Tabla de Integrales (Completa)

https://lelopezm.wordpress.com

Fórmulas u^n

1.
$$\int u^n du = \frac{u^{n+1}}{n+1} + C, \ n \neq -1$$

$$2. \int \frac{1}{u} du = \ln|u| + C$$

Integrales con la forma a + bu

3.
$$\int \frac{u}{a+bu} du = \frac{1}{b^2} (bu - a \ln|a+bu|) + C$$

4.
$$\int \frac{u}{(a+bu)^2} du = \frac{1}{b^2} \left(\frac{a}{a+bu} + \ln|a+bu| \right) + C$$

5.
$$\int \frac{u}{(a+bu)^n} du = \frac{1}{b^2} \left[\frac{-1}{(n-2)(a+bu)^{n-2}} + \frac{a}{(n-1)(a+bu)^{n-1}} \right] + C, \quad n \neq 1, 2$$

6.
$$\int \frac{u^2}{a+bu} du = \frac{1}{b^3} \left[-\frac{bu}{2} (2a-bu) + a^2 \ln|a+bu| \right] + C$$

7.
$$\int \frac{u^2}{(a+bu)^2} du = \frac{1}{b^3} \left(bu - \frac{a^2}{a+bu} - 2a \ln|a+bu| \right) + C$$

8.
$$\int \frac{u^2}{(a+bu)^3} du = \frac{1}{b^3} \left[\frac{2a}{a+bu} - \frac{a^2}{2(a+bu)^2} + \ln|a+bu| \right] + C$$

$$9. \int \frac{u^2}{(a+bu)^n} du = \frac{1}{b^3} \left[\frac{-1}{(n-3)(a+bu)^{n-3}} + \frac{2a}{(n-2)(a+bu)^{n-2}} - \frac{a^2}{(n-1)(a+bu)^{n-1}} \right] + C, \quad n \neq 1, 2, 3$$

10.
$$\int \frac{1}{u(a+bu)} du = \frac{1}{a} \ln \left| \frac{u}{a+bu} \right| + C$$

11.
$$\int \frac{1}{u(a+bu)^2} du = \frac{1}{a} \left(\frac{1}{a+bu} + \frac{1}{a} \ln \left| \frac{u}{a+bu} \right| \right) + C$$

12.
$$\int \frac{1}{u^2(a+bu)} du = -\frac{1}{a} \left(\frac{1}{u} + \frac{b}{a} \ln \left| \frac{u}{a+bu} \right| \right) + C$$

13.
$$\int \frac{1}{u^2(a+bu)^2} du = -\frac{1}{a^2} \left[\frac{a+2bu}{u(a+bu)} + \frac{2b}{a} \ln \left| \frac{u}{a+bu} \right| \right] + C$$

Integrales con la forma $a + bu + cu^2$, $b^2 \neq 4ac$

14.
$$\int \frac{1}{a+bu+cu^2} du = \begin{cases} \frac{2}{\sqrt{4ac-b^2}} \arctan \frac{2cu+b}{\sqrt{4ac-b^2}} + C, & b^2 < 4ac \\ \frac{1}{\sqrt{b^2-4ac}} \ln \left| \frac{2cu+b-\sqrt{b^2-4ac}}{2cu+b+\sqrt{b^2-4ac}} \right| + C, & b^2 > 4ac \end{cases}$$

15.
$$\int \frac{u}{a+bu+cu^2} du = \frac{1}{2c} \left(\ln|a+bu+cu^2| - b \int \frac{1}{a+bu+cu^2} du \right)$$

Integrales con la forma $\sqrt{a + bu}$

16.
$$\int u^n \sqrt{a + bu} \, du = \frac{2}{b(2n+3)} \left[u^n (a + bu)^{3/2} - na \int u^{n-1} \sqrt{a + bu} \, du \right]$$

17.
$$\int \frac{1}{u\sqrt{a+bu}} \, du = \begin{cases} \frac{1}{\sqrt{a}} \ln \left| \frac{\sqrt{a+bu} - \sqrt{a}}{\sqrt{a+bu} + \sqrt{a}} \right| + C, & a > 0 \\ \frac{2}{\sqrt{-a}} \arctan \sqrt{\frac{a+bu}{-a}} + C, & a < 0 \end{cases}$$

