An Introduction to the Database Management Systems

By Hossein Rahmani

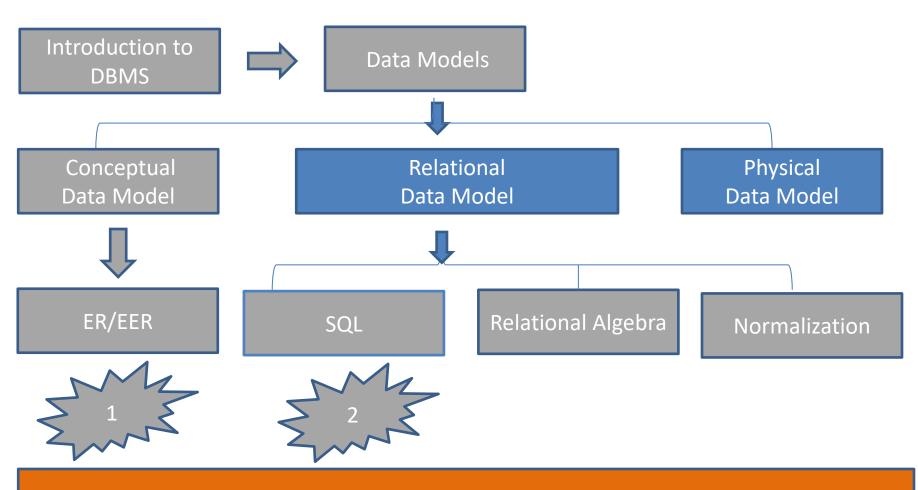
Slides originally by Book(s) Resources





Road Map

(Might change!)



Data Warehousing and On-line Analytical Processing

Data Warehouse: Basic Concepts



- Data Warehouse Modeling: Data Cube and OLAP
- Data Warehouse Design and Usage
- Data Warehouse Implementation
- Data Generalization by Attribute-Oriented Induction
- Data Cube Computation
- Summary

What is a Data Warehouse?

- Defined in many different ways, but not rigorously.
 - A decision support database that is maintained separately from the organization's operational database
 - Support information processing by providing a solid platform of consolidated, historical data for analysis.
- "A data warehouse is a <u>subject-oriented</u>, <u>integrated</u>, <u>time-variant</u>, and <u>nonvolatile</u> collection of data in support of management's decision-making process."—W. H. Inmon
- Data warehousing:
 - The process of constructing and using data warehouses

Data Warehouse—Subject-Oriented

- Organized around major subjects, such as customer, product, sales
- Focusing on the modeling and analysis of data for <u>decision</u> <u>makers</u>, <u>not</u> on <u>daily</u> operations or transaction processing
- Provide a simple and concise view around particular subject issues by excluding data that are not useful in the decision support process

Data Warehouse—Integrated

- Constructed by integrating <u>multiple</u>, <u>heterogeneous</u> data <u>sources</u>
 - relational databases, flat files, on-line transaction records
- Data <u>cleaning</u> and data <u>integration</u> techniques are applied.
 - Ensure <u>consistency</u> in naming conventions, encoding structures, attribute measures, etc. among different data sources
 - E.g., Hotel price: currency, tax, breakfast covered, etc.
 - When data is moved to the warehouse, it is converted.

Data Warehouse—Time Variant

- The <u>time horizon</u> for the data warehouse is significantly <u>longer</u> than that of operational systems
 - Operational database: <u>current</u> value data
 - <u>Data warehouse</u> data: provide information from a <u>historical</u> perspective (e.g., past 5-10 years)
- Every key structure in the data warehouse
 - Contains an <u>element of time</u>, explicitly or implicitly
 - But the key of operational data may or may not contain "time element"

Data Warehouse—Nonvolatile

- A physically separate store of data transformed from the operational environment
- Operational update of data does not occur in the data warehouse environment
 - Does not require transaction processing, recovery, and concurrency control mechanisms
 - Requires only two operations in data accessing:
 - initial loading of data and access of data

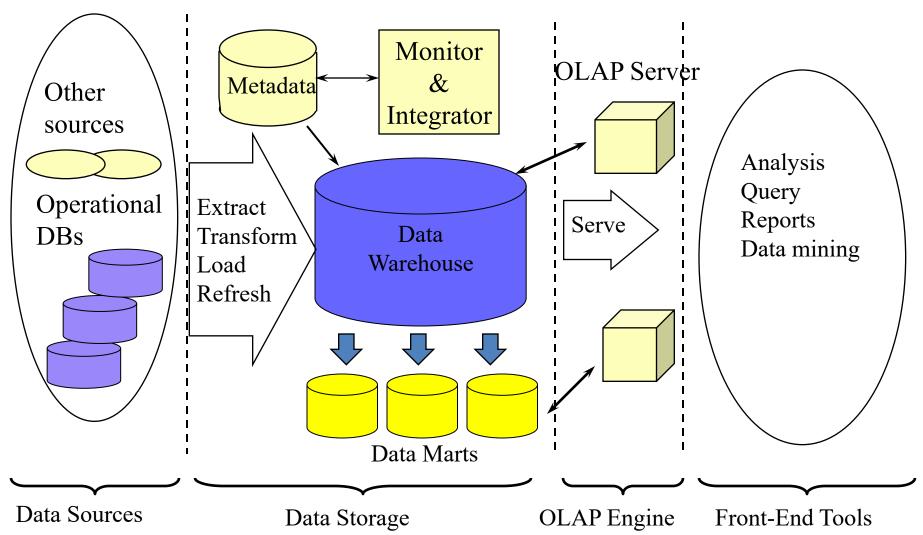
OLTP vs. OLAP

	OLTP	OLAP
users	clerk, IT professional	knowledge worker
function	day to day operations	decision support
DB design	application-oriented	subject-oriented
data	current, up-to-date detailed, flat relational isolated	historical, summarized, multidimensional integrated, consolidated
usage	repetitive	ad-hoc
access	read/write index/hash on prim. key	lots of scans
unit of work	short, simple transaction	complex query
# records accessed	tens	millions
#users	thousands	hundreds
DB size	100MB-GB	100GB-TB
metric	transaction throughput	query throughput, response

Why a Separate Data Warehouse?

