

Multicriterio y Escalas Ordinales

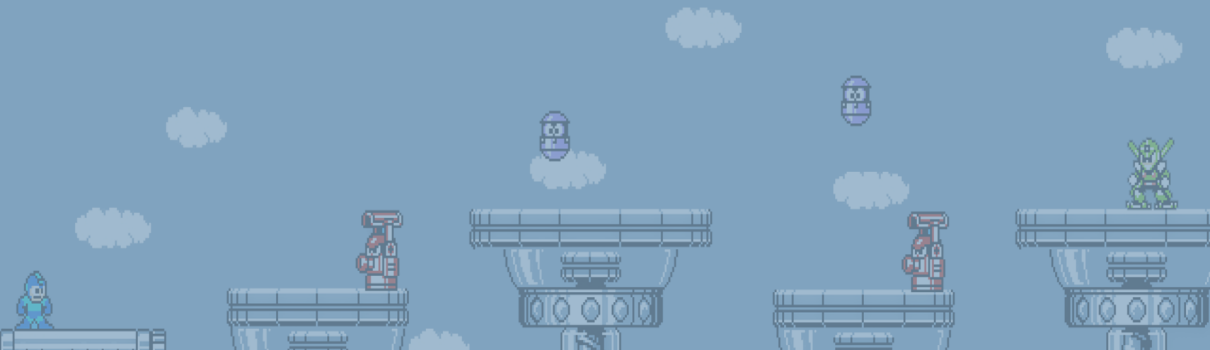
Sus becas fueron asignadas con esto

Ing. Cabral, Juan B.

Universidad Gastón Dachary

SciPyLa 2015

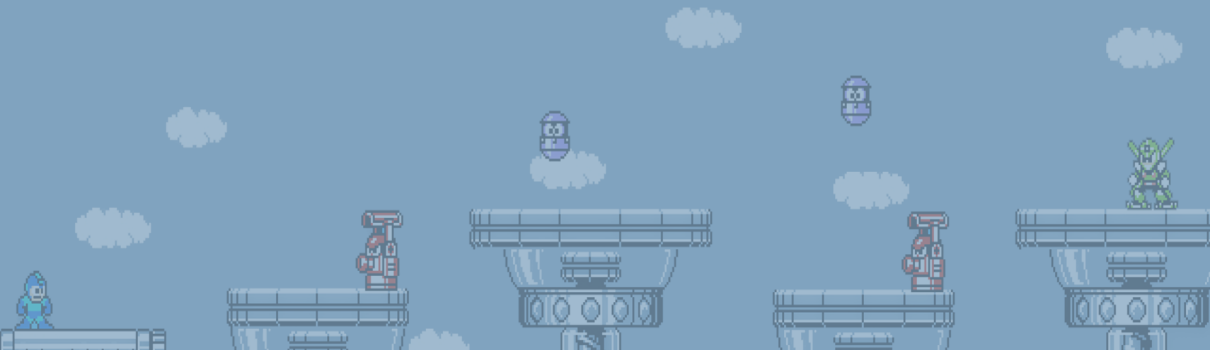
05/2015 - Posadas - Argentina



About Me

- Software engineer.
- Data scientist.
- Grad Student In Machine Learning for Astrophysics

Disclaimer: Wikipedia powered slides!



Decision-making

- The cognitive process resulting in the selection of a belief or a course of action among several alternative possibilities. Every decision-making process produces a final choice that may or may not prompt action.
- Is the study of identifying and choosing alternatives based on the values and preferences of the decision maker.

DM is one of the central activities of management and is a huge part of any process of implementation; also is a subject of active research from Edit human performance with regard to decisions has been the subject of active research from **Psychological**, **Cognitive** and **Normative** perspectives.

Also can be regarded as a problem-solving activity terminated by a solution deemed to be satisfactory. It is, therefore, a reasoning or emotional process which can be rational or irrational



Decision-making (Cont.)

Rational choice theory encompasses the notion that people try to maximize benefits while minimizing costs.