18.
$$\int \frac{1}{u^n \sqrt{a+bu}} du = \frac{-1}{a(n-1)} \left[\frac{\sqrt{a+bu}}{u^{n-1}} + \frac{(2n-3)b}{2} \int \frac{1}{u^{n-1} \sqrt{a+bu}} du \right], \ n \neq 1$$

$$19. \int \frac{\sqrt{a+bu}}{u} du = 2\sqrt{a+bu} + a \int \frac{1}{u\sqrt{a+bu}} du$$

20.
$$\int \frac{\sqrt{a+bu}}{u^n} du = \frac{-1}{a(n-1)} \left[\frac{(a+bu)^{3/2}}{u^{n-1}} + \frac{(2n-5)b}{2} \int \frac{\sqrt{a+bu}}{u^{n-1}} du \right], \ n \neq 1$$

21.
$$\int \frac{u}{\sqrt{a+bu}} \, du = \frac{-2(2a-bu)}{3b^2} \sqrt{a+bu} + C$$

22.
$$\int \frac{u^n}{\sqrt{a+bu}} du = \frac{2}{(2n+1)b} \left(u^n \sqrt{a+bu} - na \int \frac{u^{n-1}}{\sqrt{a+bu}} du \right)$$

Integrales con la forma $a^2 \pm u^2$, a > 0

$$23. \int \frac{1}{a^2 + u^2} du = \frac{1}{a} \arctan \frac{u}{a} + C$$

24.
$$\int \frac{1}{u^2 - a^2} du = -\int \frac{1}{a^2 - u^2} du = \frac{1}{2a} \ln \left| \frac{u - a}{u + a} \right| + C$$

25.
$$\int \frac{1}{(a^2 \pm u^2)^n} du = \frac{1}{2a^2(n-1)} \left[\frac{u}{(a^2 \pm u^2)^{n-1}} + (2n-3) \int \frac{1}{(a^2 \pm u^2)^{n-1}} du \right], \ n \neq 1$$

Integrales con la forma $\sqrt{u^2 \pm a^2}$, a > 0

26.
$$\int \sqrt{u^2 \pm a^2} \, du = \frac{1}{2} \left(u \sqrt{u^2 \pm a^2} \pm a^2 \ln|u + \sqrt{u^2 \pm a^2}| \right) + C$$

27.
$$\int u^2 \sqrt{u^2 \pm a^2} \, du = \frac{1}{8} \left[u(2u^2 \pm a^2) \sqrt{u^2 \pm a^2} - a^4 \ln|u + \sqrt{u^2 \pm a^2}| \right] + C$$

28.
$$\int \frac{\sqrt{u^2 + a^2}}{u} du = \sqrt{u^2 + a^2} - a \ln \left| \frac{a + \sqrt{u^2 + a^2}}{u} \right| + C$$

29.
$$\int \frac{\sqrt{u^2 - a^2}}{u} du = \sqrt{u^2 - a^2} - a \operatorname{arcsec} \frac{|u|}{a} + C$$

30.
$$\int \frac{\sqrt{u^2 \pm a^2}}{u^2} du = \frac{-\sqrt{u^2 \pm a^2}}{u} + \ln|u + \sqrt{u^2 \pm a^2}| + C$$

31.
$$\int \frac{1}{\sqrt{u^2 \pm a^2}} du = \ln|u + \sqrt{u^2 \pm a^2}| + C$$

32.
$$\int \frac{1}{u\sqrt{u^2 + a^2}} du = \frac{-1}{a} \ln \left| \frac{a + \sqrt{u^2 + a^2}}{u} \right| + C$$

33.
$$\int \frac{1}{u\sqrt{u^2 - a^2}} du = \frac{1}{a} \operatorname{arcsec} \frac{|u|}{a} + C$$

34.
$$\int \frac{u^2}{\sqrt{u^2 \pm a^2}} du = \frac{1}{2} \left(u \sqrt{u^2 \pm a^2} \mp a^2 \ln|u + \sqrt{u^2 \pm a^2}| \right) + C$$

35.
$$\int \frac{1}{u^2 \sqrt{u^2 \pm a^2}} du = \mp \frac{\sqrt{u^2 \pm a^2}}{a^2 u} + C$$

36.
$$\int \frac{1}{(u^2 \pm a^2)^{3/2}} du = \frac{\pm u}{a^2 \sqrt{u^2 \pm a^2}} + C$$