- High performance for both systems
 - DBMS— tuned for OLTP: access methods, indexing, concurrency control, recovery
 - Warehouse—tuned for OLAP: complex OLAP queries, multidimensional view, consolidation
- Different functions and different data:
 - missing data: Decision support (DS) requires historical data which operational DBs do not typically maintain
 - <u>data consolidation</u>: DS requires consolidation (aggregation, summarization) of data from heterogeneous sources
 - <u>data quality</u>: different sources typically use inconsistent data representations, codes and formats which have to be reconciled
- Note: There are more and more systems which perform OLAP analysis directly on relational databases

Data Warehouse: A Multi-Tiered Architecture



Three Data Warehouse Models

- Enterprise warehouse
 - collects all of the information about subjects spanning the entire organization
- Data Mart
 - a subset of corporate-wide data that is of value to a <u>specific</u> groups of users. Its scope is confined to specific, selected groups, such as marketing data mart
 - Independent vs. dependent (directly from warehouse) data mart
- Virtual warehouse
 - A set of <u>views</u> over <u>operational</u> databases
 - Only <u>some</u> of the possible summary views may be materialized

Extraction, Transformation, and Loading (ETL)

Data extraction

get data from multiple, heterogeneous, and external sources

Data cleaning

detect errors in the data and rectify them when possible

Data transformation

convert data from legacy or host format to warehouse format

Load

 sort, summarize, consolidate, compute views, check integrity, and build indicies and partitions

Refresh

propagate the updates from the data sources to the warehouse

Metadata Repository

- Meta data is the data defining warehouse objects. It stores:
- Description of the structure of the data warehouse
 - schema, view, dimensions, hierarchies, derived data defn, data mart locations and contents
- Operational meta-data
 - data lineage (history of migrated data and transformation path), currency of data (active, archived), monitoring information (warehouse usage statistics, error reports)
- The algorithms used for summarization
- The mapping from operational environment to the data warehouse
- Data related to system performance
 - warehouse schema, view and derived data definitions
- Business data
 - business terms and definitions, ownership of data

Data Warehousing and On-line Analytical Processing

- Data Warehouse: Basic Concepts
- Data Warehouse Modeling: Data Cube and OLAP

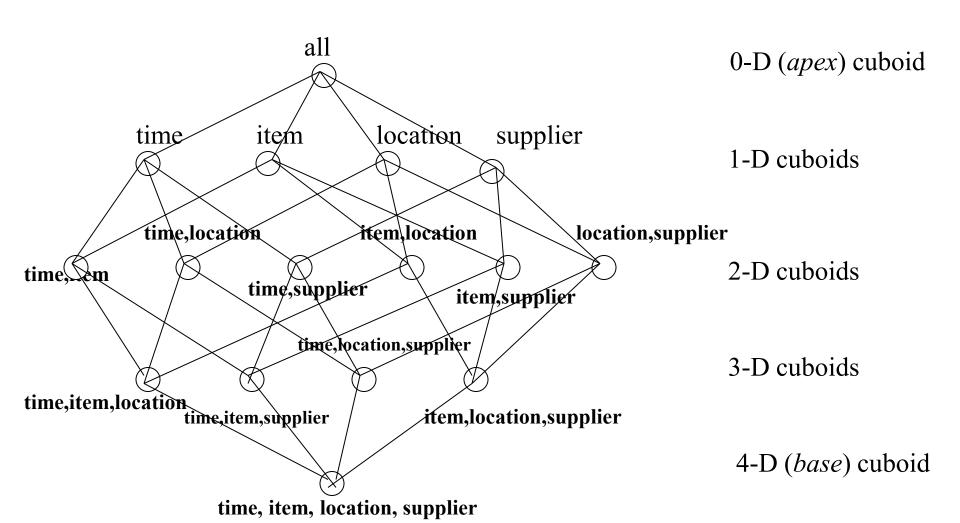


- Data Warehouse Design and Usage
- Data Warehouse Implementation
- Data Generalization by Attribute-Oriented Induction
- Data Cube Computation
- Summary

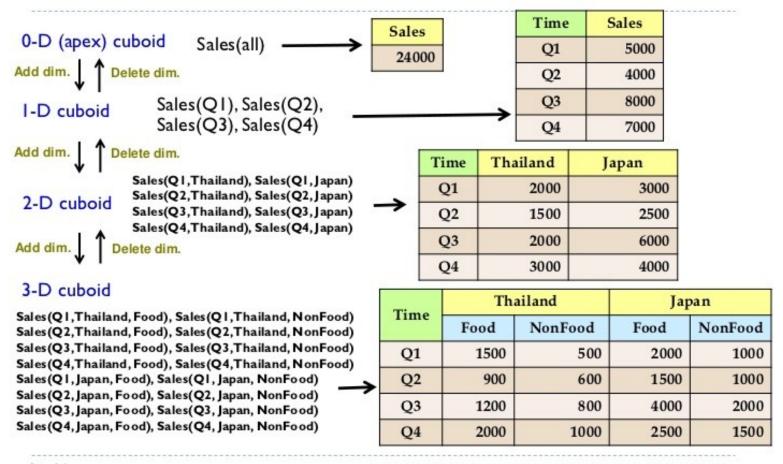
From Tables and Spreadsheets to Data Cubes

- A data warehouse is based on a multidimensional data model which views data in the form of a data cube
- A data cube, such as sales, allows data to be modeled and viewed in multiple dimensions
 - Dimension tables, such as item (item_name, brand, type), or time(day, week, month, quarter, year)
 - Fact table contains measures (such as dollars_sold) and keys to each of the related dimension tables
- In data warehousing literature, an n-D base cube is called a base cuboid.
 The top most 0-D cuboid, which holds the highest-level of summarization, is called the apex cuboid. The lattice of cuboids forms a data cube.

Cube: A Lattice of Cuboids



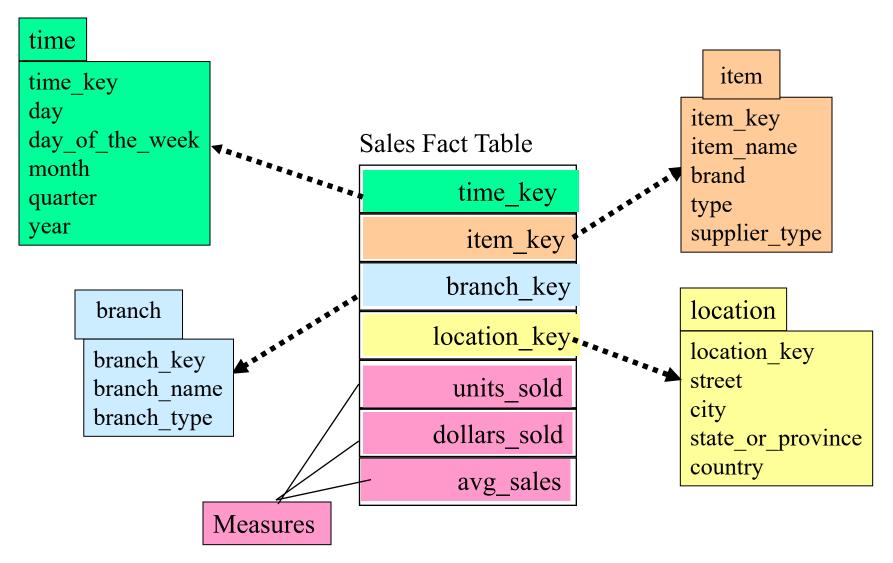
An Example of Cuboids (Dimension) (add vs. delete dimensions)



