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## 1 Memorização

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**Algorithm 1:** ksMem( $W, P, c$ )

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**input** : Weight  $W$ , profit  $P$  and capacity  $c$   
**output:** The maximum capacity of knapsack  
1 HashTable  $H \leftarrow \emptyset$ ;  
2  $i \leftarrow |W|$ ;  
3 **return**  $memo(W, P, c, i, H)$ ;

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**Algorithm 2:** memo( $W, P, c, i, H$ )

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**input** : Weight  $W$ , profit  $P$ , capacity  $c$ , position  $i$ , HashTable  $H$   
**output:** The maximum knapsack recursive memorization  
1 **if**  $i = 0$  **or**  $c = 0$  **then**  
2 | **return** 0;  
3 **end**  
4 **if**  $(c, i) \in H$  **then**  
5 | **return**  $H[(c, i)]$ ;  
6 **else if**  $W[i - 1] > c$  **then**  
7 |  $H[(c, i)] \leftarrow memo(W, P, c, i - 1, H)$ ;  
8 | **return**  $H[(c, i)]$ ;  
9 **else**  
10 | **return**  $max(P[i - 1] + memo(W, P, c - W[i - 1], i - 1, H), memo(W, P, c, i - 1, H))$ ;  
11 **return**  $memo(W, P, c, i, H)$ ;

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## 2 Tabulação

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**Algorithm 3:** ksTab( $W, P, c$ )

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**input** : Weight  $W$ , profit  $P$  and capacity  $c$   
**output:** The last element in table  
1  $T \leftarrow [n \dots m]$ ;  
2  $i \leftarrow |W|$ ;  
3 **return**  $tab(W, P, c, i, T)$ ;

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**Algorithm 4:** tab( $W, P, c, p, T$ )

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**input** : Weight  $W$ , profit  $P$ , capacity  $c$ , position  $i$ , table  $T$   
**output:** The last element in table  
1 **for**  $n$  **in**  $range(i + 1)$  **do**  
2     **for**  $m$  **in**  $range(c + 1)$  **do**  
3         **if**  $n = 0$  **or**  $m = 0$  **then**  
4              $T[n][m] \leftarrow 0$ ;  
5         **else if**  $W[n - 1] \leq m$  **then**  
6              $T[n][m] \leftarrow \max(P[n - 1] + T[n - 1][m - W[n - 1]], T[n - 1][m])$ ;  
7         **else**  
8              $T[n][m] \leftarrow T[n - 1][m]$ ;  
9         **end**  
10 **end**  
11 **return**  $T[n][m]$ ;

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