





t_k, k





t_k, k

$$(\alpha_i \overset{\$}{\leftarrow} \{0, \frac{\pi}{4} \dots \frac{7\pi}{4}\})_{i=1}^{n-1}$$



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$k, (\alpha_i)$





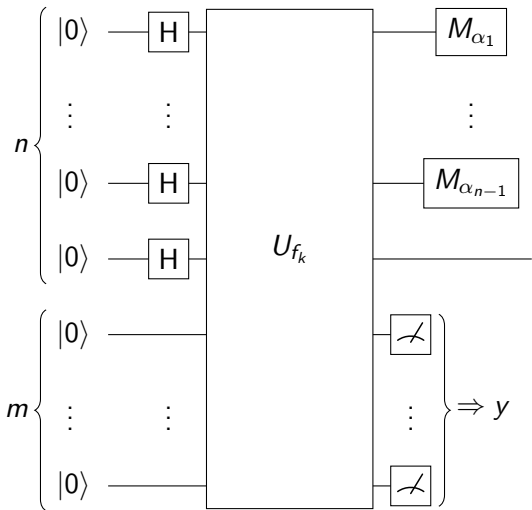
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$k, (\alpha_i)$

Compute circuit



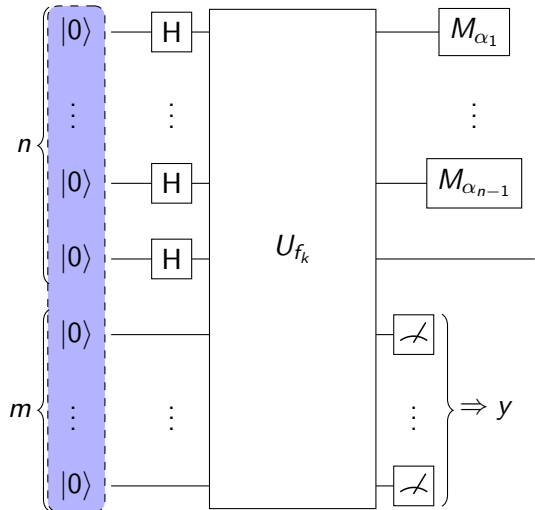


t_k, k



$k, (\alpha_i)$

Compute circuit



$|0\rangle|0\rangle$



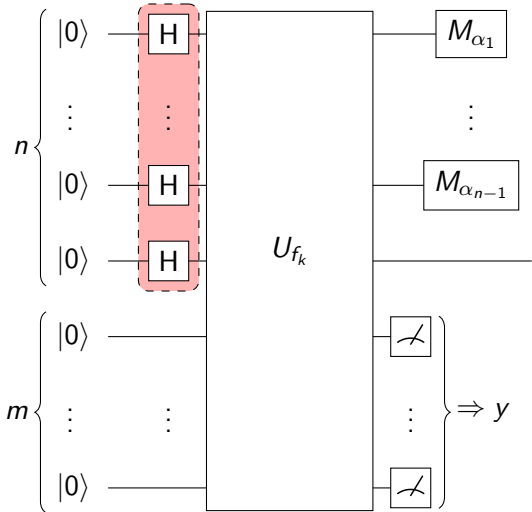
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Compute circuit



$$|0\rangle|0\rangle \Rightarrow \sum_x |x\rangle|0\rangle$$



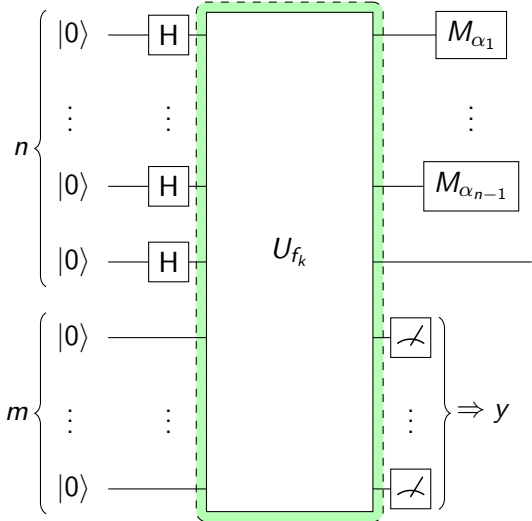
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$k, (\alpha_i)$

