## Lucas Rath

## November 24, 2018

## Question 1)

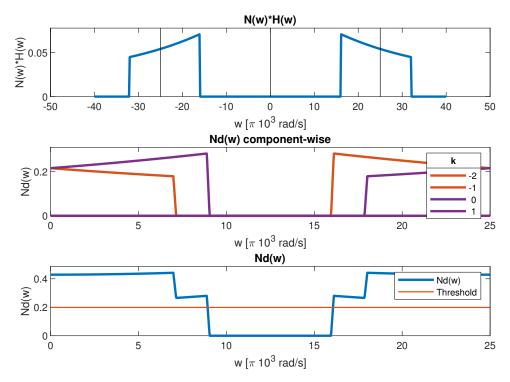


Figure 1: Case 1:  $24 < w_s < 32$ . Data generated with  $w_s = 25$ 

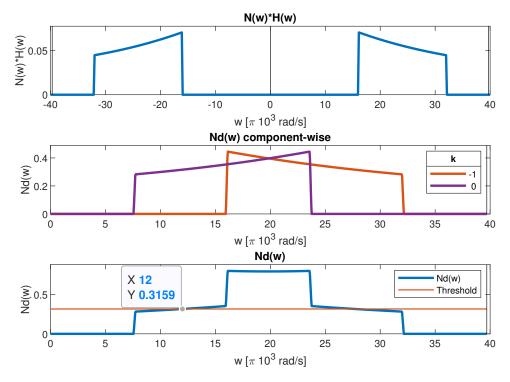


Figure 2: Case 2:  $w_s > 32$ . Data generated with  $w_s = 39.7$ 



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$$f(w) = \frac{1}{1 + jw/w_0}$$
,  $w_0 = 16 \text{ ft.} 10^3 \text{ add}$ 

$$X_{5}(m) = \begin{cases} 0, & \text{otherwise} \end{cases}$$

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- Signal Xs(1) can be perfectly reconstructed from the sampled rignal Xa(m) iff  $U_{max} \leq U_{s} \Rightarrow U_{s} \geq \lambda$ ,  $IaTT.10^{3} \Rightarrow U_{s} \geq \lambda 44 Pt.10^{3}$  and  $IaT.10^{3} \Rightarrow U_{s} \geq \lambda 44 Pt.10^{3}$
- Filtered analog right: X= (w) = / 1 + in/mo if 1 m1 < 1217.10'reds

  O Otherwise

Sompling 
$$\chi_{F(\omega)}$$
:  $\chi_{d(\omega)} = \frac{1}{\Delta t} \cdot \sum_{k=-\infty}^{\infty} \chi_{F(\omega + \omega + k)}$ 

$$at \quad \omega = 0 \qquad \chi_{d(\omega = 0)} = \frac{1}{\Delta t} \cdot \sum_{k=-\infty}^{\infty} \chi_{F(\omega + k)} = \frac{1}{\Delta t} \implies \chi_{d(\omega = 0)} = \frac{1}{\Delta t}$$

Filtered Maile signal: NF(w) = 
$$\begin{cases} \frac{0,1}{1+\delta w_{00}} & \text{if } 160.10^{3} \leq |w| \leq 32\pi.10^{3} \\ 0 & \text{otherwise} \end{cases}$$

Cose 1: 
$$(U_3) > 3 + 17.0^3 \text{ and } \longrightarrow 100 \text{ overap in } |UU| < |217.0^3 \text{ and } |K = \{-1, 0\}$$

$$|Vd(uu)| = \frac{1}{0+} \left( |VF(uu)| + |VF(uu - uu_2) \right) , * |V| |UU| < |217.5 |VF(uu)| = 0$$

$$|Vd(uu)| = \frac{1}{0+} \cdot |VF(uu - uu_2) | \Rightarrow |VF(uu)| = |VF(uu)| = 0$$

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Core 2: 247.103 
$$\frac{1}{5} < (M_5 < 3417.10^3 \frac{1}{44}) = OVERLAP In |UM < 1417.10^3 and |K= (-1, -1, 0, 1) |

Na(un) =  $\frac{1}{b+} \left( N_F (u_{-} + u_{0}) + N_F (u_{-} + u_{0}) + N_F (u_{+} + u_{0}) \right) , K \lor |u_{0}| < |$$$

