

CO₂ and Cost Impacts of a Microgrid with Electric Vehicle Charging Infrastructure: a Case Study in Southern California

Luis Fernando Enriquez-Contreras^{*†}, Matthew Barth^{*†}, Sadrul Ula[†]

^{*}*Department of Electrical and Computer Engineering*

University of California, Riverside

Riverside, United States of America

lenri001@ucr.edu, barth@ece.ucr.edu

[†]*College of Engineering, Center for Environmental Research & Technology*

University of California, Riverside

Riverside, United States of America

lenri001@ucr.edu, barth@ece.ucr.edu, sula@cert.ucr.edu

Abstract—As an important part of Intelligent Transportation Systems (ITS), this paper presents a case study at the University of California, Riverside (UCR) that evaluates the effectiveness of different transportation-based microgrid configurations in reducing both carbon dioxide (CO₂) emissions and electricity costs. CO₂ emissions are calculated using high-resolution California Independent System Operator (CAISO) CO₂ emissions data to accurately assess the environmental impact of each setup. Electric costs were also compared to determine the financial savings potential for the consumer. The results demonstrate that a peak-shaving transportation-microgrid strategy can effectively reduce CO₂ emissions in the range of 24% to 38% and costs from \$27,000 to \$29,000 per year, even when considering the additional demand from 12 vehicles charging daily at the building. However, careful consideration should be given to battery sizing, as peak-shaving has diminishing returns. Doubling the battery size may only provide an additional savings of \$2,000 per year with a negligible reduction in emissions. This highlights the importance of optimizing battery capacity to maximize cost-effectiveness and environmental impact.

Index Terms—microgrids, demand response, CO₂ emissions, modelica, EV charging

I. INTRODUCTION

A. Background

California is committed to reducing greenhouse gas emissions through various approaches, focused on the two largest: transportation and electricity generation. In California, electric vehicles (EVs) accounted for 25.4% of Q2 2023 vehicle sales [1], and the state aims to ban the sale of internal combustion engine vehicles by 2035 [2]. Concurrently, California is expanding the number of charging stations in the state, reaching over 13,844 Level 2 and 1,924 Level 3 stations [3] as of November 2023. EV technology has advanced, and new EVs can typically charge up to 80% in 20-60 minutes [4]. This is enabled by Level 3 charging, which can deliver up to 350 kilowatts

(kW), compared to Level 2 charging, which is limited to 19 kW [4]. While this reduced charging time has increased the attractiveness of EVs, it also poses a challenge for the owners of these chargers, as they can quickly generate a large amount of electricity demand. As California strives to increase the share of clean energy in its electricity mix, it also needs to reduce the CO₂ emissions from transportation by promoting electrification. This leads to two conundrums: how will California provide enough capacity for electrified transportation, and how clean is the grid to minimize the emissions associated with battery electric vehicles? One method to alleviate the pressure on the grid is to localize electricity production and EV charging by using microgrids. A microgrid is defined by the Department of Energy (DOE) and the Institute of Electrical and Electronics Engineers (IEEE) as: “a group of interconnected loads and distributed energy resources within clearly defined electrical boundaries that acts as a single controllable entity with respect to the grid. A microgrid can connect and disconnect from the grid to enable it to operate in both grid-connected or island-mode.” [5] [6]. As microgrids and EV chargers become more widespread, it is essential to study the economic and environmental impacts of EV charging, especially fast charging, and how microgrids can play an important role. EV charging differs from typical building loads, as it can rapidly ramp up to high levels at random intervals based on human behavior i.e. when they plug in. An outlier event where multiple people charge at the same time can cause a significant peak in the load.

This research holds significant implications for the advancement of intelligent transportation systems, as it aims to address the economic needs of EV charging infrastructure owners and determine the optimal configuration that benefits both EV owners and the environment by

minimizing greenhouse gas emissions. This paper delves into the impacts of transportation-microgrids equipped with Level 2 and Level 3 charging on the behavior of microgrids, associated electricity costs, and CO₂ emissions within the context of southern California. The simulations are conducted using OpenModelica, a dynamic modeling and simulation environment. This study distinguishes itself from previous research in many ways, including employing a higher time resolution for calculating CO₂ emissions, capturing data every 15 minutes.