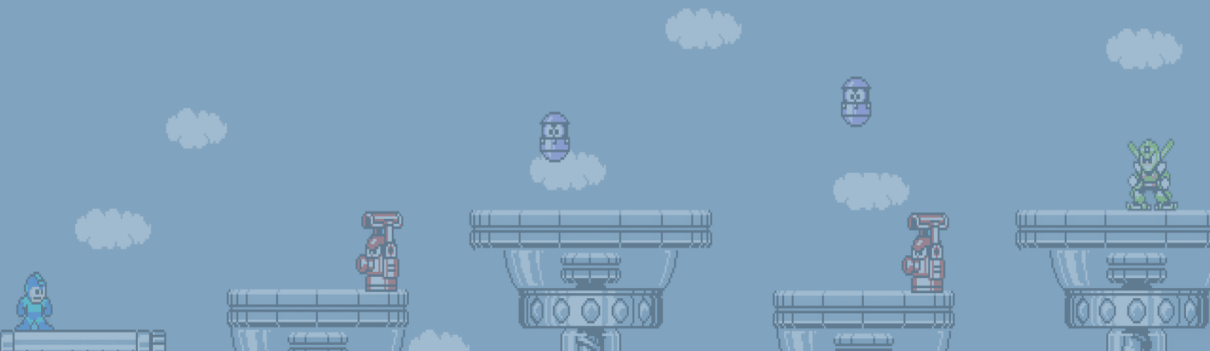
- A major part of decision-making involves the analysis of a finite set of alternatives described in terms of evaluative criteria.
- These criteria may be benefit or cost in nature. (*Maximization* and *Minimization* problems).
- The problem might be to rank these alternatives in terms of how attractive they are to the decision-maker(s) when all the criteria are considered simultaneously.

—
Solving such problems is the focus of multi-criteria decision analysis (**MCDA**), also known as multi-criteria decision-making (**MCDM**).



Rational & Irrational Decision-making

- In economics, it is thought that if humans are rational and free to make their own decisions, then they would behave according to rational choice theory.
- The people make decisions by determining the likelihood of a potential outcome, the value of the outcome, multiplying the two, and then choosing the more positive of the two outcomes.
- In reality some factors that affect decision-making abilities and cause people to make irrational decisions (availability bias)



Information Overload

—

IO is a gap between the volume of information and the tools we need to assimilate it. If the gap grows your decision is worse.

Factors

1. Personal Information Factors.
 2. Information Characteristics.
 3. Tasks and Process.
 4. Organizational Design.
 5. Information Technology.
- Hall, Ariss & Todorov (2007) described an illusion of knowledge: **too much knowledge it actually interferes with their ability to make rational decisions.**

Multiple-criteria decision analysis

Whether in our daily lives or in professional settings, there are typically multiple conflicting criteria that need to be evaluated in making decisions.

we usually weigh multiple criteria implicitly and we may be comfortable with the consequences of such decisions that are made based on only intuition.

when stakes are high, it is important to properly structure the problem and explicitly evaluate multiple criteria.

—

MCDM or MCDA is concerned with structuring and **solving** decision and planning problems involving multiple criteria.

"Solving" can be:

- Best alternative, small set of best alternatives or grouping alternatives.
- An extreme interpretation could be to find all "efficient" or "nondominated" alternatives.

A nondominated solution has the property that it is not possible to move away from it to any other solution without sacrificing in at least one criterion.

MCDA - Typologies

- **Multiple-criteria evaluation problems:** These problems consist of a finite number of alternatives, explicitly known in the beginning of the solution process. Each alternative is represented by its performance in multiple criteria. The problem may be defined as finding the best alternative for a decision maker (DM), or finding a set of good alternatives.
- **Multiple-criteria design problems (multiple objective mathematical programming problems):** In these problems, the alternatives are not explicitly known. An alternative (solution) can be found by solving a mathematical model. The number of alternatives is either infinite and not countable (when some variables are continuous) or typically very large if countable (when all variables are discrete).

Also:

- There are methods that require the DM's preference information at the start of the process, transforming the problem into essentially a single criterion problem. (**prior articulation of preferences**).
- Some methods require preference information from the DM throughout the solution process. (**progressive articulation of preferences**).
- MC design problems typically require the solution of a series of mathematical programming models in order to reveal implicitly defined solutions. (**posterior articulation of preferences**).

Representations and definitions

The MCDM problem can be represented in the criterion space or the decision space. Alternatively, if different criteria are combined by a weighted linear function, it is also possible to represent the problem in the weight space.

Criterion Space	Decision Space
"max" q	"max" $q = f(x) = (f_1(x), \dots, f_k(x))$
subject to	subject to
$q \in Q$	$q \in Q = \{f(x) : x \in X, X \subseteq R^n\},$

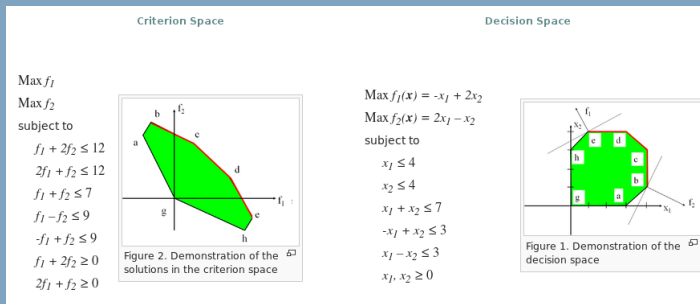
where q is the vector of k criterion functions (objective functions) and Q is the feasible set, $Q \subseteq R^k$.

