

UNIVERSITY OF CALIFORNIA, RIVERSIDE

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DEPARTMENT OF ELECTRICAL AND COMPUTER ENGINEERING

EE 105 Lab 1 Solution

MATLAB as an Engineer's Problem Solving Tool

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1 Introduction

This introductory MATLAB laboratory course equips students with fundamental skills in scientific computing. Through hands-on exercises, students will gain proficiency in:

- Matrix algebra: Manipulating and analyzing numerical data represented as matrices
- Function creation: Defining and implementing custom functions for specific math equations
- Data visualization: Generating informative plots and graphs to interpret results
- Computational optimization: Employing techniques to improve the efficiency of numerical algorithms

By applying these acquired skills, students will develop a technical report that clearly communicates the purpose, methodology, and outcomes of the MatLab program. This report will showcase his or her understanding of MATLAB and its capabilities in solving scientific and engineering problems.

2 Matrices and Arrays

```
1 clea;  
2 clc;  
3 % Matrix Multiplication  
4 % Declare A Matrix (3 x 1 Matrix)  
5 A = [pi;sqrt(2);exp(pi)];  
6 % Declare B Matrix (1 x 3 Matrix)  
7 B = [1;5;7];  
8 % Convert A Matix from a column to a row vector and muliple with column
```

```
9 % vector b to get scalar value C
10 C = A.' * B;
```

Listing 1: Matrix Multiplication

3 Scripts

```
1 clear;
2 clc;
3 % Matrix Multiplication
4 % Declare A Matrix (3 x 1 Matrix)
5 A = [pi;sqrt(2);exp(pi)];
6 % Declare B Matrix (1 x 3 Matrix)
7 B = [1;5;7];
8 % Set D to zero to start the for loop
9 D = 0;
10 % Assumes both vector A and B are of the same length
11 for i = 1:length(A)
12     D = D + A(i)*B(i); % Add previous D value (sum of previous ith
13                         % elements) to the cuurent ith element multiplication
14 end
15 display(D);
```

Listing 2: Matrix Multiplication using a For Loop

The for loop and the matrix multiplication arrive at the same result. However, matrix multiplication requires less code and is less computationally intensive than the for loop.

4 More Advanced Scripts

4.1 $f(x_i)$ Function

```
1 % Input column vector x and an output column vector y where the i-th
   element of the output vector is  $y(i) = f(x(i))$ 
2 function [y] = fx(x)
3     y = cos(x) ./ (1 + exp(3 * x)); % Outcolumn is calculated use vector
   multiplication
4 end
```

Listing 3: $f(x_i)$ Function

4.2 Plot $f(x_i)$

```
1 function plot_export(N, title_text, filename) % Input N for the number
   spacings between the elements, title_text for the name of the plots,
   and the filename in order to export the plot. Note each plot must have
   a unique filename
2 x = linspace(0, 5, N + 1);
3 y = fx(x);
4 plot(x, y); % Creates the scatter plot
5 title(title_text, 'Interpreter', 'latex'); % Adds title to the plot. Adding
   $$ between the text, and adding 'Interpreter', 'latex' to the matlab
   function, creates text with LaTeX formatting
6 xlabel('$X$', 'Interpreter', 'latex'); % Adds xlabel to the plot. Adding $$
   between the text, and adding 'Interpreter', 'latex' to the matlab
   function, creates text with LaTeX formatting
```

```
7 ylabel('$f(x)$','Interpreter','latex'); % Adds ylabel to the plot. Adding
    $$ between the text, and adding 'Interpreter', 'latex' to the matlab
    function, creates text with LaTeX formatting
8 fig = gcf; % Obtains current graphic in matlab
9 exportgraphics(fig, append(filename, '.pdf'),'ContentType','vector'); %
    Exports plot as a vector pdf image. (Requires R2020a or later)
10 end
```

Listing 4: Plot Function for $f(x_i)$

```
1 clear;
2 clc;
3 % This code automatically calculates, labels, and plots
4 N = [200, 5, 10]; % Declare the N that will be ran
5 for i = N % iterate through given N for example i = 200
6     title_text = {['$f(x)$ vs $X$'] [append('$N = ', string(i), '$') ]}; %
        Create the the title for each i. Convert the integer to a string and
        add it to the title
7     filename = append('Fig/fx_', string(i)); % Add number to the filename
        to ensure each plot has a unique filename
8     plot_export(i, title_text, filename); % With i, title_text, and
        filename determined run and export documentex each plot. Vector pdf
        plots should be in the same folder as the code location ready to be
        inserted to a tex document
9 end
```