B. Literature Review

Transportation-microgrids have gained significant traction in recent years due to the growing demand for transportation electrification. These microgrids, which combine distributed energy resources (DERs) and energy storage systems with electric vehicle (EV) charging infrastructure, offer a promising solution for integrating EVs into the power grid while minimizing environmental impact. Previous studies have investigated the economic viability of transportation-microgrids, primarily focusing on energy charges associated with EV charging. However, demand charges, which reflect the peak demand imposed on the grid, need to be addressed. This omission is particularly crucial for fast charging stations, which draw significant power during peak periods. A more comprehensive approach to economic analysis should consider both energy and demand charges, providing a more accurate assessment of the overall cost of operating a transportation-microgrid. Research has addressed the impact of EV charging demand on transportation-microgrids, often focusing on low-demand Level 2 charging. However, the increasing popularity of high-demand Level 3 charging requires a more nuanced understanding of its implications. Studies should incorporate a mix of Level 2 and Level 3 charging scenarios to accurately assess the impact of EV charging demand on microgrid operation and economics. Assessing the greenhouse gas (GHG) emissions associated with transportation-microgrids is often simplified by using average CO₂ emissions from an area's electricity production. This approach fails to capture the variations in CO₂ emissions throughout the day, which can significantly affect the environmental impact of EV charging. More sophisticated GHG emission calculations should consider the time-varying nature of CO₂ emissions, providing a more accurate representation of the environmental impact of transportation-microgrids.

Several studies have investigated the performance of electric vehicle charging stations (EVCS) under varying conditions. Reference [7], is developing a demand and stochastic model for EVCS, followed by a techno-economic assessment and an environmental impact analysis. They concluded that the optimal configuration and investment costs of EVCS with solar integration are highly dependent on feed-in tariffs and solar irradiation levels. However, their CO₂ emission calculations were based on annual averages and did not account for intraday variations. They only

considered energy charges, omitting demand charges in their economic analysis. Reference [8] proposed a control algorithm for EVCS that can minimize charging time, costs, or maximize renewable energy use depending on the scenario. They modeled charging loads using a uniform distribution during peak demand periods, assuming only Level 2 charging at 3.3 kW and excluding Level 3 charging. Reference [9] proposed an EV charging model that shifts charging events from peak demand periods to off-peak times. They found that their current method had limited impact on peak load shaving and that solar production surplus may only sometimes be diverted to EVs due to their low availability at those times. Their dataset was limited to one week and involved four EVs in a system with ten buildings. Reference [10] ran multiple scenarios with different self-consumption rates, comparing scenarios first and then calculating emissions for each. Their CO₂ emission calculations were based on whole-life-cycle CO₂ emissions without high time resolution. Reference [11] employed the Non-dominated Sorting Genetic Algorithm-II (NSGA-II) to analyze four different responses with EV penetration rates of 0%, 10%, 20%, and 30%, using a Monte Carlo load profile. They achieved remarkable results but did not elaborate on their CO₂ calculations or provide a detailed analysis of the specific impacts of Level 2 versus Level 3 charging. Reference [12] analyzed IEEE 9 and 14 bus systems, forecasting EV loads one day ahead. They utilized multiple microgrids to balance out EV charging within the system, employing a multi-objective energy management approach for optimizing microgrid operation. The forecasted EV loads did not have sudden high-demand events nor level 3 charging, which makes the forecasting model difficult to implement.

C. Peak Shaving Strategy

Peak shaving is a widely adopted strategy for mitigating high-demand charges. As demand charges are solely determined by the maximum power consumption over an entire billing period, it is assumed that consumers seek to minimize these charges to the greatest extent feasible. Energy charges, on the other hand, represent the cost associated with the total energy consumed during the billing period and are calculated as a summation rather than a maximum value. The proposed algorithm is designed to optimize cost savings managing demand and energy charges using a typical microgrid. During peak-shaving periods, the algorithm assesses the imported power, evaluates the availability of sufficient energy, and determines whether batteries can mitigate a portion or the entirety of the imported power demand.

