

# Title

Subtitle

**Author** dd mm yyyy

Outline

- Objective
- 2 Method
  - Data Analysis
- Result

# Objective

# Lagrangian Particle Tracking of Snowflakes

Find a general formula for the drag coefficient of blowing snow

$$c_D = c_D(Re, \mathsf{parameters})$$

And implement it in PoliMIce with some general rule for the choice of the main parameters.

### What is not available

- lacksquare  $c_D$  formula tuned for snowflakes
- Experimental measurements of blowing snowflakes velocities
- Shape of the typical snowflake (they are almost unique)

## What is available

- lacksquare  $c_D$  formulae tuned for arbitrary shaped bodies
- Experimental measurements of falling snowflakes terminal velocities
- General parameters that describe the shape (CAMBIARE)

## Drag coefficient formula

Find a suitable existing model to infer the main parameters in the falling regime and use them in the blowing one

#### **Snow Parameters**

Develop a method to find the discrete set of properties that on average describe a certain *cloud* 

- Objective
- 2 Method
  - Data Analysis
- Result

Data Generation

Reproduce an artificial data set from the *velocity-diameter* relation of Brandes et al - 2008. The diameter distribution is not taken into account.

404

Figure not found

#### Ganser - 1993

$$c_D = K_2 \left( \frac{24}{ReK_1 K_2} (1 + 0.1118 (ReK_1 K_2)^{0.6567}) + \frac{0.4305}{1 + \frac{3305}{ReK_1 K_2}} \right)$$

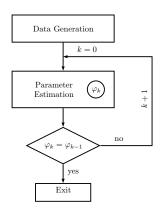
# Stokes' Shape Factor

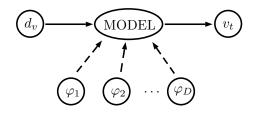
$$K_1 = \left(\frac{1}{3}\frac{d_n}{d_v} + \frac{2}{3}\Phi^{-\frac{1}{2}}\right)^{-1}$$

# Newton's Shape Factor

$$K_2 = 10^{1.8148(-\log(\Phi))^{0.5743}}$$

## General Scheme





- $\blacksquare$   $(d_v, v_t)$ : Experimental data
- $lackbox{ } \varphi_1, \varphi_2 \dots \varphi_D = \underline{\varphi}$ : Free parameters
- D: Number of parameters  $\sim$  problem dimension

## Bayes' Theorem

$$\underbrace{prob(\delta HP|D,I)}_{PosteriorProbability} \propto \underbrace{prob(D|\delta HP,I)}_{LikelihoodFunction} \cdot \underbrace{prob(\delta HP|I)}_{PriorProbability}$$

- Prior: State of knowledge (or ignorance) before analyzing the data
- Likelihood: Experimental measurements
- Posterior: State of knowledge in light of the data

# Marginalization Equation and Sum Rule

$$prob(HP|D, I) = \int_{-\infty}^{+\infty} prob(\delta HP|D, I)\delta HP = 1$$

# Problem formulation

## Prior

$$\begin{aligned} prob(HP|I) &= prob(\underline{\varphi}) : \textit{Uniform} \text{ in the range of physical solution.} \\ &= \left\{ \begin{array}{c} \frac{1}{(\varphi_{1,M} - \varphi_{1,m})(\varphi_{2,M} - \varphi_{2,m}) \dots (\varphi_{D,M} - \varphi_{D,m})} \\ 0 \end{array} \right. \end{aligned}$$

#### Likelihood

$$prob(D|HP, I) = \prod_{n=1}^{N_{data}} \sum_{k=1}^{N_{modes}} \pi_k e^{-\frac{1}{2} \left( \frac{v_{t,n} - v_t(d_{v,n}, \underline{\varphi}_k)}{\sigma_n} \right)^2}$$

# Gaussian Mixture Models

