working memory
                                         -0.07186973
                                                            0.14099539
## Discourse~Inference
                                          0.12930466
                                                            0.19994834
## Discourse~ToM
                                          0.14159692
                                                            0.24672188
                                                           -0.10090585
## Discourse~Vocabulary
                                         -0.02696729
## Discourse~Grammar
                                         -0.00735754
                                                            0.01807200
## Discourse~Working_memory
                                         -0.14682888
                                                            0.06457722
## Writing~Spelling
                                         -0.09555416
                                                            0.20318504
## Writing~Sentence_copying
                                          0.16155105
                                                           -0.18908332
## Writing~Discourse
                                          0.16155105
                                                           -0.18908332
##
                                   Sentence_copying~phantom Discourse~phantom
## Vocabulary~Working_memory
                                                  0.08826528
                                                                    0.24583688
## Grammar~Working_memory
                                                  0.08826528
                                                                    0.24583688
## Inference~Vocabulary
                                                  0.05705421
                                                                    0.10077127
## Inference~Grammar
                                                 -0.02665071
                                                                   -0.08985596
## Inference~Working memory
                                                -0.02098849
                                                                   -0.08802815
## ToM~Vocabulary
                                                -0.03303541
                                                                    0.07442881
## ToM~Grammar
                                                -0.02665071
                                                                   -0.08985596
## ToM~Working memory
                                                 -0.02098849
                                                                   -0.08802815
## Spelling~Working_memory
                                                -0.05756797
                                                                   -0.02387311
## Sentence copying~Working memory
                                                -0.05369555
                                                                    0.10337791
## Discourse~Inference
                                                 0.02990099
                                                                    0.13270063
## Discourse~ToM
                                                  0.11357489
                                                                    0.17226044
## Discourse~Vocabulary
                                                                    0.08786791
                                                -0.05219069
## Discourse~Grammar
                                                -0.02210510
                                                                    0.13456352
## Discourse~Working_memory
                                                  0.01005041
                                                                    0.13126727
## Writing~Spelling
                                                  0.05236181
                                                                    0.05720109
## Writing~Sentence_copying
                                                                    0.08586779
                                                  0.05069574
## Writing~Discourse
                                                  0.05069574
                                                                    0.08586779
                                   Writing~phantom
## Vocabulary~Working_memory
                                       -0.12163204
## Grammar~Working_memory
                                       -0.12163204
## Inference~Vocabulary
                                        0.08132341
## Inference~Grammar
                                       -0.28691915
```

```
## Inference~Working_memory
                                0.36057655
## ToM~Vocabulary
                                0.41217884
## ToM~Grammar
                              -0.28691915
## ToM~Working_memory
                               0.36057655
## Discourse~Inference
                                0.11588441
## Discourse~ToM
                                0.21492898
## Discourse~Vocabulary
                                0.07410964
## Discourse~Grammar
                                0.08140368
## Discourse~Working_memory
                                0.30589957
## Writing~Spelling
                                0.61827105
## Writing~Sentence_copying
                                0.60389707
## Writing~Discourse
                                0.60389707
```

Table 4: The sensitivity parameters lead to the maximum coefficient for each path my.table[[4]]

##		Working_memory~phantom	${\tt Grammar~phantom}$
##	Vocabulary~Working_memory	-0.176061341	0.03160994
##	<pre>Grammar~Working_memory</pre>	-0.120907356	0.14923981
##	Inference~Vocabulary	-0.110365605	-0.15220596
##	Inference~Grammar	0.002184957	-0.19855864
##	<pre>Inference~Working_memory</pre>	0.165016936	-0.01754155
##	ToM~Vocabulary	-0.110365605	-0.15220596
##	ToM~Grammar	0.002184957	-0.19855864
##	ToM~Working_memory	-0.155173551	0.08682558
##	Spelling~Working_memory	-0.176061341	0.03160994
##	${\tt Sentence_copying~Working_memory}$	-0.211921268	-0.18415235
##	Discourse~Inference	-0.014368362	-0.02012266
	Discourse~ToM	-0.120907356	
##	Discourse~Vocabulary	-0.110365605	-0.15220596
	Discourse~Grammar	-0.211921268	
	Discourse~Working_memory	-0.211921268	
	Writing~Spelling	0.072626707	
	Writing~Sentence_copying	-0.138008251	
##	Writing~Discourse	-0.167003237	
##		Vocabulary~phantom ToM	_
	Vocabulary~Working_memory	0.055384298 0	
	Grammar~Working_memory		.1848643
	Inference~Vocabulary		.2172529
	Inference~Grammar		.2098762
	Inference~Working_memory		. 1952447
	ToM~Vocabulary		.2172529
	ToM~Grammar		.2098762
	ToM~Working_memory		. 2806905
	Spelling~Working_memory		. 1217345
	Sentence_copying~Working_memory		.2293867
	Discourse~Inference		.2029898
	Discourse~ToM		.1848643
	Discourse~Vocabulary		.2172529
	Discourse~Grammar		.2293867
	Discourse~Working_memory		.2293867
##	Writing~Spelling	-0.023845171 0	.2767882

```
## Writing~Sentence_copying
                                           0.046036288 -0.1319380
## Writing~Discourse
                                          -0.030364651 -0.2257704
                                    Inference~phantom Spelling~phantom
##
## Vocabulary~Working_memory
                                          -0.07860246
                                                            0.14301228
