PhysRevD.67.084023 equation (19)

```
from shared import *
    import cdblib
    jsonfile = 'hamiltonian.json'
     cdblib.create (jsonfile)
     # ------
     # Hamiltonian constraint
    Ham := R + K_{a b} g^{a b} K_{c d} g^{c d} - K_{a b} K_{c d} g^{a c} g^{b d}. # cdb (Ham. 101, Ham)
11
    defK2ABarD := K_{i j} \rightarrow \exp(4\phi) ABar_{i j} + (1/3) g_{i j} trK.
12
    defG2GBarD := g_{a b} \rightarrow \exp(4\pi) gBar_{a b}.
13
    defG2GBarU := g^{a b} \rightarrow \exp(-4\pi) gBar^{a b}.
14
                   (Ham, defK2ABarD) # cdb (Ham. 102, Ham)
    substitute
    substitute (Ham, defG2GBarD)
                                      # cdb (Ham. 103, Ham)
    substitute (Ham, defG2GBarU)
                                      # cdb (Ham. 104, Ham)
                                      # cdb (Ham. 105, Ham)
    distribute
                   (Ham)
19
    Ham = product_sort (Ham)
                                      # cdb (Ham. 106, Ham)
    rename_dummies (Ham)
                                      # cdb (Ham. 107, Ham)
     canonicalise
                   (Ham)
                                      # cdb (Ham.108, Ham)
                   (Ham, "simplify") # cdb (Ham.109, Ham)
    map_sympy
23
^{24}
    foo := gBar_{a b} gBar^{a b} -> 3.
25
    bah := gBar_{a c} gBar^{b c} -> gBar_{a}^{b}.
27
    substitute (Ham, foo)
                                      # cdb (Ham.110, Ham)
28
                           # cdb (Ham.111,Ham)
    substitute (Ham, bah)
    eliminate_kronecker (Ham)
                                  # cdb (Ham.112,Ham)
30
31
    foo := gBar_{a b} gBar^{a b} \rightarrow 3.
    bah := gBar_{a}^{a} -> 3.
    moo := ABar_{a b} gBar^{a b} -> 0.
35
                   (Ham, foo)
                                       # cdb (Ham.113, Ham)
     substitute
```

```
(Ham, bah)
                                         # cdb (Ham.114, Ham)
     substitute
     substitute
                     (Ham, moo)
                                         # cdb (Ham.115, Ham)
38
     foo := ABar_{c d} gBar^{c a} gBar^{d b} -> ABar^{a b}.
40
41
     substitute
                    (Ham, foo)
                                         # cdb (Ham.116, Ham)
42
     rename_dummies (Ham)
                                         # cdb (Ham.117, Ham)
43
44
     cdblib.put ('Ham', Ham, jsonfile)
```

$$\mathcal{H} = R + \bar{A}_{ab}\bar{A}_{cd}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}_{cd}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(4\phi\right) \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}^{ab}\bar{g}^{cd} \exp\left(-4\phi\right) \exp\left(-4\phi\right) \exp\left(4\phi\right) \exp\left(4\phi\right) + \frac{1}{3} \operatorname{tr} K\bar{A}_{ab}\bar{g}^{ab}\bar{g}^{cd} \exp\left$$

```
# Check against prd67.
    foo := Q(Ham).
                                                          # cdb(prd67.eq19.lcb,foo)
     bah = cdblib.get('prd67.eq19.rhs','prd67.json')
                                                          # cdb(prd67.eq19.prd,bah)
     diff := @(foo) - @(bah).
     distribute
                    (diff)
     diff = product_sort (diff)
10
     rename_dummies (diff)
11
     map_sympy
                    (diff, "simplify")
                                                          # cdb(prd67.eq19.chk,diff)
     canonicalise
                    (diff)
```

$$\label{eq:prd67.eq19.lcb} \begin{split} \text{prd67.eq19.lcb} &:= R + \frac{2}{3} \text{tr} K^2 - \bar{A}^{ab} \bar{A}_{ab} \\ \text{prd67.eq19.prd} &:= R - \bar{A}_{ab} \bar{A}^{ab} + \frac{2}{3} \text{tr} K^2 \\ \text{prd67.eq19.chk} &:= 0 \end{split}$$