

## Exercise 4.5 Reformatting complex expressions

```
1 {a,b,c,d,e,f,g,h,i,j,k,l,m,n,o,p,q,r,s,t,u,v,w#}::Indices(position=independent).
2
3
4 \nabla{#}::Derivative.
5
6 def get_term (obj,n):
7
8     x^{a}::Weight(label=xnum).      # assign weights to x^{a}
9
10    foo := @(obj).                  # make a copy of obj
11    bah  = Ex("xnum = " + str(n))  # choose a target
12    keep_weight (foo,bah)          # extract the target
13
14    return foo
15
16 def reformat (obj,scale):
17
18    {x^{a},A_{a},B_{a},A_{a b},B_{a b},C_{a b},C_{a b c},g^{a b}}::SortOrder. # choose a sort order
19
20    foo  = Ex(str(scale))           # create a scale factor
21    bah := @(foo) @(obj).           # apply the scale factor, clears all fractions
22
23    distribute      (bah)           # only required if (bah) contains brackets
24    sort_product    (bah)
25    rename_dummies  (bah)
26    canonicalise    (bah)
27    factor_out      (bah,$x^{a?}$)
28
29    ans := @(bah) / @(foo).         # undo previous scaling
30
31    return ans
32
33 # -----
34
35 # a messy unformatted expression
36
```

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37  expr :=      (1/7) A_{e} x^{e}
38             - (1/3) B_{f} x^{f}
39             + (1/3) A_{a b} x^{a} x^{b}
40             + (1/9) B_{e c} x^{c} x^{e}
41             - (1/5) C_{p c} B_{d q} g^{c d} x^{p} x^{q}
42             + (3/7) A_{a b c} x^{a} x^{b} x^{c}
43             - (1/5) B_{a b} C_{c d e} g^{c d} x^{a} x^{b} x^{e}
44             + (7/11) B_{a b} B_{c d} C_{e f g} g^{b c} g^{d f} x^{a} x^{e} x^{g}. # cdb (ex-0405.100,expr)
45
46  # split the expression into seprate terms
47
48  term1 = get_term (expr,1)      # cdb(term1.101,term1)
49  term2 = get_term (expr,2)      # cdb(term2.101,term2)
50  term3 = get_term (expr,3)      # cdb(term3.101,term3)
51
52  # reformat terms and tidy fractions
53
54  term1 = reformat (term1, 21)    # cdb(term1.102,term1)
55  term2 = reformat (term2, 45)    # cdb(term2.102,term2)
56  term3 = reformat (term3,385)    # cdb(term3.102,term3)
57
58  # rebuild the expression
59
60  expr := @(term1) + @(term2) + @(term3). # cdb (ex-0405.101,expr)

```

$$\begin{aligned}
g &= \frac{1}{7}A_ex^e - \frac{1}{3}B_fx^f + \frac{1}{3}A_{ab}x^ax^b + \frac{1}{9}B_{ec}x^cx^e - \frac{1}{5}C_{pc}B_{dq}g^{cd}x^px^q + \frac{3}{7}A_{abc}x^ax^bx^c - \frac{1}{5}B_{ab}C_{cde}g^{cd}x^ax^bx^e + \frac{7}{11}B_{ab}B_{cd}C_{efg}g^{bc}g^{df}x^ax^ex^g \quad (\texttt{ex-0405.100}) \\
&= \frac{1}{21}x^a(3A_a - 7B_a) + \frac{1}{45}x^ax^b(15A_{ab} + 5B_{ab} - 9B_{ca}C_{bd}g^{dc}) + \frac{1}{385}x^ax^bx^c(165A_{abc} - 77B_{ab}C_{dec}g^{de} + 245B_{ad}B_{ef}C_{bge}g^{de}g^{fg}) \quad (\texttt{ex-0405.101})
\end{aligned}$$