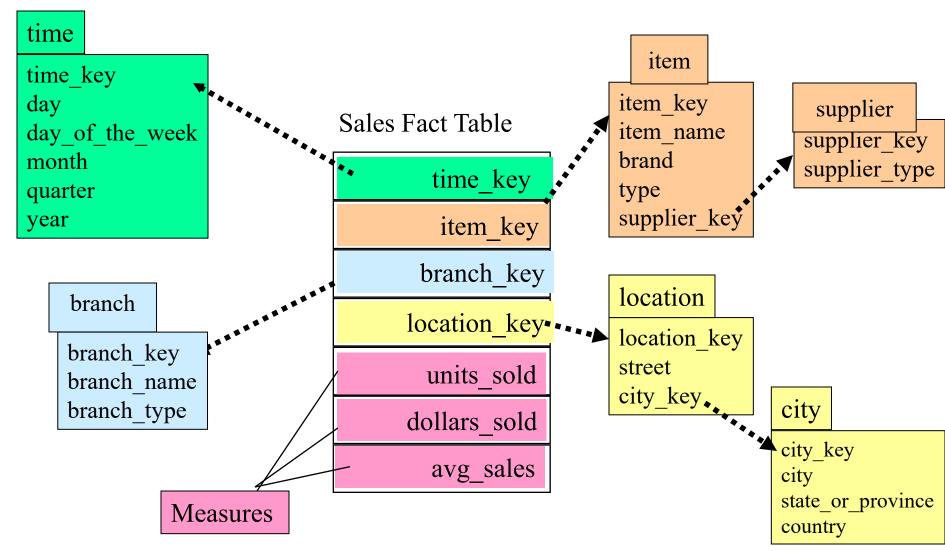
Conceptual Modeling of Data Warehouses

- Modeling data warehouses: dimensions & measures
 - Star schema: A fact table in the middle connected to a set of dimension tables
 - Snowflake schema: A refinement of star schema where some dimensional hierarchy is normalized into a set of smaller dimension tables, forming a shape similar to snowflake
 - <u>Fact constellations</u>: Multiple fact tables share dimension tables, viewed as a collection of stars, therefore called galaxy schema or fact constellation

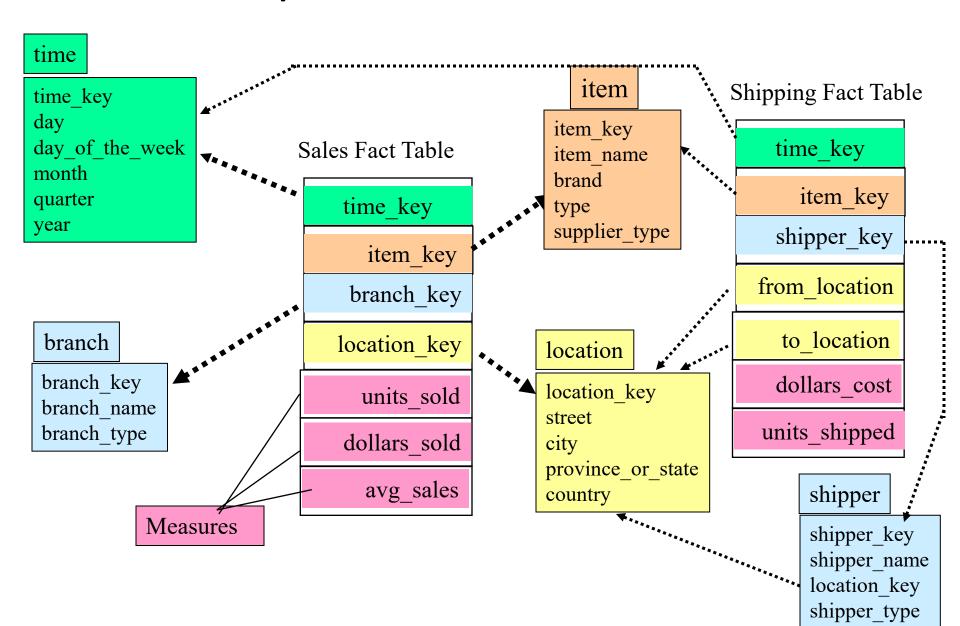
Example of Star Schema



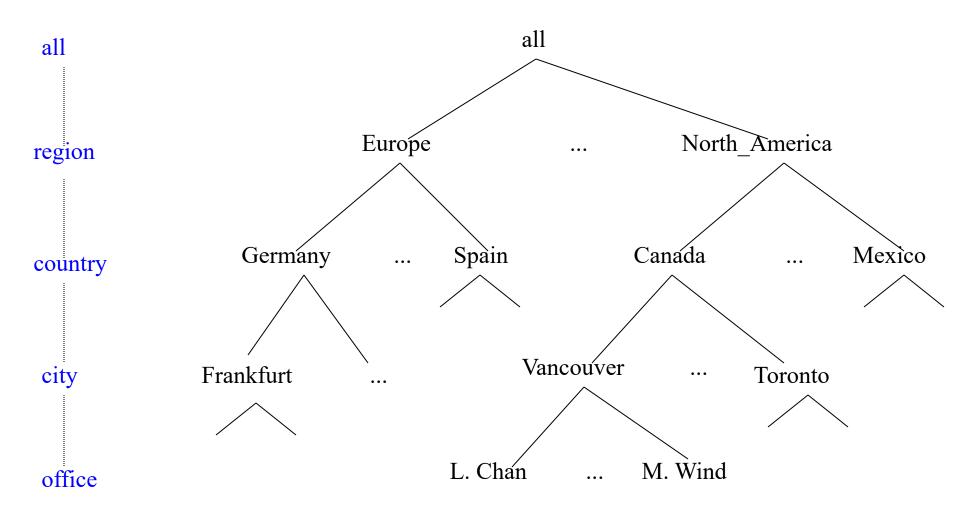
Example of **Snowflake Schema**



Example of Fact Constellation



A Concept Hierarchy: **Dimension** (location)



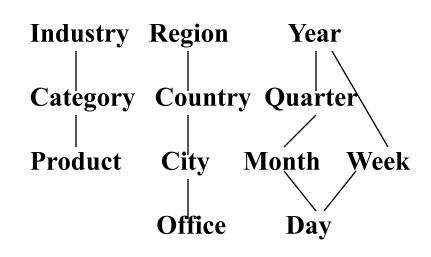
Data Cube Measures: Three Categories

- <u>Distributive</u>: if the result derived by applying the function to n aggregate values is the same as that derived by applying the function on all the data without partitioning
 - E.g., count(), sum(), min(), max()
- Algebraic: if it can be computed by an algebraic function with M
 arguments (where M is a bounded integer), each of which is
 obtained by applying a distributive aggregate function
 - E.g., avg(), min_N(), standard_deviation()
- Holistic: There does not exist an algebraic function with M arguments (where M is a constant) that characterizes the computation. E.g., median()