## Grammar~Working memory
                                          -0.00735754
                                                            0.01807200
## Inference~Vocabulary
                                          -0.15852757
                                                            0.18009840
## Inference~Grammar
                                           0.12562746
                                                            0.15355763
## Inference~Working memory
                                          -0.14682888
                                                            0.06457722
## ToM~Vocabulary
                                          -0.15852757
                                                            0.18009840
## ToM~Grammar
                                           0.12562746
                                                            0.15355763
## ToM~Working_memory
                                          -0.07186973
                                                            0.14099539
## Spelling~Working_memory
                                          -0.07860246
                                                            0.14301228
## Sentence_copying~Working_memory
                                           0.11169709
                                                            0.11546808
## Discourse~Inference
                                                            0.02211563
                                          -0.14558684
## Discourse~ToM
                                          -0.00735754
                                                            0.01807200
## Discourse~Vocabulary
                                          -0.15852757
                                                            0.18009840
## Discourse~Grammar
                                                            0.11546808
                                           0.11169709
## Discourse~Working memory
                                           0.11169709
                                                            0.11546808
## Writing~Spelling
                                           0.16155105
                                                           -0.18908332
## Writing~Sentence copying
                                           0.02871137
                                                            0.13761525
## Writing~Discourse
                                          -0.15021823
                                                           -0.05282820
##
                                    Sentence_copying~phantom Discourse~phantom
                                                                    0.02093407
## Vocabulary~Working_memory
                                                 -0.02140238
## Grammar~Working memory
                                                 -0.02210510
                                                                    0.13456352
## Inference~Vocabulary
                                                 -0.02665071
                                                                   -0.08985596
## Inference~Grammar
                                                  0.05705421
                                                                    0.10077127
## Inference~Working_memory
                                                  0.01005041
                                                                    0.13126727
## ToM~Vocabulary
                                                                   -0.08985596
                                                 -0.02665071
## ToM~Grammar
                                                  0.05705421
                                                                    0.10077127
## ToM~Working_memory
                                                 -0.05369555
                                                                     0.10337791
## Spelling~Working_memory
                                                 -0.02140238
                                                                    0.02093407
## Sentence_copying~Working_memory
                                                  0.08826528
                                                                     0.24583688
## Discourse~Inference
                                                  0.02421053
                                                                     0.04225371
## Discourse~ToM
                                                 -0.02210510
                                                                     0.13456352
## Discourse~Vocabulary
                                                 -0.02665071
                                                                   -0.08985596
## Discourse~Grammar
                                                  0.08826528
                                                                    0.24583688
## Discourse~Working memory
                                                  0.08826528
                                                                    0.24583688
## Writing~Spelling
                                                  0.05069574
                                                                    0.08586779
## Writing~Sentence_copying
                                                 -0.05513577
                                                                    0.05556959
## Writing~Discourse
                                                 -0.02098849
                                                                   -0.08802815
##
                                    Writing~phantom
## Vocabulary~Working memory
                                       -0.19619587
## Grammar~Working memory
                                         0.08140368
## Inference~Vocabulary
                                       -0.28691915
## Inference~Grammar
                                        0.08132341
## Inference~Working_memory
                                        0.30589957
## ToM~Vocabulary
                                        -0.28691915
## ToM~Grammar
                                         0.08132341
## ToM~Working_memory
                                        -0.08211608
## Spelling~Working_memory
                                        -0.19619587
## Sentence_copying~Working_memory
                                        -0.12163204
## Discourse~Inference
                                        0.44354405
## Discourse~ToM
                                        0.08140368
## Discourse~Vocabulary
                                        -0.28691915
```

```
## Discourse~Grammar -0.12163204
## Discourse~Working_memory -0.12163204
## Writing~Spelling 0.60389707
## Writing~Sentence_copying 0.57441944
## Writing~Discourse 0.36057655
```

Table 5: The sensitivity parameters lead to change in significance for each path my.table[[5]]

##		n value	n change	d Working_mer	morv~nhantom
	Discourse~Grammar	2.544519e-01	-	_	-0.21192127
	Writing~Sentence_copying	4.222710e-02			-0.08329305
	Discourse~Inference	3.608645e-02			-0.05379439
	Inference~Working_memory	2.598216e-02			-0.17606134
	Writing~Discourse	3.396553e-07			0.07262671
	Vocabulary~Working_memory	5.308198e-12	N.		NA
	Grammar~Working_memory	5.308198e-12	N.	-	NA
	Inference~Vocabulary	3.005818e-11	N	A	NA
	Inference~Grammar	1.336915e-05	N	A	NA
##	ToM~Vocabulary	6.016058e-04	N	A	NA
	ToM~Grammar	1.345400e-04	N	A	NA