Listing 5: Code to run function for $f(x_i)$

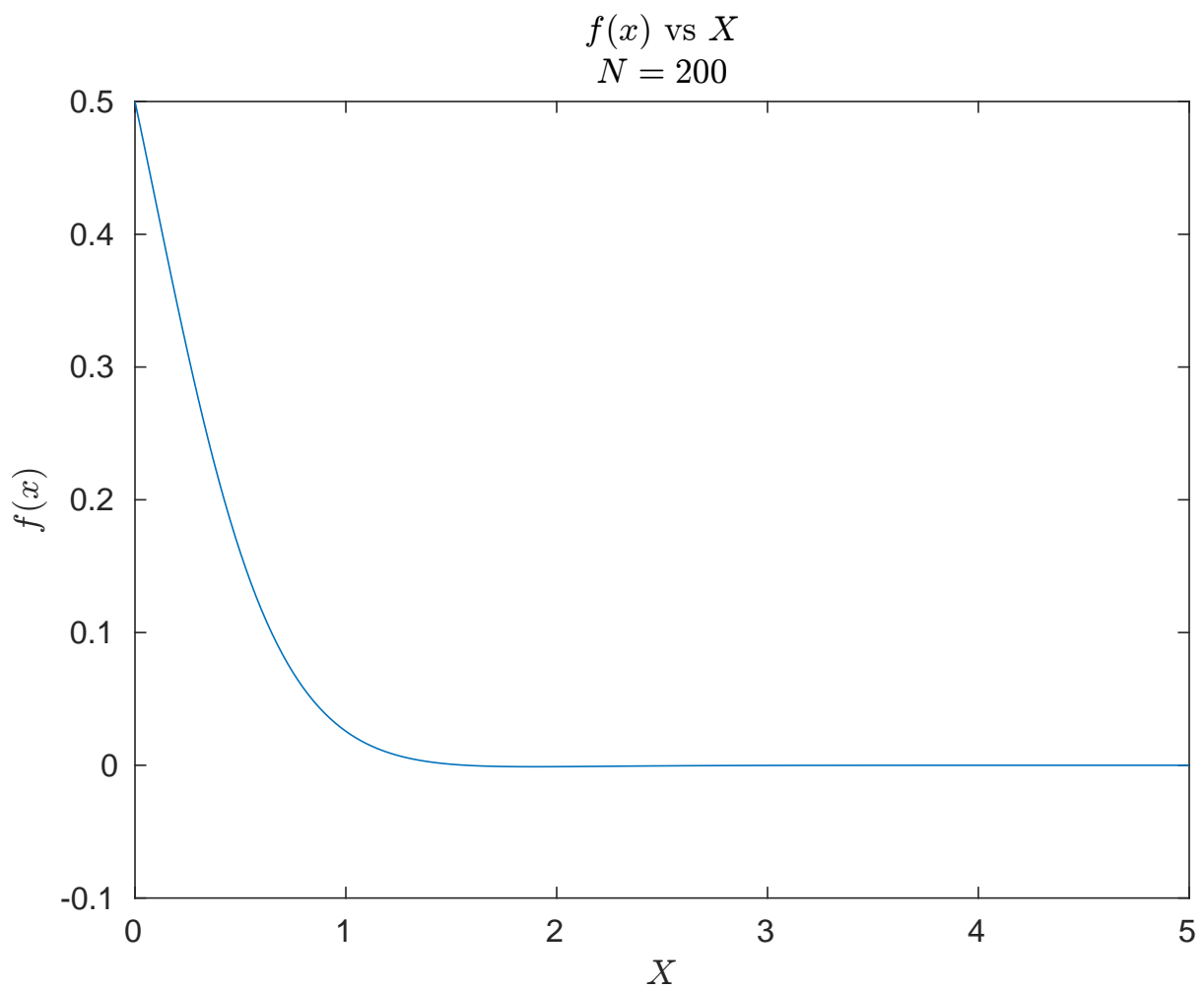


Figure 1: $f(x_i) = \frac{\cos(x_i)}{1+e^{3x_i}}$ for $N = 200$

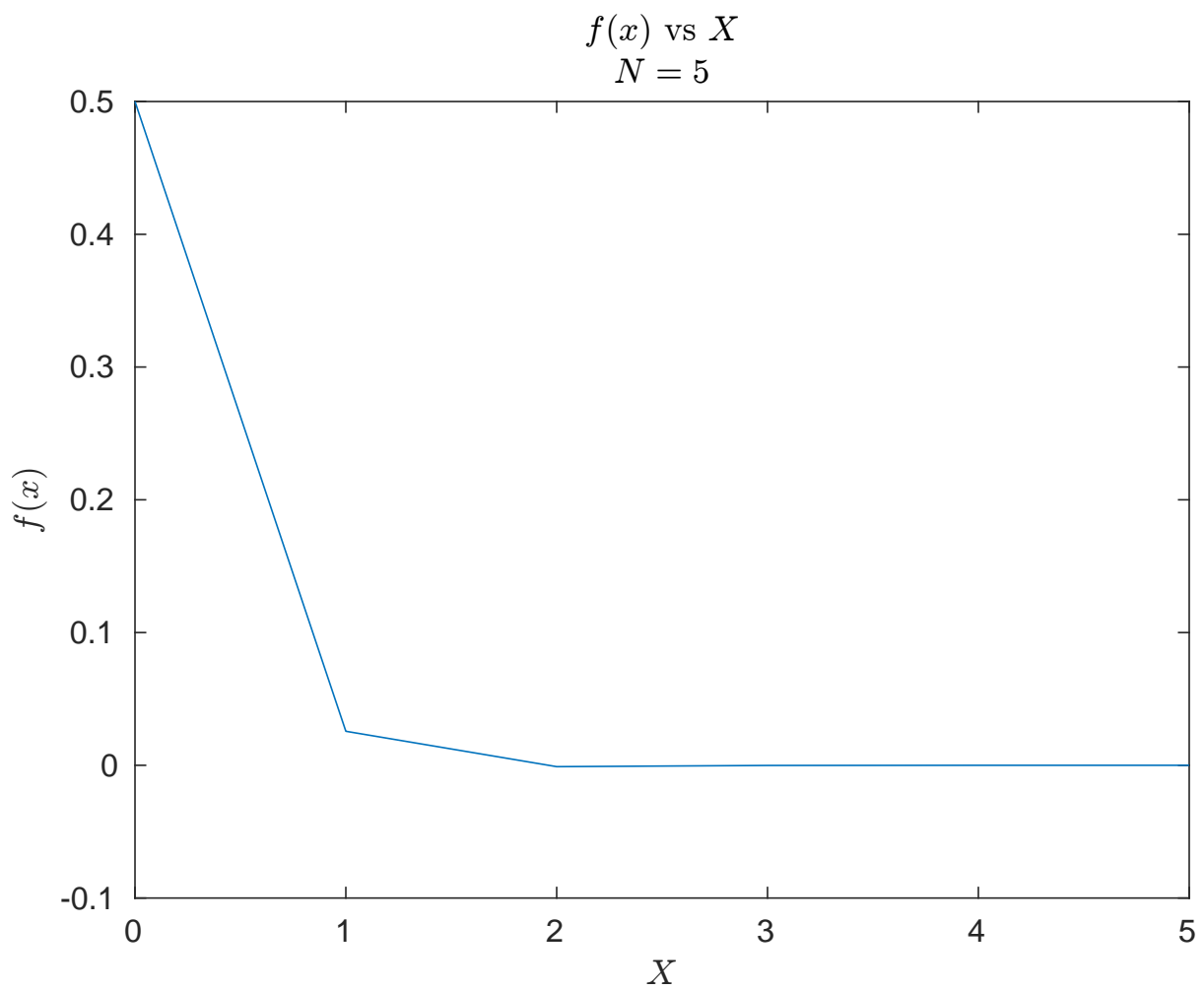


Figure 2: $f(x_i) = \frac{\cos(x_i)}{1+e^{3x_i}}$ for $N = 5$

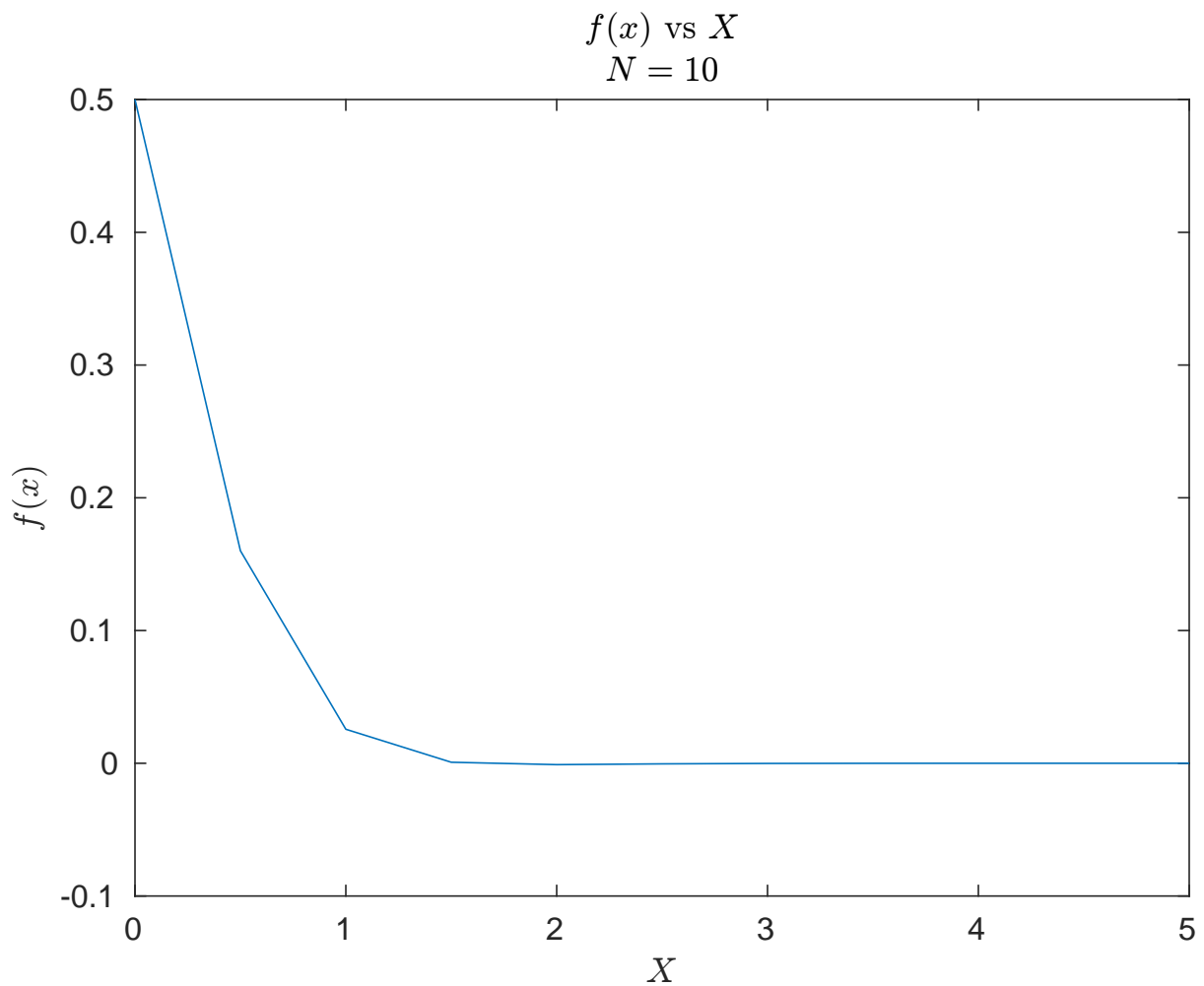


Figure 3: $f(x_i) = \frac{\cos(x_i)}{1+e^{3x_i}}$ for $N = 10$

Enhanced resolution of the domain (N) yields an increase in the overall plot resolution. This relationship is visually evident in the juxtaposed figures. Figure 1 exhibits a high domain resolution, resulting in a smooth and continuous plot devoid of discernible edges. Figures 2 and 3 conversely, demonstrate the effects of a lower domain resolution, characterized by visually apparent edges and a less refined plot appearance.

5 Area under the Curve

5.1 Standard Integration

```
1 clear;
2 clc;
3 % Find the integral using quad