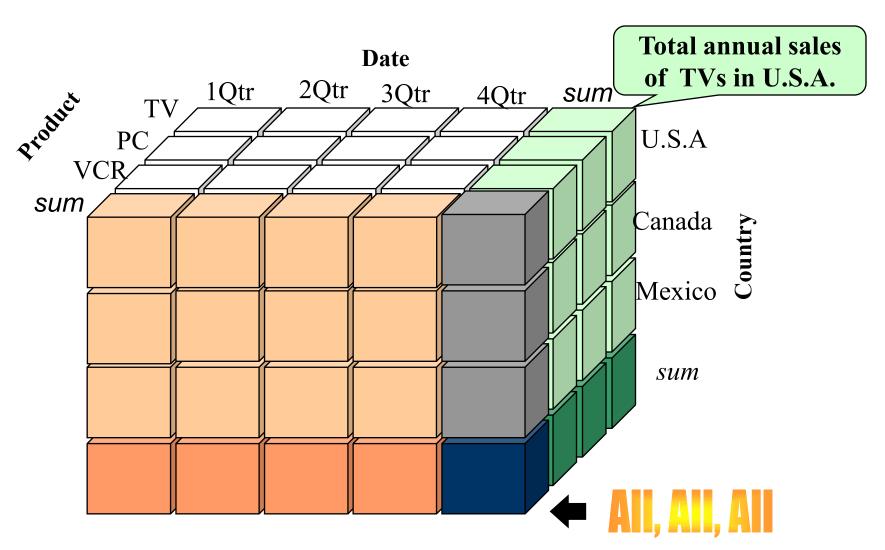
Multidimensional Data

 Sales volume as a function of product, month, and region Dimensions: Product, Location, Time

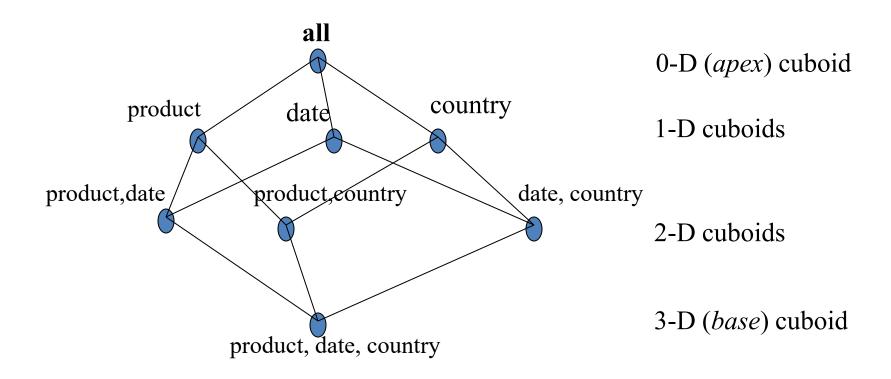
Hierarchical summarization paths Product Month