Integrales con la forma $\sqrt{a^2 - u^2}$, a > 0

37.
$$\int \sqrt{a^2 - u^2} \, du = \frac{1}{2} \left(u \sqrt{a^2 - u^2} + a^2 \arcsin \frac{u}{a} \right) + C$$

38.
$$\int u^2 \sqrt{a^2 - u^2} \, du = \frac{1}{8} \left[u(2u^2 - a^2) \sqrt{a^2 - u^2} + a^4 \arcsin \frac{u}{a} \right] + C$$

39.
$$\int \frac{\sqrt{a^2 - u^2}}{u} du = \sqrt{a^2 - u^2} - a \ln \left| \frac{a + \sqrt{a^2 - u^2}}{u} \right| + C$$

40.
$$\int \frac{\sqrt{a^2 - u^2}}{u^2} du = \frac{-\sqrt{a^2 - u^2}}{u} - \arcsin \frac{u}{a} + C$$

41.
$$\int \frac{1}{\sqrt{a^2 - u^2}} du = \arcsin \frac{u}{a} + C$$

42.
$$\int \frac{1}{u\sqrt{a^2 - u^2}} du = \frac{-1}{a} \ln \left| \frac{a + \sqrt{a^2 - u^2}}{u} \right| + C$$

43.
$$\int \frac{u^2}{\sqrt{a^2 - u^2}} du = \frac{1}{2} \left(-u \sqrt{a^2 - u^2} + a^2 \arcsin \frac{u}{a} \right) + C$$

44.
$$\int \frac{1}{u^2 \sqrt{a^2 - u^2}} du = \frac{-\sqrt{a^2 - u^2}}{a^2 u} + C$$

45.
$$\int \frac{1}{(a^2 - u^2)^{3/2}} du = \frac{u}{a^2 \sqrt{a^2 - u^2}} + C$$

Integrales con la forma sen u o $\cos u$

$$\mathbf{46.} \int \operatorname{sen} u \, du = -\cos u + C$$

48.
$$\int \sin^2 u \, du = \frac{1}{2}(u - \sin u \cos u) + C$$

50.
$$\int \operatorname{sen}^{n} u \, du = -\frac{\operatorname{sen}^{n-1} u \cos u}{n} + \frac{n-1}{n} \int \operatorname{sen}^{n-2} u \, du$$

$$52. \int u \sin u \, du = \sin u - u \cos u + C$$

54.
$$\int u^n \sin u \, du = -u^n \cos u + n \int u^{n-1} \cos u \, du$$

$$\mathbf{56.} \int \frac{1}{1 \pm \sin u} \, du = \tan u \mp \sec u + C$$

$$58. \int \frac{1}{\sin u \cos u} du = \ln |\tan u| + C$$

$$47. \int \cos u \, du = \sin u + C$$

49.
$$\int \cos^2 u \, du = \frac{1}{2}(u + \sin u \cos u) + C$$

51.
$$\int \cos^n u \, du = \frac{\cos^{n-1} u \sin u}{n} + \frac{n-1}{n} \int \cos^{n-2} u \, du$$

$$53. \int u \cos u \, du = \cos u + u \sin u + C$$

55.
$$\int u^n \cos u \, du = u^n \sin u - n \int u^{n-1} \sin u \, du$$

$$57. \int \frac{1}{1 \pm \cos u} du = -\cot u \pm \csc u + C$$

Integrales con la forma $\tan u$, $\cot u$, $\sec u$, $\csc u$

$$\mathbf{59.} \int \tan u \, du = -\ln|\cos u| + C$$

61.
$$\int \sec u \, du = \ln|\sec u + \tan u| + C$$

62.
$$\int \csc u \, du = \ln|\csc u - \cot u| + C \quad \text{o} \quad \int \csc u \, du = -\ln|\csc u + \cot u| + C$$

63.
$$\int \tan^2 u \, du = -u + \tan u + C$$

$$65. \int \sec^2 u \ du = \tan u + C$$

67.
$$\int \tan^n u \ du = \frac{\tan^{n-1} u}{n-1} - \int \tan^{n-2} u \ du, \ n \neq 1$$

68.
$$\int \cot^n u \, du = -\frac{\cot^{n-1} u}{n-1} - \int (\cot^{n-2} u) \, du, \ n \neq 1$$

69.
$$\int \sec^n u \ du = \frac{\sec^{n-2} u \tan u}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} u \ du, \ n \neq 1$$

