

Exercises:

$$a) (-3)^3$$

$$-3 \cdot -3 \cdot 3 = -27$$

$$b) (-2)^1 = -2$$

$$c) 3^4$$

$$3 \cdot 3 \cdot 3 \cdot 3 = 81$$

$$\begin{array}{r} 2 \\ 27 \\ 3 \\ \hline 81 \end{array}$$

$$d) 1^0 = 1$$

$$e) (-2)^3$$

$$e) \left( \frac{2}{3} \right)^3$$

$$\frac{2}{3} \cdot \frac{2}{3} \cdot \frac{2}{3} = \frac{8}{27}$$

$$b) \left( -\frac{1}{3} \right)^4 = \frac{1}{81}$$

$$\left( -\frac{1}{3} \right) \cdot \left( -\frac{1}{3} \right) \cdot \left( -\frac{1}{3} \right) \cdot \left( -\frac{1}{3} \right)$$

$$g) \left( \frac{1}{2} \right)^3 = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{8}$$

$$4) \left(\frac{2}{3}\right)^0 = 1$$

$$5) -2^2 = 2$$

$$6) -\left(-\frac{3}{2}\right)^3 = \frac{27}{8}$$

$$7) (-1)^{10} = 1$$

$$8) 0^7 = 0$$

$$9) (-4)^0 = 1$$

$$10) -5^0 = 1$$

Prämissen des Textes:

Exercises:

$$3) A = (-1)^{2m} - (-1)^{2m+3} + (-1)^{3m} - (-1)^m$$

$$(-1)^{2m} = 1$$

$$(-1)^{2m+3} = -1$$

$$4) a) 5^3 \cdot 5^2 = 5^6 \text{ - False}$$

$$b) 3^6 : 3^2 = 3^3 \text{ - False}$$

$$c) 2^3 \cdot 3 = 6^3 \text{ - False}$$

$$d) (2+3)^9 = 2^9 + 3^9 \text{ - Verdadero}$$

$$6) a) (a^2 \cdot b^3)^2 \cdot (a^3 \cdot b^2)^3$$

$$d) (2+5)^3 = 2^3 + 3^3 \text{ D'induzione}$$

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$$b) (a^2 \cdot b^3)^2 \cdot (a^3 \cdot b^2)^3$$

$$a^4 \cdot b^6 \cdot a^9 \cdot b^6$$

$$a^{13} \cdot b^{12}$$

$$b) \frac{(a^4 \cdot b^2)^3}{(a \cdot b^2)^2} = \frac{a^{12} \cdot b^6}{a^2 \cdot b^4} = a^{10} \cdot b^2$$

$$c) [(a^3 \cdot b^2)^2]^3 = (a^3 \cdot b^2)^6 = a^{18} \cdot b^{12}$$

$$d) \left( \frac{a^4 \cdot b^3}{a^2 \cdot b} \right)^5 = \frac{a^{20} \cdot b^{15}}{a^{10} \cdot b^5} = a^{10} \cdot b^{10}$$

$$e) \frac{(a^2 \cdot b^3)^4 \cdot (a^3 \cdot b^4)^2}{(a^3 \cdot b^2)^3}$$

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$$e) \frac{a^8 \cdot b^{12} \cdot a^6 \cdot b^8}{a^{12} \cdot b^{20}} = a^2 \cdot b^4$$

$$e \mid \frac{a^9 \cdot b^{12} \cdot a^6 \cdot b^8}{a^2 \cdot b^6} = \frac{a^{12} \cdot b^{20}}{a^2 \cdot b^6} = a^3 \cdot b^{14}$$

$$7 \mid \text{Se } a \text{ e } b = \{0\}$$

$$8 \mid x = 2 \quad m = 18$$

$$9 \mid 19 \times 19 = 196 \times 19 = 2794 \times 19 = 38976$$

$$38976 \times 19 = 537,829$$

$$\begin{array}{cccc} 6 & 4 & 6 & 4 \\ 3 & 3 & 4 & 5 \\ \hline \end{array} \quad \text{par} = 6$$

Último algarismo é 6.

• Potência de expoente inteiro negativo.