D. CO₂ Emissions

Our microgrid's solar production, shown in Fig. 1, greatly overlaps with the local solar energy production within the larger grid. With a Battery Energy Storage System (BESS), we can utilize renewable energy during peak times and at

night. In this scenario, the control algorithm is optimized to minimize cost for the consumer, however we want to see how low price EV charging aligns with actual CO₂ emission outputs. While the microgrid does not produce any direct CO₂ emissions, there are CO₂ emissions attributed to the microgrid when it pull power from main power grid. The simulation uses emission output calculations from California Independent System Operator (CAISO) for each time interval as a sum of all the powerplant CO₂ emissions (imports, natural gas, biogas, biomass, geothermal, coal) $\frac{\text{mTON}_{\text{CO}_2}}{\text{hour}}$. The CO₂ emissions output is divided by the amount of power produced (solar, wind, geothermal, biomass, biogas, small hydro, grid batteries, large hydro, imports, nuclear, coal) in MW, which gives us an emissions rate of $\frac{\text{mTON}_{\text{CO}_2}}{\text{W}}$. This is multiplied with 15 minute data kW, and a multiplier. The multiplier of $\frac{1}{4000}$ converts kW into W and to address for the four 15 minute periods in an hour. The CAISO data uses 2019 data for CO₂ instead of 2022 in order to have pre-COVID-19 CO₂ emission levels. This gives us an estimate of the amount of CO₂ emissions in $\text{mTON}_{\text{CO}_2}$ for every 15 minutes that is summed together to give us the total for the entire period. This method is similar to the one used in [13]. When the grid does not pull power from the grid or is sending power, the CO₂ emissions are assumed to be zero since we are using renewable solar energy.

II. SIMULATION IN OPENMODELICA

OpenModelica is an open-source implementation of the Modelica programming language [14]. Modelica is a programming language that is designed for dynamic systems simulation [15]. OMEdit is the GUI interface for OpenModelica, allowing the user to draw a system for simulation [16]. The microgrid scenarios are simulated in OpenModelica using the Modelica buildings library. Lawrence Berkeley National Laboratory created the Modelica buildings library for building and district energy and control systems [17]. Further, its capability for energy storage systems, bi-directional inverter, solar, and HVAC modeling make it ideal for a microgrid simulation setup. This allows us to create scenarios that do not currently exist in our microgrid, shown in Fig. 1, like running a month with solar with the same load, or running the BESS control algorithm for different electric rates. The power circuits are three-phase balanced circuits. The simulation of our case study microgrid is the grid-connected to the building netload. The model's net load is broken down into solar power, HVAC loads, regular building loads, electric vehicle chargers, and the BESS as shown in Fig.1.

A. Validation

To ensure that our model accurately portrays our real world system, a year of real world data was used to validate the P_G output. P_G is defined as the power the microgrid sends or consumes from the grid. The actual data was

compared to the simulated with a correlation coefficient of ≈ 0.965087 as shown in Figure 2.

B. Solar Generation and Building Loads

The solar power in our model is based on the historical solar data from a 100 kW photovoltaic (PV) array. The HVAC loads and the regular building loads are represented separately in this model but utilize the same method; they both use historical real world power data to represent their load in the system.

C. EV Charger Loads

Our model also considers transportation loads in the form of EV chargers. The EV chargers are represented as two models: Level 2 EV chargers, and Level 3 EV chargers. While other building loads follow a typical daily and yearly pattern, EV loads are different since they stochastically switch on and off. Our case study microgrid has four Level 2 chargers, so it can have four “steps” of 7.2 kW each, while there is only one “step” of 50 kW with the Level 3 chargers. To generate EV loads in our model, we use a Poisson random distribution to generate the number of charge sessions in a day, the arrival times, and charging durations based on real world data recorded over a year. Historical data from the Level-2 charger was utilized to determine the parameters for the Poisson random generator, consistent with the typical daily charge probability density function (PDF) depicted in Fig. 3. Additionally, the power output of the Level-2 chargers is illustrated in Fig. 4. Analysis of the historical data revealed three distinct peak charging periods occurring at 7:00, 9:00 and 13:00 respectively, with average number vehicle arrivals 6, 2, and 1 during each peak respectively. A mean charging time of 90 minutes was assumed. Leveraging these parameters, the EV random arrivals function generates random arrival times and durations. The function employs the NumPy library [18] [?] in Python to create a Poisson random distribution with means centered around the peak times. To ensure consistency across different scenarios and prevent any outlier event from the EV charging load disproportionately influencing higher demand events, a random data seed value of 10 was employed to ensure every charging event is the same. The random arrivals for Level 3 charging are modeled with three peak times at 7:00, 9:00, and 13:00, an average number of vehicle arrivals of 2, 1, and 1 respectively. Level 3 charging has a mean charging time of 30 minutes.

