Exercise 2.4 Combining rules – a problem

```
{a,b,c,d,e,f,g,h,i,j,k,l,m,n,o,p,q,r,s,t,u\#}::Indices(position=independent).
     \nabla{#}::Derivative.
     \partial{#}::PartialDerivative.
     # rules for covariant derivatives of v
     deriv1 := \\ a}{v^{b}} \rightarrow \\ partial_{a}{v^{b}}
                                   + \Gamma^{b}_{d a} v^{d}.
10
     deriv2 := \\ a}{\nabla_{b}{v^{c}}} \rightarrow \\ partial_{a}{\nabla_{b}{v^{c}}}
11
                                                + \Gamma^{c}_{d a} \nabla_{b}{v^{d}}
12
                                                - \Gamma^{d}_{b a} \nabla_{d}{v^{c}}.
13
14
     \# attempt to combine both rules for second covariant derivative of v
15
16
     substitute (deriv2,deriv1)
                                       # cdb (ex-0204.101,deriv2)
17
```

Note that the call to substitute has made changes to both sides of the rule for deriv2. This is not ideal and a better method is developed in the following exercise.

$$\nabla_a \left(\partial_b v^c + \Gamma^c{}_{db} v^d \right) \to \partial_a \left(\partial_b v^c + \Gamma^c{}_{db} v^d \right) + \Gamma^c{}_{da} \left(\partial_b v^d + \Gamma^d{}_{eb} v^e \right) - \Gamma^d{}_{ba} \left(\partial_d v^c + \Gamma^c{}_{ed} v^e \right) \tag{ex-0204.101}$$