# Performing Fractional Polynomials in R

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#### Introduction

This document is intended as a guide for modeling the relationship between a measure of training load and injury in sports research, using fractional polynomials (FP). The examples will go through standard logistic regression, and later a mixed effects logistic regression model. However, the steps to model training load using FP in a Poisson model and other regression models are the same.

### Preparation

First, load required packages.

```
library(tidyverse) # for creating figures, and for a self-made function we'll need later on library(rlang) # for creating functions with tidyverse syntax library(mfp) # the mfp package has functions for automatic determination of FP library(lme4) # package for mixed model functions library(merTools) # a sister-package to lme4 for extra functions on mixed models
```

Next step is to load your data. Here, we used the d\_example\_guide.rds data available from the GitHub repository. It is simulated from football data for the example to be reproducible. The object "d" in the r-code below can be replaced with your own data. At the minimum, your data should have:

- one column for load, measured in any metric (such as sRPE, GPS measures or ACWR)
- one column for injury, must either be a logical variable (TRUE/FALSE) or coded (0 for no injury, 1 for injury) to work in our logistic regression model.
- one column for athlete ID, coupling the load values and injuries to the right person

```
d = readRDS("d_example_guide.rds")
```

### Standard Logistic Regression

#### Fitting the model

For a regular logistic regression model, we can write:

```
fit_logistic = glm(injury ~ load, data = d)
```

Running fit\_logistic or summary(fit\_logistic) will provide us the results and information from the fit.

Fitting load with fractional polynomial terms, we can run the code below. Note that it may take a little time.

```
fit_fp = mfp(injury ~ fp(load), data = d, family = "binomial")
```

The function fp() is from the mfppackage. The model searches for the best fit of a number of possible polynomial transformations. It uses a backwards selection process.

Running summary() of the fit will provide information of how many polynomials terms were added (of 1 or 2), and to what power they were chosen. Estimate is the beta-value and represents the logodds. The p-value indicates significance of each polynomial term.

By saving the object like this:

```
fit_summary = summary(fit_fp)
```

It's possible to access different data from the fit For example, the aic, or the coefficients, to use them later:

```
fit_summary$aic
```

```
## [1] 14777.15
```

```
fit_summary$coefficients
```

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.3551343943 0.0437397223 76.70681 0.000000e+00
## I(((load + 1)/100)^1) -0.4935883599 0.0110508208 -44.66531 0.000000e+00
## I(((load + 1)/100)^3) 0.0009313095 0.0000840651 11.07843 1.596439e-28
```

To obtain Odds Ratios, we can run:

```
## Intercept load.1 load.2
## 28.649454 0.610432 1.000932
```

#### Visualization

exp(coef(fit\_fp))

With fractional polynomials, we can interpret our results numerically, but it may still be useful to create a figure of the predictions to see the relationship shape.

In a case where multiple variables have been included in the dataset, a new dataset needs to be created where the other variables have been set to a constant parameter, such as the mean age.

We make a new object name for this dataset here, so we don't overwrite our original data object:

```
pred_data = d
pred_data$age = 17
```

We then add our data to the argument, newdata in the predict() command. The argument type = "response" means we will receive probability of injury instead of logodds of injury.

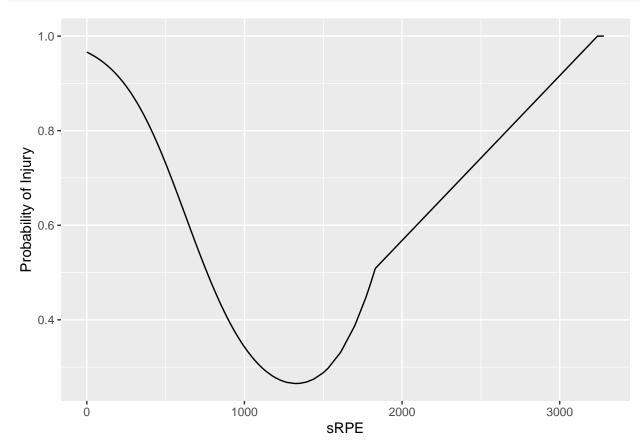
```
pred_load = predict(fit_fp, type = "response", newdata = pred_data)
```

To create a figure from our predictions, we add the predictions to our dataset with the load values used for predictions:

```
pred_data$yhat = pred_load
```

We loaded the tidyverse package, which includes the ggplot2 package. To create a simple form of ggplot2-plot:

```
ggplot(pred_data, aes(x = load, y = yhat)) +
  geom_line() +
  xlab("sRPE") +
  ylab("Probability of Injury")
```



Mapping the load values to the predicted probabilities (figure above) showed that the polynomials modelled a U-shaped relationship for the example data.

## Mixed Effects Regression Model

#### Fitting the model

A mixed effects logistic regression model is a bit more complicated most notably, because running a general linear mixed model (GLMM) isn't part of base R. Here we use the lme4 package for mixed models. Not everything in base R or other packages is compatible with the lme4 package. Most critically, the mfp() package for running fractional polynomials are not compatible with the lme4 package.

For a mixed model with binomial distribution and random intercept per athlete one can run:

