

High dimensional time series analysis



1. Tidy time series tsibbles

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Outline

- 1 Time series data
- 2 Time plots

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- 2 Time plots

Tidyverts packages

tidyverts.org



Time series data

- Four-yearly Olympic winning times
- Annual Google profits
- Quarterly Australian beer production
- Monthly rainfall
- Weekly retail sales
- Daily IBM stock prices
- Hourly electricity demand
- 5-minute freeway traffic counts
- Time-stamped stock transaction data

Class packages

```
# Data manipulation and plotting functions
library(tidyverse)
# Time series manipulation
library(tsibble)
# Forecasting functions
library(fable)
# Time series graphics and statistics
library(feasts)
# Tidy time series data
library(tsibbledata)
```

```
A tsibble: 15,150 \times 6 [1Y]
##
  # Kev:
                Country [263]
##
      Year Country
                                GDP Imports Exports Population
##
      <dbl> <fct>
                              <dbl>
                                      <dbl>
                                              <dbl>
                                                         <dbl>
       1960 Afghanistan 537777811.
                                       7.02
                                               4.13
                                                       8996351
##
       1961 Afghanistan
                                       8.10
                                               4.45
                                                       9166764
##
                         548888896.
##
    3
       1962 Afghanistan
                         546666678.
                                       9.35
                                               4.88
                                                       9345868
       1963 Afghanistan
                                      16.9
                                               9.17
                                                       9533954
##
                         751111191.
                                               8.89
                                                       9731361
##
    5
       1964 Afghanistan
                         800000044.
                                      18.1
       1965 Afghanistan 1006666638.
##
    6
                                      21.4
                                              11.3
                                                       9938414
##
       1966 Afghanistan 1399999967.
                                      18.6
                                               8.57
                                                       10152331
##
       1967 Afghanistan 1673333418.
                                      14.2
                                               6.77
                                                       10372630
##
    9
       1968 Afghanistan 1373333367.
                                      15.2
                                               8.90
                                                       10604346
##
       1969 Afghanistan 1408888922.
                                      15.0
                                              10.1
                                                       10854428
  # ... with 15,140 more rows
```

```
A tsibble: 15,150 x 6 [1Y]
##
    Key:
                Country [263]
##
       Year Country
                                GDP Imports Exports Population
##
      Index <fct>
                              <dbl>
                                      <dbl>
                                              <dbl>
                                                         <dbl>
       1960 Afghanistan 537777811.
                                       7.02
                                               4.13
                                                       8996351
##
       1961 Afghanistan
                                       8.10
                                               4.45
                                                       9166764
##
                         548888896.
##
    3
       1962 Afghanistan
                         546666678.
                                       9.35
                                               4.88
                                                       9345868
       1963 Afghanistan
                                      16.9
                                               9.17
                                                       9533954
##
    4
                         751111191.
                                               8.89
                                                       9731361
##
    5
       1964 Afghanistan
                         800000044.
                                      18.1
       1965 Afghanistan 1006666638.
##
    6
                                      21.4
                                              11.3
                                                       9938414
##
       1966 Afghanistan 1399999967.
                                      18.6
                                               8.57
                                                       10152331
##
       1967 Afghanistan 1673333418.
                                      14.2
                                               6.77
                                                       10372630
##
    9
       1968 Afghanistan 1373333367.
                                      15.2
                                               8.90
                                                       10604346
##
       1969 Afghanistan 1408888922.
                                      15.0
                                              10.1
                                                       10854428
##
   # ... with 15,140 more rows
```

```
A tsibble: 15,150 x 6 [1Y]
##
     Key:
                Country [263]
##
       Year Country
                                GDP Imports Exports Population
##
      Index
             Kev
                              <dbl>
                                       <dbl>
                                               <dbl>
                                                          <dbl>
       1960 Afghanistan
                         537777811.
                                       7.02
                                                4.13
                                                        8996351
##
       1961 Afghanistan
                                       8.10
                                                4.45
                                                        9166764
##
    2
                         548888896.
##
    3
       1962 Afghanistan
                         546666678.
                                       9.35
                                                4.88
                                                        9345868
       1963 Afghanistan
                                       16.9
                                                9.17
                                                        9533954
##
    4
                         751111191.
                                                8.89
                                                        9731361
##
    5
       1964 Afghanistan
                         800000044.
                                       18.1
       1965 Afghanistan 1006666638.
##
    6
                                       21.4
                                               11.3
                                                        9938414
##
       1966 Afghanistan 1399999967.
                                       18.6
                                                8.57
                                                       10152331
##
       1967 Afghanistan 1673333418.
                                       14.2
                                                6.77
                                                       10372630
##
    9
       1968 Afghanistan 1373333367.
                                       15.2
                                                8.90
                                                       10604346
##
       1969 Afghanistan 1408888922.
                                       15.0
                                               10.1
                                                       10854428
##
   # ... with 15,140 more rows
```

```
A tsibble: 15,150 x 6 [1Y]
##
     Key:
                Country [263]
##
       Year Country