4 Q = quad(@fx, 0, 5); % Function, lower bound, upper bound
```

Listing 6: $\int_0^5 \frac{\cos(x)}{1+e^{3x}} dx$

$$\int_0^5 \frac{\cos(x)}{1+e^{3x}} dx \approx 0.201$$

5.2 Riemann Integral Approximation Equations

5.2.1 Right Rectangular Approximation

```
1 clear;
2 clc;
3 N = 25; % 5 rectangles for every number
4 dx = 5/N; % divide by the range
5 x_bar = dx:dx:5; % x domain for bar plot. Instead of starting at 0, right
    rectangular approximation starts i + 1, 0 + dx
6 y_bar = fx(x_bar); % range for bar plot
7 x_line = 0:1/1000:5; % Add a high resolution domain
8 y_line = fx(x_line); % range for scatter plot
9 bar(x_bar-dx/2, y_bar, 1, 'green'); % Creates the bar plot
10 hold on; % Add a second line to the plot
11 plot(x_line, y_line, 'red'); % Creates the scatter plot
```

```
12 title('Right rectangular approximation  $Q_{\{2\}}$ ','Interpreter','latex'); %  
    Adds title to the plot. Adding $$ between the text, and adding '  
    Interpreter', 'latex' to the matlab function, creates text with LaTeX  
    formatting  
13 xlabel('$X$', 'Interpreter','latex'); % Adds xlabel to the plot. Adding $$  
    between the text, and adding 'Interpreter', 'latex' to the matlab  
    function, creates text with LaTeX formatting  
14 ylabel('$f(x)$', 'Interpreter','latex'); % Adds ylabel to the plot. Adding  
    $$ between the text, and adding 'Interpreter', 'latex' to the matlab  
    function, creates text with LaTeX formatting  
15 legend('$Q_{\{2\}}$', '$f(x)$', 'Interpreter','latex'); % Adds legend to the  
    plot. Adding $$ between the text, and adding 'Interpreter', 'latex' to  
    the matlab function, creates text with LaTeX formatting  
16 fig = gcf; % Obtains current graphic in matlab  
17 exportgraphics(fig, 'Fig/q2_bar_plot.pdf', 'ContentType','vector'); %  
    Exports plot as a vector pdf image. (Requires R2020a or later)
```

