



Large-scale 3D Modeling from Crowdsourced Data

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ETH zürich



Microsoft

URCV

Sparse Modeling

Johannes L. Schönberger

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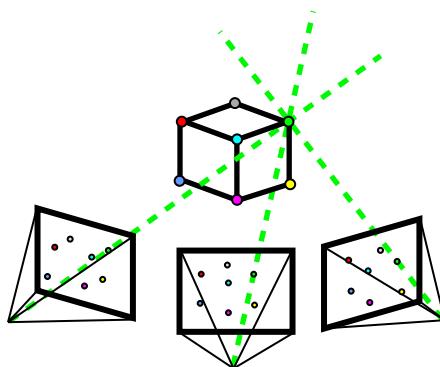
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Microsoft **URCV**

Outline

1. Structure-from-Motion algorithm



2. Challenges in crowdsourced data



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Large-scale 3D Modeling from Crowdsourced Data

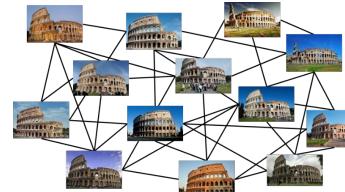
Pipeline

Unstructured Images



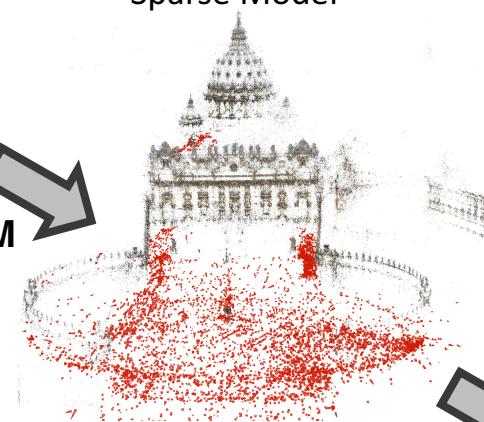
Assoc.

Scene Graph



SFM

Sparse Model



MVS

Dense Model



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Large-scale 3D Modeling from Crowdsourced Data

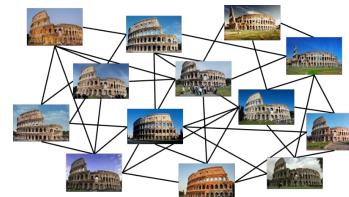
Pipeline

Unstructured Images



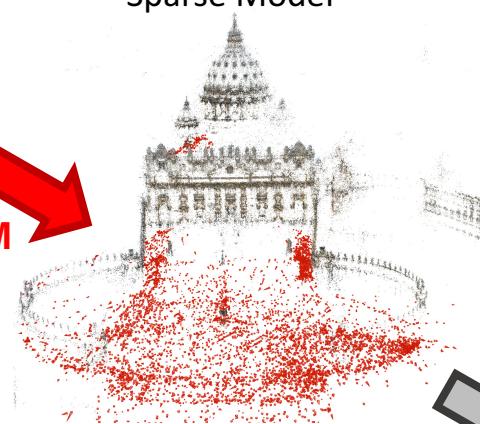
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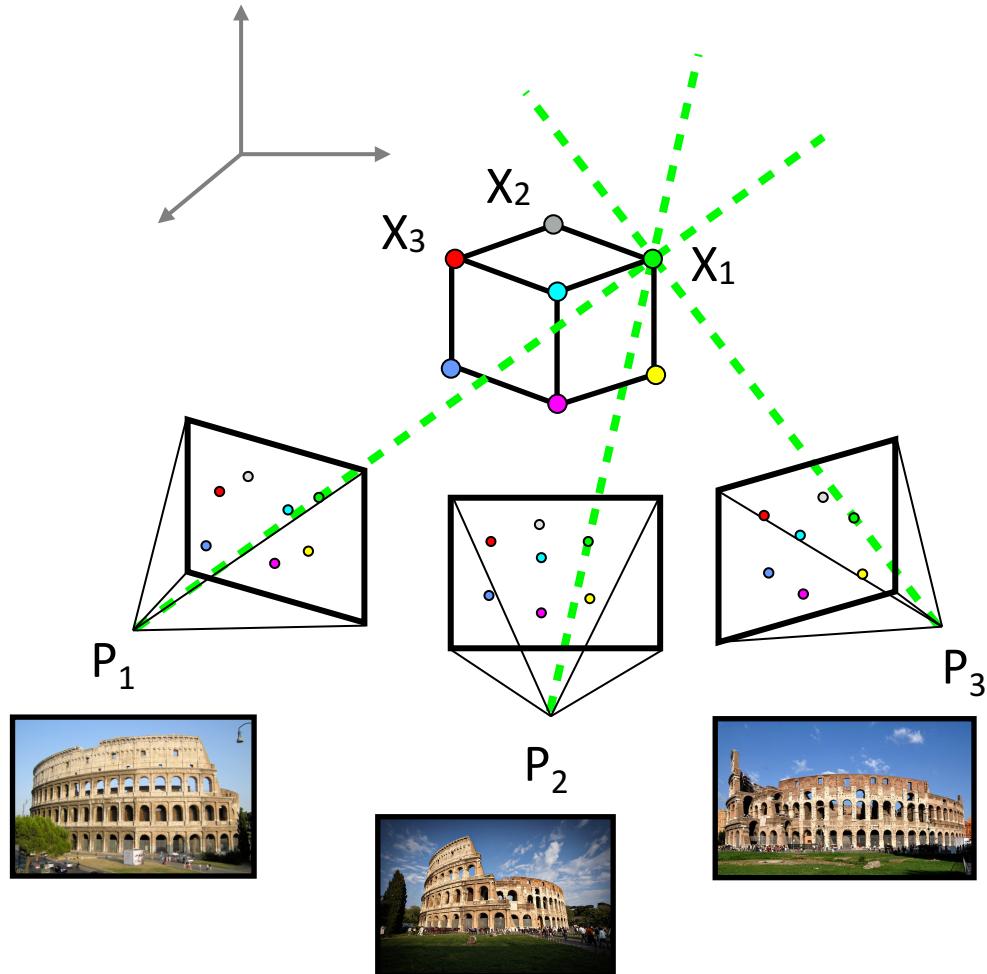
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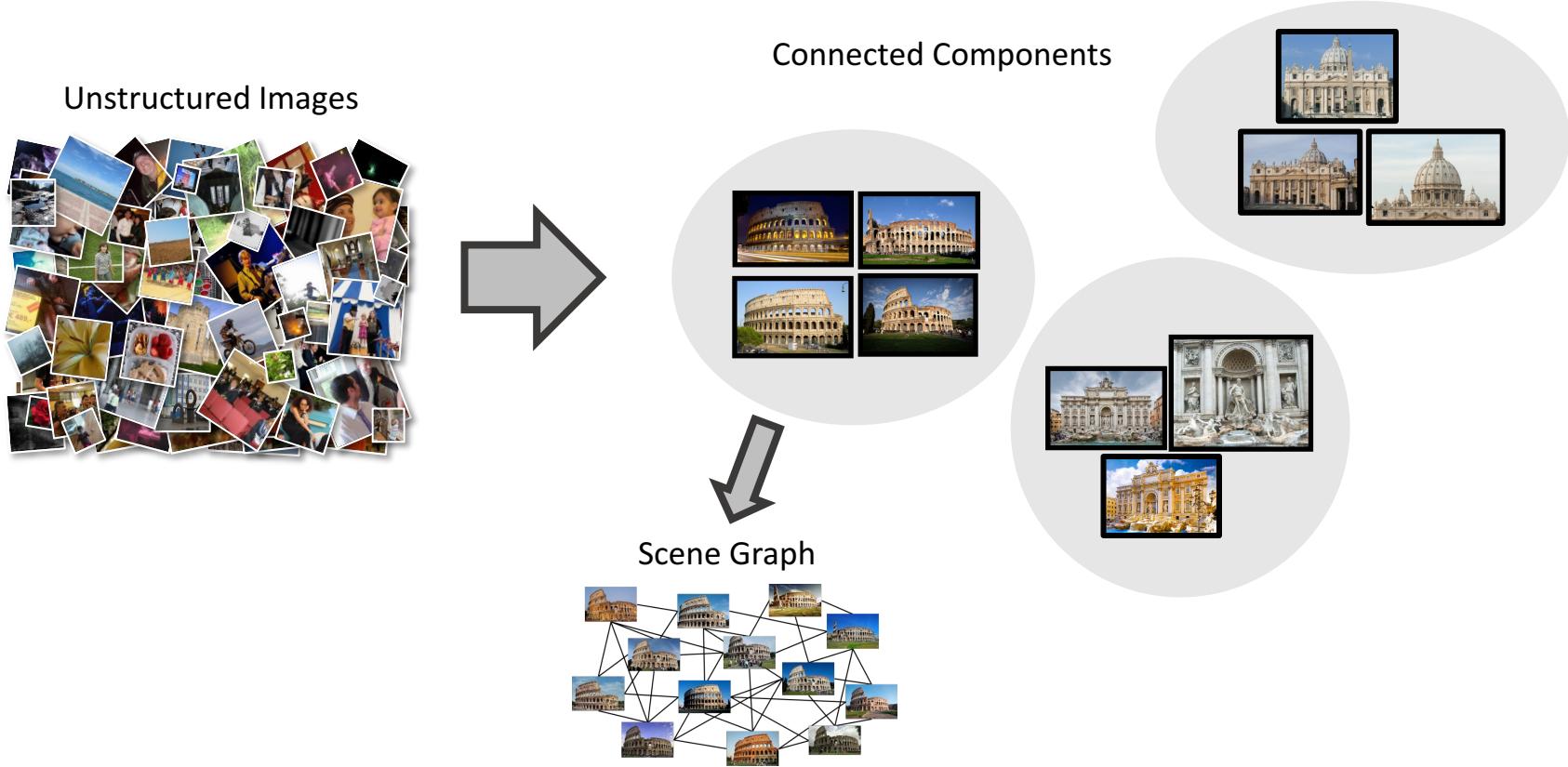
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Structure-from-Motion

- Joint estimation of ...
 - Structure \mathbf{X}_i
 - Cameras \mathbf{P}_j
- ... from motion, i.e.
 - images at different viewpoints



Data Association



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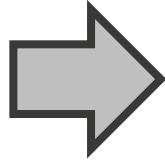


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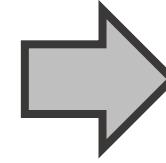
Large-scale 3D Modeling from Crowdsourced Data

Data Association

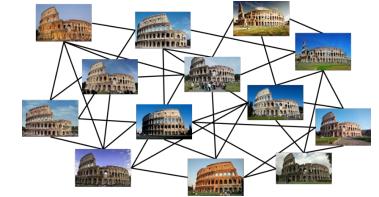
Unstructured Images



Two-View Geometry



Scene Graph



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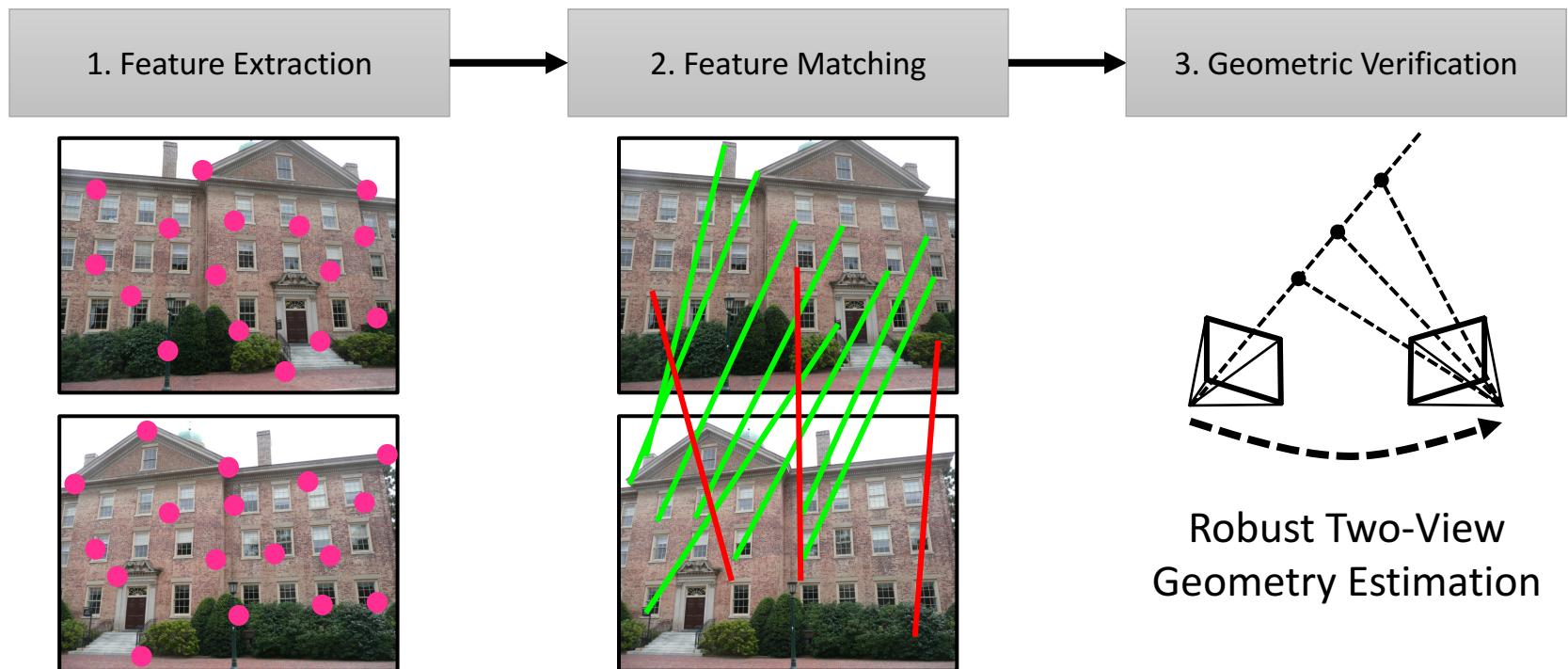


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Large-scale 3D Modeling from Crowdsourced Data

Data Association



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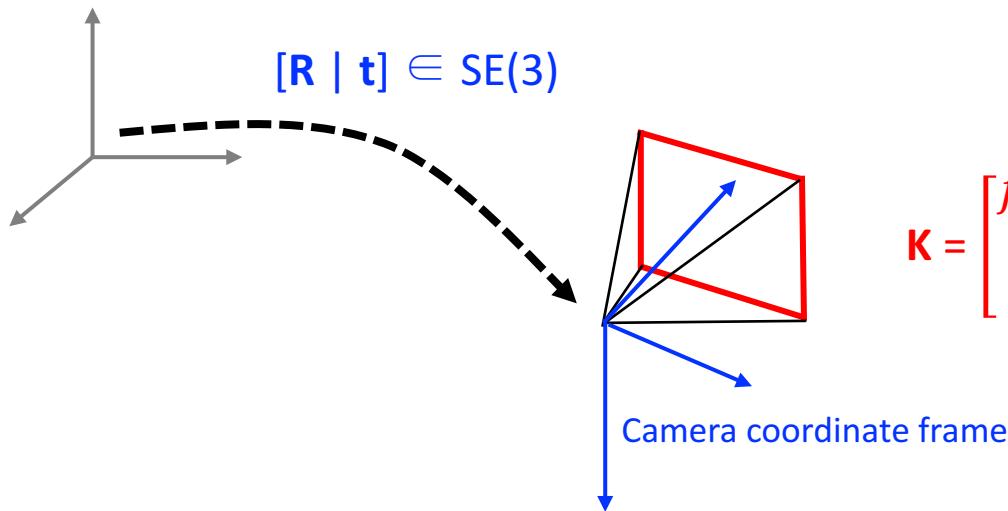
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Large-scale 3D Modeling from Crowdsourced Data

Two-View Geometry

- Absolute camera geometry: $\mathbf{P} = \mathbf{K} [\mathbf{R} \mid \mathbf{t}]$

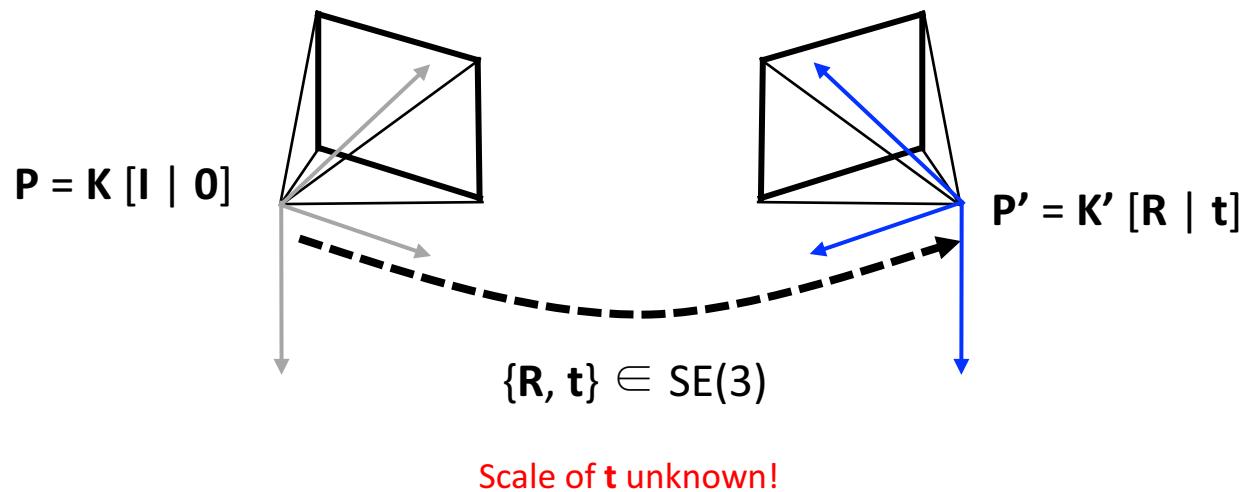
World coordinate frame



$$\mathbf{K} = \begin{bmatrix} f_x & \alpha & p_x \\ 0 & f_y & p_y \\ 0 & 0 & 1 \end{bmatrix}$$