                                 GDP Imports Exports Population
                          Measured variables
##
      Index
             Kev
       1960 Afghanistan
                         537777811.
                                        7.02
                                                4.13
                                                        8996351
##
       1961 Afghanistan
                                        8.10
                                                4.45
                                                        9166764
##
                         548888896.
##
    3
       1962 Afghanistan
                         546666678.
                                        9.35
                                                4.88
                                                        9345868
       1963 Afghanistan
                                       16.9
                                                9.17
                                                        9533954
##
                         751111191.
                         800000044.
                                                        9731361
##
    5
       1964 Afghanistan
                                       18.1
                                                8.89
##
    6
       1965 Afghanistan 1006666638.
                                       21.4
                                               11.3
                                                        9938414
##
       1966 Afghanistan 139999967.
                                       18.6
                                                8.57
                                                       10152331
##
       1967 Afghanistan 1673333418.
                                       14.2
                                                6.77
                                                       10372630
##
    9
       1968 Afghanistan 1373333367.
                                       15.2
                                                8.90
                                                       10604346
##
       1969 Afghanistan 1408888922.
                                       15.0
                                               10.1
                                                       10854428
   # ... with 15,140 more rows
```

```
## # A tsibble: 24,320 x 5 [10]
##
  # Kev:
               Region, State, Purpose [304]
##
     Quarter Region State Purpose Trips
##
       <qtr> <chr> <chr> <chr>
                                    <dbl>
                           Business 135.
##
   1 1998 Q1 Adelaide SA
                           Business 110.
##
   2 1998 Q2 Adelaide SA
   3 1998 Q3 Adelaide SA Business 166.
##
##
   4 1998 Q4 Adelaide SA
                           Business 127.
   5 1999 Q1 Adelaide SA
                           Business 137.
##
##
   6 1999 O2 Adelaide SA
                           Business
                                     200.
                           Business 169.
##
   7 1999 Q3 Adelaide SA
##
   8 1999 Q4 Adelaide SA
                           Business 134.
##
   9 2000 Q1 Adelaide SA
                           Business 154.
  10 2000 Q2 Adelaide SA
                           Business
                                    169.
## # ... with 24,310 more rows
```

```
## # A tsibble: 24,320 x 5 [10]
##
  # Kev:
               Region, State, Purpose [304]
##
     Quarter Region State Purpose
                                    Trips
             <chr> <chr> <chr>
##
     Index
                                    <dbl>
                           Business 135.
##
   1 1998 Q1 Adelaide SA
##
   2 1998 Q2 Adelaide SA
                           Business 110.
   3 1998 Q3 Adelaide SA
                           Business 166.
##
##
   4 1998 Q4 Adelaide SA
                           Business 127.
   5 1999 Q1 Adelaide SA
                           Business
##
                                    137.
##
   6 1999 O2 Adelaide SA
                           Business
                                     200.
                           Business
##
   7 1999 Q3 Adelaide SA
                                     169.
##
   8 1999 Q4 Adelaide SA
                           Business 134.
##
   9 2000 Q1 Adelaide SA
                           Business 154.
  10 2000 Q2 Adelaide SA
                           Business
                                     169.
## # ... with 24,310 more rows
```

```
## # A tsibble: 24,320 x 5 [10]
##
  # Kev:
               Region, State, Purpose [304]
##
     Quarter Region State Purpose
                                     Trips
                                     <fdb>
##
      Index
              Kevs
                            Business
##
   1 1998 Q1 Adelaide SA
                                      135.
##
   2 1998 O2 Adelaide SA
                            Business
                                     110.
   3 1998 Q3 Adelaide SA
                            Business 166.
##
##
   4 1998 Q4 Adelaide SA
                            Business 127.
   5 1999 Q1 Adelaide SA
##
                            Business
                                     137.
##
   6 1999 O2 Adelaide SA
                            Business
                                      200.
                            Business
##
   7 1999 Q3 Adelaide SA
                                      169.
##
   8 1999 Q4 Adelaide SA
                            Business 134.
##
   9 2000 Q1 Adelaide SA
                            Business
                                     154.
  10 2000 Q2 Adelaide SA
                            Business
                                      169.
  # ... with 24,310 more rows
```

```
## # A tsibble: 24,320 x 5 [10]
##
  # Kev:
               Region, State, Purpose [304]
##
     Quarter Region State Purpose
                                     Trips
##
      Index
              Kevs
                                      Measure
                            Business
##
   1 1998 Q1 Adelaide SA
                                      135.
##
   2 1998 O2 Adelaide SA
                            Business
                                     110.
   3 1998 Q3 Adelaide SA
                            Business 166.
##
##
   4 1998 Q4 Adelaide SA
                            Business 127.
   5 1999 Q1 Adelaide SA
##
                            Business
                                     137.
##
   6 1999 O2 Adelaide SA
                            Business
                                      200.
                            Business
##
   7 1999 Q3 Adelaide SA
                                      169.
##
   8 1999 Q4 Adelaide SA
                            Business 134.
##
   9 2000 Q1 Adelaide SA
                            Business
                                     154.
  10 2000 Q2 Adelaide SA
                            Business
                                      169.
  # ... with 24,310 more rows
```

```
## # A tsibble: 24,320 x 5 [10]
##
   # Kev:
                Region, State, Purpose [304]
##
      Quarter Region State Purpose
                                       Trips
##
      Index
               Kevs
                                        Measure
                              Business
##
    1 1998 Q1 Adelaide SA
                                        135.
##
    2 1998 O2 Adelaide SA
                              Business
                                        110.
                                               Domestic visitor
    3 1998 Q3 Adelaide SA
                              Business
                                        166.
##
                                               nights in thousands
                              Business
                                        127.
##
    4 1998 Q4 Adelaide SA
                                               by state/region and
    5 1999 Q1 Adelaide SA
##
                              Business
                                        137.
                                               purpose.
##
    6 1999 Q2 Adelaide SA
                              Business
                                        200.
                              Business
                                        169.
##
    7 1999 Q3 Adelaide SA
##
    8 1999 Q4 Adelaide SA
                              Business
                                        134.
##
    9 2000 Q1 Adelaide SA
                              Business
                                        154.
   10 2000 Q2 Adelaide SA
                              Business
                                        169.
   # ... with 24,310 more rows
```