D. BESS and Peak Shaving

The BESS is modeled as a battery connected to a bidirectional inverter. The BESS output is controlled by generated data from the control algorithm. The BESS output is computed in real-time by using a peak shaving algorithm utilizing BESS SOC and the grid meter output. The algorithm charges the battery when excess solar power is exported to the grid, and when the battery needs to be charged. Our algorithm reads the net load from the grid

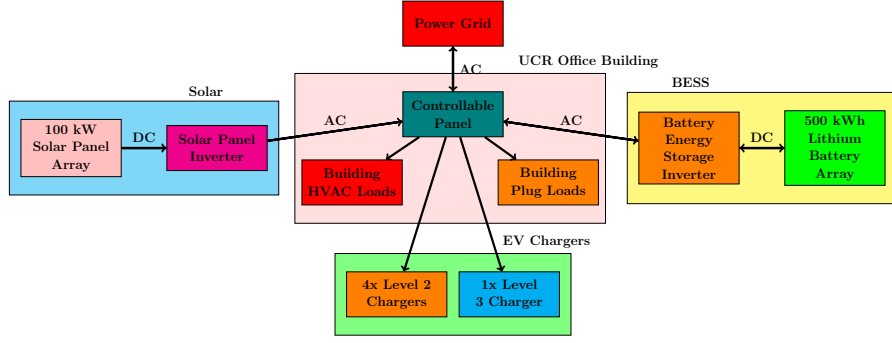


Fig. 1: Microgrid Architecture of our Case Study Example BESS: Battery Energy Storage System

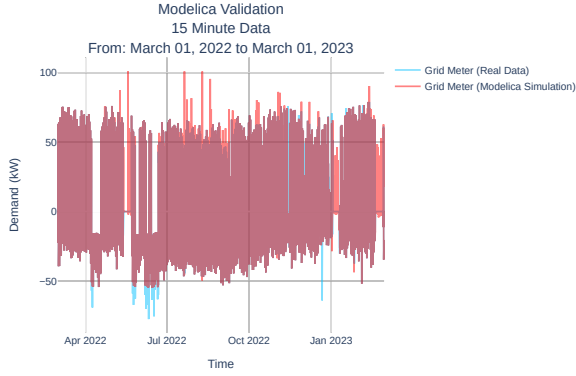


Fig. 2: Whole Year Validation of the Microgrid Architecture in OpenModelica. The bright blue and red is the real data and simulated data respectively. The dark red is the overlap between real and simulated data.

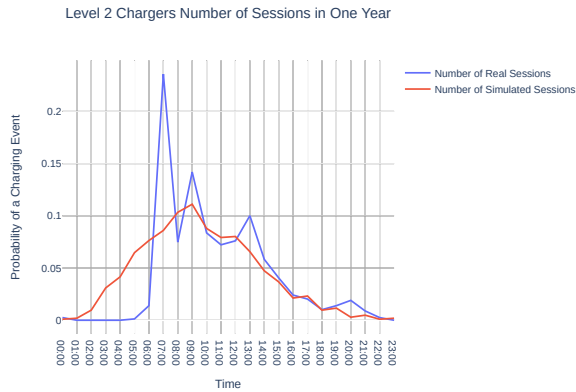


Fig. 3: Validation of the Level 2 EV Charger Stochastic Process that Compares the Probability Density Function of Actual Charging Data to the Poisson Process

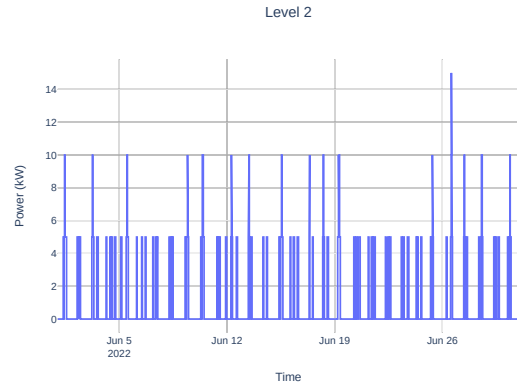


Fig. 4: Example Level 2 Chargers Simulated Power Draw in OpenModelica

model and determines the amount of CO₂ being produced during that interval. Algorithm 1 shows the peak shaving algorithm sufficient for a flat rate demand response.