##	ToM~Working_memory	1.096483e-03	N	A	NA
	Spelling~Working_memory	2.976197e-11	N	A	NA
	Sentence_copying~Working_memory	3.306180e-04	N	A	NA
##	Discourse~ToM	1.360093e-03	N.	A	NA
##	Discourse~Vocabulary	4.345386e-03	N.	A	NA
##	Discourse~Working_memory	7.941219e-03	N.	A	NA
##	Writing~Spelling	3.442786e-05	N	A	NA
##		Grammar~phant	om Vocabui	lary~phantom	ToM~phantom
##	Discourse~Grammar	-0.1841523	55	-0.05422046	0.22938668
##	Writing~Sentence_copying	0.0094026	67	0.02524991	-0.06890207
##	Discourse~Inference	-0.1130469	28	-0.01528202	0.25107119
##	Inference~Working_memory	0.0316099			0.12173446
	Writing~Discourse	0.1178423			0.27678824
	Vocabulary~Working_memory		NA	NA	NA
	Grammar~Working_memory		NA	NA	NA
	Inference~Vocabulary		NA	NA	NA
	Inference~Grammar		NA	NA	NA
	ToM~Vocabulary		NA	NA	NA
	ToM~Grammar		NA	NA	NA
	ToM~Working_memory		NA	NA	NA
	Spelling~Working_memory		NA NA	NA	NA
	Sentence_copying~Working_memory		NA NA	NA	NA
	Discourse Yearhulann		NA MA	NA NA	NA
	Discourse Vocabulary		NA NA	NA NA	NA NA
	Discourse~Working_memory		NA NA	NA NA	
##	Writing~Spelling	Inference~pha			NA
	Discourse~Grammar	0.1116		0.1154681	
	Writing~Sentence_copying	0.1506		-0.1555506	
	Discourse~Inference	0.1006		0.1050860	
	Inference~Working_memory	-0.0786		0.1430123	
	Writing~Discourse	0.1615		-0.1890833	
	Vocabulary~Working_memory	0.1010	NA	NA	
				-111	

```
## Grammar~Working_memory
                                                    NA
                                                                     NA
## Inference~Vocabulary
                                                    NΑ
                                                                     NΑ
## Inference~Grammar
                                                    NA
                                                                     NA
## ToM~Vocabulary
                                                    NΑ
                                                                     NΑ
## ToM~Grammar
                                                    NA
                                                                     NA
## ToM~Working_memory
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                                                                     NA
## Spelling~Working memory
                                                    NA
                                                                     NA
## Sentence copying~Working memory
                                                                     NA
                                                    NΑ
## Discourse~ToM
                                                    NΔ
                                                                     NA
## Discourse~Vocabulary
                                                    NA
                                                                     NA
## Discourse~Working_memory
                                                    NA
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## Writing~Spelling
                                                    NA
                                                                     NA
                                    Sentence_copying~phantom Discourse~phantom
## Discourse~Grammar
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## Writing~Sentence_copying
                                                  -0.05921337
                                                                    0.001210933
## Discourse~Inference
                                                   0.05885676
                                                                    0.132617696
## Inference~Working_memory
                                                  -0.02140238
                                                                    0.020934066
## Writing~Discourse
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                                                   0.05069574
## Vocabulary~Working_memory
                                                                              NA
                                                           NΑ
## Grammar~Working memory
                                                           NA
                                                                              NA
## Inference~Vocabulary
                                                           MΔ
                                                                              NΑ
## Inference~Grammar
                                                           NA
                                                                              NA
## ToM~Vocabulary
                                                                              NA
                                                           MΔ
## ToM~Grammar
                                                           NA
                                                                              NA
## ToM~Working_memory
                                                           NΑ
                                                                              NΑ
## Spelling~Working memory
                                                           NA
                                                                              NA
## Sentence_copying~Working_memory
                                                           NΑ
                                                                              NA
## Discourse~ToM
                                                                              NA
## Discourse~Vocabulary
                                                                              NA
                                                           NΑ
## Discourse~Working_memory
                                                           NA
                                                                              NA
## Writing~Spelling
                                                           NA
                                                                              NA
##
                                    Writing~phantom
## Discourse~Grammar
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## Writing~Sentence_copying
                                          0.2289633
## Discourse~Inference
                                          0.2951056
## Inference~Working memory
                                         -0.1961959
## Writing~Discourse
                                          0.6038971
## Vocabulary~Working_memory
                                                  NΔ
## Grammar~Working memory
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## Inference~Vocabulary
                                                  NA
## Inference~Grammar
                                                  NA
## ToM~Vocabulary
                                                  NA
## ToM~Grammar
                                                  NA
## ToM~Working_memory
                                                  NA
## Spelling~Working_memory
                                                  NA
## Sentence_copying~Working_memory
                                                  NA
## Discourse~ToM
                                                  NA
## Discourse~Vocabulary
                                                  NA
## Discourse~Working_memory
                                                  NA
## Writing~Spelling
                                                  NA
```