

Exercise 4.5 Reformatting complex expressions

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1 {a,b,c,d,e,f,g,h,i,j,k,l,m,n,o,p,q,r,s,t,u,v,w#}::Indices(position=independent).
2
3
4 \nabla{#}::Derivative.
5
6 def get_term (obj,n):
7
8     x^{a}::Weight(label=xnum).      # assign weights to x^{a}
9
10    foo := @(obj).                  # make a copy of obj
11    bah = Ex("xnum = " + str(n))   # choose a target
12    keep_weight (foo,bah)          # extract the target
13
14    return foo
15
16 def reformat (obj,scale):
17
18    {x^{a},A_{a},B_{a},A_{a b},B_{a b},C_{a b},C_{a b c},g^{a b}}::SortOrder. # choose a sort order
19
20    foo = Ex(str(scale))            # create a scale factor
21    bah := @(foo) @(obj).            # apply the scale factor, clears all fractions
22
23    distribute      (bah)           # only required if (bah) contains brackets
24    sort_product    (bah)
25    rename_dummies  (bah)
26    canonicalise    (bah)
27    factor_out      (bah,$x^{a?}$)
28
29    ans := @(bah) / @(foo).          # undo previous scaling
30
31    return ans
32
33 # -----
34
35 # a messy unformatted expression
36
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37 expr := (1/7) A_{e} x^{e}
38 - (1/3) B_{f} x^{f}
39 + (1/3) A_{a b} x^{a} x^{b}
40 + (1/9) B_{e c} x^{c} x^{e}
41 - (1/5) C_{p c} B_{d q} g^{c d} x^{p} x^{q}
42 + (3/7) A_{a b c} x^{a} x^{b} x^{c}
43 - (1/5) B_{a b} C_{c d e} g^{c d} x^{a} x^{b} x^{e}
44 + (7/11) B_{a b} B_{c d} C_{e f g} g^{b c} g^{d f} x^{a} x^{e} x^{g}. # cdb (ex-0405.100,expr)
45
46 # split the expression into seprate terms
47
48 term1 = get_term (expr,1) # cdb(term1.101,term1)
49 term2 = get_term (expr,2) # cdb(term2.101,term2)
50 term3 = get_term (expr,3) # cdb(term3.101,term3)
51
52 # reformat terms and tidy fractions
53
54 term1 = reformat (term1, 21) # cdb(term1.102,term1)
55 term2 = reformat (term2, 45) # cdb(term2.102,term2)
56 term3 = reformat (term3,385) # cdb(term3.102,term3)
57
58 # rebuild the expression
59
60 expr := @(term1) + @(term2) + @(term3). # cdb (ex-0405.101,expr)

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$$\begin{aligned}
g &= \frac{1}{7}A_e x^e - \frac{1}{3}B_f x^f + \frac{1}{3}A_{ab}x^a x^b + \frac{1}{9}B_{ec}x^c x^e - \frac{1}{5}C_{pc}B_{dq}g^{cd}x^p x^q + \frac{3}{7}A_{abc}x^a x^b x^c - \frac{1}{5}B_{ab}C_{cde}g^{cd}x^a x^b x^e + \frac{7}{11}B_{ab}B_{cd}C_{efg}g^{bc}g^{df}x^a x^e x^g \quad (\text{ex-0405.100}) \\
&= \frac{1}{21}x^a (3A_a - 7B_a) + \frac{1}{45}x^a x^b (15A_{ab} + 5B_{ab} - 9B_{ca}C_{bd}g^{dc}) + \frac{1}{385}x^a x^b x^c (165A_{abc} - 77B_{ab}C_{dec}g^{de} + 245B_{ad}B_{ef}C_{bge}g^{de}g^{fg}) \quad (\text{ex-0405.101})
\end{aligned}$$