Listing 7: $\int_0^5 \frac{\cos(x)}{1+e^{3x}} dx$

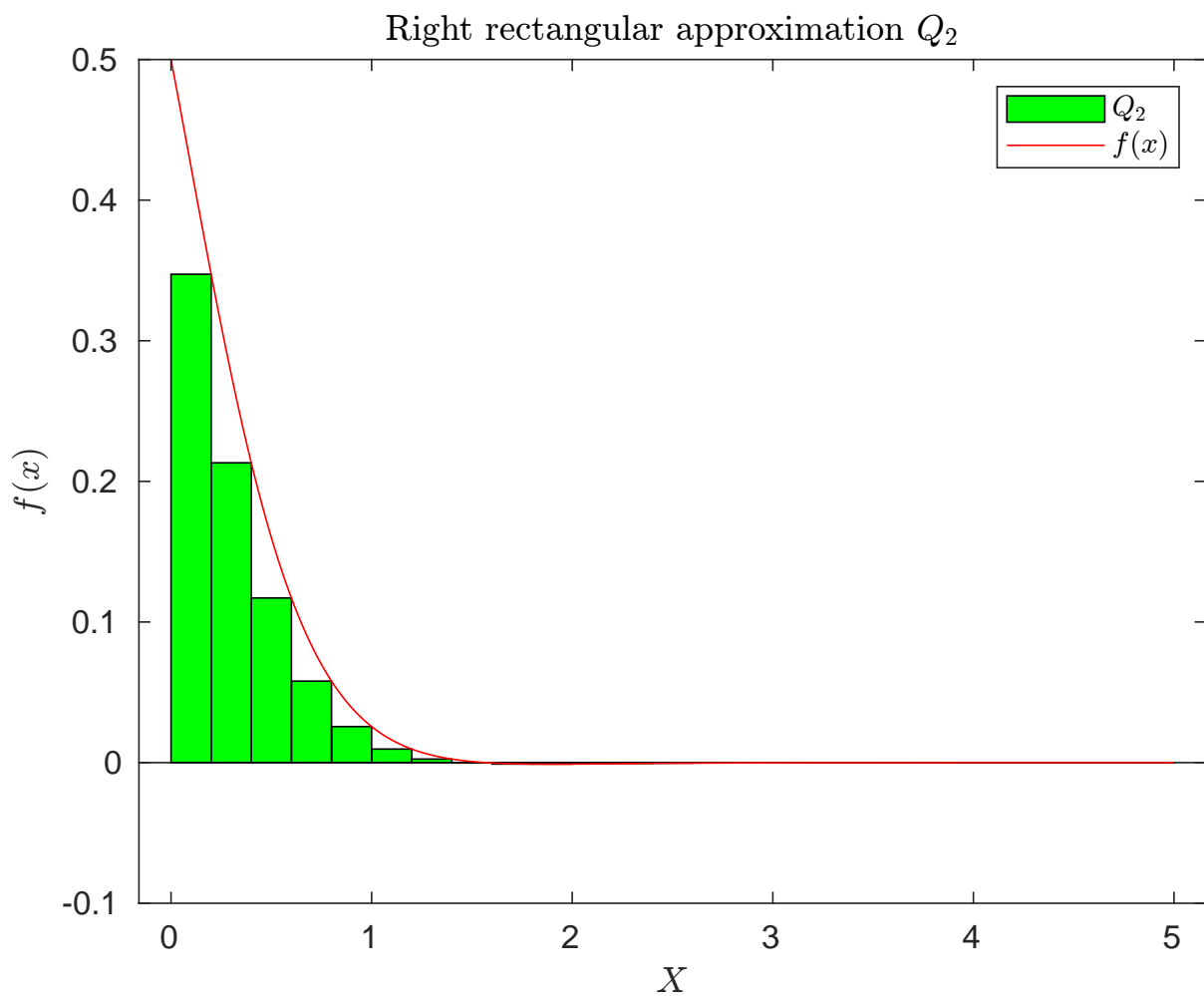


Figure 4: Right rectangular approximation for Q_2

5.2.2 Tradeoffs

Decreasing dx increases the resolution of the domain and the accuracy of the approximation. However, a higher resolution requires more computational power. This is akin to higher resolution images requiring more space.

5.2.3 Trapezoidal approximation derivation

Given that the area under the first line segment can be approximated:

$$f(x_0) dx_0 + 0.5(f(x_1) - f(x_0)) dx_0$$

$$f(x_0) dx_0 + \frac{f(x_1)}{2} dx_0 - \frac{f(x_0)}{2} dx_0$$

This means that the next area can be approximated:

$$f(x_1) dx_1 + \frac{f(x_2)}{2} dx_1 - \frac{f(x_1)}{2} dx_1$$

This can continue so forth until the N-th area can be approximated as:

$$f(x_{N-1}) dx_{N-1} + \frac{f(x_N)}{2} dx_{N-1} - \frac{f(x_{N-1})}{2} dx_{N-1}$$

Summing these terms up yields the equation Q_3

$$Q_3 = f(x_0) \frac{dx_0}{2} + \sum_{i=1}^{N-1} f(x_i) dx_i + f(x_N) \frac{dx_{N-1}}{2}$$