If Q is defined explicitly or implicitly (by a set of alternatives), the resulting problem is called a Multiple Criteria Evaluation or Design problem.

X is the feasible set and x is the decision variable vector of size n .

The quotation mark indicates the maximization is not well-defined.

Representations and definitions (cont.)



Definitions:

Definition 1. $q^* \in Q$ is nondominated if there does not exist another $q \in Q$ such that $q \geq q^*$ and $q \neq q^*$.

Definition 2. $x^* \in X$ is efficient if there does not exist another $x \in X$ such that $f(x) \geq f(x^*)$ and $f(x) \neq f(x^*)$.

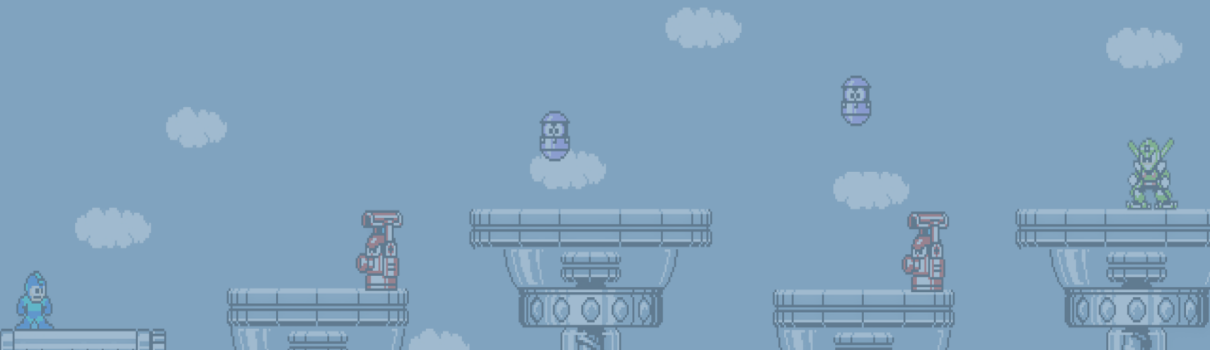
Definition 3. $q^* \in Q$ is weakly nondominated if there does not exist another $q \in Q$ such that $q > q^*$.

Definition 4. $x^* \in X$ is weakly efficient if there does not exist another $x \in X$ such that $f(x) > f(x^*)$.

- **Ideal point:** (in criterion space) represents the best (the maximum for maximization problems and the minimum for minimization problems) of each objective function, and typically corresponds to an infeasible solution.
- **Nadir point:** (in criterion space) represents the worst (the minimum for maximization problems and the maximum for minimization problems) of each objective function among the points in the nondominated set, and is typically a dominated point.

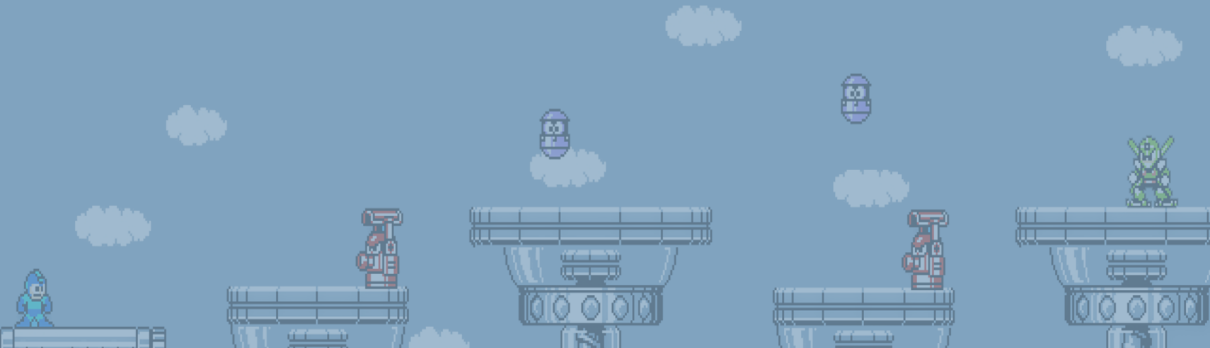
Decision-Makin Paradox

- Hay muchos metodos MCDA (normativos y descriptivos); y cada uno clama ser el mejor. Sin embargo muchos de estos metodos retornan diferentes resultados para los mismos problemas con exactamente los mismos datos.
- Encontrar un el mejor metodo es un problema de MCDA en si mismo.
- Naturalmente es necesario conocer el mejor metodo a-priori.