A Sample Data Cube

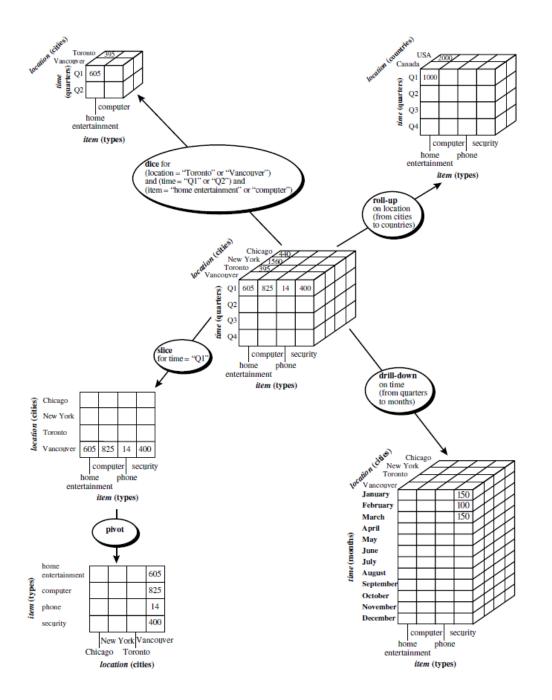


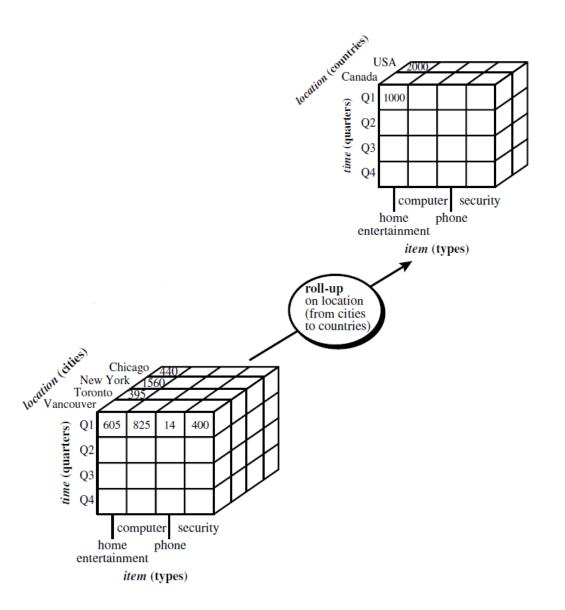
Cuboids Corresponding to the Cube

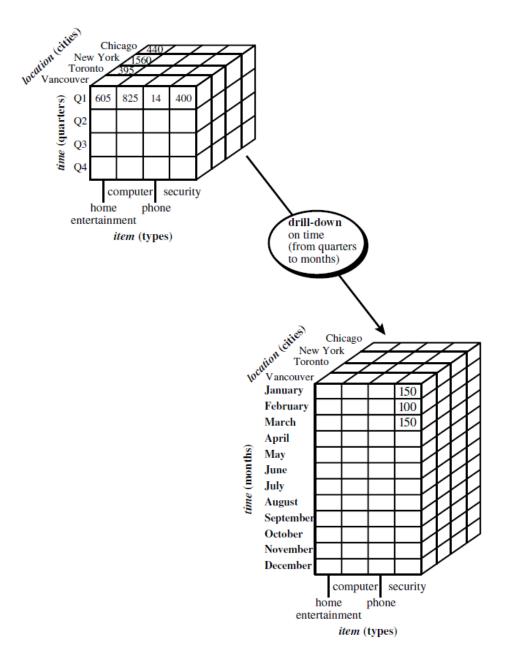


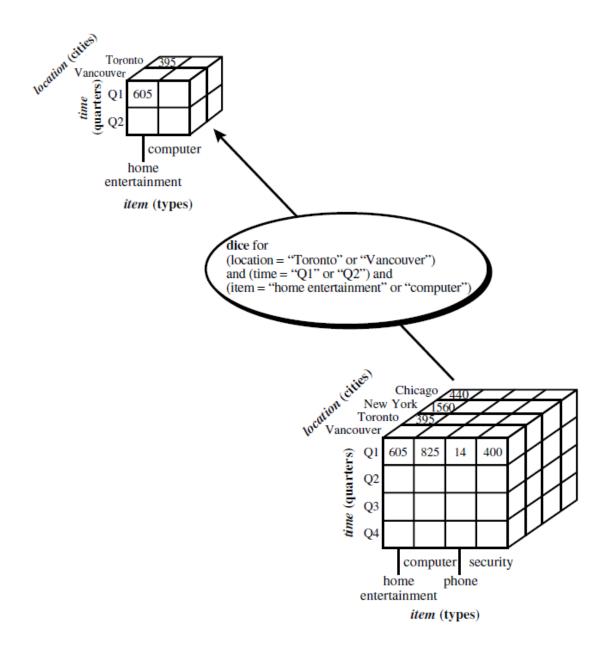
Typical OLAP Operations

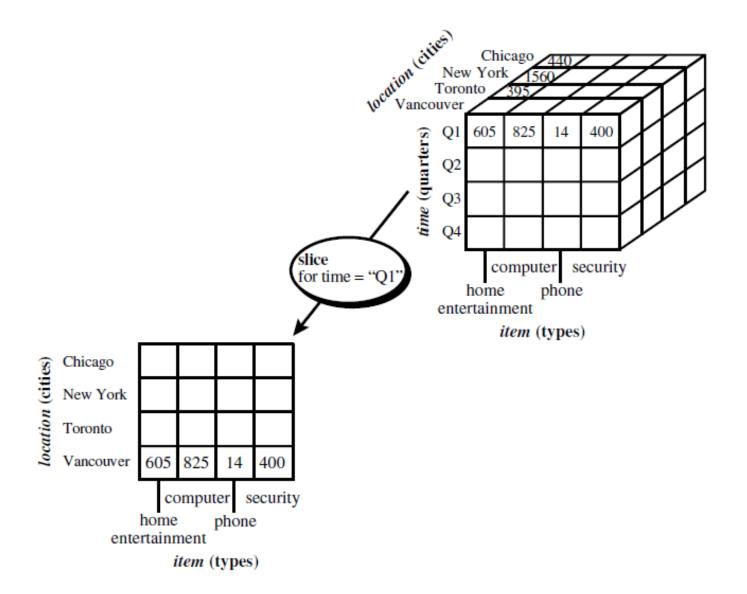
- Roll up (drill-up): summarize data
 - by climbing up hierarchy or by dimension reduction
- Drill down (roll down): reverse of roll-up
 - from higher level summary to lower level summary or detailed data, or introducing new dimensions
- Slice and dice: project and select
- Pivot (rotate):
 - reorient the cube, visualization, 3D to series of 2D planes



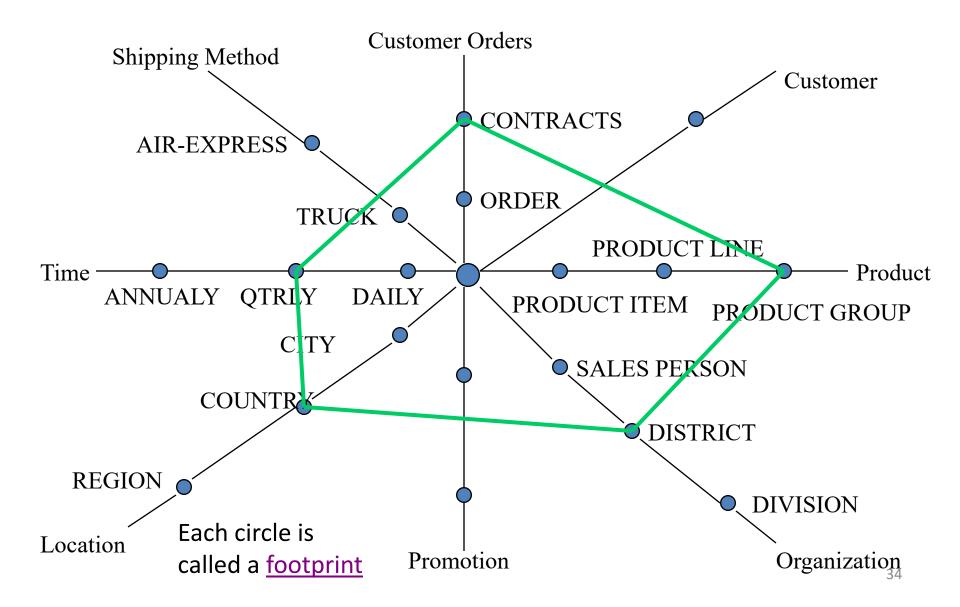








A Star-Net Query Model



Data Warehousing and On-line Analytical Processing

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- Data Warehouse Design and Usage



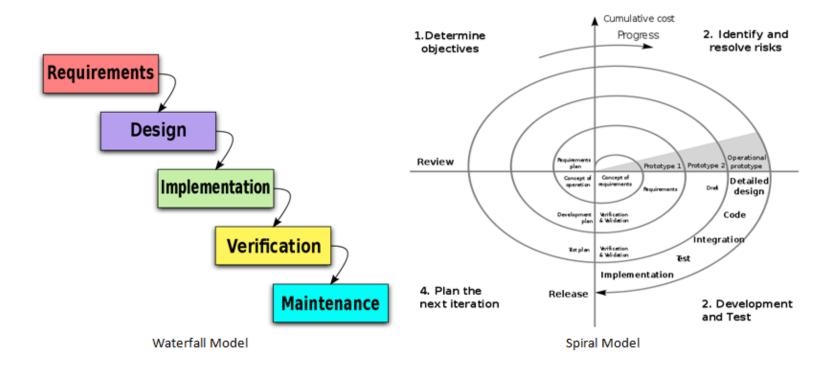
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Design of Data Warehouse: A Business Analysis Framework

- Four views regarding the design of a data warehouse
 - Top-down view
 - allows selection of the relevant information necessary for the data warehouse
 - Data source view
 - exposes the information being captured, stored, and managed by operational systems (Such as ERD etc)
 - Data warehouse view
 - consists of fact tables and dimension tables
 - Business query view
 - sees the perspectives of data in the warehouse from the view of end-user