5.2.4 $Q_3 = \frac{Q_1}{Q_2}$

Given that:

$$Q_1 = \sum_{i=1}^{N-1} f(x_i) dx_i$$

$$Q_2 = \sum_{i=2}^N f(x_i) dx_{i-1}$$

$$Q_3 = f(x_1) \frac{dx_1}{2} + \sum_{i=2}^{N-1} f(x_i) dx_i + f(x_N) \frac{dx_{N-1}}{2}$$

All dx_i are equal to each other. Substituting in Q_1 and Q_2 in to Q_3 gives:

$$Q_3 = \frac{1}{2} \left(\sum_{i=1}^{N-1} f(x_i) dx_i + \sum_{i=2}^N f(x_i) dx_{i-1} \right)$$

$$Q_3 = \frac{1}{2} \left(f(x_1) dx_1 + \sum_{i=2}^{N-1} f(x_i) dx_i + \sum_{i=2}^{N-1} f(x_i) dx_i + f(x_N) dx_{N-1} \right)$$

$$Q_3 = f(x_1) \frac{dx_1}{2} + \sum_{i=2}^{N-1} f(x_i) dx_i + f(x_N) \frac{dx_{N-1}}{2}$$

5.2.5 Q_1 and Q vs N

```

1 function Q_1 = q1_sum(N)
2 dx = (5-0)/(N-1);
3 x = 0:dx:5;
4 y = fx(x);
5 A = [ones(N-1, 1); 0];
6 Q_1 = y*A*dx;
7 end

```

Listing 8: Q_1 Function

```

1 clear;
2 clc;
3 % N starts at 2 and ends at 200
4 N = 2:1:200;
5 % Domain for Q1
6 Q_1N = zeros(1, length(N));
7 % Populate each ith value with the furutre q1 N calculation
8 for i = N
9     Q_1N(i-1) = q1_sum(i);
10 end
11 % Create the domain for for the integral calcualtion

```

```
12 Q_N = ones(1, length(N));
13 % Find the integral using quad
14 Q = quad(@fx, 0, 5); % Function, lower bound, upper bound
15 % Convert the integral value from a scalar value to line of a constant
16 % value
17 Q_N = Q_N*Q;
18 % Create the domain for for error calculation
19 Q_1error = zeros(1, length(N));
20 % Subtract the summation from the actual value to calculate the error
21 Q_1error = ((Q_1N - Q_N) / Q) * 100;
22 % Declare the figure
23 figure;
24 % Declare the subplot
25 % First subplot
26 subplot(2, 1, 1);
27 % Plot the approximation
28 plot(N, Q_1N, 'blue');
29 hold on;
30 % Plot the integral line
31 plot(N, Q_N, 'red');
32 % Add tilte
33 title('$Q_{1}$ and $Q$ vs $N$', 'Interpreter', 'latex');
34 % Add x axis label
35 xlabel('$N$', 'Interpreter', 'latex');
36 % Add y axis label
37 ylabel('$Q_{1}$ and $Q$', 'Interpreter', 'latex');
```



```
38 % Add legend
39 legend('$Q_{1}$', '$Q$', 'Interpreter','latex' );
40 % Second subplot
41 subplot(2, 1, 2);
42 % Plot the error line in a seprate subplot
43 plot(N, Q_1error, 'blue');
44 title('$Q_{1}$ Error vs $N$', 'Interpreter','latex');
45 % Add x axis label
46 xlabel('$N$', 'Interpreter','latex');
47 % Add y axis label
48 ylabel('% Error', 'Interpreter','latex');
49 fig = gcf; % Obtains current graphic in matlab
50 exportgraphics(fig, 'Fig/q1_sum_error_plot.pdf', 'ContentType','vector'); %
    Exports plot as a vector pdf image. (Requires R2020a or later)
```

