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BLG 336E  
The L<sup>A</sup>T<sub>E</sub>X  
Report

**Analysis of Algorithms II, Project 1**  
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# 1 Description of Code

## 1.1 Pseudo-code

### 1.1.1 Graph Implementation

I implement the code which creates (n x n) adjacency matrix as a graph. If the squared distance between i-th vertex and j-th vertex is less then or equal to the strength of i-th and j-th, then there is an edge between two vertices.

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**Algorithm 1** Set Edges

---

```
function SETEDGES(*nodes, numberVertices)
     $i \leftarrow 0$ 
    while  $i < \text{numberVertices}$  do
        while  $j < \text{numberVertices}$  do
            if  $i \leftarrow j$  then
                 $\text{adjMatrix}[i][j] \leftarrow 0$ 
            end if
             $x - \text{distance} \leftarrow \text{nodes}[i].\text{GET-X-COORDINATE} - \text{nodes}[j].\text{GET-X-COORDINATE}()$ 
             $y - \text{distance} \leftarrow \text{nodes}[i].\text{GET-Y-COORDINATE} - \text{nodes}[j].\text{GET-Y-COORDINATE}()$ 
             $\text{squared-distance} \leftarrow \text{POW}(x - \text{distance}, 2) + \text{POW}(y - \text{distance}, 2)$ 
            if  $\text{squared-distance} \leq \text{nodes}[i].\text{GET-STRENGTH-LEVEL}$  and  $\text{squared-distance} \leq$ 
 $\text{nodes}[j].\text{GET-STRENGTH-LEVEL}$  then
                 $\text{adjMatrix}[i][j] \leftarrow 1$ 
                 $\text{adjMatrix}[j][i] \leftarrow 1$ 
            end if
        end while
    end while
end function
```

---

### 1.1.2 Breadth First Search Implementation

Graph traversed using Breadth First Search(BFS) algorithm to find the minimum amount of pass from the starting point to the target point.

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**Algorithm 2** Breadth First Search

---

```
function BREADTHFIRSTSEARCH(numberVertices, sourceVertex, distance, predecessor)
    visited  $\leftarrow$  vector of bool with number of vertices elements, initialized to false
    q  $\leftarrow$  queue of int
    q.PUSH(sourceVertex)
    visited[sourceVertex]  $\leftarrow$  true
    distance[sourceVertex]  $\leftarrow$  0
    while !q.EMPTY() do
        visitedVertex  $\leftarrow$  q.FRONT()
        q.POP()
        i  $\leftarrow$  0
        while i < numberVertices do
            if adjMatrix[visitedVertex][i]  $\leftarrow$  1 and (!visited[i]) then
                q.PUSH(i)
                distance[i]  $\leftarrow$  distance[visitedVertex] + 1
                predecessor[i] = visitedVertex
                visited[i] = true
            end if
        end while
    end while
end function
```

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### 1.1.3 Depth First Search Implementation

It was tested whether the graph contains a cycle starting from the source vertex and returning to this vertex using Depth First Search(DFS) algorithm. If it contains this cycle, the path traversed is saved.

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**Algorithm 3** Depth First Search

---

```
function CONTAINSCYCLE(vertex, visited, predecessor, savedPath, sourceVertex, numberVertices)
    visited[vertex]  $\leftarrow$  true
    i  $\leftarrow$  0
    while i < numberVertices do
        if adjMatrix[sourceVertex][vertex]  $\leftarrow$  1 and (predecessor[vertex]! = sourceVertex)
        then
            return true
        end if
        if adjMatrix[i][vertex]  $\leftarrow$  1 and (!visited[i]) then
            predecessor[i]  $\leftarrow$  vertex
            if CONTAINSCYCLE(i, visited, predecessor, savedPath, sourceVertex, numberVertices) then
                return true
            end if
        end if
    end while
    return false
end function
```

---

---

**Algorithm 4** Depth First Search

---

```
function DEPTHFIRSTSEARCH(numberVertices, sourceVertex, start, distance, predecessor)
    visited  $\leftarrow$  vector of bool with number of vertices elements, initialized to false
    predecessor  $\leftarrow$  vector of int with number of vertices, initialize to -1
    savedPath  $\leftarrow$  vector of int
    visited[sourceVertex]  $\leftarrow$  true
    i  $\leftarrow$  0
    while i < numberVertices do
        if adjMatrix[sourceVertex][i]  $\leftarrow$  1 and (!visited[i]) then
            predecessor[i] = sourceVertex
            if CONTAINSCYCLE(i, visited, predecessor, savedPath, sourceVertex, numberVer-
            tices) then
                print path
            end if
            if (!CONTAINSCYCLE(i, visited, predecessor, savedPath, sourceVertex, num-
            berVertices)) then
                print -1
            end if
        end if
        end while
    end function
```

---

## 1.2 Time Complexity

The graph has  $n$  vertices, the time complexity to build an adjacency matrix is  $O(n^2)$ . Finding the adjacent vertices of selected vertex requires checking all elements in the row. This takes linear time  $O(n)$ . Summing over all the  $n$  iterations, the total running time is  $O(n^2)$ . In the Breadth First Search function, the for loop loops  $n$  times, and the while loop loops  $n$  times depending on this number, resulting in  $n^2$ . In the DFS algorithm, it returns  $n$  times in the for loop in the Depth First Search function and calls the Contains Cycle function, and inside that function it returns  $n$  times in the for loop, so it becomes  $n^2$ . Therefore, time complexity of BFS and DFS are  $O(n^2)$ .

