

This is our goal:

for(y : <logicalFormula> <- x)P

P|Q

$a_{TBarb} = \text{for}(y <- x)[y]1 \mid x!(\varnothing^2) - \text{comm}(x, \backslash y.[y]1, \varnothing^2) \rightarrow [y]1\{ @\varnothing^2 / y \}$

$a_{TSend} = \text{for}(y <- x)[y]1 \mid x!(Q) - \text{comm}(x, \backslash y.[y]1, Q) \rightarrow [y]1\{ @\varnothing^2 / y \}$

$a_{TRecv} = \text{for}(y <- x)P \mid x!(\varnothing^2) - \text{comm}(x, \backslash y.P, \varnothing^2) \rightarrow [y]1\{ @\varnothing^2 / y \}$

$a_{TK} = \text{for}(y <- x)K1[[y]1] \mid x!(K2[\varnothing^2]) - \text{comm}(x, \backslash y.K1[[y]1], K2[\varnothing^2]) \rightarrow K1[[y]1]\{ @K2[\varnothing^2] / y \}$

$a_L = \text{comm}(x, \backslash y.[y]1, \varnothing^2)$

$L ::= a_L \mid a_L(-,Q) \mid a_L(P, -) \mid a_L \circ \langle K1,K2 \rangle \mid L|L$

$a = \text{comm}(x, c, t)$

$a \circ \langle K1, K2 \rangle = \text{comm}(x, \backslash y.K1[y, c(y)], K2 \circ t)$

$\text{sigma} = \text{unify}(\text{src}(a_T), S)$

$K_{Par} = \varnothing \mid P$

$K_{Par}[S] \rightarrow a_L \rightarrow K_{Par}[\text{trgt}(a_T) \text{ sigma}]$

$\text{sigma} = \text{unify}(\text{src}(a_T), S)$

$K_{Par}[S] \rightarrow a_L \rightarrow K_{Par}[\text{trgt}(a_T) \{ K1[\text{sigma}([y]1)] / K1[y]1, K2[\text{sigma}(\varnothing^2)] / K2[\varnothing^2] \}]$

Examples

$\text{for}(y <- x)0 \mid x!(5)$

$\text{for}(y <- x)0 \mid x!(7)$

bisimilar

$\text{for}(y <- x)y!(0) \mid x!(5)$

$\text{for}(y <- x)y!(0) \mid x!(7)$

not bisimilar

$t \odot u$

$a_T = \varnothing^1 \odot \varnothing^2 - \odot(\varnothing^1, \varnothing^2) \rightarrow f(\varnothing^1, \varnothing^2)$

$\varnothing^1 \odot u - \odot(\varnothing^1, u) \rightarrow f(\varnothing^1, u)$

$t \odot \varnothing^2 - \odot(t, \varnothing^2) \rightarrow f(t, \varnothing^2)$

$K1[\varnothing^1] \odot K2[\varnothing^2] - \odot(K1[\varnothing^1], K2[\varnothing^2]) \rightarrow f(K1[\varnothing^1], K2[\varnothing^2])$

$a_L = \varnothing^1 \odot \varnothing^2$

$L ::= a_L \mid a_L(-,u) \mid a_L(t, -) \mid a_L \circ \langle K1,K2 \rangle \mid L \odot L$

$\text{sigma} = \text{unify}(\text{src}(a_T), s)$

$K_{\odot} = \varnothing \odot v$

$K_{\odot}[s] \rightarrow a_L \rightarrow K_{\odot}[t \text{ sigma}]$

Nota bene: in the current account ... has no binding and the rho version only has asymmetric binding. But, ambient has no binding for interaction and the MeTTa calculus has symmetric binding. So ... has 4 possibilities (no binding, binding left, binding right, binding both).