Two-View Geometry

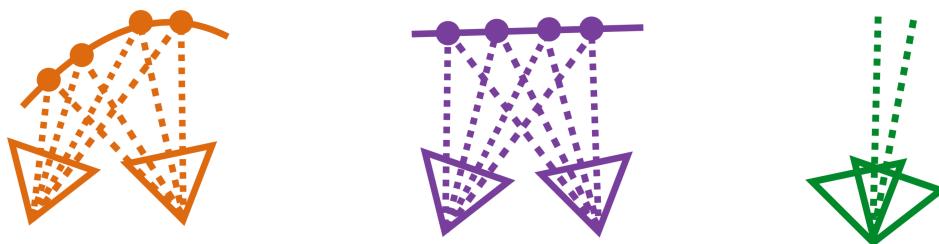
- Relative camera geometry: P, P'



Two-View Geometry

- Model selection

General	Planar	Panoramic
<ul style="list-style-type: none">• Fundamental matrix F (<i>uncalibrated</i>)• Essential matrix E (<i>calibrated</i>)	<ul style="list-style-type: none">• Homography H	<ul style="list-style-type: none">• Homography H
<ul style="list-style-type: none">• 7 correspondences• 5 correspondences	<ul style="list-style-type: none">• 4 correspondences	<ul style="list-style-type: none">• 4 correspondences



Hartley and Zisserman 2004, "Multiple View Geometry"



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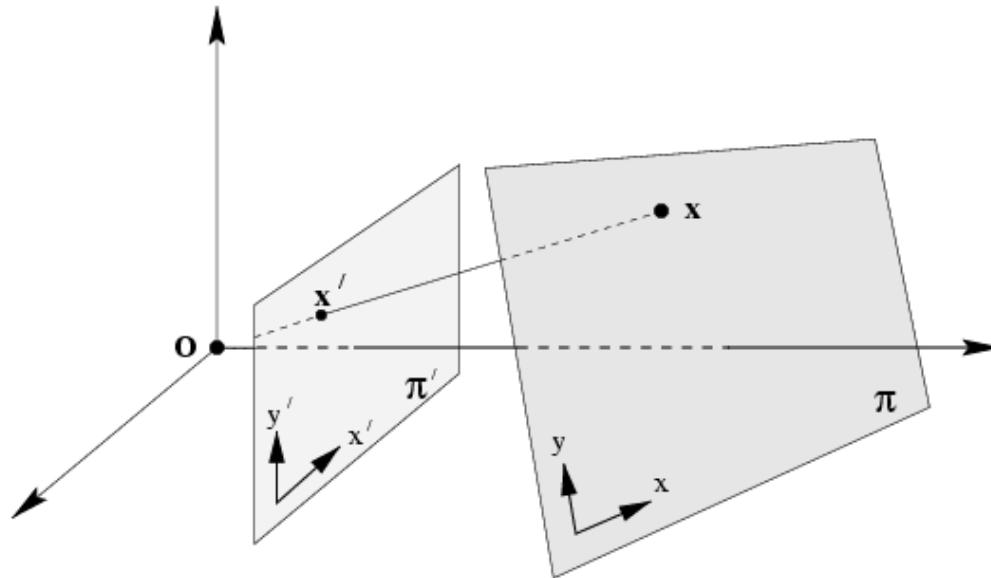


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Large-scale 3D Modeling from Crowdsourced Data

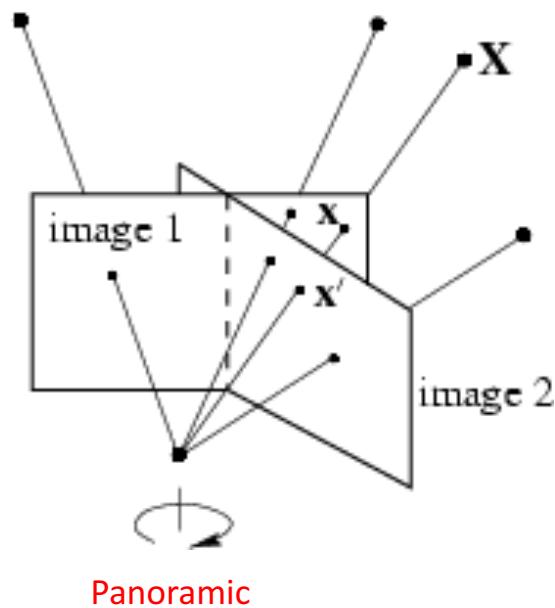
Two-View Geometry

- Homography $\mathbf{H} \in \mathbb{R}^{3 \times 3}$
Linear transformation between two planes in \mathbb{P}^2

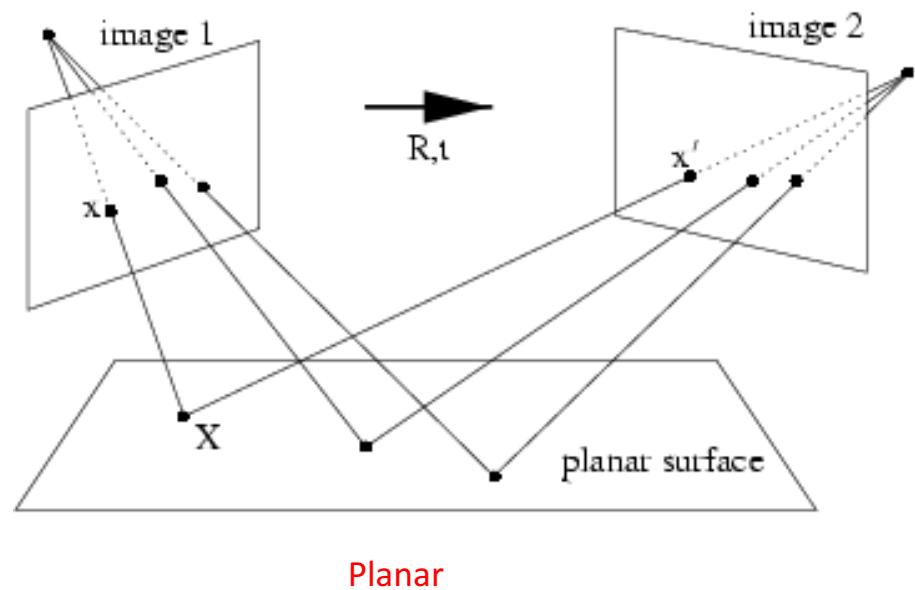


Two-View Geometry

- Homography



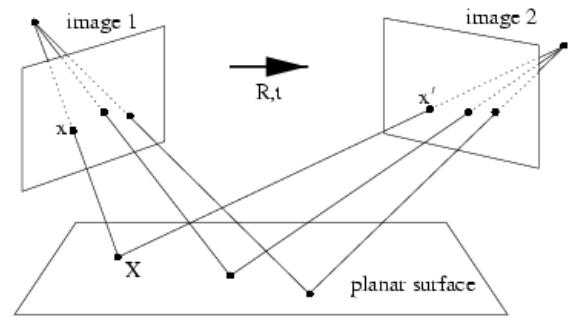
Panoramic



Planar



Two-View Geometry



- Homography
 - In the calibrated case
 - Two cameras: $P = K [I \mid 0]$ and $P' = K' [R \mid t]$
 - A plane: $\pi = (n^T, d)^T$
 - The homography is given by $x' = H x$

$$H = K' (R - tn^T/d) K^{-1}$$

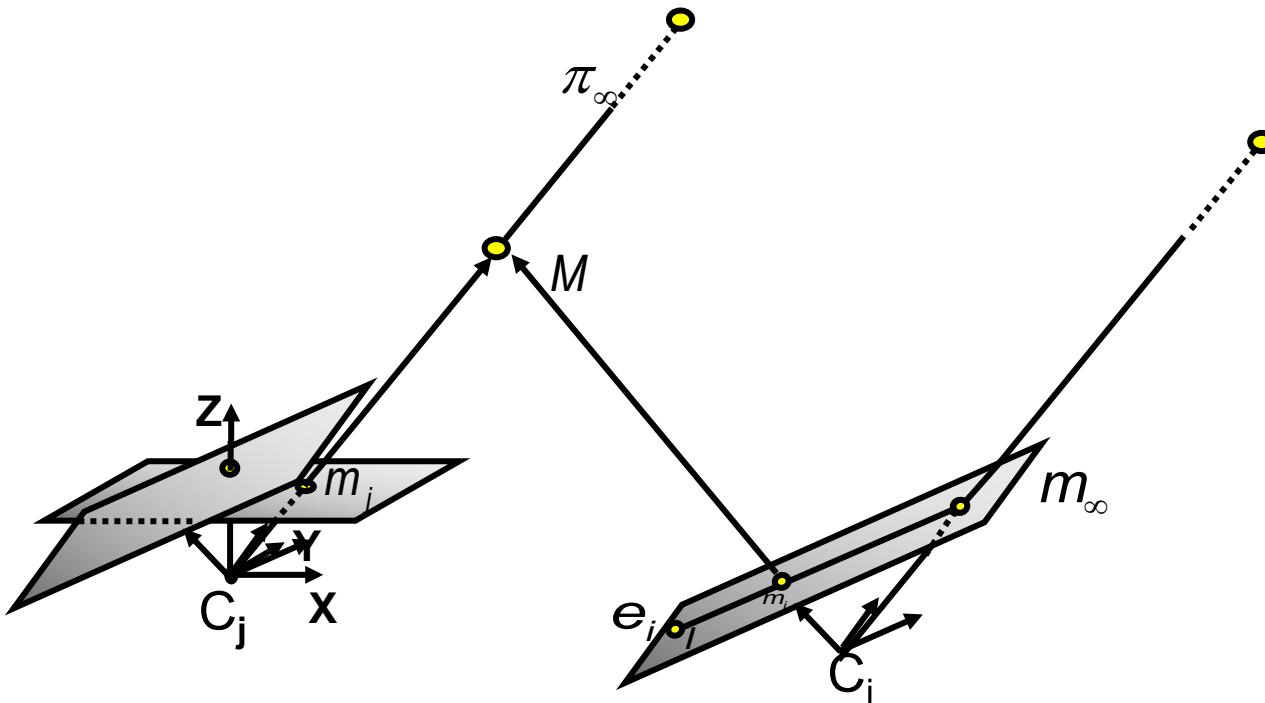
Two-View Geometry

$$m_\infty = H_\infty m_i$$

- Fundamental matrix \mathbf{F}

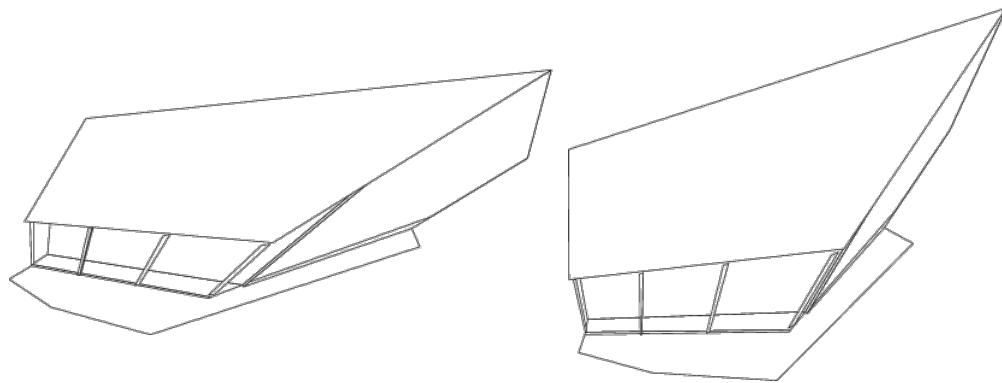
$$l = [e]_X m_\infty = \underbrace{[e]_X H_\infty}_F m_i$$

$$m_j l = \underbrace{m_j F m_i}_\text{epipolar constraint} = 0$$



Two-View Geometry

- Projective ambiguity



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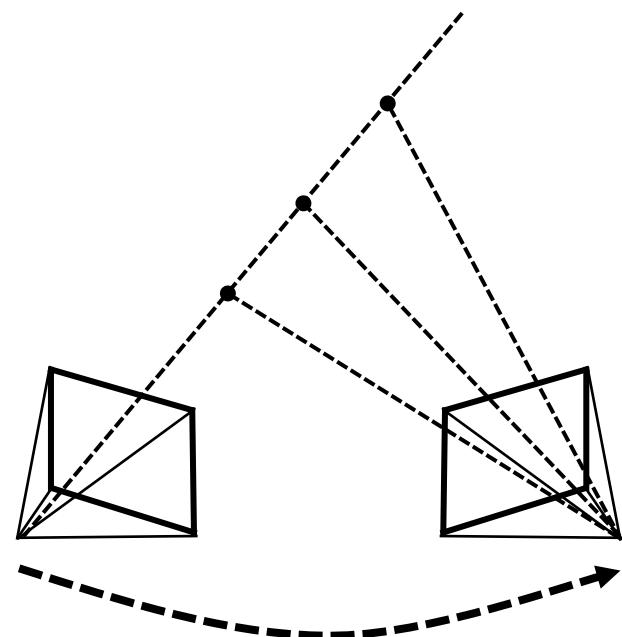
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Two-View Geometry

- Essential matrix \mathbf{E}

$$\mathbf{E} = \mathbf{K}^T \mathbf{F} \mathbf{K}' = \mathbf{t}_x \mathbf{R}$$



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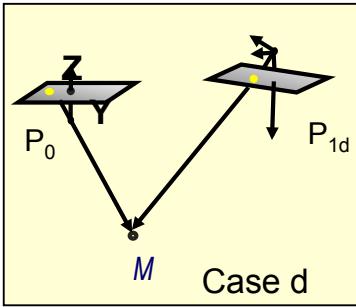
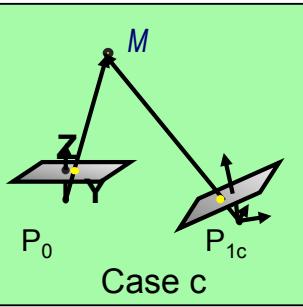
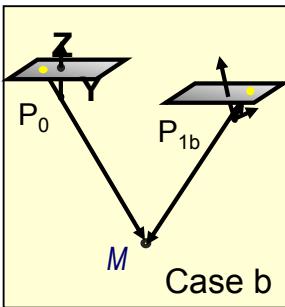
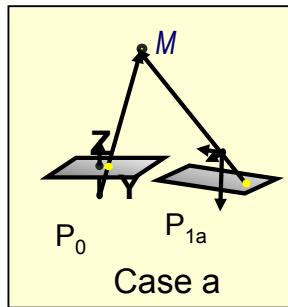
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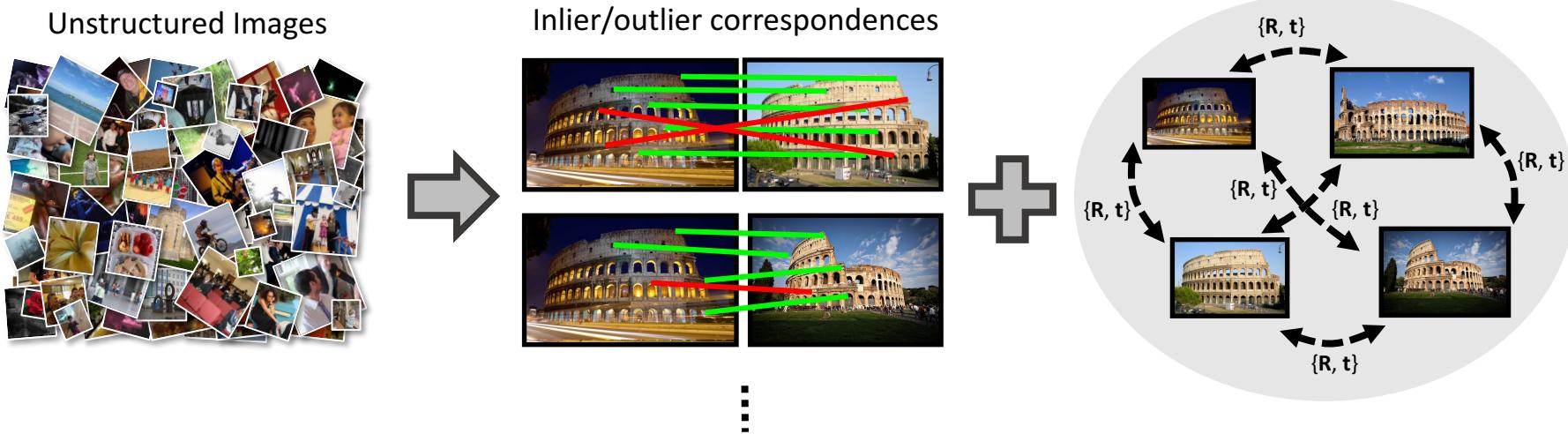
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Two-View Geometry

- Robust estimation using RANSAC
- Model selection (\mathbf{F} , \mathbf{E} , \mathbf{H})
 - Inlier maximization
 - GRIC criterion Torr 1998, "An assessment of information criteria for motion model selection"
 - QDEGSAC Frahm and Pollefeys 2006, "RANSAC for (quasi-) degenerate data (QDEGSAC)"
- Decompose \mathbf{E} , \mathbf{H} to $\{\mathbf{R}, \mathbf{t}\}$

