## PhysRevD.62.044034 equation (11)

```
from shared import *
     import cdblib
     jsonfile = 'eqtn11.json'
     cdblib.create (jsonfile)
     DhijDt = cdblib.get ('adm.DhijDt', 'adm.json')
     DKijDt = cdblib.get ('adm.DKijDt', 'adm.json')
10
11
     trK := trK \rightarrow g^{i} j K_{i}.
12
     gdotK := g^{i} j K_{i} -> trK.
13
14
     Kup := g^{i} a g^{i} b K_{i} -> K^{i} a b.
16
     Ham := g^{i} j R_{i} > K_{i} K^{i} - trK trK.
18
     Kij := K_{ij} -> A_{ij} + (1/3) g_{ij} trK. # prd62 eqn 07
19
     Lij := K^{i} = K^{i} + (1/3) g^{i} + (1/3) g^{i} trK. # prd62 eqn 07
21
     trA1 := A_{ij} g^{i} -> 0.
                                                      # Aij is trace free
     trA2 := A^{i} j g_{i} -> 0.
23
^{24}
     Asq := A_{i j} A^{i j} -> ABar_{i j} ABar^{i j}.
25
26
     gdotg := g_{i j} g^{i} -> 3.
28
     # dK/dt
30
31
     dotK := \partial_{t}{trK}.
                                        # cdb (eq11.101,dotK)
33
                                         # cdb (eq11.102,dotK)
                    (dotK,trK)
     substitute
                    (dotK)
                                         # cdb (eq11.103,dotK)
     product_rule
35
                    (dotK,DhijDt)
                                         # cdb (eq11.104,dotK)
     substitute
```

```
substitute
                     (dotK,DKijDt)
                                          # cdb (eq11.105,dotK)
     distribute
                     (dotK)
                                          # cdb (eq11.106,dotK)
     substitute
                     (dotK,gdotK)
                                           # cdb (eq11.107,dotK)
39
     substitute
                     (dotK,Kup)
                                           # cdb (eq11.108,dotK)
40
     dotK = product_sort (dotK)
                                           # cdb (eq11.109,dotK)
41
     substitute
                     (dotK, Ham)
                                           # cdb (eq11.110,dotK)
42
     distribute
                     (dotK)
                                           # cdb (eq11.111,dotK)
     substitute
                    (dotK,Kij)
                                           # cdb (eq11.112,dotK)
                                           # cdb (eq11.113,dotK)
     substitute
                     (dotK,Lij)
45
     distribute
                     (dotK)
                                          # cdb (eq11.114,dotK)
46
                     (dotK,trA1)
                                          # cdb (eq11.115,dotK)
     substitute
47
                     (dotK,trA2)
                                           # cdb (eq11.116,dotK)
     substitute
48
     substitute
                     (dotK,Asq)
                                          # cdb (eq11.117,dotK)
49
                                          # cdb (eq11.118,dotK)
     substitute
                     (dotK,gdotg)
                     (dotK, "simplify")
                                          # cdb (eq11.119,dotK)
     map_sympy
51
52
     DKDt := \partial_{t}{trK} -> @(dotK).
53
54
     cdblib.put ('DKDt',DKDt,jsonfile)
```

```
# Check against prd62.
    foo := @(dotK).
                                                           # cdb(eq11.1cb,foo)
                                                          # cdb(eq11.prd,bah)
     bah = cdblib.get('prd62.eq11.rhs','prd62.json')
    diff := @(foo) - @(bah).
    distribute
                    (diff)
    diff = product_sort (diff)
10
    rename_dummies (diff)
11
    map_sympy
                    (diff, "simplify")
                                                           # cdb(eq11.chk,diff)
     canonicalise
                    (diff)
```

$$\begin{split} & \texttt{eq11.lcb} := -\,g^{ab}D_{ab}N + N\bar{A}_{ab}\bar{A}^{ab} + \frac{1}{3}\operatorname{tr}K^2N \\ & \texttt{eq11.prd} := -\,g^{ij}D_{ij}N + N\left(\bar{A}_{ij}\bar{A}^{ij} + \frac{1}{3}\operatorname{tr}K^2\right) \\ & \texttt{eq11.chk} := 0 \end{split}$$