## 2 Maintain a List of Discovered Nodes

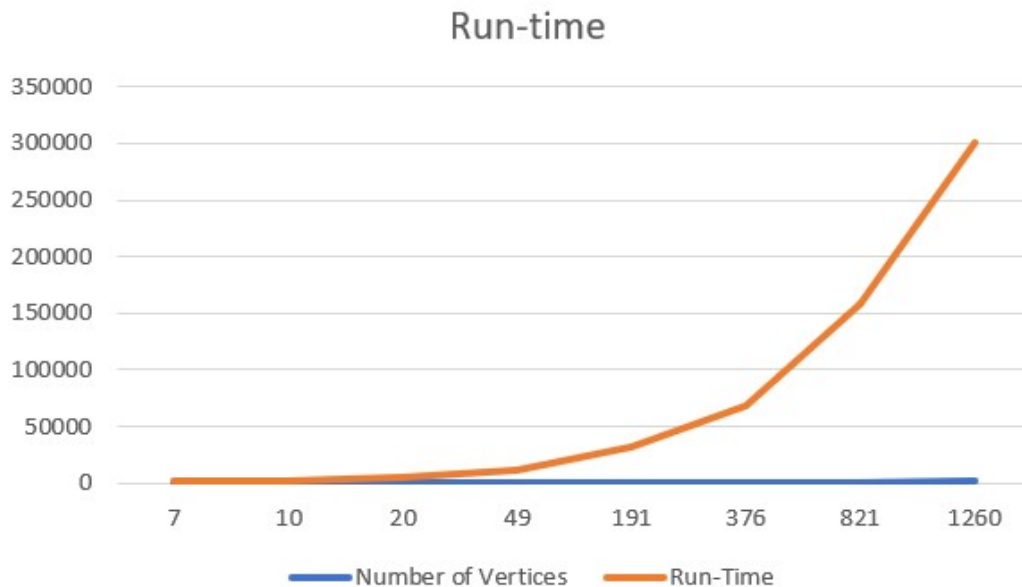
By saving visited nodes, we eliminate the possibility of being visited again. Each node can be visited once. Otherwise, we could traverse the same node multiple times. If we do not mark a node as visited, it will go to another node and come back. This creates a loop. Therefore, the BFS and DFS algorithms will not terminate. We need to keep a visited array for the algorithms to work correctly.

### 3 Relationship between Number of Kids and Memory Complexity

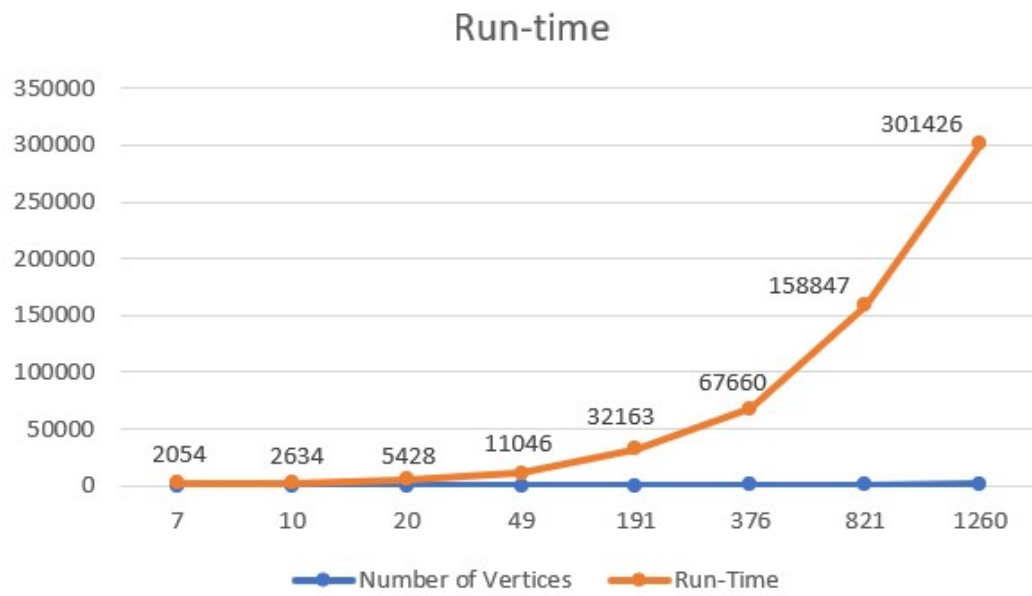
#### 3.1 Space Complexity

The adjacency matrix of a graph requires  $O(V^2)$  memory where  $V$  is the number of vertices. The space complexity of BFS and DFS can be expressed as  $O(V)$ , where  $V$  is the number of vertices, because when finding shortest path I used a queue that takes the number of vertices and when finding a cycle I used a vector that takes the number of vertices. Increasing the number of kids means increasing the number of vertices. Creating an adjacency matrix is proportional to the square of the number of vertices. Since the space complexity of BFS and DFS depend on the vertex number, the space complexity of the BFS and DFS increases linearly.

#### 3.2 Run-Time



**Figure 1:** The graph for run-time in microseconds for all cases



**Figure 2:** The graph for run-time in microseconds with labels for all cases