Algorithm 1: Peak Shaving

```

1 net_load, SOC ← Modelica Data Output if
  condition then
2   | net_load ≤ -15 kW and SOC > 20 % and net_load
   |   ≥ -100 kW BESS_inverter = -net_load - 15 kW
3 else if net_load ≤ -100 kW and SOC > 20 % then
4   | BESS_inverter = -100 kW
5 else if net_load ≥ 0 kW and SOC < 90 % and
   |   net_load ≤ 100 kW then
6   | BESS_inverter = -net_load
7 else if net_load ≥ 0 kW and SOC < 90 % then
8   | BESS_inverter = 100 kW
9 else
10  | BESS_inverter = 0

```

III. RESULTS

The charging setup is modified in OpenModelica for different layouts and scenarios. The scenarios are described

in Table I.

Scenario 1 represents the baseline case where only the building loads, such as the air conditioners, appliances, and lights, are connected to the grid. Scenario 2 represents the case where a building installs four Level 2 and one Level 3 charger. Scenario 3 is the first case that utilizes a microgrid, which includes 100 kW of solar power and 500 kWh of battery storage. This scenario demonstrates the peak-shaving capabilities of a microgrid without EV chargers, creating a high demand. This can be thought of as the baseline case for the BESS microgrid. Scenarios 4, 5, 6, 7, and 8 represent a transportation-microgrid with EV chargers; the BESS capacity is varied to different sizes to show which BESS size offers the lowest cost and the lowest CO₂ emissions.

Each scenario is run independently of the other, and the power outputs of the different components in the simulation are shown in Fig. 5. Scenarios 1 and 2 are constantly negative, meaning they pull power from the grid. Scenarios 3-8, on the other hand, are mostly positive or limited to -15 kW, meaning it either exports power to the grid or consumes only 15 kW. The reason for the 15-kW floor is that with the utility company's electric rate, a minimum of 15 kW is charged for the demand, meaning that a zero-demand microgrid will not make a financial difference for the user.

While the peak shaving algorithm should limit the amount of power consumed at any time to 15 kW, there are still times when the BESS cannot supply the building with power. This happens when the BESS is too depleted, and there is little to no solar power to replenish it, as shown in Figure 8. The two main reasons for these events are multiple cloudy days and electrical faults. The larger the battery capacity, the depletion of the battery occurs less frequently, and the microgrid can better weather events of low solar output. Most of the low solar power events occur, during the winter months.

Figures 5, 6, and 7 show box plots of the power output. Fig. 5 is for the entire year, while Figures 6 and 7 show selected months. The box plots show that all three figures' mean and 75th percentile are almost identical at 15 kW. This implies that peak shaving is functioning correctly most of the time. However, the outliers show when the BESS fails to keep the power pulled from the grid at 15 kW. Fig. 5 shows that Scenarios 4 - 8 have almost identical values. However, this is because the figure is maximum for the entire year. Only a few of the billing months have a solar outage long enough to cause a BESS depletion that causes a demand peak almost as large as the no BESS scenario (Scenario 2). Just one outlier will change the demand charge for the entire billing month. In some months, the maximum demand peak of Scenario 2 and 3 are similar since they have the same load, but for most of the months, it is reduced significantly, reflected in the reduced demand charges of the building.

The average daily CO₂ emissions from each scenario are

TABLE I: Simulated Scenarios of the example UCR Microgrid using Different Layouts and Electric Pricing Structures

Scenario	
1	Standard Building with no EV Chargers
2	Standard Building with Level 2 and Level 3 Charging
3	Microgrid Building with 100 kW Solar, 500 kWh BESS, No EV Charging
4	Microgrid Building with 100 kW Solar, 100 kWh BESS, Level 2, and Level 3 Charging
5	Microgrid Building with 100 kW Solar, 250 kWh BESS, Level 2, and Level 3 Charging
6	Microgrid Building with 100 kW Solar, 500 kWh BESS, Level 2, and Level 3 Charging
7	Microgrid Building with 100 kW Solar, 1 MWh BESS, Level 2, and Level 3 Charging
8	Microgrid Building with 100 kW Solar, 1 MWh BESS, Level 2, and Level 3 Charging

