illustration for the case of constant smoothing length h

2h

common choice
for the support

2h

SPH-particle

highlighted SPH-particle
to better see the support

the auxiliary grid can be used to find neightbors
that can potentially contribute to the density at
the green particle (and all others in this grid-cell)