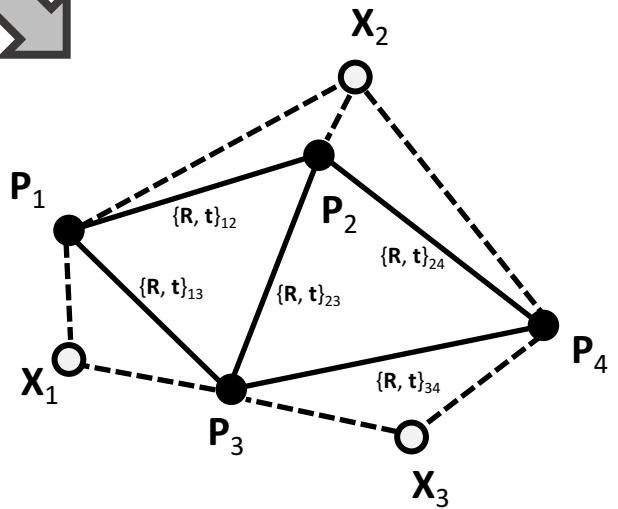
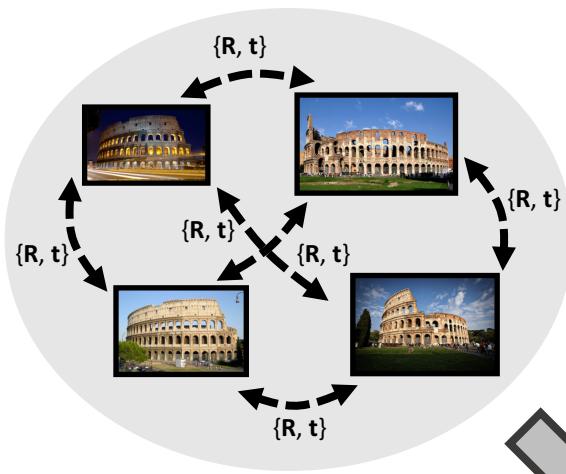
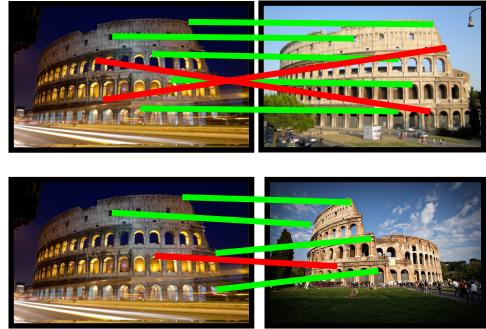


Scene Graph



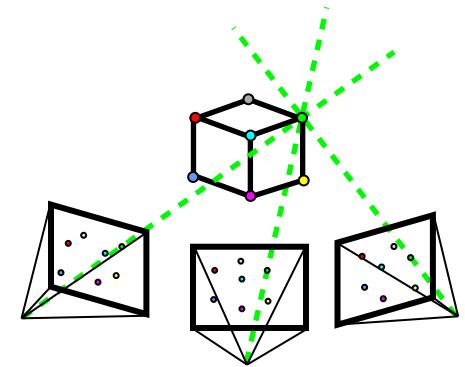
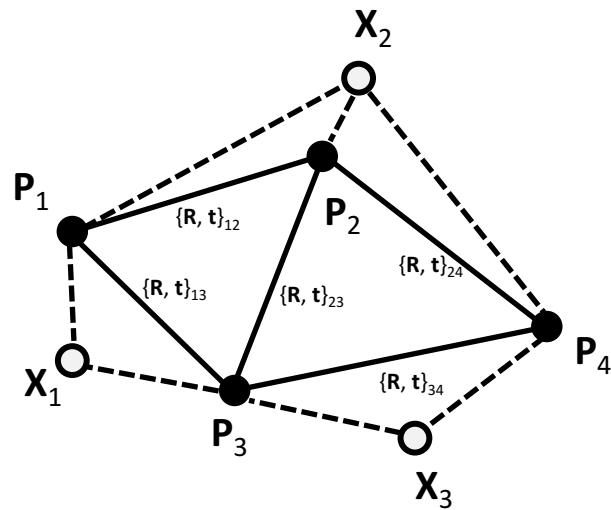
Scene Graph

Inlier/outlier correspondences



Structure-from-Motion

- From relative to absolute cameras and structure



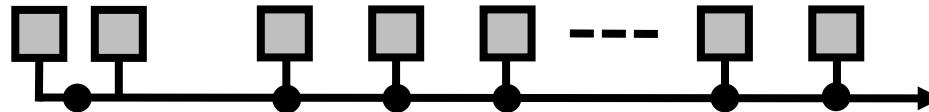
Scale of t unknown!
Outlier correspondences!
Outlier image pairs!



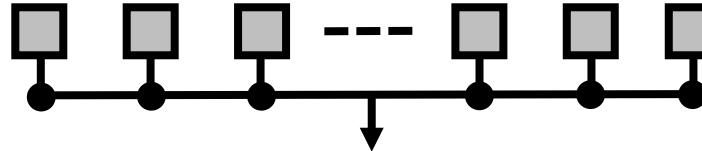
Structure-from-Motion

- 3 paradigms

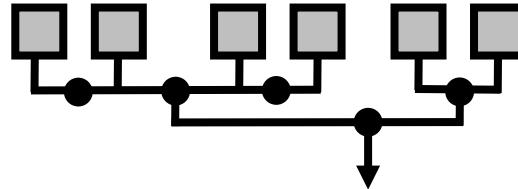
- Incremental



- Global



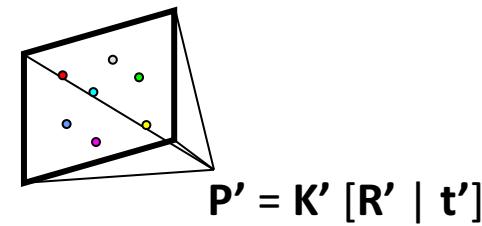
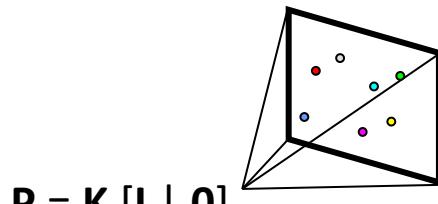
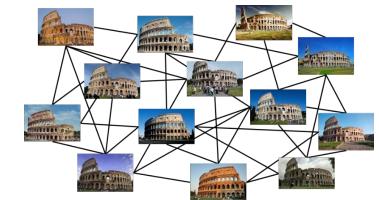
- Hierarchical



Incremental SfM

- Initialization

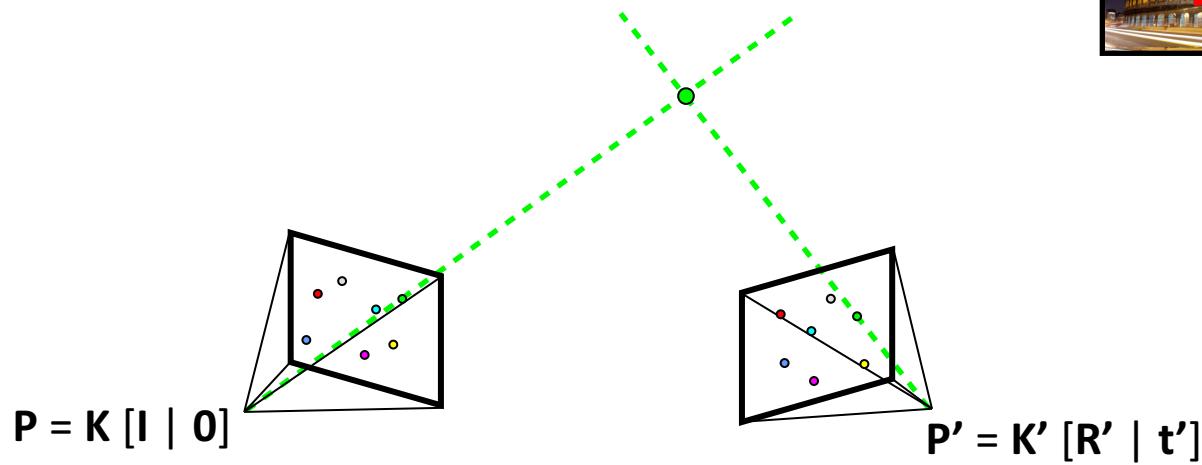
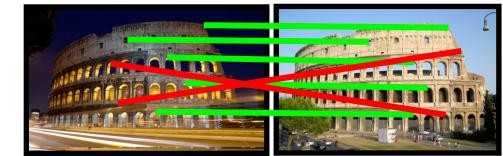
1. Choose two non-panoramic views ($\|t\| \neq 0$)



Incremental SfM

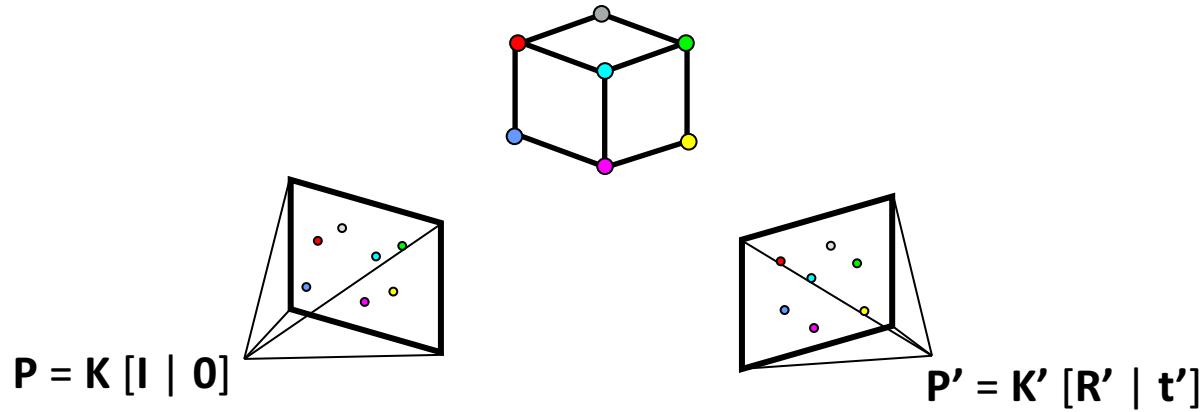
- Initialization

1. Choose two non-panoramic views ($\|t\| \neq 0$)
2. Triangulate inlier correspondences



Incremental SfM

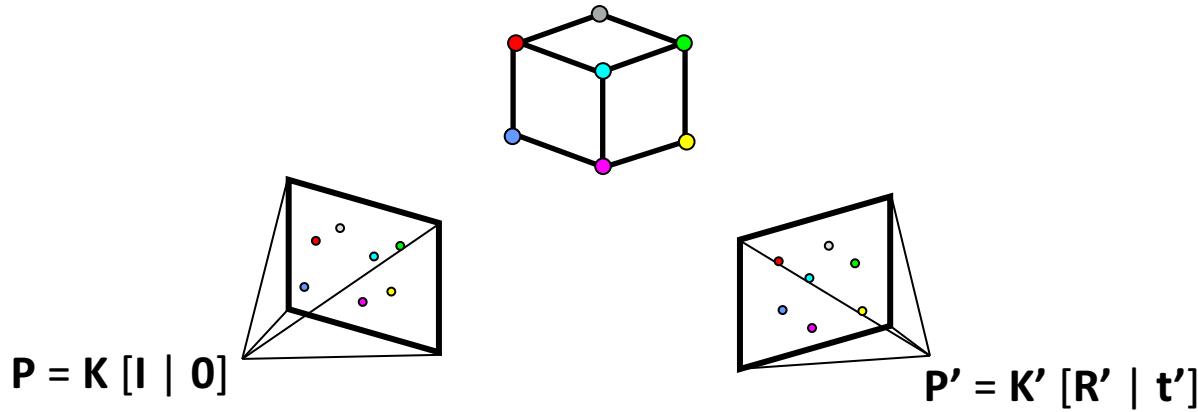
- Initialization
 1. Choose two non-panoramic views ($\|t\| = 1$)
 2. Triangulate inlier correspondences



Incremental SfM

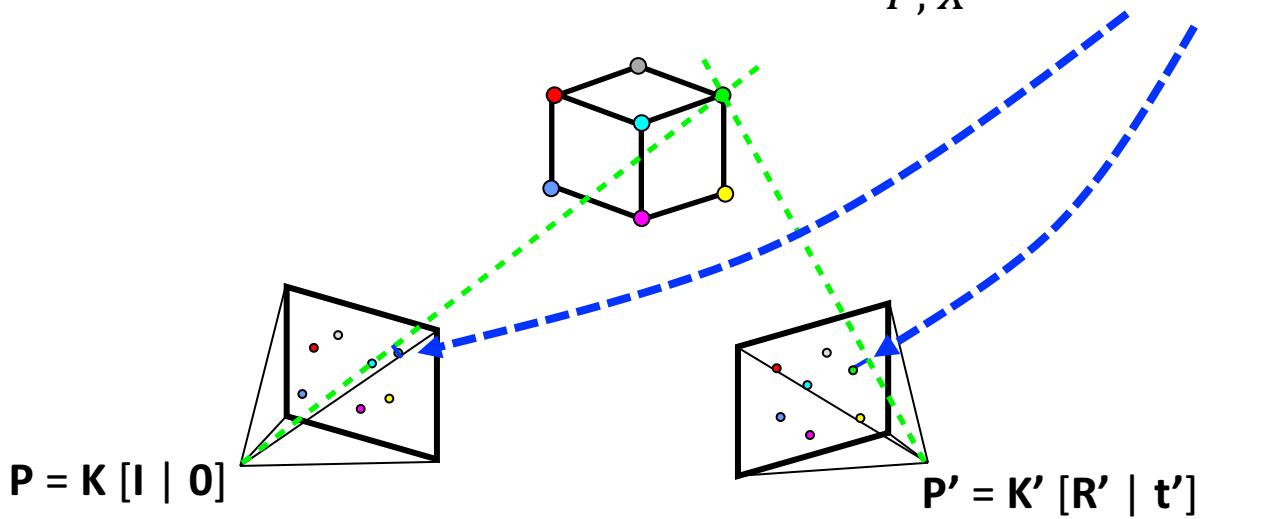
- Initialization

1. Choose two non-panoramic views ($\|t\| = 1$)
2. Triangulate inlier correspondences
3. Bundle adjustment



Incremental SfM

- Bundle adjustment
 - Non-linear refinement of structure and motion
 - Minimize reprojection error: $\min_{P, X} \|x - \pi(P, X)\|$



Ceres-Solver, <http://ceres-solver.org/>

Triggs et al., "Bundle Adjustment – A Modern Synthesis"



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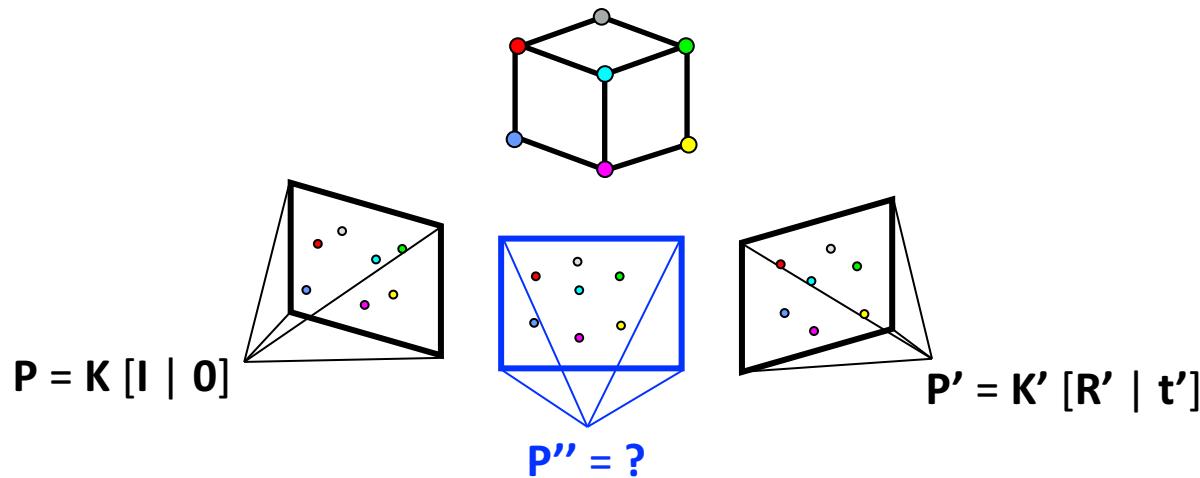


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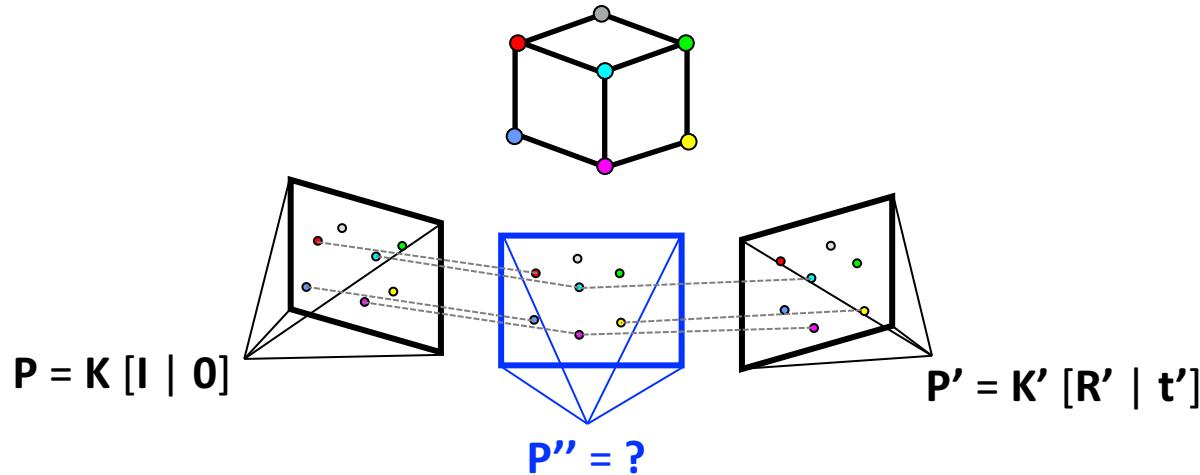
Incremental SfM