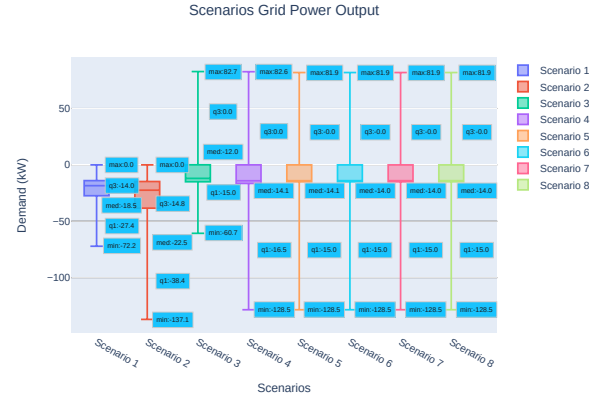


Fig. 5: Power measured from the meter for the entire year

shown in Fig. 10. Scenario 2, with its increased charging events, shows about a 26% increase of CO₂ emissions compared to Scenario 1. The CO₂ emissions from the transportation-microgrids are lower than a conventional building, even with the additional load from the EV chargers. While adding 17% to 45% more CO₂ emissions compared to a microgrid without EV charging infrastructure (Scenario 3), those CO₂ emissions are easily offset by charging an average of 12 EVs per day. Table II shows each scenario's emissions and electric price amounts.

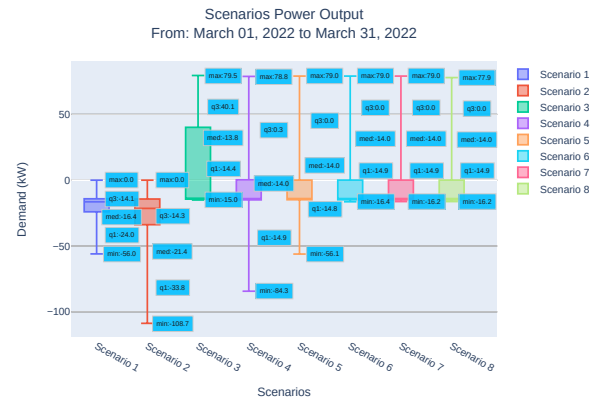


Fig. 6: Power measured from the meter for the month of March

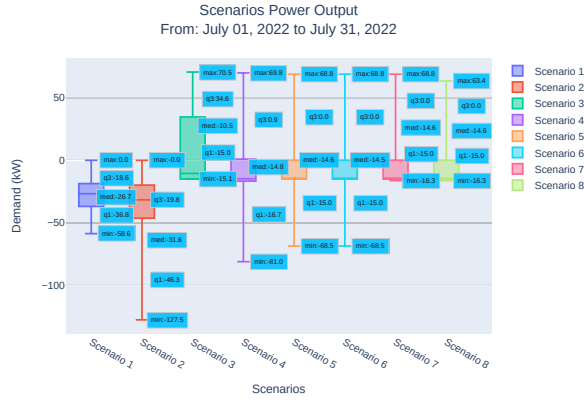


Fig. 7: Power measured from the meter for the month of July

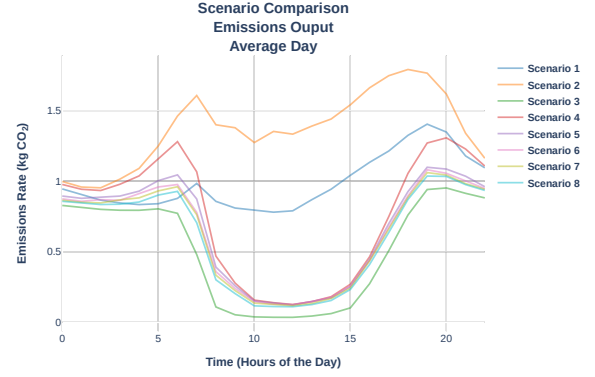


Fig. 10: CO₂ Emissions Outputs Averages During Times of Day, using a microgrid setup

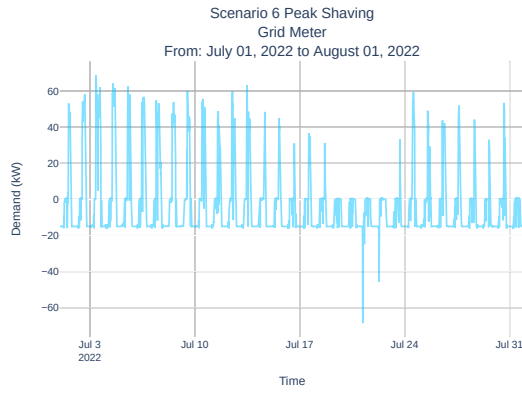


Fig. 8: Peak Shaving Failure after Battery Depletion (500 kWh)