A tsibble allows storage and manipulation of time series in R.

It contains:

- Measured variable(s): numbers of interest
- An index: time information about the observation
- Key variable(s): optional unique identifiers for each series

Example

```
library(tsibble)
v <- tsibble(year = 2012:2016,</pre>
 y = c(123,39,78,52,110), index = year)
٧
## # A tsibble: 5 x 2 [1Y]
##
    year
## <int> <dbl>
## 1 2012 123
## 2 2013 39
## 3 2014 78
## 4 2015
          52
```

For observations more frequent than once per year, we need to use a time class function on the index.

```
Z
## # A tibble: 5 x 2
    Month Observation
##
## <chr>
                    <dbl>
## 1 2019 Jan
                       50
## 2 2019 Feb
                       23
## 3 2019 Mar
                       34
## 4 2019 Apr
                       30
```

For observations more frequent than once per year, we need to use a time class function on the index.

```
z %>%
  mutate(Month = yearmonth(Month)) %>%
  as tsibble(index = Month)
## # A tsibble: 5 x 2 [1M]
        Month Observation
##
##
        <mth>
                     <dbl>
## 1 2019 Jan
                        50
## 2 2019 Feb
                        23
```

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Common time index variables can be created with these functions:

| Frequency | Function |
|-----------|-----------------|
| Annual | start:end |
| Quarterly | yearquarter() |
| Monthly | yearmonth() |
| Weekly | yearweek() |
| Daily | as_date(),ymd() |
| Sub-daily | as_datetime() |

The key to many time series

olympic_running

```
## # A tsibble: 312 x 4 [4Y]
## # Key: Length, Sex [14]
      Year Length Sex Time
##
     <int> <int> <chr> <dbl>
##
      1896
## 1
             100 men
                       12
##
   2
      1900
             100 men 11
## 3
      1904
             100 men 11
##
      1908
                    10.8
   4
             100 men
##
   5
      1912
             100 men
                      10.8
```