- Absolute camera registration



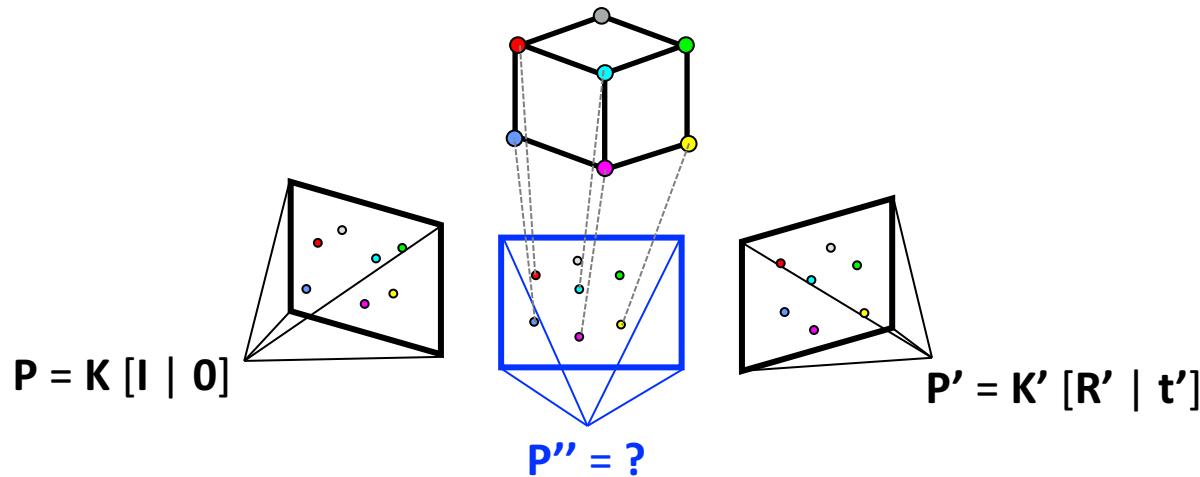
Incremental SfM

- Absolute camera registration
 1. Find 2D-3D correspondences



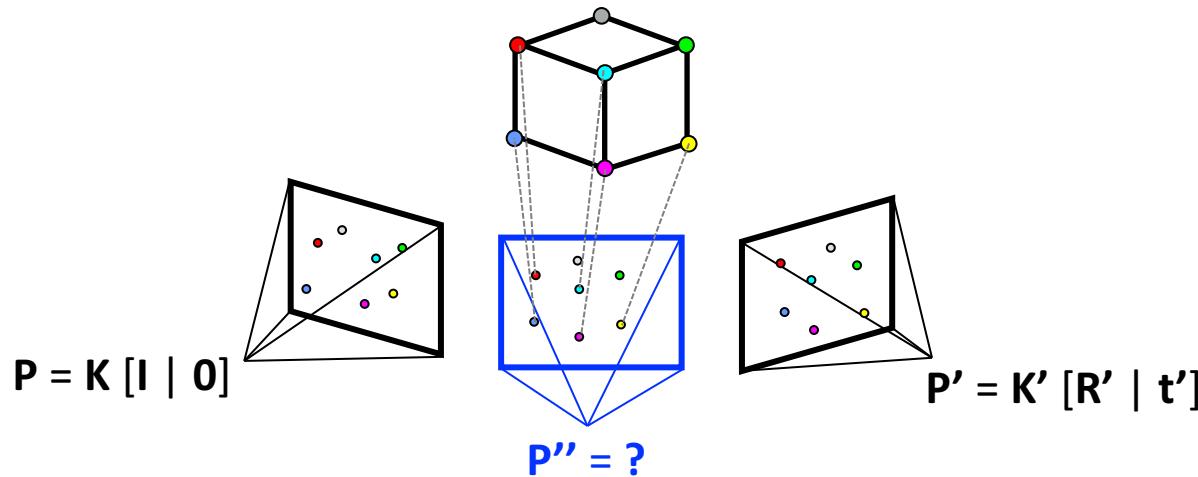
Incremental SfM

- Absolute camera registration
 1. Find 2D-3D correspondences



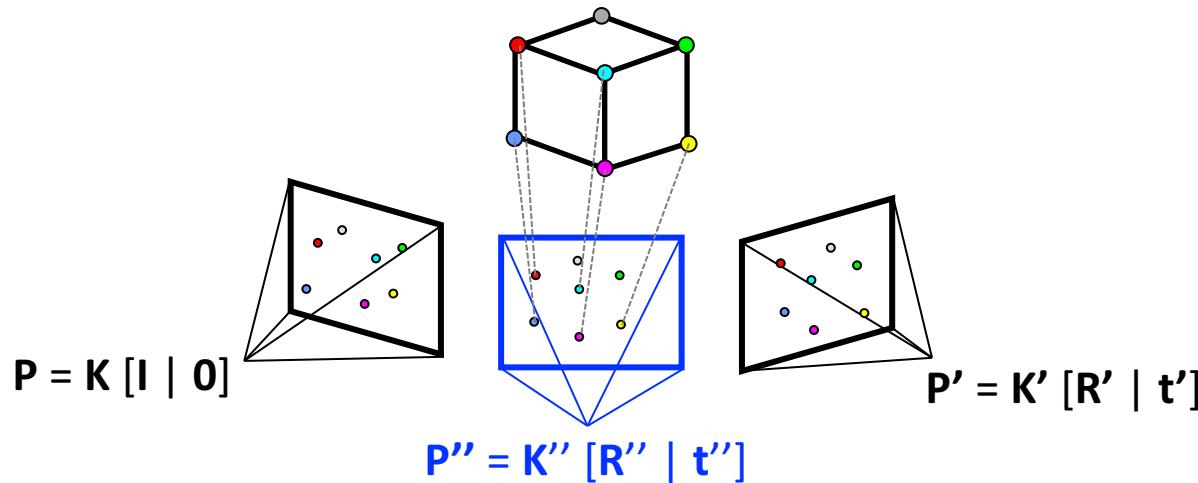
Incremental SfM

- Absolute camera registration
 1. Find 2D-3D correspondences
 2. Solve Perspective-n-Point problem

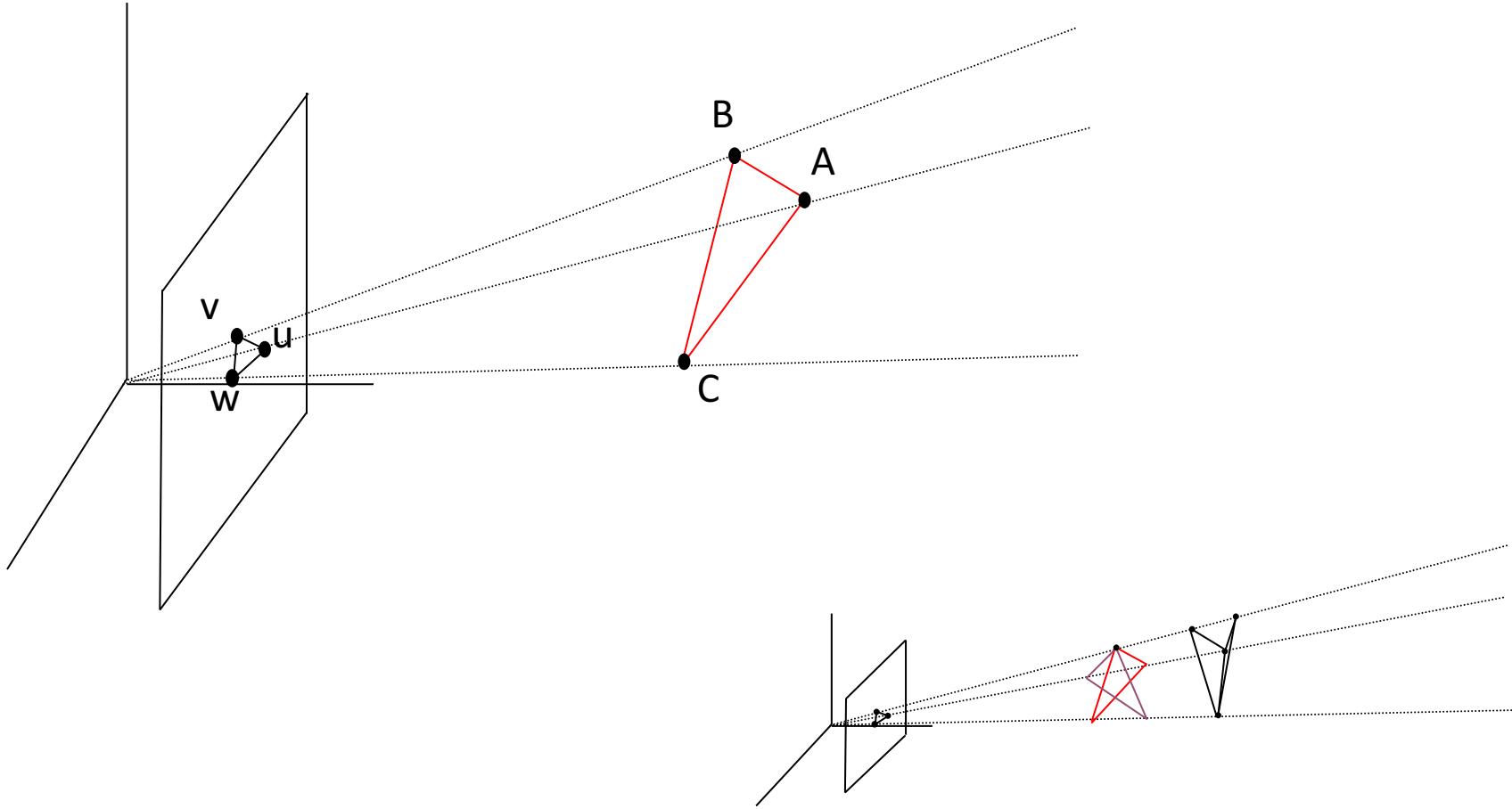


Incremental SfM

- Absolute camera registration
 1. Find 2D-3D correspondences
 2. Solve Perspective-n-Point problem



Perspective-3-Point Problem



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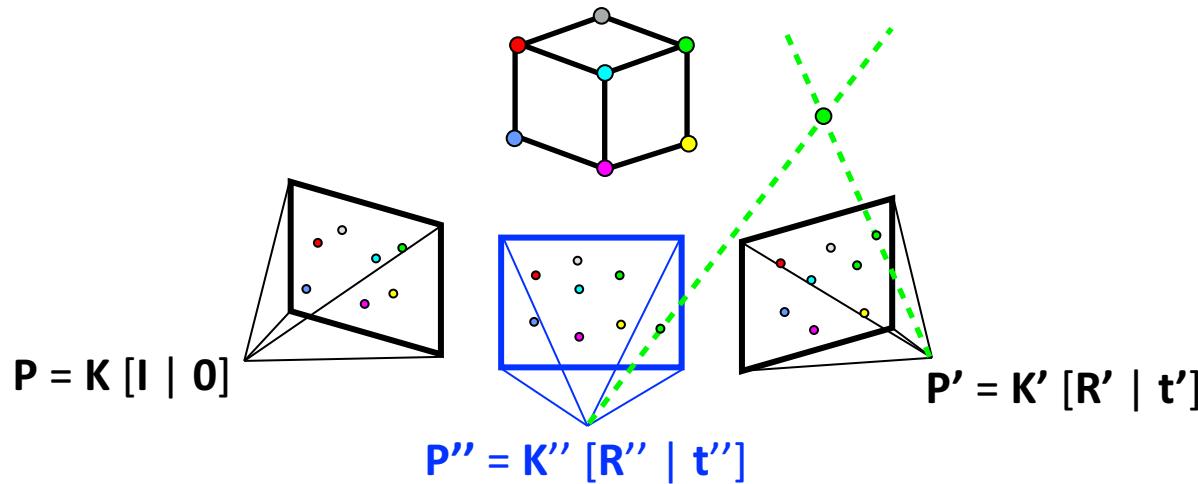
URCV

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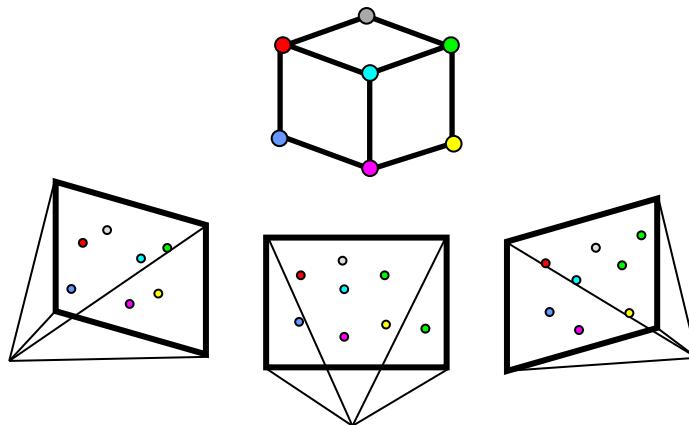
Incremental SfM

- Absolute camera registration
 1. Find 2D-3D correspondences
 2. Solve Perspective-n-Point problem
 3. Triangulate new points



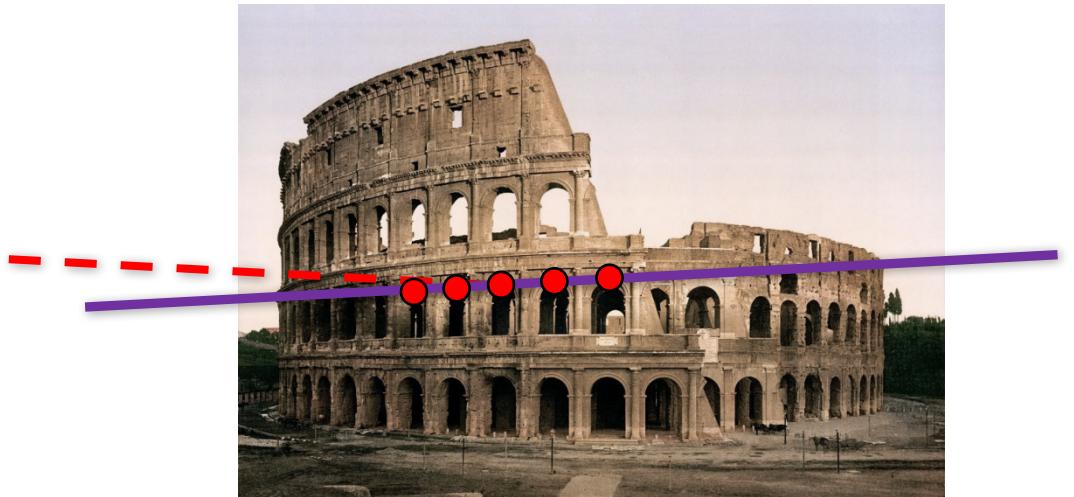
Incremental SfM

- Bundle adjustment $\min_{P, X} \|x - \pi(P, X)\|$



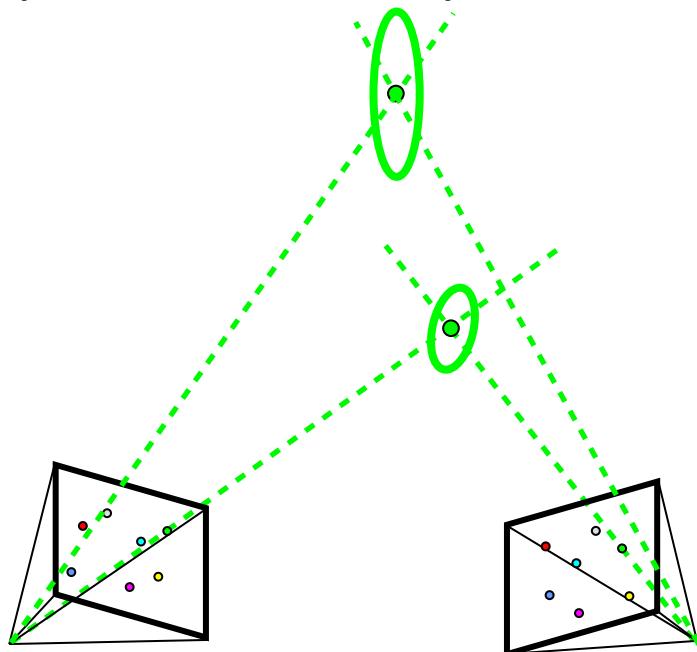
Incremental SfM

- Outlier filtering
 - Remove points with large reprojection error

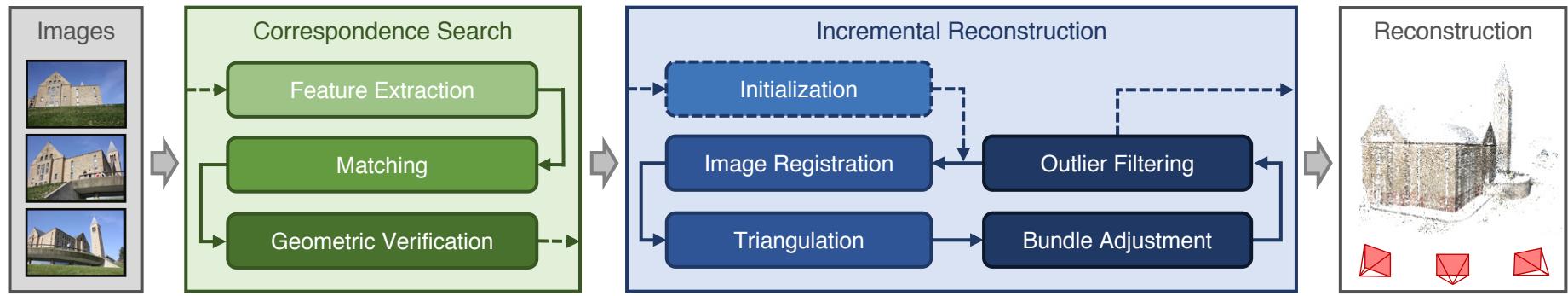


Incremental SfM

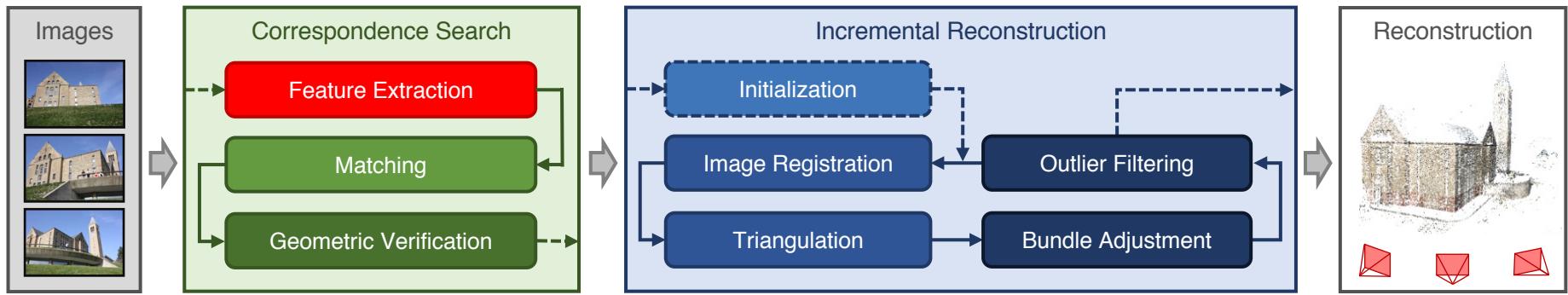
- Outlier filtering
 - Remove points with large reprojection error
 - Remove points at “infinity”