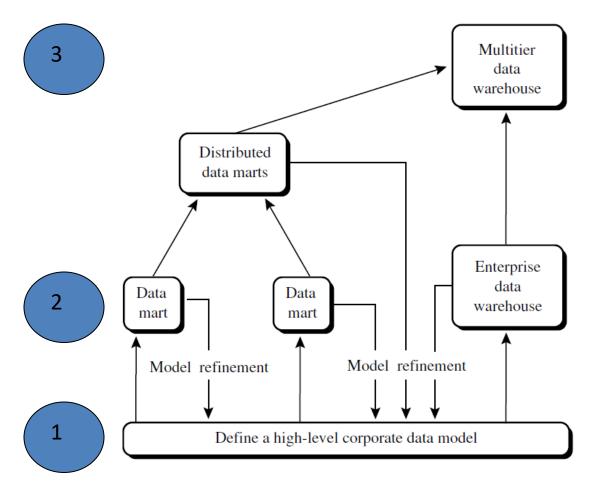
Data Warehouse Design Process

- Top-down, bottom-up approaches or a combination of both
 - <u>Top-down</u>: Starts with overall design and planning (mature)
 - Bottom-up: Starts with experiments and prototypes (rapid)
- From software engineering point of view
 - Waterfall: structured and systematic analysis at each step before proceeding to the next
 - Spiral: rapid generation of increasingly functional systems, short turn around time, quick turn around
- Typical data warehouse design process
 - Choose a business process to model, e.g., orders, invoices, etc.
 - Choose the <u>grain</u> (atomic level of data) of the business process
 - Choose the dimensions that will apply to each fact table record
 - Choose the measure that will populate each fact table record



Data Warehouse Development: A Recommended Approach

Implement the DW in an Incremental and Evolutionary Manner



Data Warehouse Usage

- Three kinds of data warehouse applications
 - Information processing
 - supports querying, basic statistical analysis, and reporting using crosstabs, tables, charts and graphs
 - Analytical processing
 - multidimensional analysis of data warehouse data
 - supports basic OLAP operations, slice-dice, drilling, pivoting
 - Data mining
 - knowledge discovery from hidden patterns
 - supports associations, constructing analytical models, performing classification and prediction, and presenting the mining results using visualization tools

From On-Line Analytical Processing (OLAP) to On Line Analytical Mining (OLAM)

- OLAM integrates OLAP with data mining to uncover knowledge in multidimensional databases.
- Why online analytical mining?
 - High quality of data in data warehouses
 - DW contains integrated, consistent, cleaned data
 - Available information processing structure surrounding data warehouses
 - ODBC, OLEDB, Web accessing, service facilities, reporting and OLAP tools
 - OLAP-based exploratory data analysis
 - Mining with drilling, dicing, pivoting, etc.
 - On-line selection of data mining functions
 - Integration and swapping of multiple mining functions, algorithms, and tasks

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Efficient Data Cube Computation

- Data cube can be viewed as a lattice of cuboids
 - The bottom-most cuboid is the base cuboid
 - The top-most cuboid (apex) contains only one cell
- Materialization of data cube
 - Materialize <u>every</u> (cuboid) (full materialization), <u>none</u> (no materialization), or <u>some</u> (partial materialization)
 - Selection of which cuboids to materialize
 - Based on size, sharing, access frequency, etc.

Indexing OLAP Data: Bitmap Index

- Index on a particular column
- Each value in the column has a bit vector: bit-op is fast
- The length of the bit vector: # of records in the base table
- The i-th bit is set if the i-th row of the base table has the value for the indexed column
- not suitable for high cardinality domains
- A recent bit compression technique, Word-Aligned Hybrid (WAH), makes it work for high cardinality domain as well [Wu, et al. TODS'06]

Base table

Index on Region

Index on Type

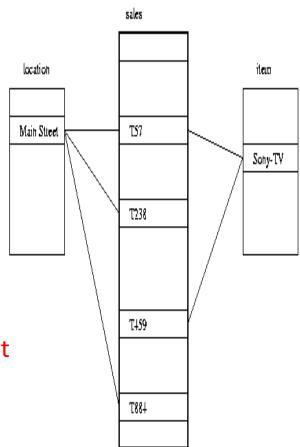
Cust	Region	Type
C1	Asia	Retail
C2	Europe	Dealer
C3	Asia	Dealer
C4	America	Retail
C5	Europe	Dealer

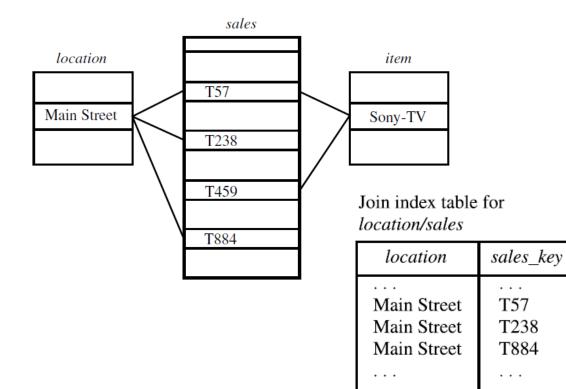
Re	cID	Asia	Europe	America
		1	0	0
2	2	0	1	0
3	3	1	0	0
	ļ	0	0	1
Ę	5	0	1	0

RecID	Retail	Dealer
1	1	0
2	0	1
3	0	1
4	1	0
5	0	1

Indexing OLAP Data: Join Indices

- Join index: JI(R-id, S-id) where R (R-id, ...) ▷ ▷ S (S-id, ...)
- Traditional indices map the values to a list of record ids
 - It materializes relational join in JI file and speeds up relational join
- In data warehouses, join index relates the values of the <u>dimensions</u> of a start schema to <u>rows</u> in the <u>fact</u> table.
 - E.g. fact table: Sales and two dimensions city and product
 - A join index on city maintains for each distinct city a list of R-IDs of the tuples recording the Sales in the city
 - Join indices can span multiple dimensions





Join index table for *item/sales*

item	sales_key
Sony-TV	T57
Sony-TV	T459

Join index table linking two dimensions *location/item/sales*

location	item	sales_key
Main Street	Sony-TV	T57

Efficient Processing OLAP Queries

- Determine which operations should be performed on the available cuboids
 - Transform drill, roll, etc. into corresponding SQL and/or OLAP operations, e.g., dice
 = selection + projection

Efficient Processing OLAP Queries (Example)

- Suppose that we define a datacube for ALLElectronics of the form
- sales[time, item, location]: sum(salles_in_euro)
- Dimension hierarchies
 - time: day < month < quater < year</p>
 - Item: item name < brand < type</p>

- **Determine which materialized cuboid(s)** should be selected for OLAP op.
 - Let the query to be processed be on {brand, province_or_state} with the condition "year = 2004", and there are 4 materialized cuboids available:
 - 1) {year, item_name, city}
 - 2) {year, brand, country}
 - 3) {year, brand, province_or_state}
 - 4) {item_name, province_or_state} where year = 2004

Which should be selected to process the query?

- Finer granularity data cannot be generated from coarsergranularity data
- Cuboid 2 cannot be used since country is more general concept then province_or_state
- Cuboids 1, 3, 4 can be used
 - They have the same set or superset of the dimensions of the query
 - The selection clause in the query can imply the selection in the cuboid
 - The abstraction levels for the *item* and location *dimension* in these cuboids are at a finer level than *brand* and *province_or_state*

How would the costs of each cuboid compare?