Listing 9: Plot Q_1 and Q vs N

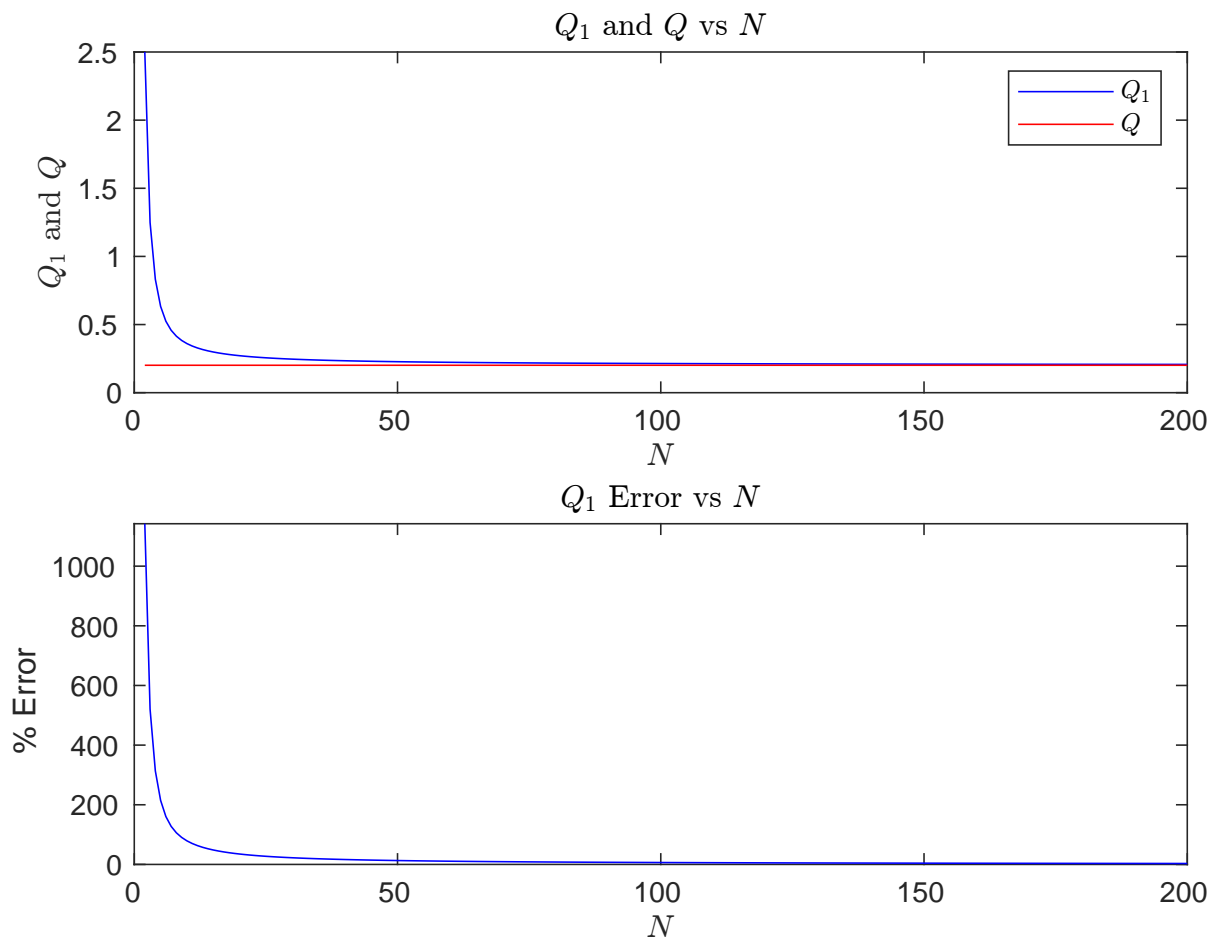


Figure 5: Q_1 and Q vs N and the % Error for Q_1

Q_1 in Figure 5 converges to Q at around $N = 75$

5.2.6 Q_2 and Q vs N

```

1 function Q_2 = q2_sum(N)
2 dx = (5-0)/(N);
3 x = dx:dx:5;
4 y = fx(x);
5 A = [ones(N-1, 1); 0];
6 Q_2 = y*A*dx;
7 end

```

Listing 10: Q_2 Function

```
1 clear;
2 clc;
3 % N starts at 2 and ends at 200
4 N = 2:1:200;
5 % Domain for Q1
6 Q_2N = zeros(1, length(N));
7 % Populate each ith value with the furutre q1 N calculation
8 for i = N
9     Q_2N(i-1) = q2_sum(i);
10 end
11 % Create the domain for for the integral calcaultion
12 Q_N = ones(1, length(N));
13 % Find the integral using quad
14 Q = quad(@fx, 0, 5); % Function, lower bound, upper bound
15 % Convert the integral value from a scalar value to line of a constant
16 % value
17 Q_N = Q_N*Q;
18 % Create the domain for for error calculation
19 Q_2error = zeros(1, length(N));
20 % Subtract the summation from the actual value to calculate the error
21 Q_2error = ((Q_2N - Q_N) / Q) * 100;
22 % Declare the figure
23 figure;
24 % Declare the subplot
```

```
25 % First subplot
26 subplot(2, 1, 1);
27 % Plot the approximation
28 plot(N, Q_2N, 'blue');
29 hold on;
30 % Plot the integral line
31 plot(N, Q_N, 'red');
32 % Add tilte
33 title('$Q_{2}$ and $Q$ vs $N$', 'Interpreter', 'latex');
34 % Add x axis label
35 xlabel('$N$', 'Interpreter', 'latex');
36 % Add y axis label
37 ylabel('$Q_{2}$ and $Q$', 'Interpreter', 'latex');
38 % Add legend
39 legend('$Q_{2}$', '$Q$', 'Interpreter', 'latex' );
40 % Second subplot
41 subplot(2, 1, 2);
42 % Plot the error line in a seprate subplot
43 plot(N, Q_2error, 'blue');
44 title('$Q_{2}$ Error vs $N$', 'Interpreter', 'latex');
45 % Add x axis label
46 xlabel('$N$', 'Interpreter', 'latex');
47 % Add y axis label
48 ylabel('% Error', 'Interpreter', 'latex');
49 fig = gcf; % Obtains current graphic in matlab
50 exportgraphics(fig, 'Fig/q2_sum_error_plot.pdf', 'ContentType', 'vector'); %
```