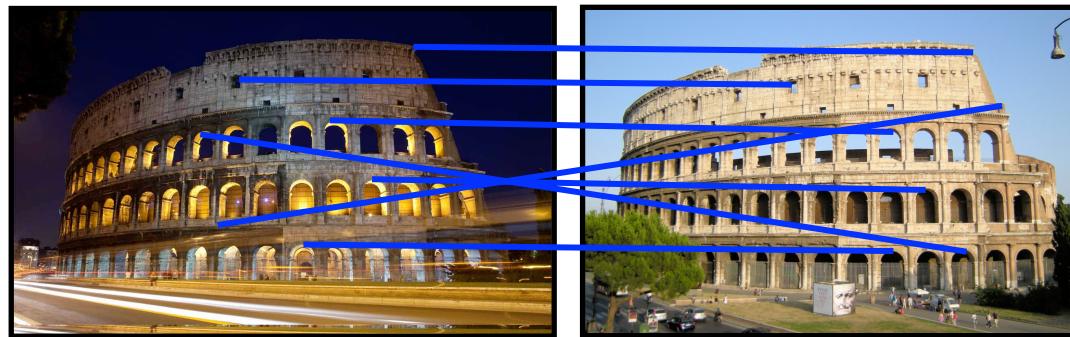
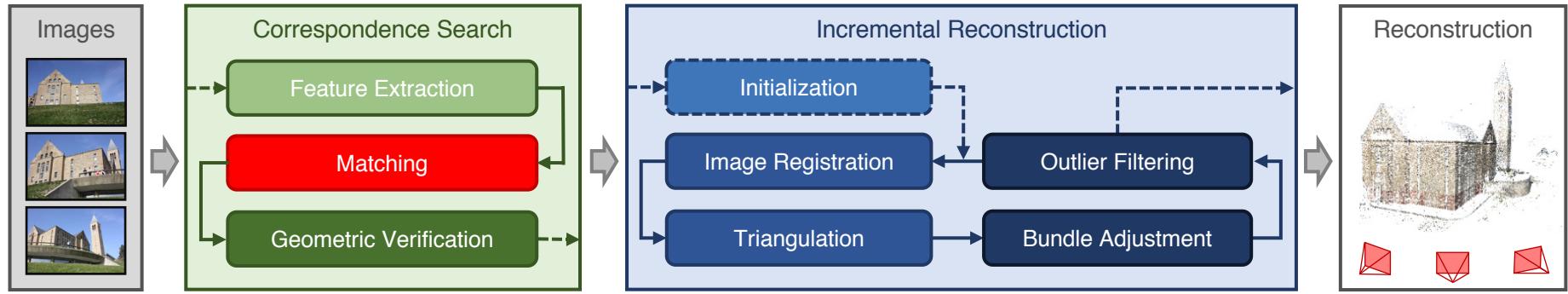
Incremental SfM



Incremental SfM



Incremental SfM



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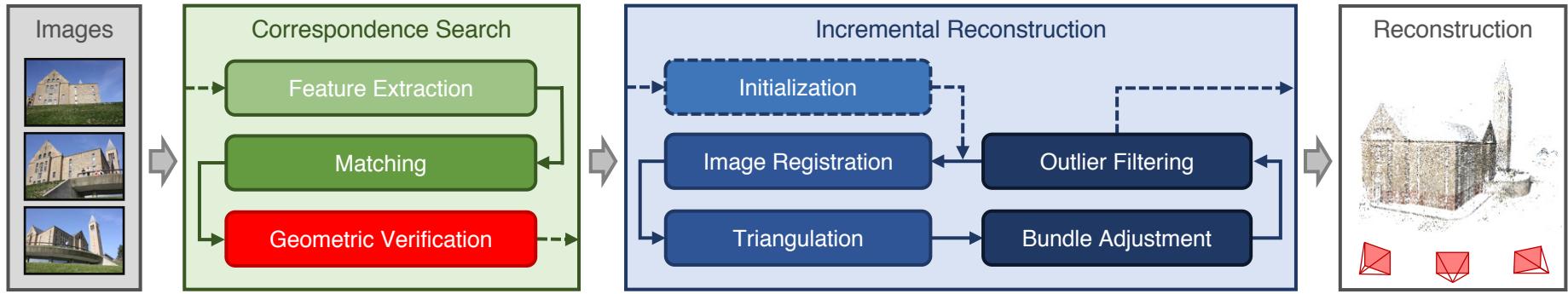
Microsoft



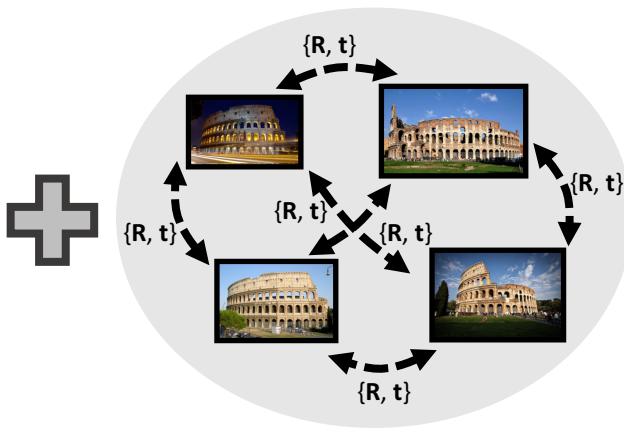
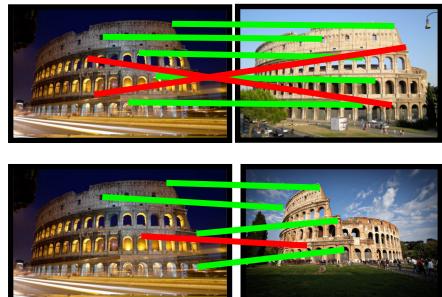
URCV

Large-scale 3D Modeling from Crowdsourced Data

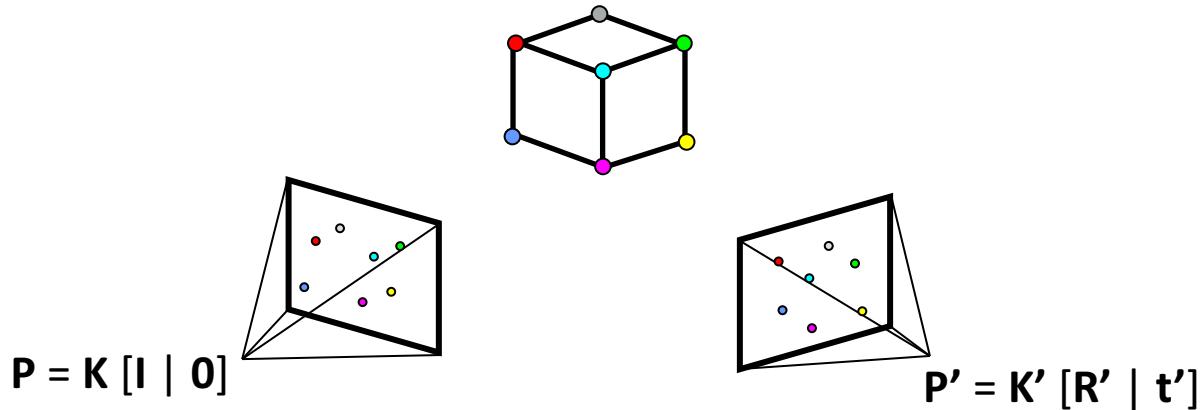
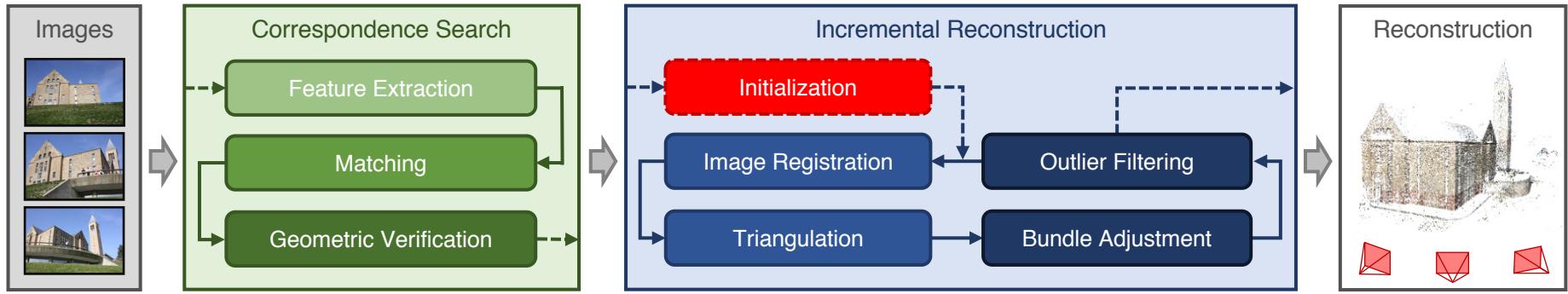
Incremental SfM



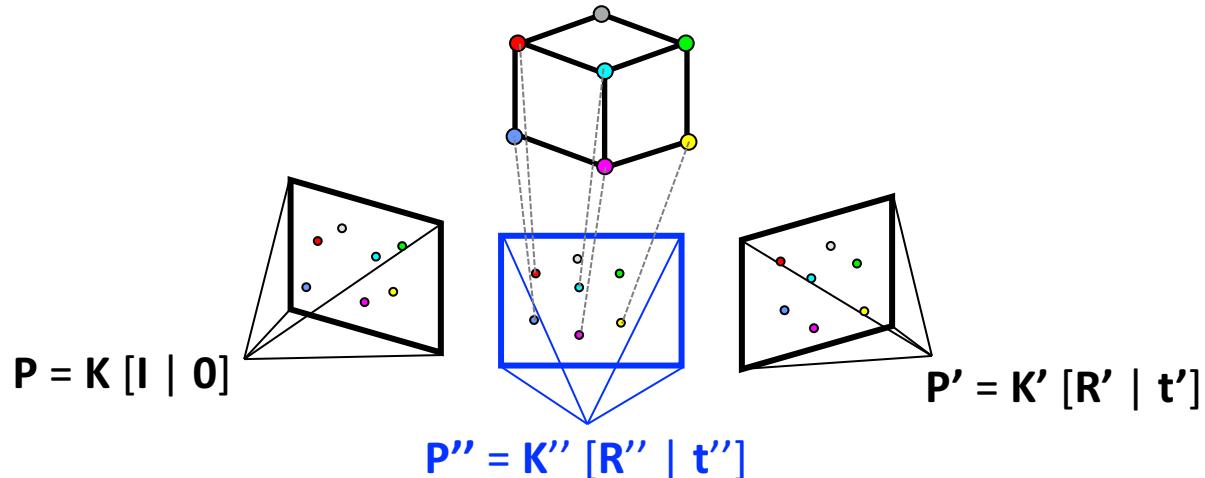
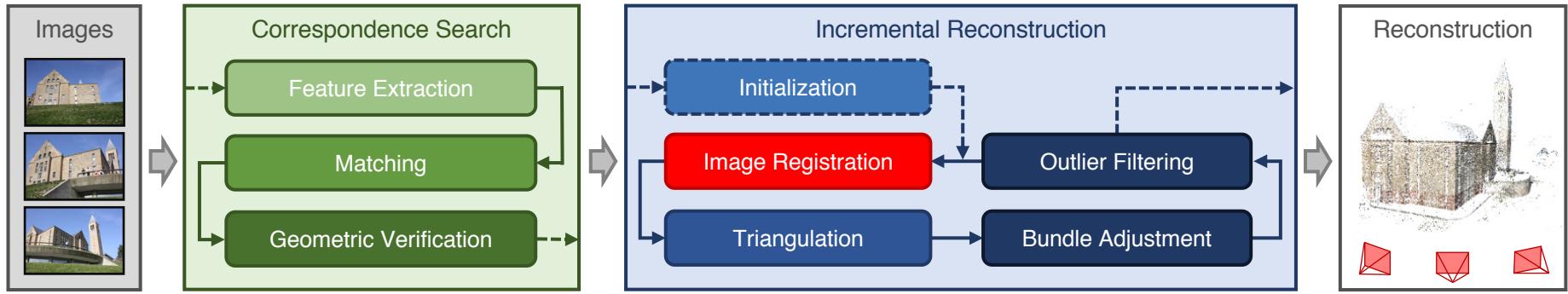
Inlier/outlier correspondences



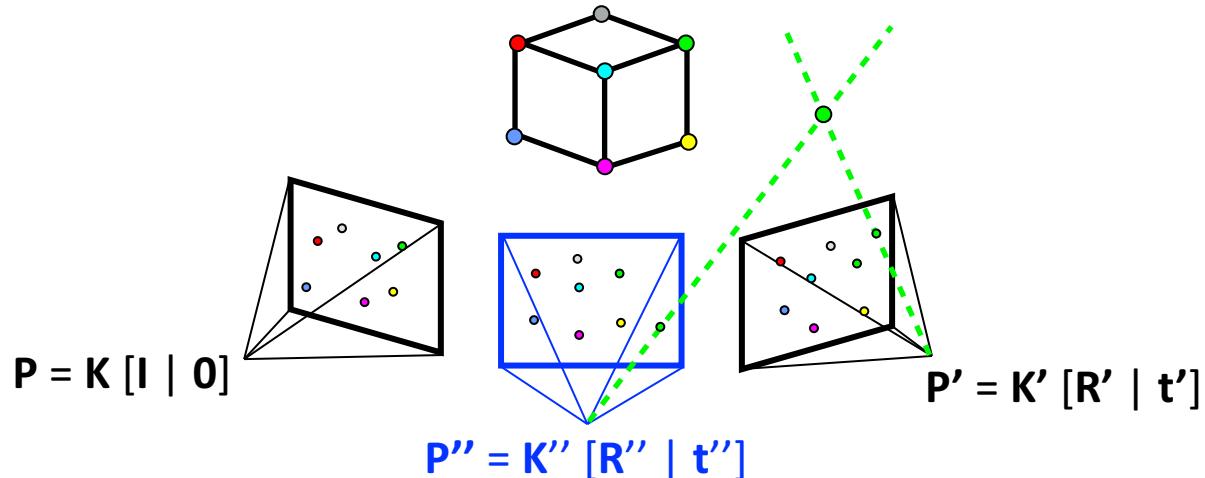
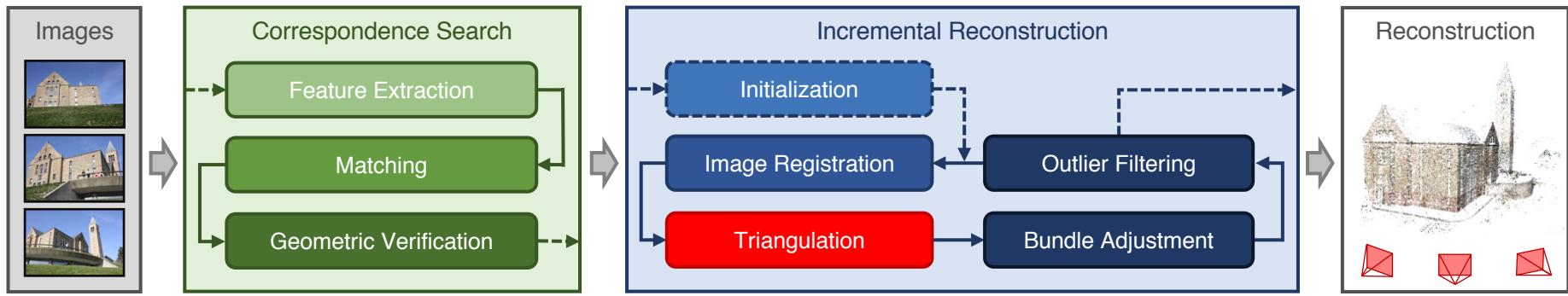
Incremental SfM