- Cuboid 1 would cost the most, since both item_name and city are at a lower level than brand and province_or_state
- If not many *year* values associated with *items* in the cube, and there are several *item names* for each *brand*, then cuboid 3 will be better than cuboid 4
- Efficient indices available for cuboid 4, cuboid 4 better choice (bitmap indexes)

OLAP Server Architectures

Relational OLAP (ROLAP)

- Use relational or extended-relational DBMS to store and manage warehouse data and OLAP middle ware
- Include optimization of DBMS backend, implementation of aggregation navigation logic, and additional tools and services
- Greater scalability
- Multidimensional OLAP (MOLAP)
 - Sparse array-based multidimensional storage engine
 - Fast indexing to pre-computed summarized data
- Hybrid OLAP (HOLAP) (e.g., Microsoft SQLServer)
 - Flexibility, e.g., low level: relational, high-level: array

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Attribute-Oriented Induction

- How it is done?
 - Collect the task-relevant data (initial relation) using a relational database query
 - Perform generalization by <u>attribute removal</u> or <u>attribute</u> <u>generalization</u>
 - Apply aggregation by merging identical, generalized tuples and accumulating their respective counts
 - Interaction with users for knowledge presentation

Attribute-Oriented Induction: An Example

Example: Describe general characteristics of graduate students in the University database

 Step 1. Fetch relevant set of data using an SQL statement, e.g.,

```
Select * (i.e., name, gender, major, birth_place,
birth_date, residence, phone#, gpa)
from student
```

where student_status in {"Msc", "MBA", "PhD" }

- Step 2. Perform attribute-oriented induction
- Step 3. Present results in generalized relation, cross-tab, or rule forms

Class Characterization: An Example

Initial Relation

Name	Gender	Major	Birth-Place	Birth_date	Residence	Phone #	GPA
Jim	M	CS	Vancouver,BC,	8-12-76	3511 Main St.,	687-4598	3.67
Woodman			Canada		Richmond		
Scott	M	CS	Montreal, Que,	28-7-75	345 1st Ave.,	253-9106	3.70
Lachance			Canada		Richmond		
Laura Lee	F	Physics	Seattle, WA, USA	25-8-70	125 Austin Ave.,	420-5232	3.83
•••	•••	•••	•••	•••	Burnaby	•••	•••
Removed	Retained	Sci,Eng,	Country	Age range	 City	Removed	Excl,
22020 / 04		Bus	Country	rige range	City	Removed	VG,

Prime Generalized Relation

Gender	Major	Birth_region	Age_range	Residence	GPA	Count
M	Science	Canada	20-25	Richmond	Very-good	16
F	Science	Foreign	25-30	Burnaby	Excellent	22
•••				•••		

Birth_Region Gender	Canada	Foreign	Total
M	16	14	30
F	10	22	32
Total	26	36	62

Basic Principles of Attribute-Oriented Induction

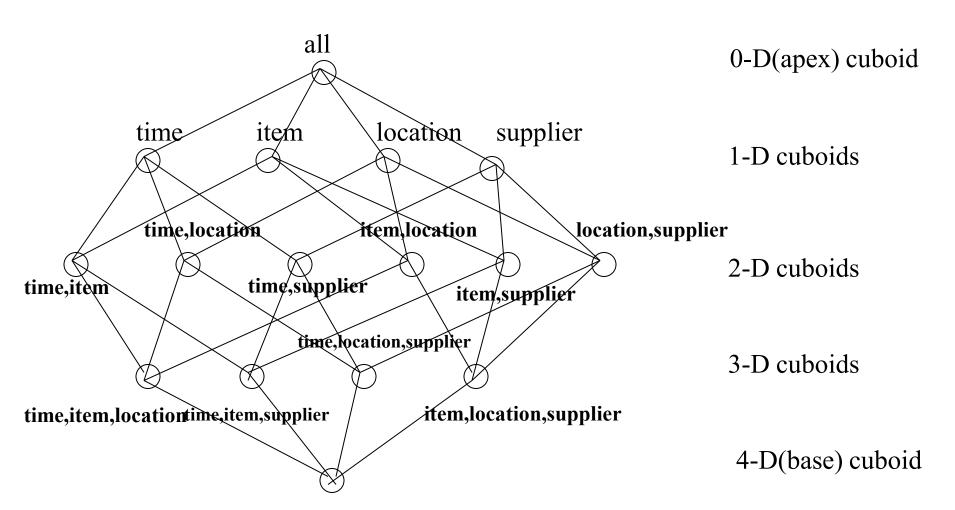
- <u>Data focusing</u>: task-relevant data, including dimensions, and the result is the initial relation
- <u>Attribute-removal</u>: remove attribute *A* if there is a large set of distinct values for *A* but (1) there is no generalization operator on *A*, or (2) *A*'s higher level concepts are expressed in terms of other attributes
- Attribute-generalization: If there is a large set of distinct values for A, and there exists a set of generalization operators on A, then select an operator and generalize A
- Attribute-threshold control: (number of distinct values)
 - typical 2-8, specified/default
- Generalized relation threshold control: control the final relation/rule size

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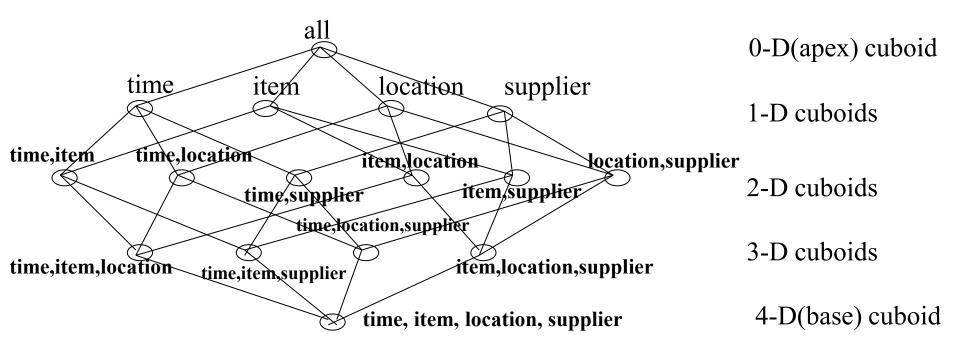


Data Cube: A Lattice of Cuboids



time, item, location, supplier

Data Cube: A Lattice of Cuboids



- Base vs. aggregate cells; ancestor vs. descendant cells; parent vs. child cells
 - 1. (9/15, milk, Urbana, Dairy_land)
 - 2. (9/15, milk, Urbana, *)
 - 3. (*, milk, Urbana, *)
 - 4. (*, milk, Urbana, *)
 - 5. (*, milk, Chicago, *)
 - 6. (*, milk, *, *)

Cube Materialization

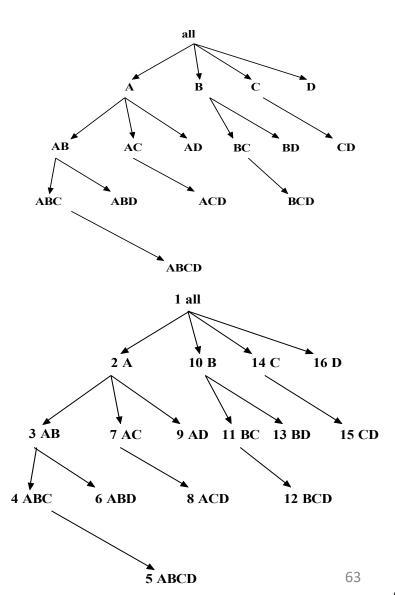
- Compute data cubes in advance
 - Readily available for query processing
- Cube materialization (i.e., pre-computation)
- Precompute the full cube (i.e., all the cells of all of the cuboids for a given data cube).
 - N dimensions -> 2^N
 - Even more cuboids if we consider concept hierarchies for each dimension
 - Size of each cuboid depends on the cardinality of its dimensions.
 - Huge and often excessive amounts of memory.