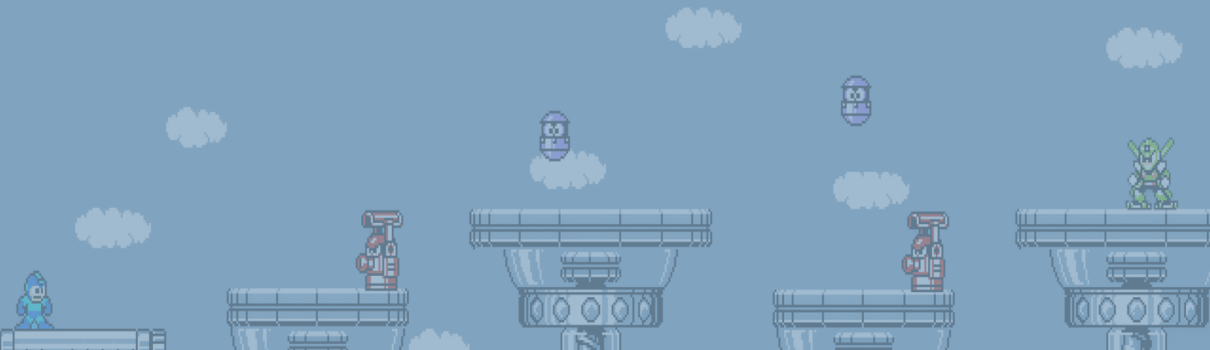
Decision-Makin Paradox (cont.)

- A traves de un estudio [\[Triantaphyllou1989\]](#) [\[Triantaphyllou,2000\]](#)_ Se realizo un experimento de selección de metodos utilizando 4 metodos. WSM, WPM y dos variantes de AHP. Cuando se usaba un metodo X (perteneciente a los anteriores, indicaba que Y era el mejor. Cuando se utilizaba Y el resultado decia que Z era mejor.
- Para enunciar el problema se utilizaron 2 criterios: #. Todo metodo debe ser tan precido en problemas multidimensionales como
uni-dimensionales (se comparo resultados con WSUM) es lo llamaso ranking reversal tipo 5.
 1. Resultados de Analisis de ranking reversals tipo 2.



Ranking Reversal

- Esencialmente son: Test Cases
- La idea es modificar las alternativas de tal forma que "suponemos" que las mejores alternativas no cambian.



Ranking Reversal (cont.)

Si tenemos tres Alternativas $A > B > C$

Tipos:

- **Tipo 1:** Agregamos una alternativa D igual o parecida a B o C y validamos que la mejor alternativa no cambie.
- **Tipo 2:** Reemplazamos B por D siendo $D > B$. Esperamos que A siga siendo la mejor.
- **Tipo 3:** Descomponemos el problema en problemas de 2 alternativas por ves, y verificamos que ninguno de ellos no se contradiga con el problema mayor.
- **Tipo 4:** Igual al tipo 3 pero solo comparamos entre ellos ignorando el general.
- **Tipo 5:** Comparaciones unidimensionales vs multidimensionales.

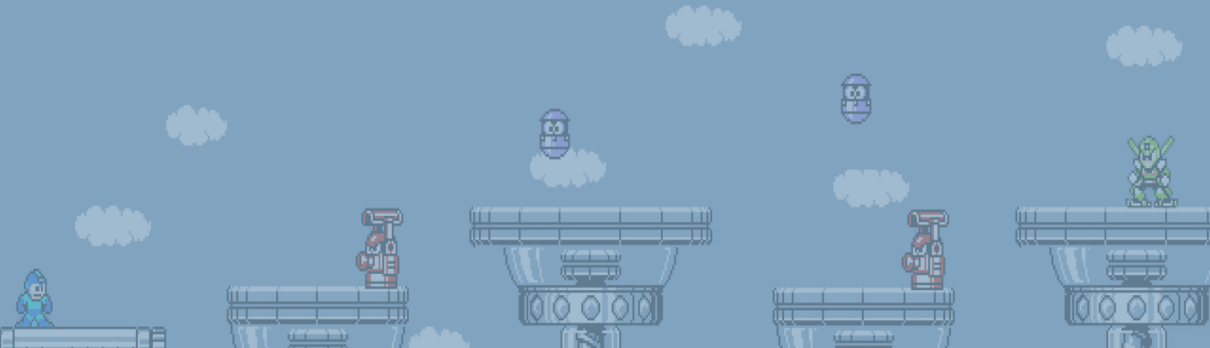


Ranking Reversal (cont.)

- Puede que una falla en un ranking reversal sea un resultado deseado.
- Se da en situaciones racionales.
- Conjetura: Intuyo que pasa en Machine Learning.

Ejemplo:

- Un comprador M1 que le gusta el lujo, Un comprador M2 que no tiene dinero.
- Un auto A1 lujoso y caro y un auto A2 barato y con poco confort.
- $M1 = A1 > A2$ y $M2 = A2 > A1$



¿Preguntas?

- Charla:
- **Contactos:**
 - jbcabral.com
 - Juan B Cabral <jbc.develop@gmail.com>

