Exercise 1.1 Verify symmetry of $\Gamma^a{}_{bc}$

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{a,b,c,d,e,f,h,i,j,k,l,m,n,o,p,q,r,s,t,u\#}::Indices.
     g_{a b}::Metric.
     \partial{#}::PartialDerivative.
     Gamma := Gamma^{a}_{b c} -> (1/2) g^{a d} ( partial_{b}_{g_{d c}})
                                                 + \partial_{c}{g_{b d}}
                                                 - \partial_{d}{g_{b c}} ).
10
    diff := \Gamma_{a}(b c) - \Gamma_{a}(b).  # cdb (ex-0101.101,diff)
11
12
                   (diff, Gamma)
                                                    # cdb (ex-0101.102, diff)
     substitute
13
                   (diff)
                                                    # cdb (ex-0101.103,diff)
     distribute
     canonicalise (diff)
                                                    # cdb (ex-0101.104,diff)
```

$$\Gamma^{a}_{bc} - \Gamma^{a}_{cb} = \frac{1}{2} g^{ad} \left(\partial_{t} g_{dc} + \partial_{t} g_{bd} - \partial_{d} g_{bc} \right) - \frac{1}{2} g^{ad} \left(\partial_{t} g_{db} + \partial_{t} g_{cd} - \partial_{d} g_{cb} \right)$$

$$= \frac{1}{2} g^{ad} \partial_{t} g_{dc} + \frac{1}{2} g^{ad} \partial_{t} g_{bd} - \frac{1}{2} g^{ad} \partial_{d} g_{bc} - \frac{1}{2} g^{ad} \partial_{t} g_{db} - \frac{1}{2} g^{ad} \partial_{t} g_{cd} + \frac{1}{2} g^{ad} \partial_{d} g_{cb}$$

$$= 0$$