This module specifies the iterator structure used in the go-immutable-radix project (https://github.com/hashicorp/go-immutable-radix/).

The iterator is meant to seek to some point in a radix tree and read all the subsequent values until it is over. It supports seeking by prefix and by lower bound.

MODULE RadixIterator

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LOCAL INSTANCE RadixTrees
LOCAL INSTANCE Sequences
LOCAL INSTANCE FiniteSets
LOCAL INSTANCE Integers
LOCAL INSTANCE TLC
 CmpOp is the comparison operator for ordered iteration. This should be TRUE
 if the first value is less than the second value.
CONSTANT CmpOp(\_, \_)
 TRUE iff the sequence s contains no duplicates. Copied from CommunityModules.
LOCAL isInjective(s) \stackrel{\triangle}{=} \forall i, j \in DOMAIN \ s : (s[i] = s[j]) \Rightarrow (i = j)
 Converts a set to a sequence that contains all the elements of S exactly once.
 {\bf Copied\ from\ } {\it Community Modules}.
LOCAL setToSeq(S) \stackrel{\Delta}{=} CHOOSE f \in [1 .. Cardinality(S) \rightarrow S] : isInjective(f)
 Copied from CommunityModules.
LOCAL mapThenFoldSet(op(\_, \_), base, f(\_), choose(\_), S) \stackrel{\triangle}{=} LET \quad iter[s \in SUBSET S] \stackrel{\triangle}{=}
            IF s = \{\} THEN base
ELSE LET x \triangleq choose(s)
                          op(f(x), iter[s \setminus \{x\}])
          iter[S]
  IN
 foldLeft folds op on all elements of seq from left to right, starting
 with the first element and base. Copied from CommunityModules.
LOCAL foldLeft(op(_, _), base, seq) \stackrel{\triangle}{=}
  mapThenFoldSet(LAMBDA x, y : op(y, x), base,
                          LAMBDA i : seq[i],
                          LAMBDA s: CHOOSE i \in s: \forall j \in s: i \geq j,
                          DOMAIN seq)
 Internal logic for Iterate.
RECURSIVE iterate(\_, \_)
iterate(T, prefix) \stackrel{\triangle}{=}
     current \stackrel{\triangle}{=} IF Len(T.Value) > 0 THEN \langle T.Value \rangle ELSE \langle \rangle
```

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current value of node (if exists)  orderedEdges \stackrel{\triangle}{=} SortSeq(setToSeq(\mathsf{DOMAIN}\ T.Edges),\ CmpOp) \\  ordering that we'll visit edges \\  children \stackrel{\triangle}{=} [i \in 1 \ldots Len(orderedEdges) \mapsto \\  iterate(T.Edges[orderedEdges[i]],\ prefix \circ T.Prefix)] \\  children values, this is a tuple of tuples \\  flatChildren \stackrel{\triangle}{=} foldLeft(\mathsf{LAMBDA}\ x,\ y: x \circ y,\ \langle\rangle,\ children) \\   children as a single tuple of values \\   IN \ current \circ flatChildren \\  Iterate implements the core iteration algorithm. Given a sequence of nodes \\  this will return a sequence (not a set, since this is ordered) of keys that \\  are visited in the tree. \\ Iterate(Stack) \stackrel{\triangle}{=} \\  foldLeft(\mathsf{LAMBDA}\ x,\ y: x \circ y,\ \langle\rangle,\ [i \in 1 \ldots Len(Stack) \mapsto iterate(Stack[i],\ \langle\rangle)]) \\
```

- ***** Modification History
- * Last modified Thu Jul 01 17:27:34 PDT 2021 by mitchellh
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