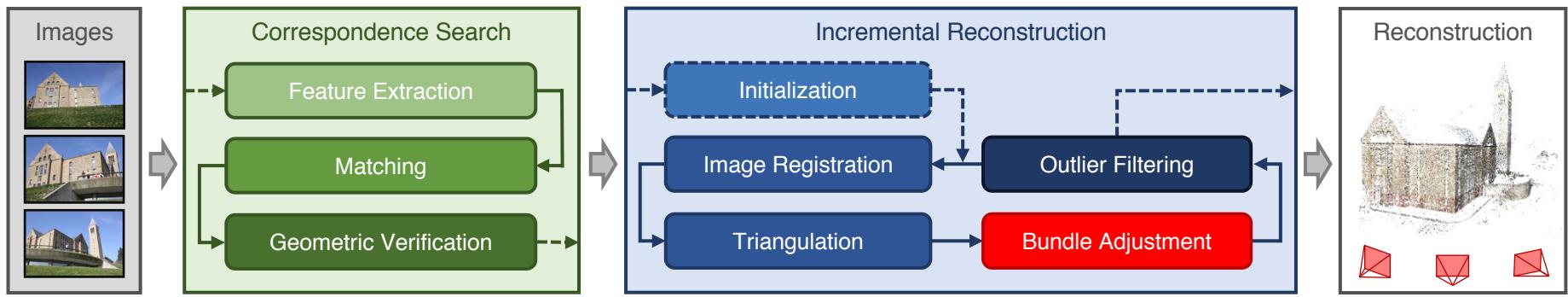
Incremental SfM



Incremental SfM



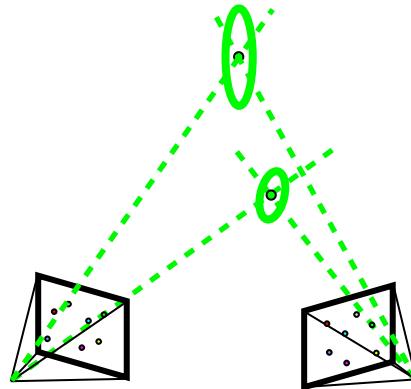
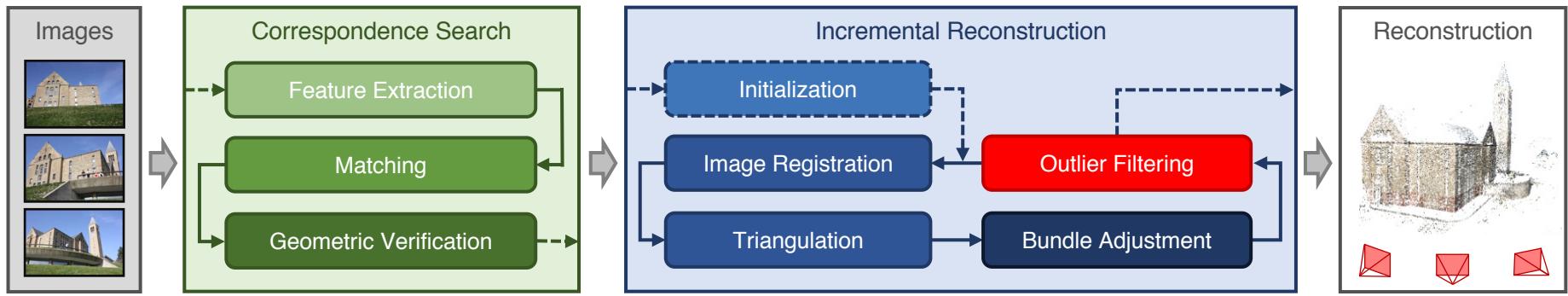
Incremental SfM



$$\min_{P, X} \|x - \pi(P, X)\|$$



Incremental SfM



Demo: Incremental SfM



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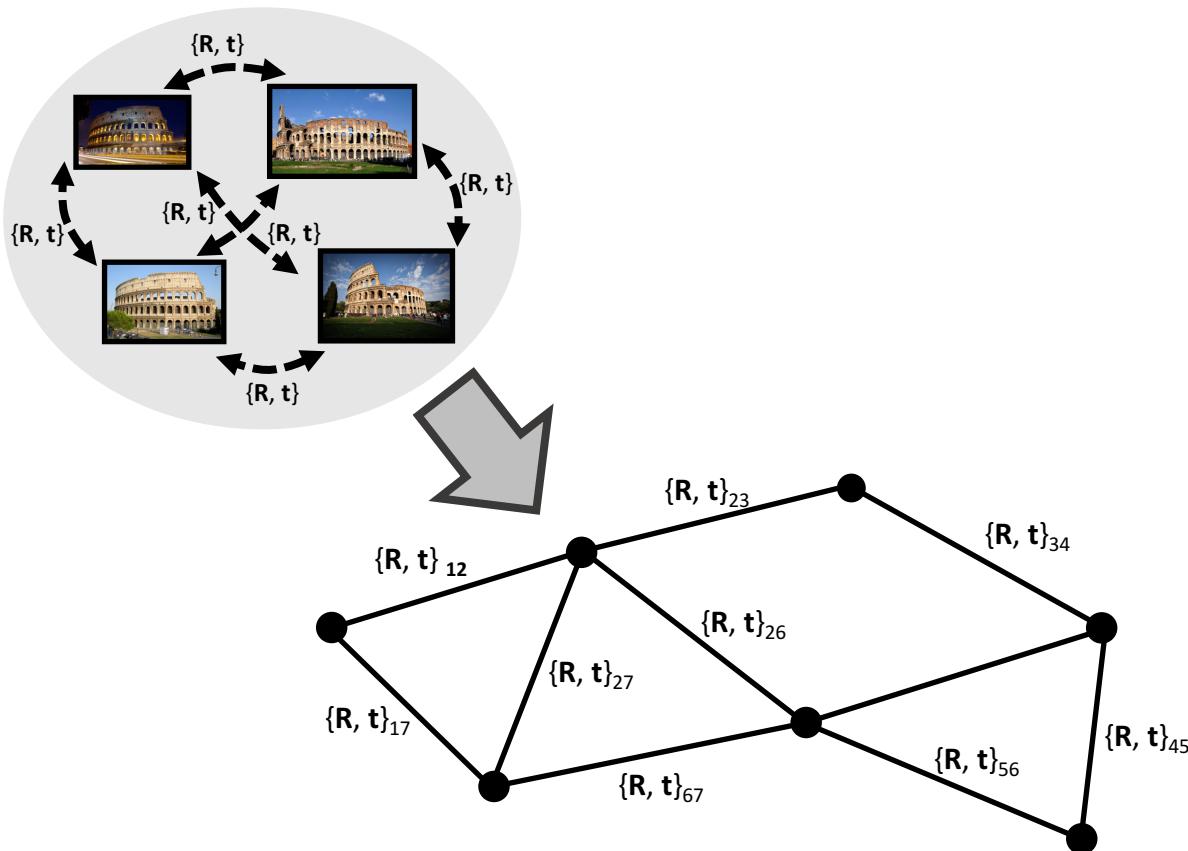


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Global SfM

● Image
— Two-View Geometry

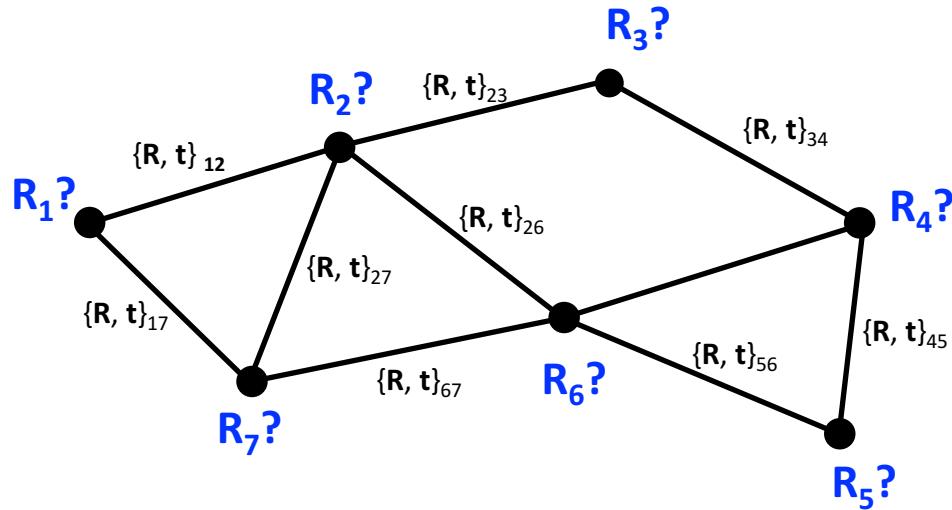


Global SfM

● Image
— Two-View Geometry

1. Estimate global rotations: $\min_R \|R_{ij} - R_j R_i^T\|$

Chatterjee and Govindu 2013, "Efficient and Robust Large-Scale Rotation Averaging"

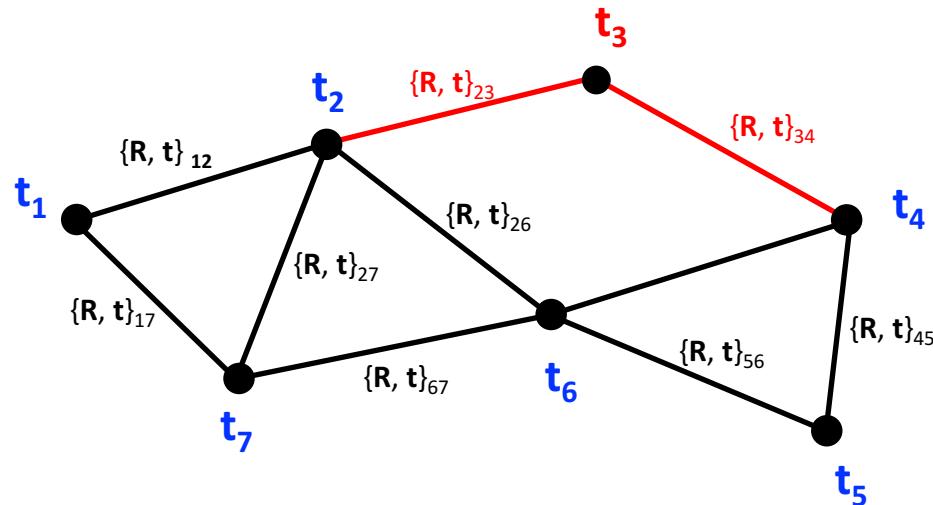


Global SfM

● Image
— Two-View Geometry

1. Estimate global rotations: $\min_R \|\mathbf{R}_{ij} - \mathbf{R}_j \mathbf{R}_i^T\|$

Filter relative rotations: $\|\mathbf{R}_{ij} - \mathbf{R}_j \mathbf{R}_i^T\| > \epsilon$

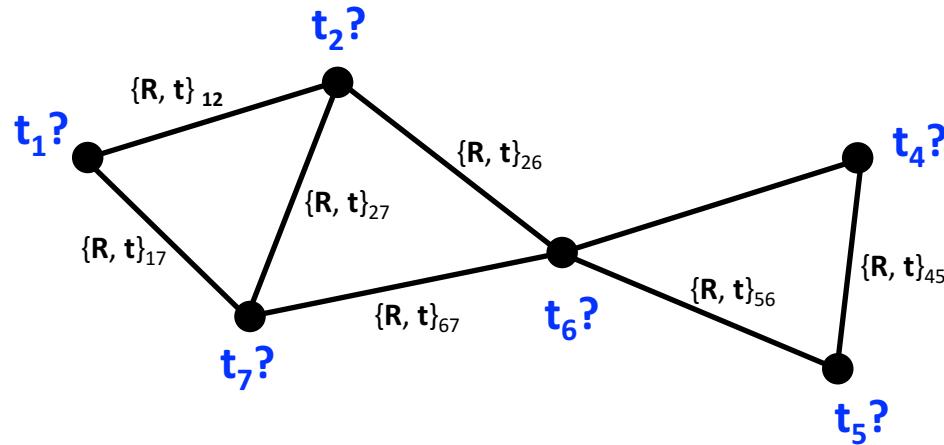


Global SfM

- Image
- Two-View Geometry

1. Estimate and filter global rotations

2. Estimate global translations: $\min_t \left\| t_{ij} - \frac{t_i - t_j}{\|t_i - t_j\|} \right\|$



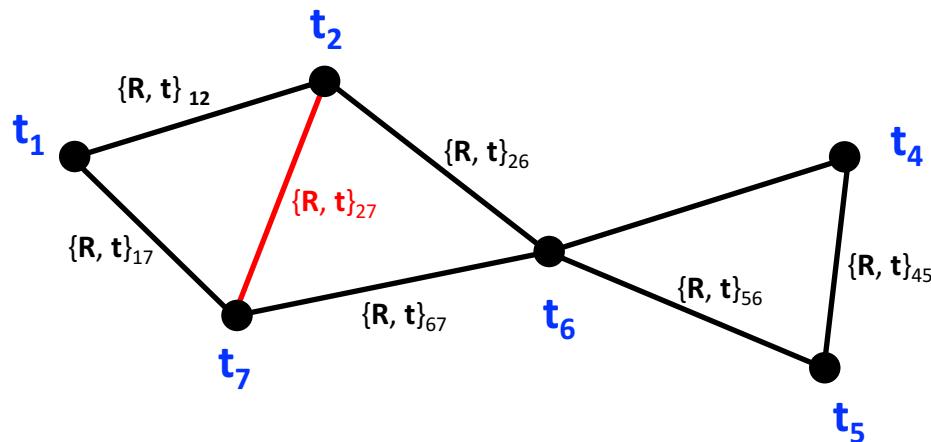
Global SfM

● Image
— Two-View Geometry

1. Estimate and filter global rotations

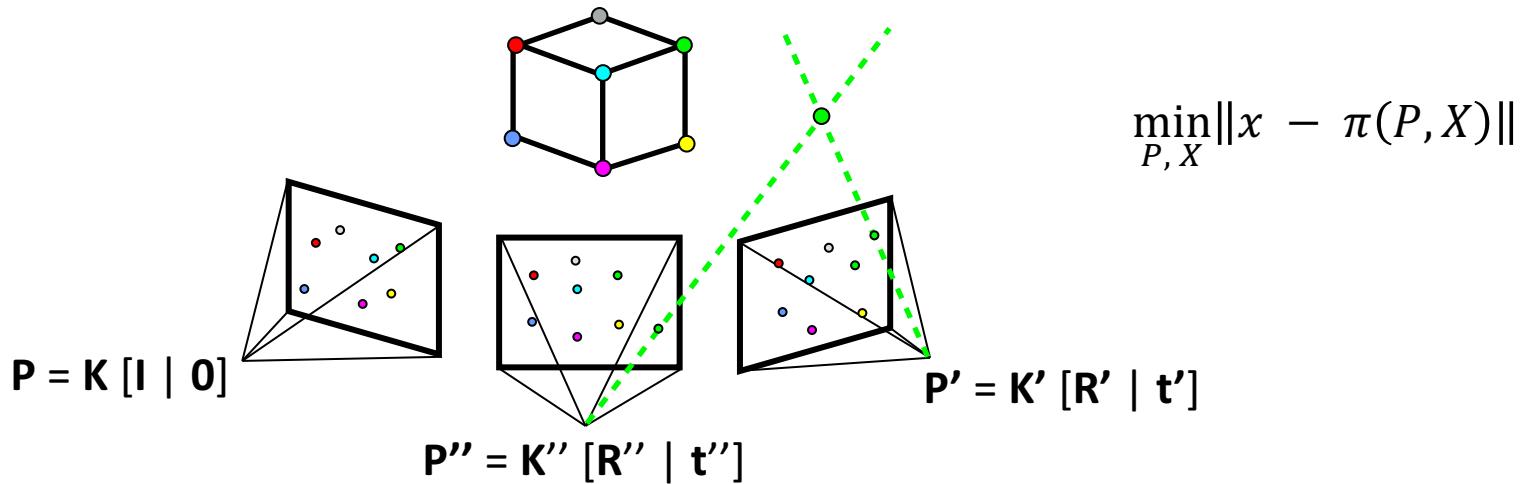
2. Estimate global translations: $\min_R \left\| t_{ij} - \frac{t_i - t_j}{\|t_i - t_j\|} \right\|$

Filter relative translations: $\left\| t_{ij} - \frac{t_i - t_j}{\|t_i - t_j\|} \right\| > \epsilon$

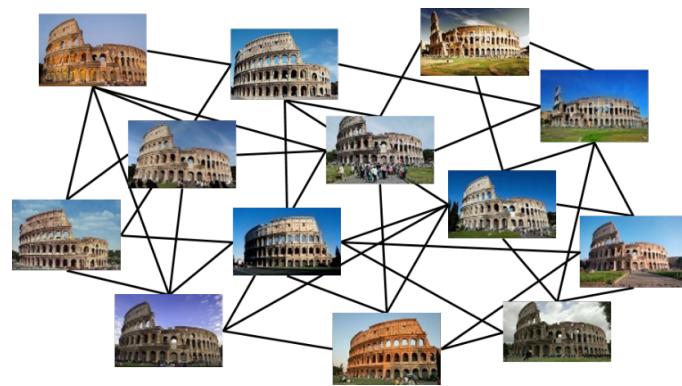


Global SfM

1. Estimate and filter global rotations
2. Estimate and filter global translations
3. Triangulate and refine with bundle adjustment



Hierarchical SfM



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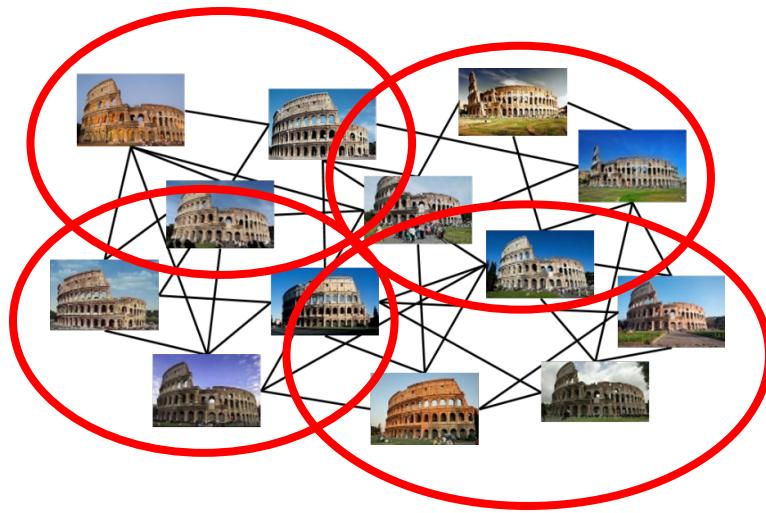