## Question 2)

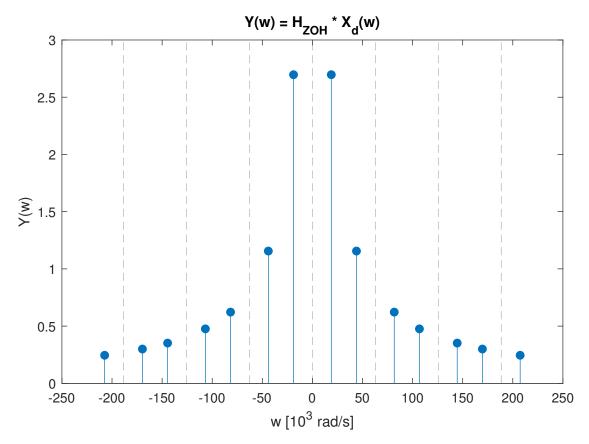


Figure 3: Frequency response of the sampled and reconstructed Y(w)

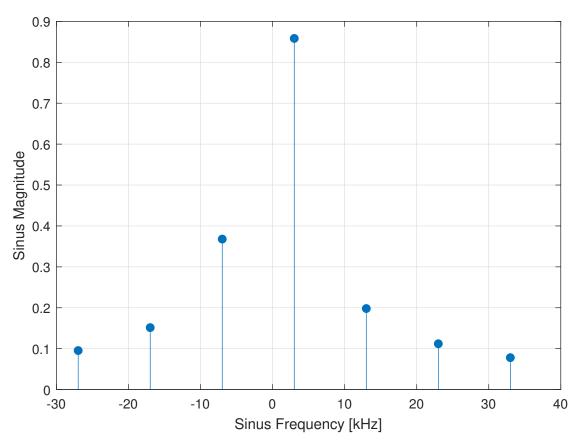


Figure 4: Magnitude and frequency for the 7 first harmonics of y(t)

$$Xd(m) = Min(atrm fo/f_2) = Min(uon.bt) = \underbrace{e^{-iuwnbt}}_{ai}$$

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$$Applying DTFT in Xd we get:$$

$$Xa(w) = DTFT(\underbrace{e^{iuwnbt}}_{ai} - e^{-iuwnbt}) = Ws.(\underbrace{\tilde{S}(ua-uu)}_{ai} - \tilde{S}(ua+uu))$$

$$An kauum: Hzau(w) = bt. e^{-iuwnbt}$$

$$Tr. w/ws$$

$$So the Alconotuction of Xa(n) in the fugure glossen will be:$$

$$Y(u) = Xd(u).[Hzau(w)] = Ws.(\underbrace{\tilde{S}(ua-uu)}_{ai} - \tilde{S}(ua+uu)). bt. e^{-iuwnbt}$$

$$Nim(lt. uu/us)$$

$$Nim(uu/us)$$

$$Ni$$

Applying now the invale Family 
$$EFT$$
:

$$y(t) = \frac{1}{\lambda \pi} \int_{-\infty}^{\infty} Y(u) \cdot e^{iut} du = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left( \frac{\delta(u - u_0 + ku_0) - \delta(u + u_0 + ku_0)}{\lambda i} - \frac{\delta(u + u_0 + ku_0)}{\lambda i} \right) e^{iu(t - \delta t/\lambda)} \cdot \text{sinc}(u|us) \cdot du$$

$$= \sum_{k=-\infty}^{\infty} \int_{-\infty}^{\infty} \left( \frac{\delta(u - u_0 + ku_0) - \delta(u + u_0 - ku_0)}{\lambda i} \right) \cdot e^{iu(t - \delta t/\lambda)} \cdot \text{sinc}(u|us) \cdot du$$

$$= \sum_{k=-\infty}^{\infty} \frac{1}{\lambda^2} \cdot \left[ e^{i(u_0 - ku_0)(t - \delta t/\lambda)} \cdot \text{sinc}(\frac{u_0 - ku_0}{us}) - e^{i(u_0 - ku_0)(t - \delta t/\lambda)} \cdot \text{sinc}(\frac{u_0 - ku_0}{us}) \right]$$

$$= \sum_{k=-\infty}^{\infty} \frac{1}{\lambda^2} \cdot \left[ e^{i(u_0 - ku_0)(t - \delta t/\lambda)} \cdot \text{sinc}(\frac{u_0 - ku_0}{us}) \right] \cdot \text{sinc}(\frac{u_0 - ku_0}{us})$$

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