Exercise 6.8 The Kasner cosmology

```
{t, x, y, z}::Coordinate.
    {a,b,c,d,e,f,g,h#}::Indices(values={t, x, y, z}, position=independent).
    \partial{#}::PartialDerivative.
    p1::LaTeXForm("p_1").
    p2::LaTeXForm("p_2").
    p3::LaTeXForm("p_3").
    g^{a b}::InverseMetric. # essential when using complete (gab, $g^{a b}$)
10
11
    Gamma := Gamma^{a}_{f g} \rightarrow 1/2 g^{a b} ( partial_{g}_{g_b} f)
12
                                              + \partial_{f}{g_{b g}}
13
                                              - \partial_{b}{g_{f g}} ).
14
15
    16
                              - \partial_{g}{\Gamma^{d}_{e f}}
17
                              + \Gamma^{d}_{b f} \Gamma^{b}_{e g}
18
                              - \Gamma^{d}_{b g} \Gamma^{b}_{e f}.
19
20
    Rab := R_{a b} -> R^{c}_{a c b}.
21
22
    gab := \{ g_{t} = -1, \}
23
             g_{x} = t**(2*p1),
             g_{y} = t**(2*p2),
             g_{z} = t**(2*p3).
                                                              # cdb(ex-0608.101,gab)
27
    complete (gab, $g^{a b}$)
                                                              # cdb(ex-0608.102,gab)
28
29
    substitute (Rabcd, Gamma)
    substitute (Rab, Rabcd)
31
32
               (Gamma, gab, rhsonly=True)
    evaluate
                                                              # cdb(ex-0608.103, Gamma)
33
               (Rabcd, gab, rhsonly=True)
                                                              # cdb(ex-0608.104,Rabcd)
     evaluate
34
               (Rab, gab, rhsonly=True)
                                                              # cdb(ex-0608.105,Rab)
    evaluate
```

$$[g_{tt} = -1, \ g_{xx} = t^{2p_1}, \ g_{yy} = t^{2p_2}, \ g_{zz} = t^{2p_3}]$$

$$[g_{tt} = -1, \ g_{xx} = t^{2p_1}, \ g_{yy} = t^{2p_2}, \ g_{zz} = t^{2p_3}, \ g^{tt} = -1, \ g^{xx} = t^{-2p_1}, \ g^{yy} = t^{-2p_2}, \ g^{zz} = t^{-2p_3}]$$

$$(ex-0608.101)$$

$$[g_{tt} = -1, \ g_{xx} = t^{2p_1}, \ g_{yy} = t^{-2p_2}, \ g^{zz} = t^{-2p_3}]$$

$$(ex-0608.102)$$

$$[g_{tt} = -1, \ g_{xx} = t^{-2p_1}, \ g^{yy} = t^{-2p_2}, \ g^{zz} = t^{-2p_3}]$$

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$$[g_{tt} = -1, \ g_{xx} = t^{-2p_1}, \ g^{zz} = t^{-2p_3}, \ g^{zz} = t^{-2$$

$$\begin{cases} \Box_{xx}^{t} t = p_{1}t^{(2p_{1}-2)}(p_{1}-1) \\ \Box_{yy}^{t} t = p_{2}t^{(2p_{2}-2)}(p_{2}-1) \\ \Box_{xx}^{t} t = p_{1}(2p_{2}-2)(p_{3}-1) \\ \Box_{tx}^{t} t = p_{1}(p_{1}-1)t^{-2} \\ \Box_{tx}^{t} t = p_{1}(p_{1}-1)t^{-2} \\ \Box_{tx}^{t} t = p_{1}(p_{2}-1)t^{-2} \\ \Box_{tx}^{t} t = p_{1}(2p_{2}-2)(p_{1}-1) \\ \Box_{xt}^{t} t = p_{1}(2p_{2}-2)(p_{1}-1) \\ \Box_{xt}^{t} t = p_{1}(2p_{2}-2)(p_{3}-1) \\ \Box_{yt}^{t} t = p_{2}t^{(2p_{2}-2)}(p_{3}-1) \\ \Box_{tx}^{t} t = p_{1}(-p_{1}+1)t^{-2} \\ \Box_{tt}^{t} t = p_{1}(-p_{1}+1)t^{-2} \\ \Box_{tt}^{t} t = p_{2}(-p_{2}+1)t^{-2} \\ \Box_{tt}^{t} t = p_{3}(-p_{3}+1)t^{-2} \\ \Box_{xt}^{t} t = p_{1}(-p_{1}+1)t^{-2} \\ \Box_{xt}^{t} t = p_{1}(-p_{1}+1)t^{-2} \\ \Box_{xt}^{t} t = p_{1}(-p_{1}+1)t^{-2} \\ \Box_{xt}^{t} t = p_{1}(-p_{2}+1)t^{-2} \\ \Box_{xt}^{t} t = p_{1}(-p_{1}+1)t^{-2} \\ \Box_{xt}^{t} t = p_{1}(-p$$