Partial materialization

- Instead of computing the full cube, we can compute only
 - A subset of the data cube's cuboids,
 or
 - Subcubes consisting of subsets of cells from the various cuboids.
- Trade-off between storage space and response time for OLAP.

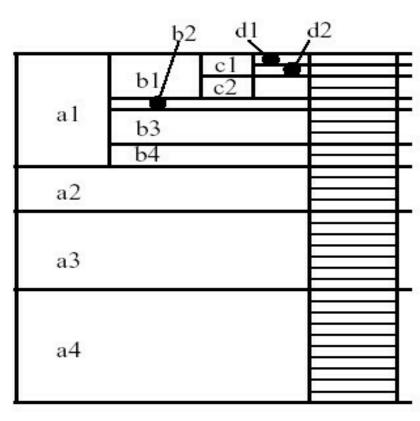
Bottom-Up Computation (BUC)

- Bottom-up cube computation (Note: top-down in our view!)
- Divides dimensions into partitions and facilitates iceberg pruning
 - If a partition does not satisfy min_sup, its descendants can be pruned
 - If $minsup = 1 \Rightarrow$ compute full CUBE!
- No simultaneous aggregation



BUC: Partitioning

- Usually, entire data set can't fit in main memory
- Sort distinct values
 - partition into blocks that fit
- Continue processing



- Performance of BUC is sensitive to the order of the dimensions and to skew in the data.
 - The most discriminating dimensions should be processed first
 - More partitions greater opportunity for pruning

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Summary

- Data warehousing: A multi-dimensional model of a data warehouse
 - A data cube consists of dimensions & measures
 - Star schema, snowflake schema, fact constellations
 - OLAP operations: drilling, rolling, slicing, dicing and pivoting
- Data Warehouse Architecture, Design, and Usage
 - Multi-tiered architecture
 - Business analysis design framework
 - Information processing, analytical processing, data mining, OLAM (Online Analytical Mining)
- Implementation: Efficient computation of data cubes
 - Partial vs. full vs. no materialization
 - Indexing OALP data: Bitmap index and join index
 - OLAP query processing
 - OLAP servers: ROLAP, MOLAP, HOLAP
- Data generalization: Attribute-oriented induction

Summary

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods
 - MultiWay Array Aggregation
 - BUC

Quiz 1

Suppose that a data warehouse consists of the three dimensions *time*, *doctor*, and *patient*, and the two measures *count* and *charge*, where *charge* is the fee that a doctor charges a patient for a visit.

- (a) Enumerate three classes of schemas that are popularly used for modeling data warehouses.
- (b) Draw a schema diagram for the above data warehouse using one of the schema classes listed in (a).
- (c) Starting with the base cuboid [day, doctor, patient], what specific OLAP operations should be performed in order to list the total fee collected by each doctor in 2004?
- (d) To obtain the same list, write an SQL query assuming the data is stored in a relational database with the schema fee (day, month, year, doctor, hospital, patient, count, charge).

Quiz 2

• Apply attribute-oriented induction On the following table:

class	$birth_place$	count
Daggagagagaga	USA	180
Programmer	others	120
DBA	USA	20
DBA	others	80

References (I)

- S. Agarwal, R. Agrawal, P. M. Deshpande, A. Gupta, J. F. Naughton, R. Ramakrishnan, and S. Sarawagi. On the computation of multidimensional aggregates. VLDB'96
- D. Agrawal, A. E. Abbadi, A. Singh, and T. Yurek. Efficient view maintenance in data warehouses. SIGMOD'97
- R. Agrawal, A. Gupta, and S. Sarawagi. Modeling multidimensional databases. ICDE'97
- S. Chaudhuri and U. Dayal. An overview of data warehousing and OLAP technology. ACM SIGMOD Record, 26:65-74, 1997
- E. F. Codd, S. B. Codd, and C. T. Salley. Beyond decision support. Computer World, 27, July 1993.
- J. Gray, et al. Data cube: A relational aggregation operator generalizing group-by, cross-tab and sub-totals. Data Mining and Knowledge Discovery, 1:29-54, 1997.
- A. Gupta and I. S. Mumick. Materialized Views: Techniques, Implementations, and Applications. MIT Press, 1999.
- J. Han. Towards on-line analytical mining in large databases. ACM SIGMOD Record, 27:97-107, 1998.
- V. Harinarayan, A. Rajaraman, and J. D. Ullman. Implementing data cubes efficiently.
 SIGMOD'96
- J. Hellerstein, P. Haas, and H. Wang. Online aggregation. SIGMOD'97

References (II)

- C. Imhoff, N. Galemmo, and J. G. Geiger. Mastering Data Warehouse Design: Relational and Dimensional Techniques. John Wiley, 2003
- W. H. Inmon. Building the Data Warehouse. John Wiley, 1996
- R. Kimball and M. Ross. The Data Warehouse Toolkit: The Complete Guide to Dimensional Modeling. 2ed. John Wiley, 2002
- P. O'Neil and G. Graefe. Multi-table joins through bitmapped join indices. *SIGMOD Record*, 24:8–11, Sept. 1995.
- P. O'Neil and D. Quass. Improved query performance with variant indexes. SIGMOD'97
- Microsoft. OLEDB for OLAP programmer's reference version 1.0. In http://www.microsoft.com/data/oledb/olap, 1998
- S. Sarawagi and M. Stonebraker. Efficient organization of large multidimensional arrays. ICDE'94
- A. Shoshani. OLAP and statistical databases: Similarities and differences. PODS'00.
- D. Srivastava, S. Dar, H. V. Jagadish, and A. V. Levy. Answering queries with aggregation using views. VLDB'96
- P. Valduriez. Join indices. ACM Trans. Database Systems, 12:218-246, 1987.
- J. Widom. Research problems in data warehousing. CIKM'95
- K. Wu, E. Otoo, and A. Shoshani, Optimal Bitmap Indices with Efficient Compression, ACM Trans. on Database Systems (TODS), 31(1): 1-38, 2006