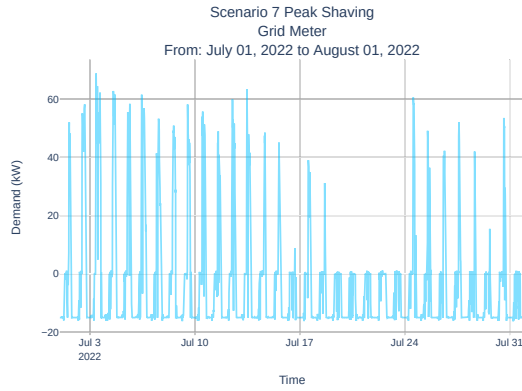


Fig. 9: Peak Shaving Success with 1 MWh battery

TABLE II: Microgrid Utility Prices and CO₂ Emissions Output under Different Pricing Scenarios and Pricing Structures

Scenario	Demand Charges (\$)	Energy Charges (\$)	Total Cost (\$)	CO ₂ Emissions (mTons)
1	7695	22736	30431	34
2	17343	32289	49632	47
3	3904	0	3904	18
4	14341	8209	22550	26
5	13193	8937	22130	23
6	12909	9239	22148	22
7	10835	9418	20253	22
8	9811	9577	19388	21

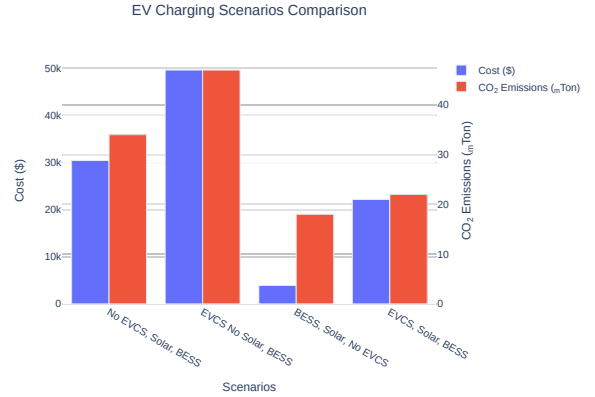


Fig. 11: EV Charging Scenarios Comparison

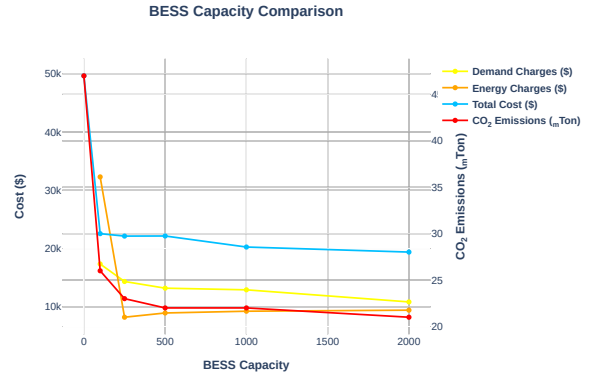


Fig. 12: Cost and CO₂ Emissions for Different Battery Capacities

IV. CONCLUSIONS

Transportation-microgrids have emerged as a compelling solution for mitigating the electrical costs and emission levels associated with EV charging infrastructure. A comprehensive analysis of various scenarios reveals transportation-microgrids' significant economic and environmental benefits compared to conventional systems, as depicted in Fig. 11. For the transportation-microgrid systems, the estimated annual savings range from \$8,000 to \$10,000, even with the additional demand from EV chargers. Compared to a building with EV chargers but without a microgrid, the annual savings are even more substantial, reaching \$27,000 to \$29,000. This implies that transportation-microgrids can amplify the savings from switching from a conventional building by a factor of three. Furthermore, transportation-microgrids can reduce CO₂ emissions by 24% to 38% compared to a conventional building and by 45% to 55% compared to a scenario where the building also has EV chargers. Consequently, users are strongly incentivized to adopt transportation-microgrids rather than simply installing EV chargers at their buildings.

