PA: Peano Arithmetic

Peano arithmetic is a [formal axiomatic system]. Infinitely many [axioms] can be built by replacing φ, ψ, θ with formulas in the language of PA. In PA a theorem is a formula that is either an [axiom] or can be derived from finitely many axioms with finitely many rules of inference.

![Logical Axiom Schemes](000J)

![Equality Axioms](000K)

![Non-logical Axioms](000L)

Inference Scheme

- 1. from φ and $\varphi \to \psi$, infer ψ
- 2. from φ , infer $(\forall x)\varphi$
- 3. from φ , infer $\tilde{\varphi}$

 $\tilde{\varphi}$ can be any formula obtained by renaming variables in φ .