70.
$$\int \csc^n u \ du = -\frac{\csc^{n-2} u \cot u}{n-1} + \frac{n-2}{n-1} \int \csc^{n-2} u \ du, \ n \neq 1$$

71.
$$\int \frac{1}{1 \pm \tan u} du = \frac{1}{2} (u \pm \ln|\cos u \pm \sin u|) + C$$

73.
$$\int \frac{1}{1 \pm \sec u} du = u + \cot u \mp \csc u + C$$

60.
$$\int \cot u \, du = \ln|\sin u| + C$$

$$\mathbf{64.} \int \cot^2 u \, du = -u - \cot u + C$$

$$\mathbf{66.} \int \csc^2 u \, du = -\cot u + C$$

72.
$$\int \frac{1}{1 \pm \cot u} du = \frac{1}{2} (u \mp \ln|\sin u \pm \cos u|) + C$$

74.
$$\int \frac{1}{1 \pm \csc u} du = u - \tan u \pm \sec u + C$$

Integrales con funciones trigonométricas inversas

75.
$$\int \operatorname{arcsen} u \, du = u \operatorname{arcsen} u + \sqrt{1 - u^2} + C$$

77.
$$\int \arctan u \, du = u \arctan u - \ln \sqrt{1 + u^2} + C$$

79.
$$\int \operatorname{arcsec} u \, du = u \operatorname{arcsec} u - \ln \left| u + \sqrt{u^2 - 1} \right| + C$$

80.
$$\int \operatorname{arccsc} u \, du = u \operatorname{arccsc} u + \ln |u + \sqrt{u^2 - 1}| + C$$

76.
$$\int \arccos u \, du = u \arccos u - \sqrt{1 - u^2} + C$$

78.
$$\int \operatorname{arccot} u \, du = u \operatorname{arccot} u + \ln \sqrt{1 + u^2} + C$$

Integrales con la forma e^u

$$\mathbf{81.} \int e^u \, du = e^u + C$$

83.
$$\int u^n e^u \, du = u^n e^u - n \int u^{n-1} e^u \, du$$

85.
$$\int e^{au} \sin bu \, du = \frac{e^{au}}{a^2 + b^2} (a \sin bu - b \cos bu) + C$$

86.
$$\int e^{au} \cos bu \, du = \frac{e^{au}}{a^2 + b^2} (a \cos bu + b \sin bu) + C$$

82.
$$\int ue^u \, du = (u-1)e^u + C$$

84.
$$\int \frac{1}{1+e^u} du = u - \ln(1+e^u) + C$$

Integrales con la forma $\ln u$

87.
$$\int \ln u \, du = u(-1 + \ln u) + C$$

89.
$$\int u^n \ln u \, du = \frac{u^{n+1}}{(n+1)^2} [-1 + (n+1) \ln u] + C, \ n \neq -1$$

90.
$$\int (\ln u)^2 du = u [2 - 2 \ln u + (\ln u)^2] + C$$

88.
$$\int u \ln u \, du = \frac{u^2}{4} (-1 + 2 \ln u) + C$$

91.
$$\int (\ln u)^n du = u(\ln u)^n - n \int (\ln u)^{n-1} du$$

Integrales con funciones hiperbólicas

$$92. \int \cosh u \, du = \sinh u + C$$

$$\mathbf{94.} \int \operatorname{sech}^2 u \, du = \tanh u + C$$

$$96. \int \operatorname{sech} u \tanh u \, du = -\operatorname{sech} u + C$$

93.
$$\int \operatorname{senh} u \, du = \cosh u + C$$

$$95. \int \operatorname{csch}^2 u \, du = -\coth u + C$$

$$97. \int \operatorname{csch} u \operatorname{coth} u \, du = -\operatorname{csch} u + C$$

Integrales con funciones hiperbólicas inversas (en forma logarítmica)

98.
$$\int \frac{du}{\sqrt{u^2 \pm a^2}} = \ln(u + \sqrt{u^2 \pm a^2}) + C$$

99.
$$\int \frac{du}{a^2 - u^2} = \frac{1}{2a} \ln \left| \frac{a + u}{a - u} \right| + C$$

100.
$$\int \frac{du}{u\sqrt{a^2 \pm u^2}} = -\frac{1}{a} \ln \frac{a + \sqrt{a^2 \pm u^2}}{|u|} + C$$