```
fit_mixed = glmer(injury ~ load + (1 | p_id), family = "binomial", data = d)
```

For a mixed model with binomial distribution, random intercept and random slope per athlete

```
fit_mixed_slope = glmer(injury ~ load + (load | p_id), family = "binomial", data = d)
```

Since running the mfp()-function won't work inside glmer(), we need another solution. One solution would be manually model every possible incarnation of an FP2 model and manually determine the best fit.

Here we've made an automatized solution. Below is a function, glmer\_fp() that searches for the best FP fit in a standard regression model with the mfp-function we used earlier. The FP-formula that was found to be the best one is then extracted from the standard model and run in a random effects model using glmer(). the default is a logistic regression (binomial distribution of outcome measure).

The function was created using tidyverse, rlang (which is why we loaded these at the top), the lme4 and mfp package.

```
# the function has the following arguments:
                    The dataset with the load and injury variable
\# d
# injury
                    The variable used to denote injury.
                    Can be heealth problems or any other definition of injury.
#
# load
                    The load variable in the dataset.
# rdm_effect
                    The random effect term.
                    Must be surrounded by quotes "". Examples are "(1/your_id_variable)"
#
                    for a random intercept and "(load/your_id_variable)"
                    for a random slope + random intercept.
# family
                    Determine the model family. The defualt is binomial,
                    meaning the models will run logistic regression.
#
                    can be sett to "poisson" or other alternatives, see ?glmer()
# for a multivariable model, extra covariates will have to be added
# using + after fp(!!load), i.e. !!injury \sim fp(!!load) + sex + age,
# but the names must match those in the data
# and the function will no longer be general
glmer_fp = function(d, injury, load, rdm_effect, family = "binomial"){
  injury = enexpr(injury)
 load = enexpr(load)
  # run mfp to find best FP terms
  prox_fit = eval_bare(expr(mfp(!!injury ~ fp(!!load), data = d, family = family)))
  fp_form = prox_fit$formula
  # automatically use that formula in a random effects model
  formula_start = paste0("!!",fp_form[2], " ", fp_form[1])
  formula = paste0(formula_start, " ", fp_form[3], " + ",rdm_effect,"")
  glmm_fit = eval_bare(expr(glmer(as.formula(formula), family = family, data = d)))
  glmm fit
```

An example of using the function with a random intercept and random slope:

```
fit_mixed = glmer_fp(d, injury, load, "(load|p_id)")
```

An example of using the function with a random intercept only:

```
fit_mixed_intercept = glmer_fp(d, injury, load, "(1|p_id)")
```

If both were able to converge, we can determine best fit with AIC:

```
AIC(fit_mixed)

## [1] 14744.94

AIC(fit_mixed_intercept)

## [1] 14742.65
```

As seen above, the random intercept model had the lowest AIC and therefore the better fit.

#### Visualization

Since we now have the random effect, we must set the example data to a fixed athlete as our example. we make a new object name for this dataset here, so we don't overwrite our original data object:

```
pred_data_mixed = d
pred_data_mixed$p_id = 1
```

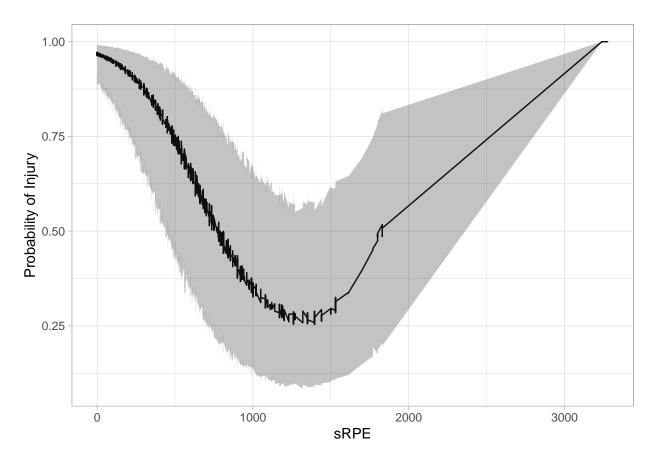
For GLMM, we use the predictInterval() function that also predict the confidence intervals. This is why we loaded the merTools package. predictInterval() can't be used on anything but a glmer()-created object from the lme4-package. Note that estimating the confidence intervals might take some time. Code below:

We add the load data we used for predictions to our predicted values:

```
pred_load_mixed_ci$load = pred_data_mixed$load
```

For a simple ggplot2-plot with confidence intervals:

```
ggplot(pred_load_mixed_ci, aes(x = load, y = fit, min = lwr, max = upr)) +
geom_line() +
geom_ribbon(alpha = 0.3) + # alpha is for transparency
theme_light() + # a simple way to clean up
xlab("sRPE") +
ylab("Probability of Injury")
```



If you don't want multiple predictions per load value, you can predict based on a distinct set of values. Code below:

#### Final plot:

```
ggplot(pred_load_mixed_distinct, aes(x = load, y = fit, min = lwr, max = upr)) +
  geom_line() +
  geom_ribbon(alpha = 0.3) +
  theme_light() +
  xlab("sRPE") +
  ylab("Probability of Injury")
```

