

Message Authentication

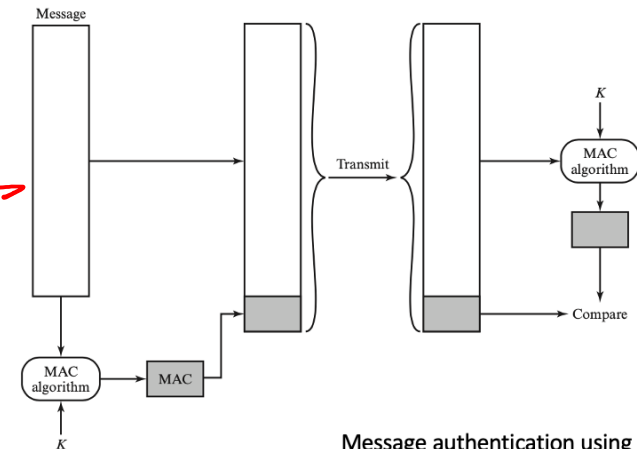
Message authentication

- message authentication is concerned with:

- 1. • protecting the integrity of a message
- 2. • validating identity of originator
- 3. • non-repudiation of origin (dispute resolution)

- then three alternative functions used:

- ✓ • message encryption – symmetric
- message authentication code (MAC) ←
- digital signature



Message authentication using MAC

Message encryption

- Symmetric message encryption by itself also provides a measure of authentication
- if symmetric encryption is used then:
 - receiver knows sender must have created it
 - since only sender and receiver know key used
 - know content cannot be altered

yes

the sender encrypted msg.
I use the same key
only belongs to the sender

group key



Homework 1 questions

- Symmetric Block Cypher provides authentication and confidentiality
 - Ans: True

Message encryption

- if public-key encryption is used:
 - encryption provides no confidence of sender
 - since anyone potentially knows public-key
 - so, need to recognize corrupted messages
 - however, if *private key*
 - sender **signs** message using their private-key
 - then encrypts with recipients' public key
 - have both secrecy and authentication
 - but at cost of two public-key uses on message

two pairs keys

Symmetric — *confidential*
 authentication

Asymmetric — *authentication*
only one pair
private key

signed
private-key
PK

Reasons to avoid encryption authentication

- Encryption software is quite slow
- Encryption hardware costs are nonnegligible
- Encryption hardware is optimized toward large data sizes
- An encryption algorithm may be protected by a patent

① MAC (Hash function)

RC4

② Digital Signature

Hash Function

Hash functions

- Hash function: $h = H(M)$

- M can be of any size
- h is always of fixed size
- Typically, $h \ll \text{size}(M)$