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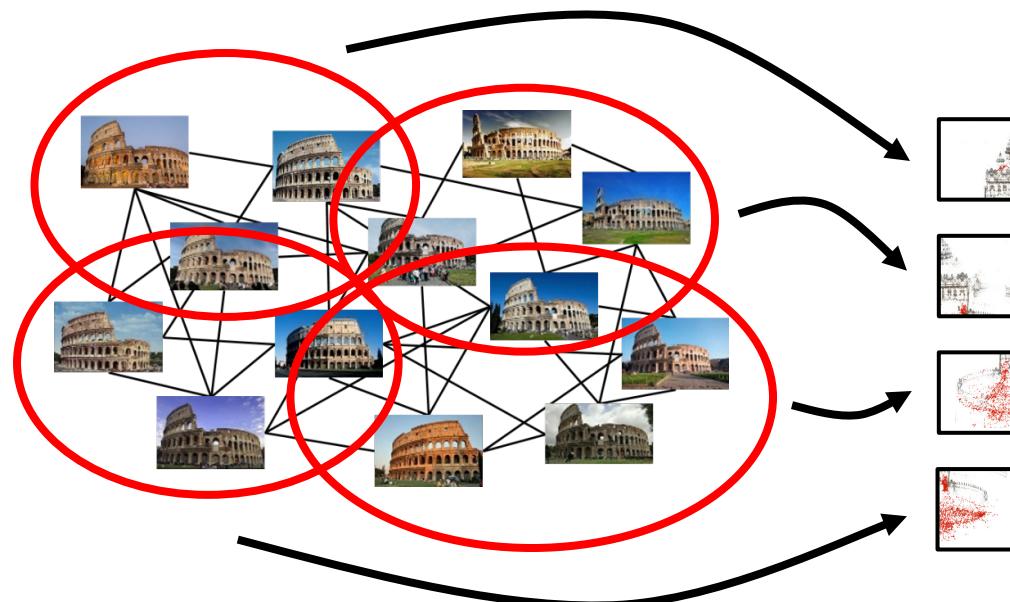
Hierarchical SfM

1. Hierarchical clustering of scene graph



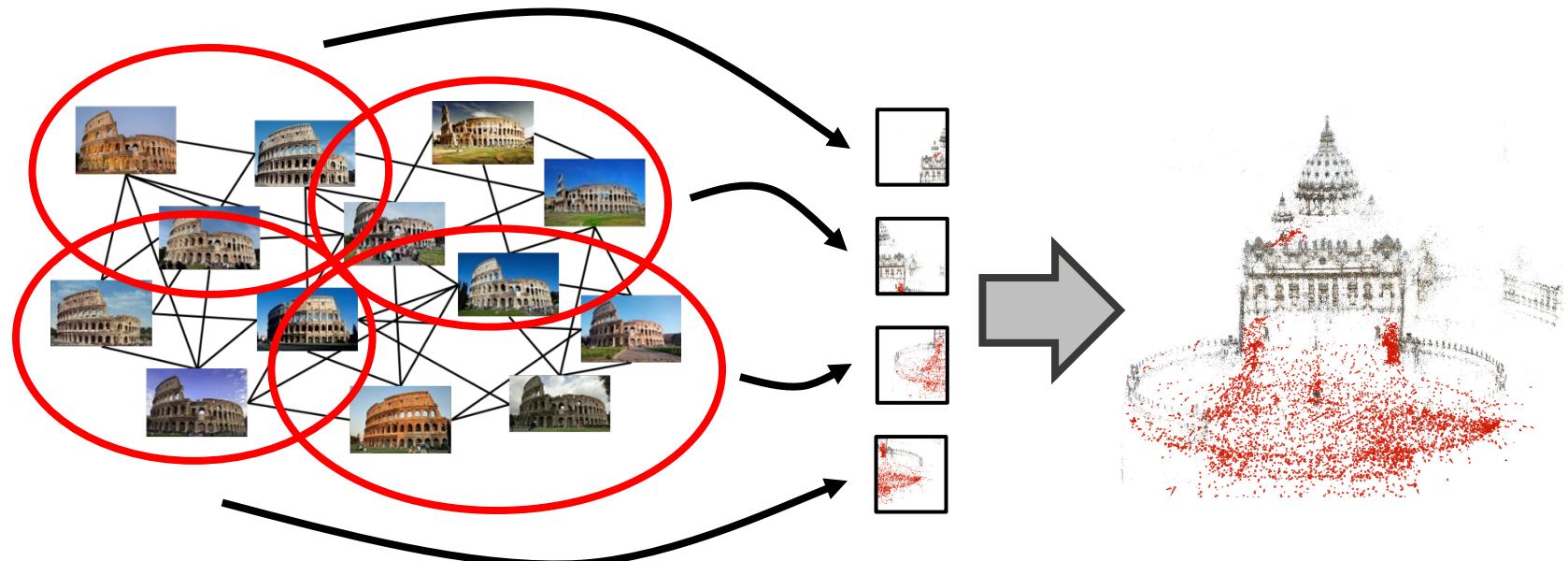
Hierarchical SfM

1. Hierarchical clustering of scene graph
2. Reconstruct clusters independently
(using incremental or global SfM)



Hierarchical SfM

1. Hierarchical clustering of scene graph
2. Reconstruct clusters independently
3. Merge clusters using similarity transformations



Structure-from-Motion

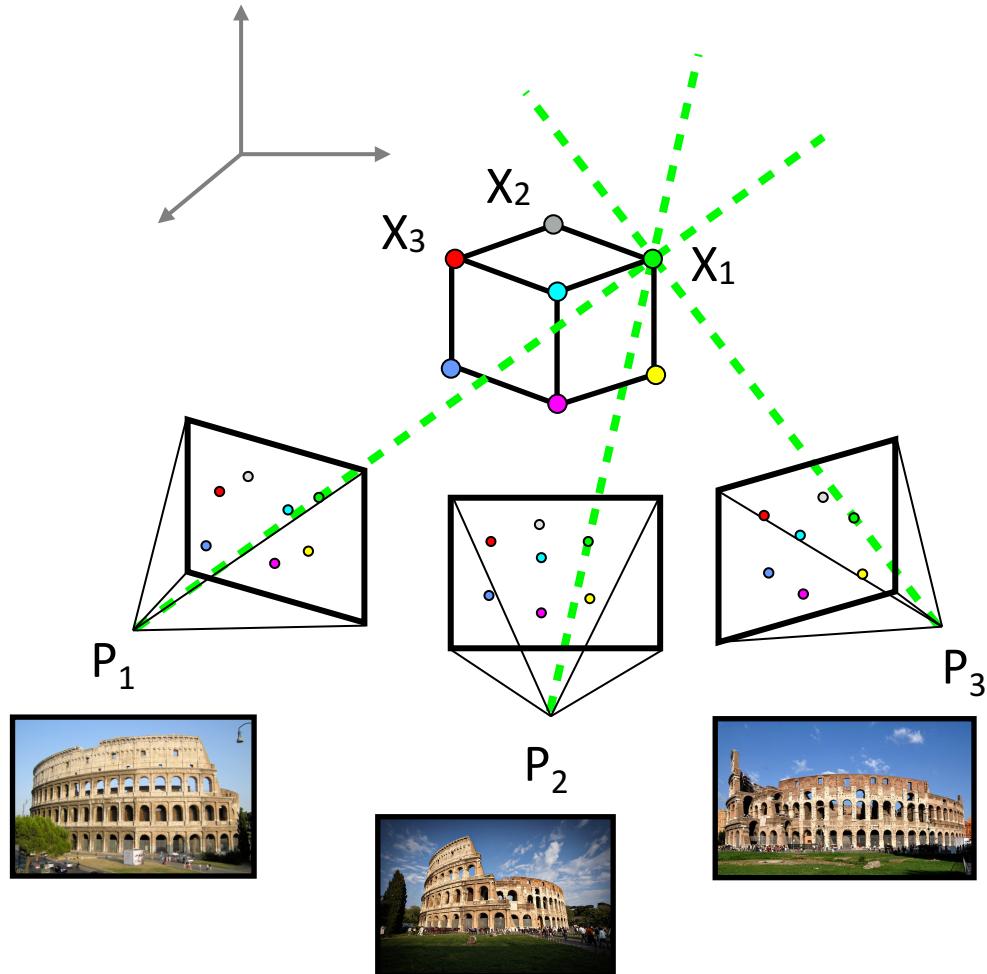
- Comparison

Method	Efficiency	Robustness	Accuracy
Incremental	-	++	+
Global	+	+	+
Hierarchical	++	-	-



Structure-from-Motion

- Joint estimation of ...
 - Structure \mathbf{X}_i
 - Cameras \mathbf{P}_j
- ... from motion, i.e.
 - images at different viewpoints



Challenges

Crowdsourced Data



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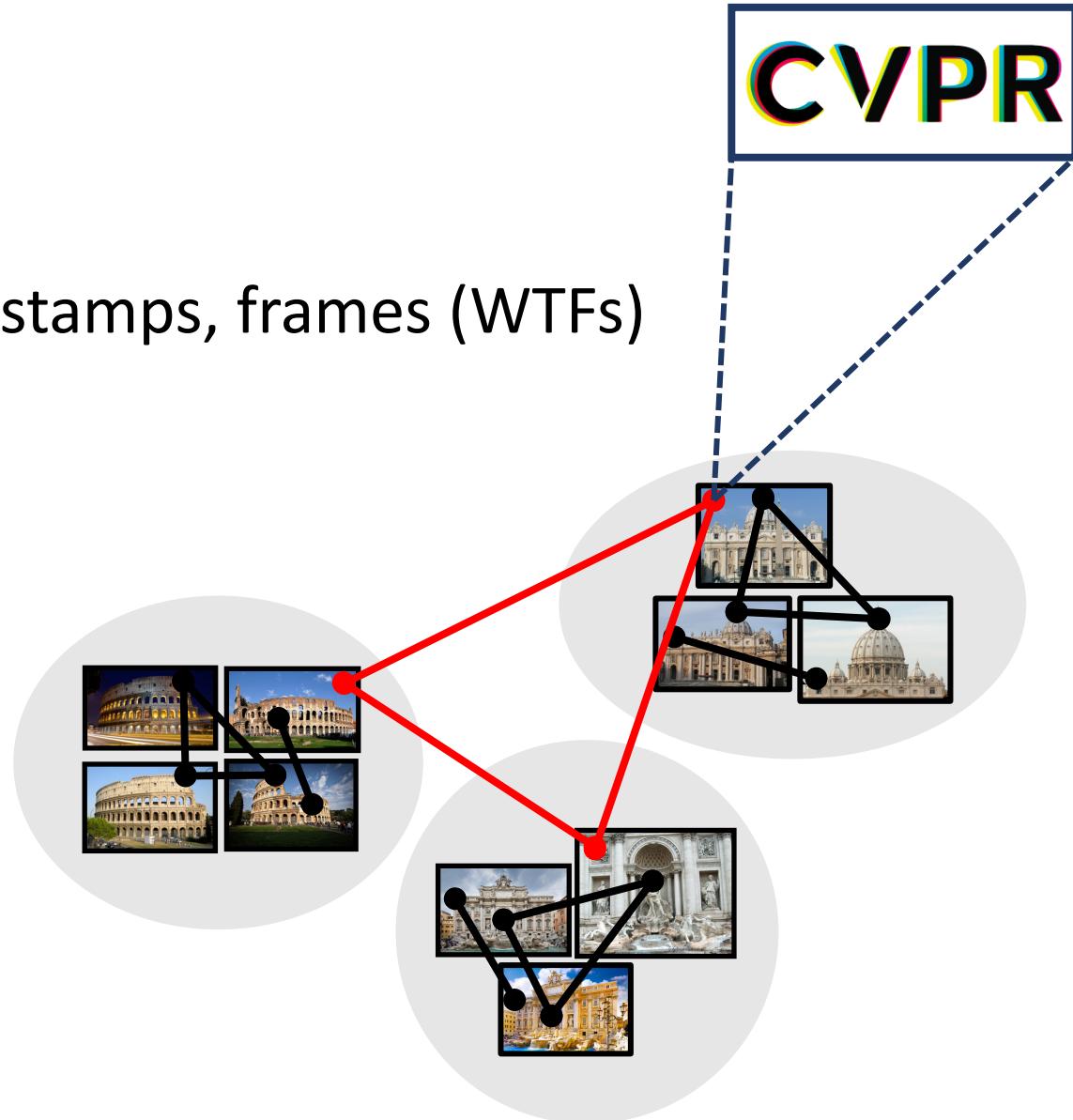


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WTFs

- Watermarks, timestamps, frames (WTFs)



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WTFs

- Detect pure translation at image border



Weyand et al. 2015, "Fixing WTFs: Detecting Image Matches caused by WTFs in Internet Photos"
Heinly et al. 2015, "Reconstructing the World in Six Days"



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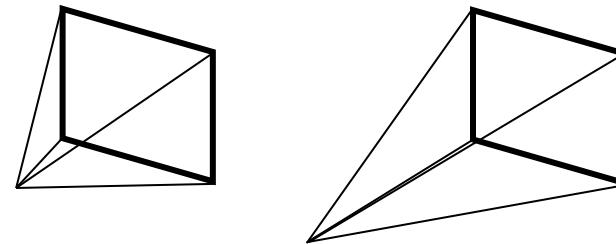
Microsoft URCV

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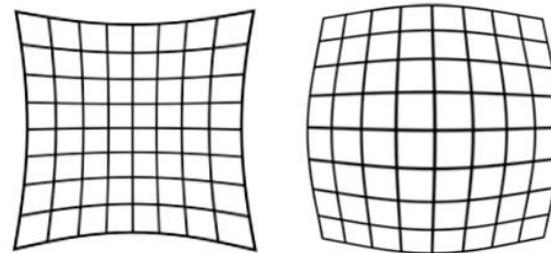
Calibration



- Focal length unknown
 - EXIF inaccurate/missing



- Image distortion



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Calibration

- Self-calibration
 - Two-view geometry estimation, e.g.
 - Stewenius et al. 2008, “A minimal solution for relative pose with unknown focal length”
 - Kukelova et al. 2015, “Efficient Solution to the Epipolar Geometry for Radially Distorted Cameras”
 - Absolute camera estimation
 - P4Pf, P4Pfr, etc.
Bujnak, Kukelova, Pajdla et al.
 - P3.5P
Wu 2015, “Pose Estimation with Unknown Focal Length”
 - Refinement in bundle adjustment

$$\min_{P, X, \mathbf{C}} \|x - \pi(P, X, \mathbf{C})\|$$



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Large-scale 3D Modeling from Crowdsourced Data

Scale ambiguity

- Inherent scale ambiguity of SfM



Scale ambiguity

- Use GPS EXIF tags for geo-registration



- Use semantics to infer scale
(e.g., prior on size of cars, trees, people, etc.)



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Dynamic objects

- Standard SfM formulation only for static objects



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Dynamic objects

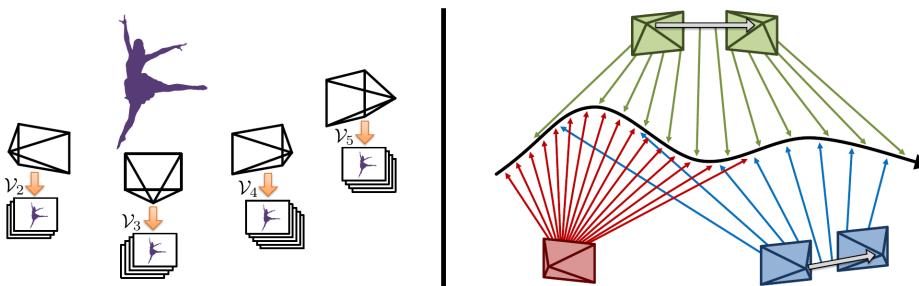
- From crowdsourced videos

Zheng et al. 2015, "Sparse Dynamic 3D Reconstruction from Unynchronized Videos"
Ji et al. 2014, "3D Reconstruction of Dynamic Textures in Crowdsourced Data"



- From crowdsourced images

Zheng et al. 2014, "Joint Object Class Sequencing and Trajectory Triangulation (JOST)"



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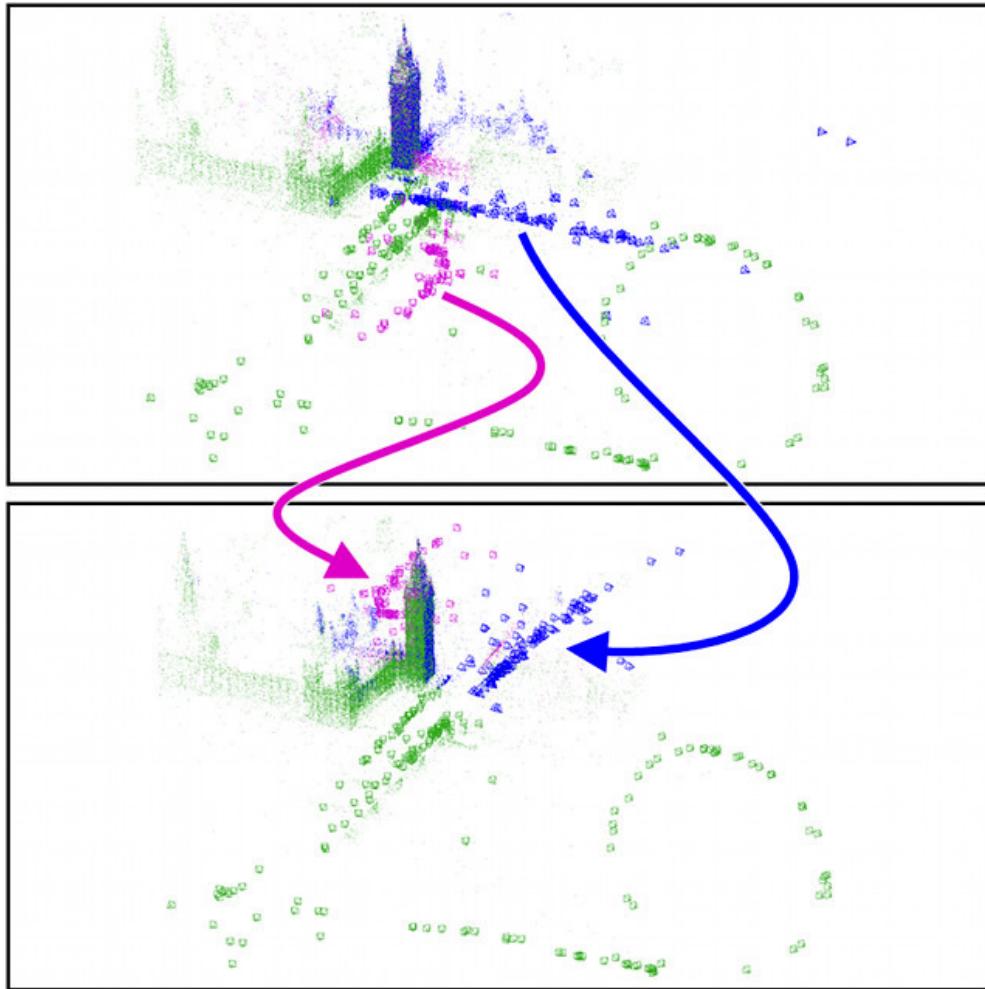
Large-scale 3D Modeling from Crowdsourced Data

