EECS 112 & CSE 132, FALL 2017

Homework 4

Due date: December 1, 2017

Student ID:					Name:

- 1. Below is a list of 64-bit memory address references, given as word addresses: 0x03, 0xb4, 0x2b, 0x02, 0xbf, 0x58, 0xbe, 0x0e, 0xb5, 0x2c, 0xba, 0xfd Consider a direct-mapped cache with 16 one-word blocks. Assume that cache is initially empty.
- 1.a. Write down a sequence of characters showing the result of each reference. 'H' for a hit, 'P' for a miss without having to replace a block already in cache, 'R' for a miss requiring replacement. For instance if first four references are miss on empty cache, second four are hits, and third four references are misses requiring replacement, the character sequence will be 'PPPPHHHHRRRR'

Cache Size: 16 -> 4 bit addressable index = 1 bit hex index tag PPPP PPPR PPPP adhress 0 0,03 V PI 7 0 P4 3 Ox 2B V 13 PZ 4 0x02 ~ P4 68 ς Ox8F U PS 4 0x58 v P6 7 OXBE V PO ę PC 9 OXOEV RI 110 0x85 V P8 BXZG V P9 C Pli OxBA U PIO OXFDV PI

Assume word addressable

1.b. Repeat 1.a. for a direct mapped cache with two-word blocks and the same total number of blocks as 1.a.

address		Result	Content after reference
address	(- 1	ICBUIC	Consens after reference
0x03	+=1	ρ	/ mem(0x02) > < 1, mem(0x03)>
0000 0011		1	() MENIOROS) > (1, 1 TOMICO X O S)
	1:2	h	
0x84	• •	P	(2, mem (0xβ4)) < 2, men (0xβ5)>
1011 0100		,	July of the state
	1:5	-	
0×2B		P	(5, mon(OxZA)>(5, men(0xZB)>
0010 101			
•	1:1		(0. 25)
$0x^{\infty}$		-	$\langle 1, mem (0 \times 02) \rangle \langle 1, mem (0 \times 03) \rangle$
0000 0000			•
0×8F	 - 7		4
UXDT		P	<pre><7, mem(0xBE)><7, mem(0xBF)></pre>
1011 1111			•
0 _x 58	1-4	n	(0.50)
		P	<4, mem (0x58)><4, mem (0x59)>
0101 1000	1.9		
OXBE	1=7	1.1	(7, mem(0xBE)>(7, mem(0xBF)>
		H	(), MEM (UXDE I) (), MEM (UXD.)
1011 1110	+ =7		
0×0E	7-7	R	(7, men (0x0E)><7, men (0x0F)>
0000 1110			(), mem (UXUC) / \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
_	 - 2		
0xB5	• -	H	(2, mem (0xB4)>(2, mem (0xB5)>
1011 0101		\ \ \ .	,
	4=6	2	10 1 20
0x2C		9	<6, mem(0x2c)>(6, mem(0x2D)>
0010 1104			
	+=5		/ 5 /A AAN / 5 (p. 25)
OxBA		R	<5, mem(0xBA)>(5, mem (0xBB)>
1911 1010			,
0.50	+=2	0	(E (0 EC)) (0 ED)
OxFD		R	<5, mem(0xFC)><5, mem(0xFD))
1111 1101			

1.c. Repeat 1.a. for a direct mapped cache with four-word blocks and the same total number of blocks as 1.a.

Reference	R	esult	Content after reference
0000 001) 0×03 f:	20	P	$\langle 0, mem(0x00) \rangle \langle 0, mem(0x01) \rangle \langle 0, mem(0x02) \rangle \langle 0, mem(0x03) \rangle$
0×84	=1	P	<pre></pre> <pre><</pre>
	= 1	R	<pre><1 ,mem(0x78)><1,mem(0x29)><1,mem(0x2A)><1,mem(0x2B)></pre>
0000 0010	=0	Н	<0,nem(0x00)><0,nem(0x01)><0,nem(0x02)><0,nem(0x03)>
0xBF	-3	Р	$\langle 3,mem(OxBC)\rangle\langle 3,mem(OxBD)\rangle\langle 3,mem(OxBE)\rangle\langle 3,mem(OxBF)\rangle$
0x58	₹ Z	Р	$\langle 7, mem(0x58) \rangle \langle 2, mem(0x59) \rangle \langle 7, mem(0x5A) \rangle \langle 2, mem(0x5B) \rangle$
0×BE +-		Н	$\langle 3, mem(OxBC) \rangle \langle 3, mem(OxBD) \rangle \langle 3, mem(OxBE) \rangle \langle 3, mem(OxBF) \rangle$
OXOE	=3	R	$\langle 3, mem(OxOC) \rangle \langle 3, mem(OxOD) \rangle \langle 3, mem(OxOE) \rangle \langle 3, mem(OxOF) \rangle$
0×85		R	$\langle 1,mem(OxB4)\rangle\langle 1,mem(OxB5)\rangle\langle 1,mem(OxB6)\rangle\langle 1,mem(OxB7)\rangle$
0018 (100 0×2C		R	$\langle 3, mem(Ox2C) \rangle \langle 3, mem(Ox2D) \rangle \langle 3, mem(Ox2E) \rangle \langle 3, mem(Ox2F) \rangle$
	-2	R	$\langle 2,mem(OxB8)\rangle\langle 2,mem(OxB9)\rangle\langle 2,mem(OxBA)\rangle\langle 2,mem(OxBB)\rangle$
0×F0 1111 (101	-3	R	$\langle 3, mem(OxFC) \rangle \langle 3, mem(OxFP) \rangle \langle 3, mem(OxFE) \rangle \langle 3, mem(OxFF) \rangle$