→ input message

$M \gg h$

h → small bandwidth

→ compression

lossy compression

$H(\cdot)$

compression

no loss compression

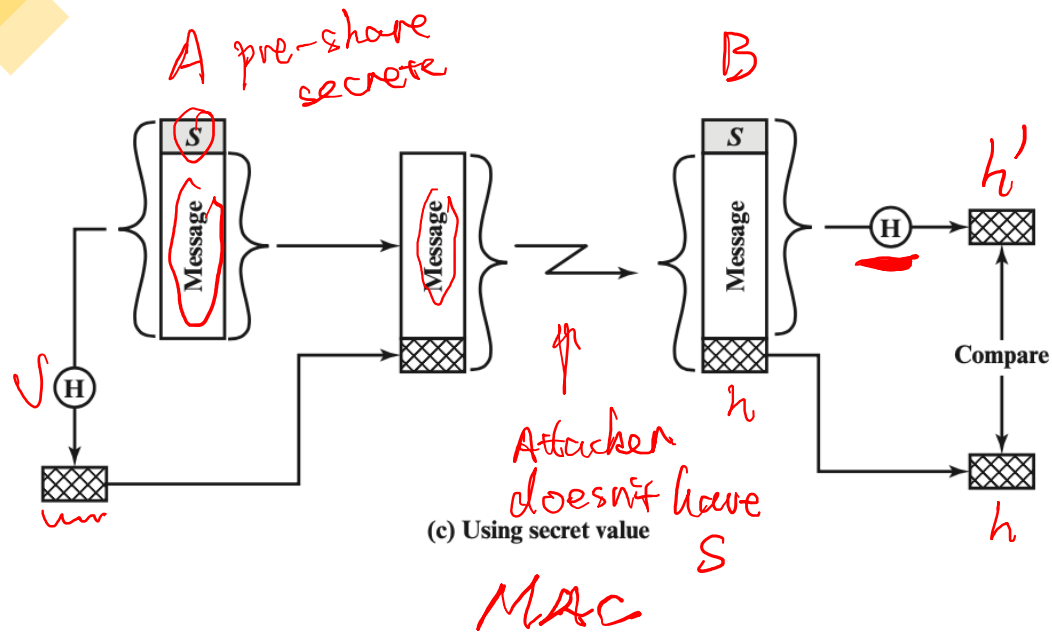
collision

LLM,



loss → hallucination

One use case - using hash function



- Initialization: A and B share a common secret, S_{AB}
- Message, M
- A calculates $MD_M = H(S_{AB} || M)$
- B recalculates MD'_M , and check
- $MD'_M = MD_M$

Requirements for secure hash functions

- 1. can be applied to any sized message M
 - 2. produces fixed-length output h
 - 3. is easy to compute $h = H(M)$ for any message M
 - 4. given h is infeasible to find x s.t. $H(x) = h$
 - one-way property or preimage resistance
 - 5. given x is infeasible to find x' s.t. $H(x') = H(x)$
 - weak collision resistance or second pre-image resistant
 - 6. infeasible to find any pair of x, x' s.t. $H(x') = H(x)$
 - strong collision resistance
- Handwritten notes:*
- $\{$ definition (next to item 1)
 - fast to compute (next to item 3)
 - easy fast $H(x)$ (next to item 4)
 - one-way (next to item 4)
 - attacker (next to item 5)

Hash Function: Collision Resistance

- **Collision:** Two different inputs with the same output

- $x \neq x'$ and $H(x) = H(x')$

5 & 6

$M \gg n$ fast.

- Can we design a hash function with no collisions?

- No, because there are more inputs than outputs (pigeonhole principle)

- However, we want to make finding collisions *infeasible* for an attacker

- **Collision resistance:** It is infeasible to (i.e. no polynomial time attacker can) find any pair of inputs $x' \neq x$ such that $H(x) = H(x')$

no possibility for no collision
if H^{-1}

Attacker $x' \Rightarrow H(x') = H(x)$

H^{-1}

Secure hash function

- A hash function that satisfies the first five properties is referred to as a weak hash function
- **Security:** random/unpredictability, no predictable patterns for how changing the input affects the output
 - Changing 1 bit in the input causes the output to be completely different
 - Also called "random oracle" assumption

$0101 \rightarrow H(0101)$
 randomize the output $H(x)$
 ↓
 uniform entropy security
 (1) output uniform
 (2) One-way
 (3) reduce collision ↓

$x \rightarrow H(x)$
 $x' \rightarrow H(x')$
 guess ← smart way use observing statistics of $H(x')$
 $H(x_1')$
 $H(x_2')$
 $H(x_3')$

avoided
 avoided

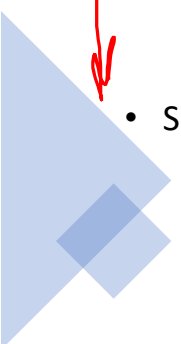
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- A message digest
 - a cryptographic hash function containing a string of digits created by a one-way hashing formula
 - provides data integrity
- Examples: SHA-1 (Secure Hash Algorithm 1), SHA-2, SHA-3, MD5

Hash Function: Examples

- MD5
 - Output: 128 bits
 - Security: Completely broken
- SHA-1
 - Output: 160 bits
 - Security: Completely broken in 2017
 - Was known to be weak before 2017, but still used sometimes
- SHA-2
 - Output: 256, 384, or 512 bits (sometimes labeled SHA-256, SHA-384, SHA-512)
 - Not currently broken, but some variants are vulnerable to a length extension attack
 - Current standard
- SHA-3 (Keccak)
 - Output: 256, 384, or 512 bits
 - Current standard (not meant to replace SHA-2, just a different construction)

same



Length Extension Attacks

- **Length extension attack:** Given $H(x)$ and the length of x , but not x , an attacker can create $H(x || m)$ for any m of the attacker's choosing
 - [Length extension attack - Wikipedia](#)
- SHA-256 (256-bit version of SHA-2) is vulnerable
- SHA-3 is not vulnerable