
MODULE *RadixTreesValidation*

EXTENDS *FiniteSets*, *Integers*, *RadixTrees*, *Sequences*, *TLC*

Set of characters to use for the alphabet of generated strings.
 CONSTANT *Alphabet*

Length of input strings generated
 CONSTANT *MinLength*, *MaxLength*
 ASSUME

$\wedge \{MinLength, MaxLength\} \subseteq Nat$
 $\wedge MinLength \leq MaxLength$
 $\wedge MinLength > 0$

Number of unique elements to construct the radix tree with. This
 is a set of numbers so you can test with inputs of multiple sizes.
 CONSTANT *ElementCounts*
 ASSUME *ElementCounts* $\subseteq Nat$

Inputs is the set of input strings valid for the tree.
 $Inputs \triangleq \text{UNION } \{[1 \dots n \rightarrow Alphabet] : n \in MinLength \dots MaxLength\}$

InputSets is the full set of possible inputs we can send to the radix tree.
 $InputSets \triangleq \{T \in \text{SUBSET } Inputs : Cardinality(T) \in ElementCounts\}$

Trees are the set of all radix trees for our inputs. This is a sequence
 where $s[1]$ is the input and $s[2]$ is the tree. We keep the input for testing.
 $Trees \triangleq \{\langle input, RadixTree(input) \rangle : input \in InputSets\}$

All leaf nodes should be values, there is no such thing as a leaf
 node that doesn't represent a value.

RECURSIVE *LeafsAreValues*(-)
 $LeafsAreValues(T) \triangleq$
 $\vee \wedge Cardinality(\text{DOMAIN } T.Edges) > 0$ if it has edges, its leaves must be values
 $\wedge \forall e \in \text{DOMAIN } T.Edges : LeafsAreValues(T.Edges[e])$
 $\vee \wedge Cardinality(\text{DOMAIN } T.Edges) = 0$ if it has no edges, it must be a value
 $\wedge Len(T.Value) > 0$

The range of a radix tree should be the set of its inputs.
 $RangeIsInput(input, tree) \triangleq input = Range(tree)$

The expression that should be checked for validity in the model.
 $Valid \triangleq$
 $\forall pair \in Trees :$
 $\text{LET } input \triangleq pair[1]tree \triangleq pair[2] \text{IN}$

$\vee \wedge \textit{RangeIsInput}(\textit{input}, \textit{tree})$
 $\wedge \textit{LeafsAreValues}(\textit{tree})$
 $\vee \textit{Print}(\langle \textit{input}, \textit{tree} \rangle, \text{FALSE})$

\ * Modification History
\ * Last modified *Fri Jul 02 13:48:34 PDT 2021* by *mitchellh*
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