As you've solved earlier that the radial part of the hydrogen atom Hamiltonian

the expectation value for the "moments" with respect to energy eigenstates satisfy

 $8 \text{KE} \langle \Gamma^{K-1} \rangle + (K-1) [K(K-2) - 4l(l+1)] \langle \Gamma^{K-3} \rangle + 4(2m-1) \langle \Gamma^{K-2} \rangle = 0$

Using the fact that Hankel matrix of the moments $\langle r^{K} \rangle$, i.e. $\langle r^{0} \rangle, \langle r^{1} \rangle, \langle r^{2} \rangle - \langle r^{1} \rangle, \langle r^{2} \rangle, \langle r^{3} \rangle - \langle r^{1} \rangle, \langle r^{2} \rangle, \langle r^{3} \rangle - \langle r^{1} \rangle, \langle r^{2} \rangle, \langle r^{3} \rangle - \langle r^{1} \rangle, \langle r^{2} \rangle, \langle r^{3} \rangle - \langle r^{1} \rangle, \langle r^{2} \rangle, \langle r^{3} \rangle - \langle r^{1} \rangle, \langle r^{2} \rangle, \langle r^{3} \rangle - \langle r^{3} \rangle - \langle r^{2} \rangle, \langle r^{3} \rangle - \langle r^{3} \rangle -$

must be positive semidefinite, please derive the allowed region of energy values as we increase the matrix size. Provide analysis with regards to the convergence property for different angular momentum sector l.

Can you derive other recurssion relations to impose extra constraint? What are

the effect of these new constraint?