The key to many time series

```
olympic running %>% as_tsibble(
 key = id(Length, Sex), index = Year)
## Warning: id() is deprecated for creating ke
## Please use key = c(Length, Sex).
## # A tsibble: 312 x 4 [4Y]
## # Key: Length, Sex [14]
##
```

Year Length Sex Time

<int> <int> <dbl> ## 1 1896 100 men 12

2 1900 100 men 11

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Australian GDP

```
aus_economy <- global_economy %>%
  filter(Country == "Australia")
```

```
## # A tsibble: 58 x 6 [1Y]
```

| ## | # | Key: | Counti | ry [1] | | | |
|----|---|-------------|-------------|-------------|-------------|-------------|------|
| ## | | Year | Country | GDP | Imports | Exports | Popu |
| ## | | <dbl></dbl> | <fct></fct> | <dbl></dbl> | <dbl></dbl> | <dbl></dbl> | |
| ## | 1 | 1060 | Auctrolia | 10572100407 | 1/1 | 12.0 | 10 |

10 13.0 ## 1960 Australia 185/318848/. 14.1

1961 Australia 19648336880. 15.0 12.4 10

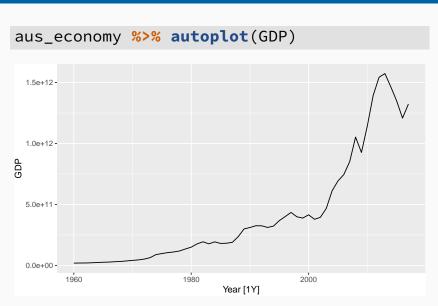
1962 Australia 19888005376. ## 12.6 13.9

10 1963 Australia 21501847911. 13.8 13.0 ##

10 1964 Australia 23758539590. ## 13.8 14.9 11 5

1965 Australia 25931235301. 15.3 13.2 11 1966 Australia 27261731437. ## 15.1 12.9 11

Australian GDP

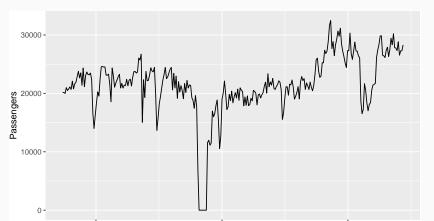


Outline

- 1 Time series data
- 2 Time plots

Time plots

```
ansett %>%
  filter(Airports=="MEL-SYD", Class=="Economy") %>%
  autoplot(Passengers)
```

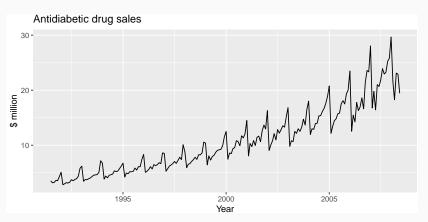


Time plots

```
## # A tsibble: 204 x 3 [1M]
##
         Month TotalC Cost
         <mth> <dbl> <dbl>
##
    1 1991 Jul 3526591 3.53
##
   2 1991 Aug 3180891 3.18
##
   3 1991 Sep 3252221 3.25
##
##
   4 1991 Oct 3611003 3.61
    5 1991 Nov 3565869
##
                        3.57
    6 1991 Dec 4306371
##
                        4.31
##
   7 1992 Jan 5088335 5.09
    8 1992 Feb 2814520 2.81
##
```

Time plots

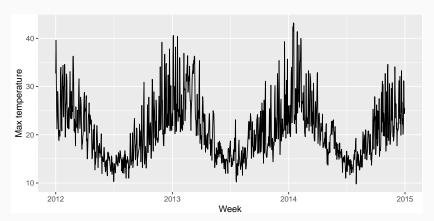
```
a10 %>% autoplot(Cost) +
  ylab("$ million") + xlab("Year") +
  ggtitle("Antidiabetic drug sales")
```



Your turn

- Create plots of the following time series: Bricks from aus_production, Lynx from pelt, Google from gafa_stock
- Use help() to find out about the data in each series.
- For the last plot, modify the axis labels and title.

```
maxtemp %>%
autoplot(Temperature) +
xlab("Week") + ylab("Max temperature")
```



```
maxtemp %>%
  ggplot(aes(x = Day, y = Temperature)) +
  geom_point() +
  xlab("Week") + ylab("Max temperature")
```