Compute circuit



$$|0\rangle|0\rangle \Rightarrow \sum_x |x\rangle|0\rangle \Rightarrow \sum_x |x\rangle|f_k(x)\rangle$$



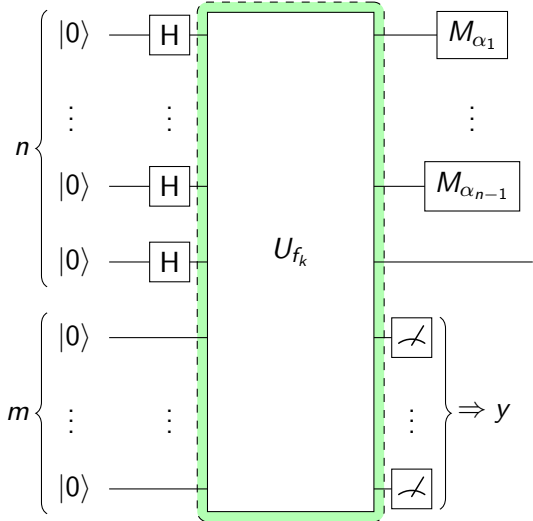
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Compute circuit



$$|0\rangle|0\rangle \Rightarrow \sum_x |x\rangle|0\rangle \Rightarrow \sum_x |x\rangle|f_k(x)\rangle = \sum_y (|x\rangle + |x'\rangle) \otimes |y\rangle$$



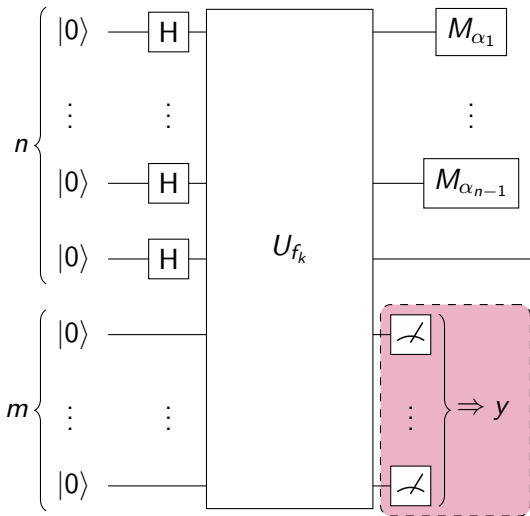
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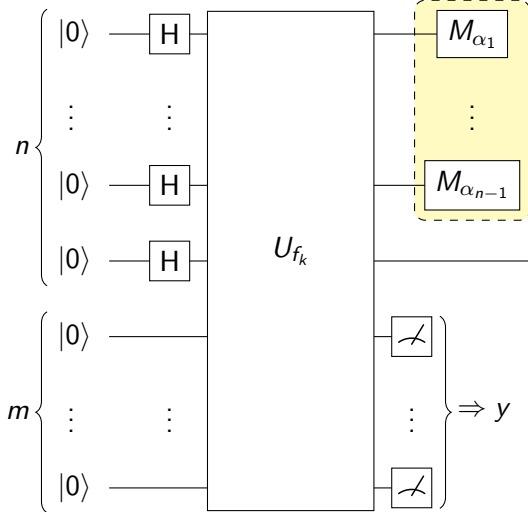
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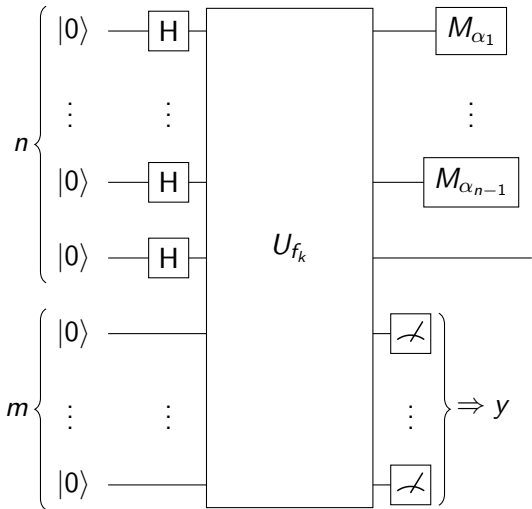
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$k, (\alpha_i)$