Exports plot as a vector pdf image. (Requires R2020a or later)

Listing 11: Plot Q_2 and Q vs N

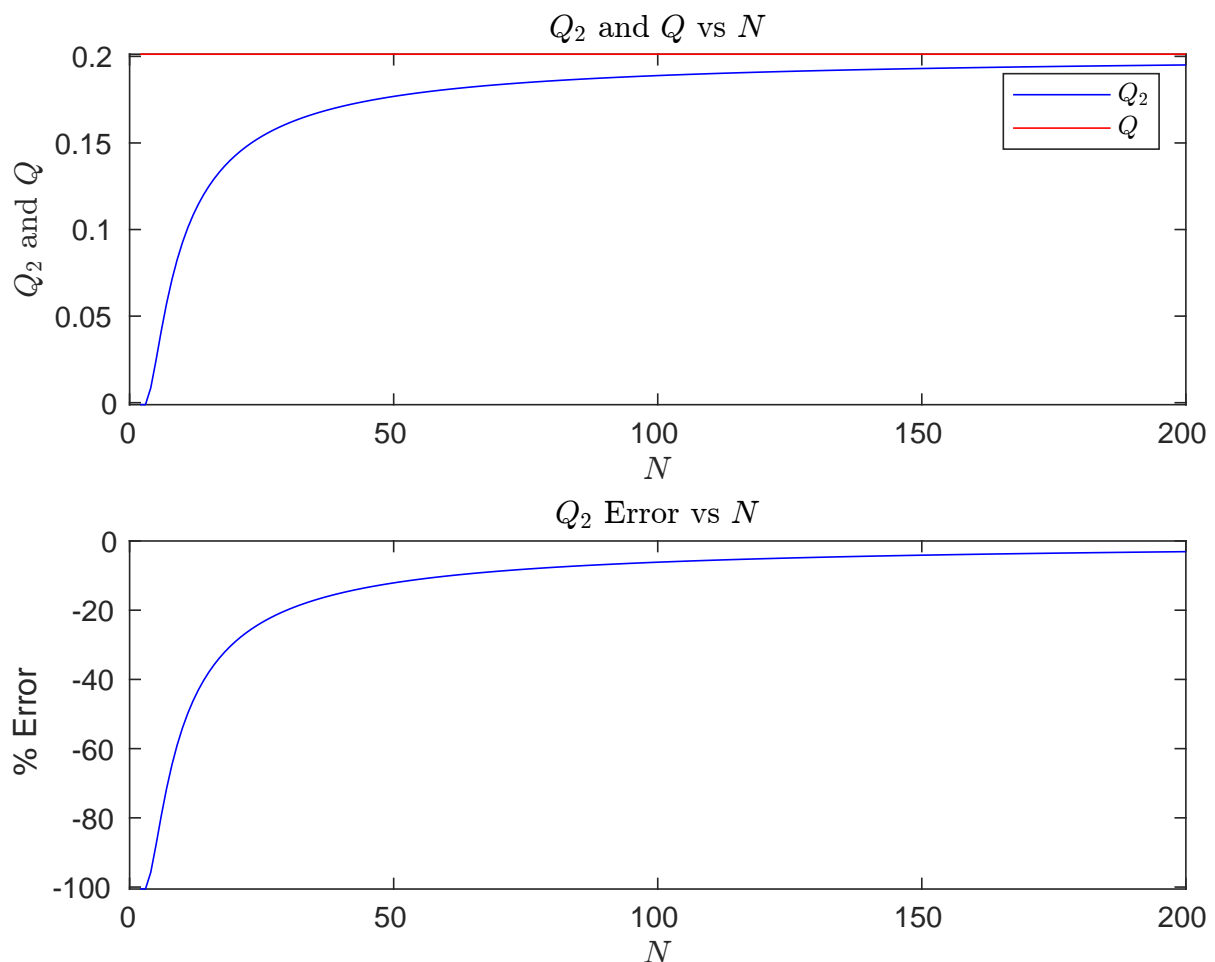


Figure 6: Q_2 and Q vs N and the % Error for Q_2

Q_2 in Figure 6 converges to Q at around $N = 100$

6 Conclusion

This laboratory exercise showcases MATLAB's versatility across diverse scientific and engineering domains. It notably highlights the fundamental concept of trade-offs in engineering.

Riemann summation serves as a poignant example, empowering students to grapple with the delicate balance between accuracy and computational efficiency—a fundamental skill for effective engineering design.