1.d. Which cache choice is optimum for the given access sequence?

2. Consider a direct mapped cache with a total data capacity of 2^B bytes, and a block size of 2^b bytes. Assume that the input byte address is A bits. Calculate the total number of bits required to fabricate this cache. You should consider both valid and dirty bit.

3. Cache block size (B) can affect both miss rate and miss latency. Find the block size that minimizes the total miss latency given the following miss rates (same for instruction and data cache) for various block sizes if:

8: 4%

16: 3%

32: 2%

64: 1.5%

128: 1%

3.1. Miss penalty is 20 ×B cycles

	miss latency	cycles	— 1
8:44		6.4	Best:
(c: 3%	3% ·20·16	9,6	B=8
32:2%	7%.20.32	12.8	
54:1.5%	1.5%.20.64	19.2	
128: 1%	. 1% .20.128	Z5, 6	

3.2. Miss penalty is 20 +B cycles

		1,12 1.08	Best:
37	2%.52	1,04	B=32
128	1,5%,84 1%,148	1.2.6 1.48	

3.3 Miss penalty is constant

	-	.04 k .03 K	Best!
32 24	% K	.ozk	B=128
64 1.5		.oisk	
128 17	6.K	.01 K	

4.Assume that main memory accesses take 70 ns and that 36% of all instructions access data memory. The following table shows data for L1 caches attached to each of two processors, P1 and P2.

	L1 Size	L1 Miss Rate	L1 Hit Time
P1	2 KiB	8.0%	0.66 ns
P2	4 KiB	6.0%	0.90 ns

4.1. Assuming that the L1 hit time determines the cycle times for P1 and P2, what are their respective clock rates?

$$f_{Pl} = 1/t_{LIK} = 1/0.66ns = 1.515 GHz$$

 $f_{Pz} = 1/t_{LIK} = 1/0.90ns = 1.111 GHz$

4.2. What is the Average Memory Access Time for P1 and P2 (in cycles)?

AMAT=
$$c_{n:t} + R_0 + e_{miss} \cdot c_{miss}$$

AMAT_{P1}= $[+0.08 \cdot \Gamma 70/.667 = 1 + 0.08 \cdot 107 = 9.56 \text{ cycles}$
AMAT_{P2}= $[+0.06 \cdot \Gamma 70/.907 = 1 + 0.06 \cdot 78 = 5.68 \text{ cycles}$

5. Solve problem 1.b replacing the direct-mapped cache with the following cache designs (total number of blocks and block size is the same as problem 1.b). Each valid entry should look like $<i,\{tag1,lru1\}$, ..., $\{tag_n,lru_n\}>$, where n is the number of blocks you can put in a row, and lru is the true LRU counter.

5.a. 2-way set associative cache

Reference	Result	Content after reference
0000 0011		$\langle 1, \{(0x0, mem(0x3), \{ni\}, ni\} \}\rangle$
1011 0100 0×B4 +=5		₹2, ₹
0×2B +=5		<5,1
000 0000 +=1		८।,१
0x8F 1=7		رح, {
0x58 1=4		८५,६
0×BE 1=7		<i>۲</i> ٦,٤
0x0E +7		۲ ⁷ , ﴿
0xB5 +=2		<2, ξ
0x2C +=6		<6 _, {
101/ 1010 Oxby tes		< 5
0xFD +-6		< G

5.b. 4-way set associative cache

Reference	Result	Content after reference

5.c. For this specific example, what is the advantage of 4-way compared to 2-way?

It increases temporal	locality.