Compute circuit



\Rightarrow Produces $|+\theta\rangle$

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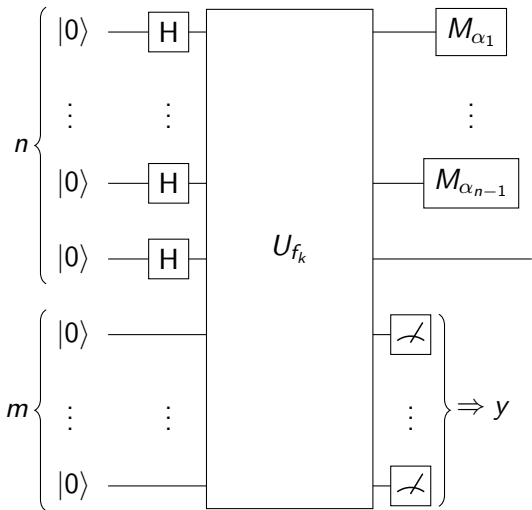


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$k, (\alpha_i)$

Compute circuit

$y, (b_i)$



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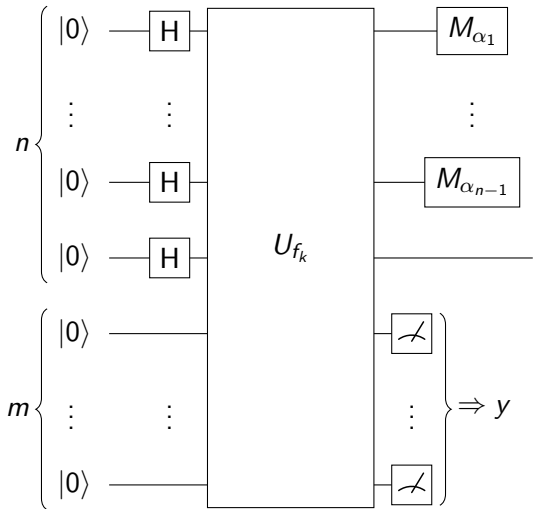
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$k, (\alpha_i)$

Compute circuit

$y, (b_i)$

$$(x, x') := \text{Inv}(t_k, y)$$



\Rightarrow Produces $|+\theta\rangle$

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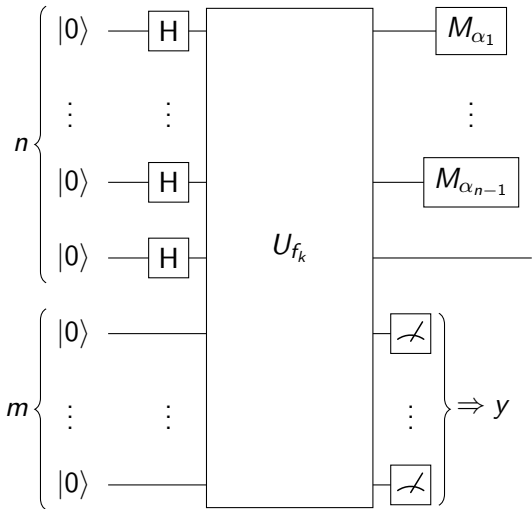
$k, (\alpha_i)$

Compute circuit

$y, (b_i)$

$$(x, x') := \text{Inv}(t_k, y)$$

$$\theta := \frac{\pi}{4} (-1)^{x_n} \sum_{i=1}^{n-1} (x_i - x'_i) (4b_i + \alpha_i)$$



\Rightarrow Produces $|+\theta\rangle$

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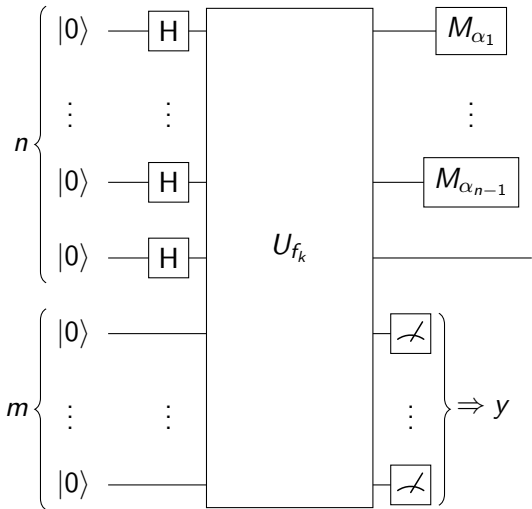


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