Repetitive Structures

- Symmetries in man-made structures



Repetitive Structures



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Repetitive Structures

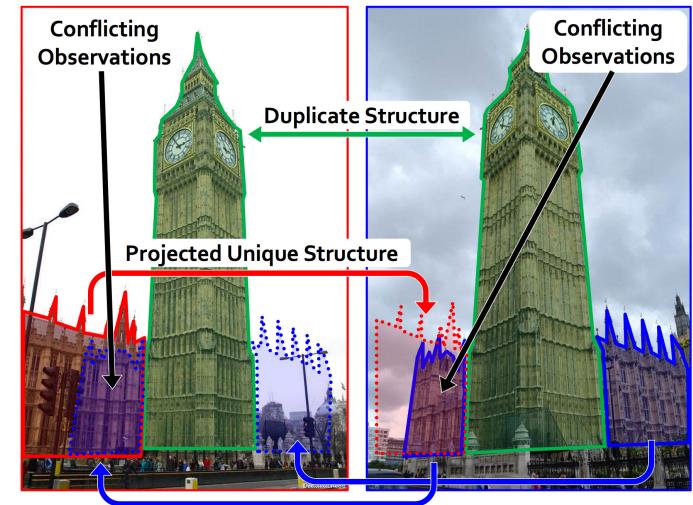
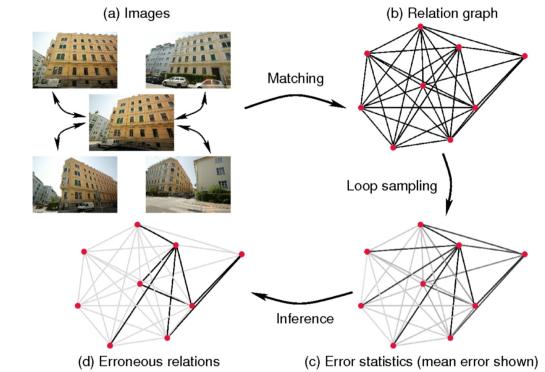
- Pre-processing
 - Remove inconsistent scene graph edges

Zach et al. 2010, "Disambiguating visual relations using loop constraints"

Wilson and Snavely 2013, "Network Principles for SfM: Disambiguating Repeated Structures with Local Context"

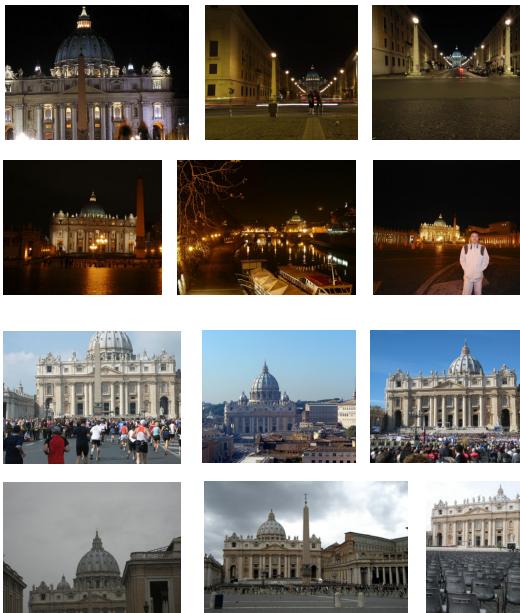
- Post-processing
 - Identify and correct duplicate structures

Heinly et al. 2014, "Correcting for Duplicate Scene Structure in Sparse 3D Reconstruction"



Illumination Change

- Day-night matching difficult / not possible



Night

Day



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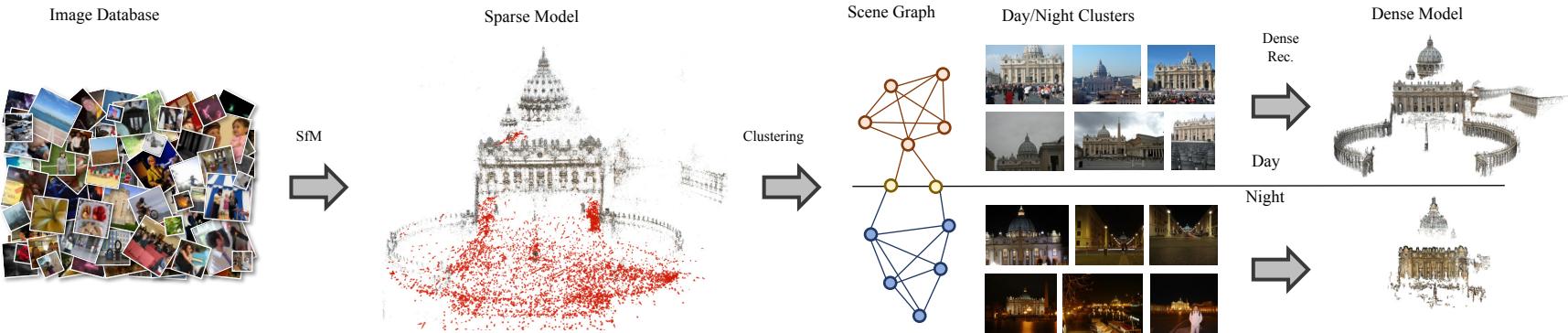
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Illumination Change



- Leverage transition images during dusk / dawn



Zhou et al. 2016, "Evaluating Local Features for Day-Night Matching"
Verdie et al. 2015, "TILDE: A Temporally Invariant Learned Detector"
Radenovic et al. 2016, "From Dusk Till Dawn: Modeling in the Dark"



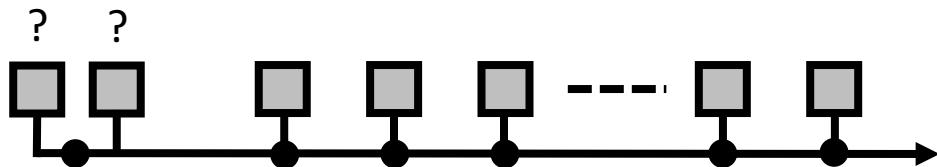
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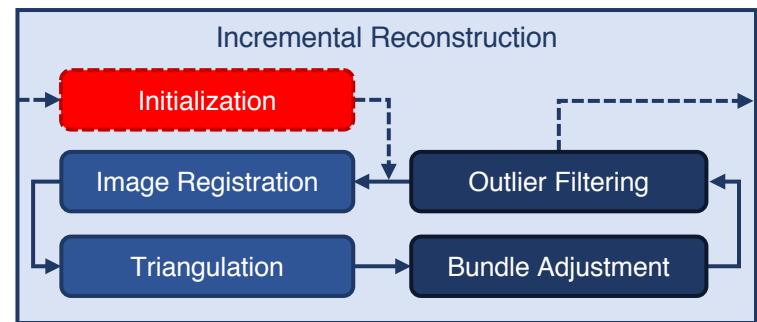
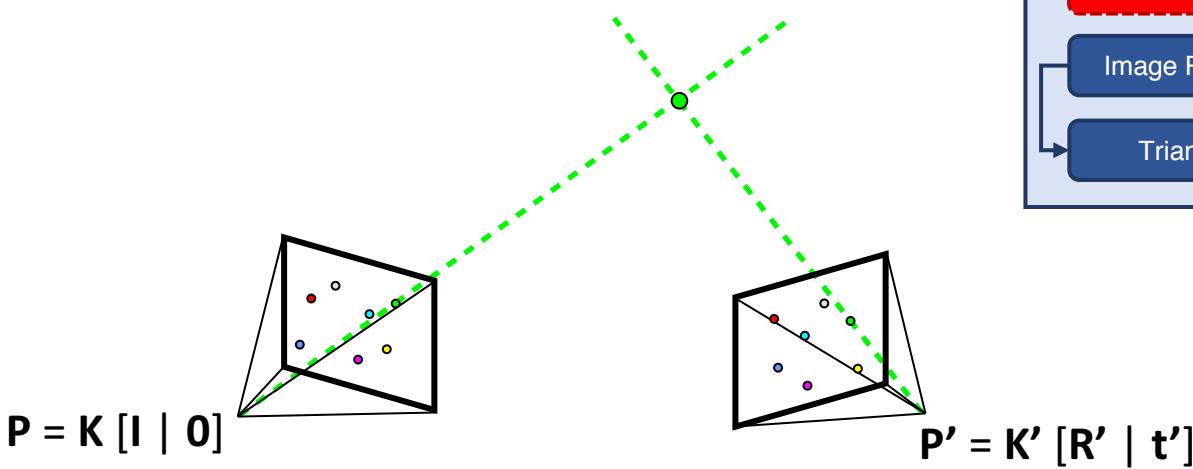
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Initial View Selection

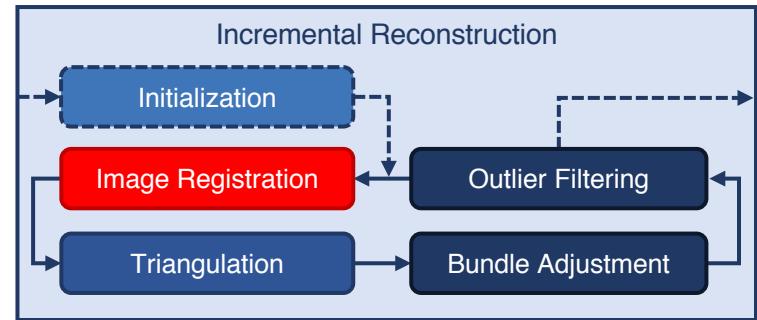
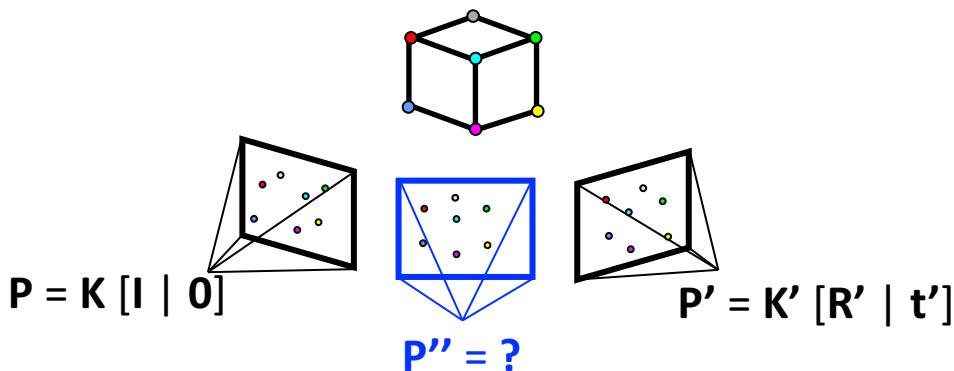
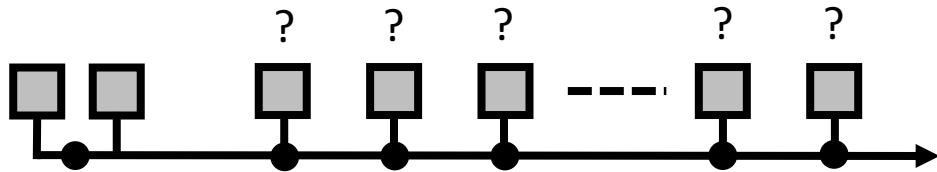


Trade-off:

- Triangulation angle
- Num. correspondences

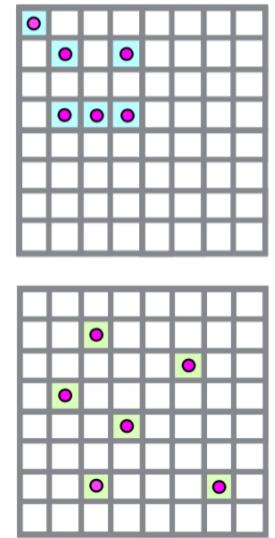
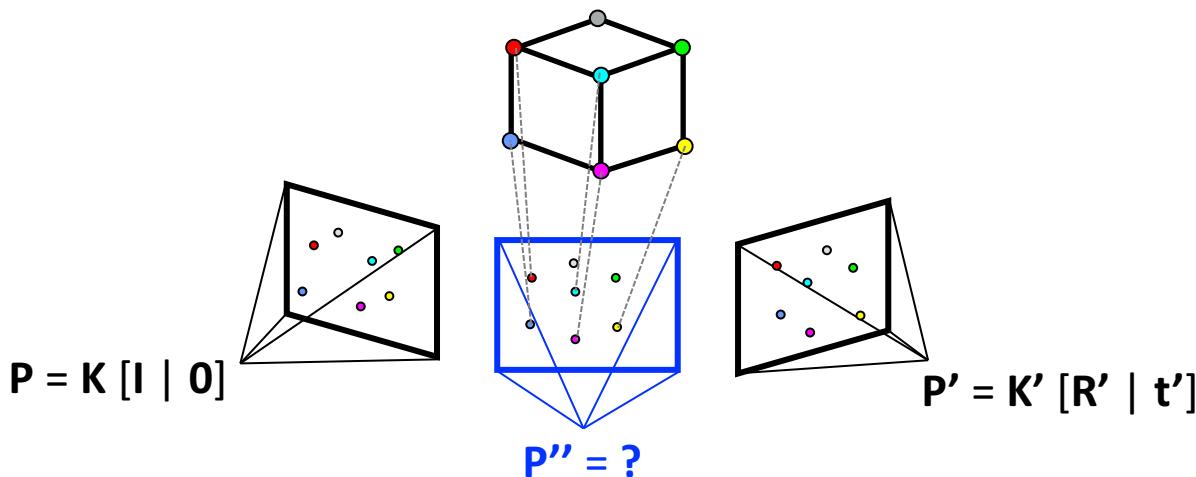


Next-Best View Selection



Next-Best View Selection

- Maximize number of 2D-3D correspondences

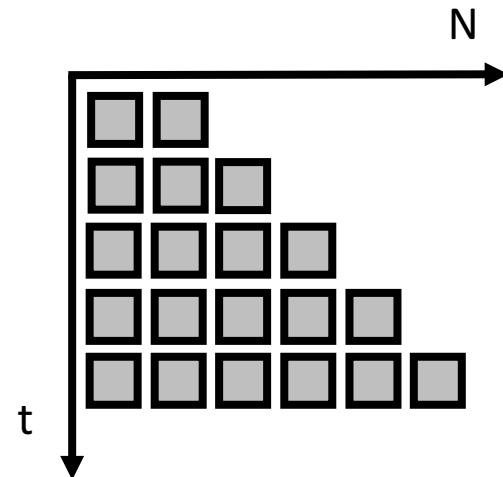
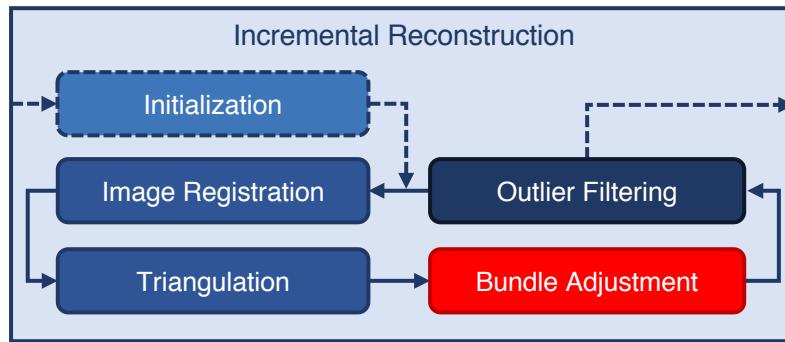


Snavely 2008, "Scene reconstruction and visualization from internet photo collections"
Schönberger and Frahm 2016, "Structure-from-Motion Revisited"



Scalability

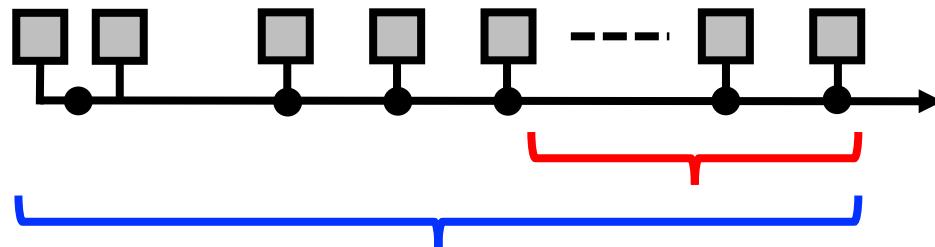
- $O(N^3)$ complexity in bundle adjustment



Scalability

- Efficient bundle adjustment
 1. Local after each camera registration
 2. Global after model grows by constant factor
- Inexact step algorithms (PCG)
 - $O(N)$ complexity

Agarwal et al. 2010, “Bundle-Adjustment in the Large”
Wu 2013, “Towards Linear-Time Incremental Structure-from-Motion”



Open Source Pipeline

Unstructured Images



SfM

Sparse Model



MVS

Dense Model



COLMAP - 3D reconstruction pipeline:

<https://github.com/colmap/colmap>



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Questions?

Structure-from-Motion Revisited

Johannes L. Schönberger, Jan-Michael Frahm

CVPR 2016

Code available at:

<https://github.com/colmap/colmap>



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