It is important to note that, increasing the battery capacity does not necessarily guarantee improved microgrid performance. Fig. 12 illustrates the different battery capacities evaluated in this microgrid setup. The largest capacity is 20 times the smallest battery, but the corresponding cost and CO₂ reductions are not 20-fold. Addressing the most challenging solar power outages requires a significant increase in battery capacity, while providing only marginal CO₂ and cost savings in return. As shown in the billing month of July in Figures 8 and 9, doubling the battery capacity can eliminate some peaks from a couple of cloudy days. However, the additional savings of \$2,000 per year do not justify the cost of the extra capacity. Lastly, a 15 kW demand price floor has an adverse impact on CO₂ emissions, as it discourages users from maintaining a zero net load in a peak shaving setup.

In conclusion, transportation-microgrids represent a promising solution for reducing the environmental and economic impact of EV charging infrastructure. However, careful consideration of battery capacity and demand price structures is crucial to optimize the microgrid's performance and cost-effectiveness.

V. FUTURE WORK

Future research will explore different, more advanced control strategies to optimize the electric costs and CO₂ emissions of the transportation-microgrid. These strategies will include throttling charging during high peak times, maximizing the use of the clean energy produced by the solar panels, and minimizing the power drawn from the grid during high CO₂ times. The effect of the new net energy metering policy in California on the value of the BESS system will also be assessed.

REFERENCES

- [1] [Online]. Available: <https://www.gov.ca.gov/2023/08/02/milestone-1-in-4-new-cars-sold-in-california-were-zero-emission/>
- [2] [Online]. Available: <https://www.gov.ca.gov/2020/09/23/governor-newsom-announces-california-will-phase-out-gasoline/>
- [3] [Online]. Available: https://afdc.energy.gov/stations/#/analyze?country=US&fuel=ELEC&ev_levels=2®ion=US-CA
- [4] [Online]. Available: <https://www.transportation.gov/rural/ev/toolkit/ev-basics/charging-speeds>
- [5] D. T. Ton and M. A. Smith, "The us department of energy's microgrid initiative," *The Electricity Journal*, vol. 25, no. 8, pp. 84–94, 2012.
- [6] K. R. Padiyar and A. M. Kulkarni, *Microgrids: Operation and Control*, 2019, pp. 415–453.
- [7] N. Himabindu, S. Hampannavar, B. Deepa, and M. Swapna, "Analysis of microgrid integrated photovoltaic (pv) powered electric vehicle charging stations (evcs) under different solar irradiation conditions in india: A way towards sustainable development and growth," *Energy reports*, vol. 7, pp. 8534–8547, 2021.
- [8] S.-G. Yoon and S.-G. Kang, "Economic microgrid planning algorithm with electric vehicle charging demands," *Energies*, vol. 10, no. 10, p. 1487, 2017.
- [9] A. Purvins, C.-F. Covrig, and G. Lempidis, "Electric vehicle charging system model for accurate electricity system planning," *IET Generation, Transmission & Distribution*, vol. 12, no. 17, pp. 4053–4059, 2018.
- [10] M. Khemir, M. Rojas, R. Popova, T. Feizi, J. F. Heinekamp, and K. Strunz, "Real-world application of sustainable mobility in urban microgrids," *IEEE Transactions on Industry Applications*, vol. 58, no. 2, pp. 1396–1405, 2022.
- [11] Y. Huang, H. Masrur, M. S. H. Lipu, H. O. R. Howlader, M. M. Gamil, A. Nakadomari, P. Mandal, and T. Senjyu, "Multi-objective optimization of campus microgrid system considering electric vehicle charging load integrated to power grid," *Sustainable Cities and Society*, vol. 98, p. 104778, 2023.
- [12] B. Tan and H. Chen, "Multi-objective energy management of multiple microgrids under random electric vehicle charging," *Energy*, vol. 208, p. 118360, 2020.
- [13] J. Garrido, M. J. Barth, L. Enriquez-Contreras, A. J. Hasan, M. Todd, S. Ula, and J. Yusuf, "Dynamic data-driven carbon-based electric vehicle charging pricing strategy using machine learning," in *2021 IEEE International Intelligent Transportation Systems Conference (ITSC)*. IEEE, 2021, pp. 1670–1675.
- [14] [Online]. Available: <https://openmodelica.org/>
- [15] [Online]. Available: <https://modelica.org/modelicalanguage.html>
- [16] [Online]. Available: <https://openmodelica.org/doc/OpenModelicaUsersGuide/latest/omedit.html>
- [17] [Online]. Available: <https://simulationresearch.lbl.gov/modelica/>
- [18] [Online]. Available: <https://numpy.org/>