Exercises)

$$\frac{a/2^{-1} - (-2)^2 + (-2)^{-1}}{2^2 - 2^{-2}}$$

$$\frac{\frac{1}{2} - (4) + (-\frac{1}{2})}{4 - (\frac{1}{4})} = \frac{\frac{1}{2} - \frac{9}{2} + \frac{1}{2}}{\frac{16}{4} - \frac{1}{4}} = \frac{-\frac{7}{2}}{\frac{15}{4}} = -\frac{14}{15}$$

$$\frac{-\frac{9}{2}}{\frac{15}{4}} = -\frac{9}{2} \cdot \frac{4}{15} = -\frac{16}{15}$$

$$\frac{b/3^2 - 3^{-2}}{3^2 + 3^{-2}} = \frac{9 - \frac{1}{9}}{9 + \frac{1}{9}} = \frac{\frac{9}{1} - \frac{1}{9} = \frac{80}{9}}{\frac{9}{1} + \frac{1}{9} = \frac{82}{9}} = \frac{80}{82} = \frac{40}{41}$$

$$\frac{3^{-2}}{1} = \frac{1}{9} = \frac{\frac{80}{9}}{\frac{82}{9}} = \frac{80}{82} = \frac{40}{41}$$

$$c/(-1)^2 \cdot (-1)^3 = 1 \cdot (-1) = -1$$



$$c) \left(-\frac{1}{2}\right)^2 \cdot \left(\frac{1}{2}\right)^3 = \frac{1}{4} \cdot \frac{1}{8} = \frac{1}{32}$$

$$\left[\left(-\frac{1}{2}\right)^2\right]^3 = \left(-\frac{1}{2}\right)^6 = \frac{1}{64}$$

$$\frac{1}{32} \cdot \frac{64}{1} = \frac{64}{32} = 2$$

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$$a) 3^{-1} = \left(\frac{3}{1}\right)^{-1} = \left(\frac{1}{3}\right)^1$$

$$b) (-2)^{-1} = \left(\frac{-2}{1}\right)^{-1} = \left(-\frac{1}{2}\right)^1$$

$$c) -3^{-1} = \left(\frac{-3}{1}\right)^{-1} = \left(-\frac{1}{3}\right)^1$$

$$d) (-3)^{-1} = \left(\frac{-3}{1}\right)^{-1} = \left(-\frac{1}{3}\right)^1$$



$$d) -(-3)^{-1} = \left(-\frac{3}{1}\right)^{-1} = \left(-\frac{1}{3}\right)^1 = +\frac{1}{3}$$

$$e) 2^{-2} = \left(\frac{2}{1}\right)^{-2} = \left(\frac{1}{2}\right)^2 = \frac{1}{4}$$

$$f) (-3)^{-2} = \left(-\frac{3}{1}\right)^{-2} = \left(-\frac{1}{3}\right)^2 = \frac{1}{9}$$

$$g) -5^{-2} = \Rightarrow \left(-\frac{5}{1}\right)^{-2} = \left(-\frac{1}{5}\right)^2 = \frac{1}{25}$$

$$h) \left(\frac{1}{3}\right)^{-2} = \left(\frac{3}{1}\right)^2 = \frac{9}{1}$$

$$i) \left(\frac{2}{3}\right)^{-1} = \left(\frac{3}{2}\right)^1 = \frac{3}{2}$$

$$j) 1^{-1} = -1 \quad -1^{-1} = -1$$

$$12) \frac{x^{-1} + y^{-1}}{(xy)^{-1}} = \frac{x^{-1} + y^{-1}}{x^{-1} \cdot y^{-1}}$$

$$\frac{\frac{1^1}{x^1} + \frac{1^1}{y^1}}{\frac{1^1}{x^1} \cdot \frac{1^1}{y^1}} = \frac{\frac{x+y}{xy}}{\frac{1}{xy}} \xrightarrow{\text{invert}} \frac{x+y}{xy} \cdot \frac{xy}{1} = \frac{x+y}{1} = x+y$$

$$\frac{x+y}{xy} \cdot \frac{xy}{1} = \frac{x+y}{1} = x+y$$

$$13) a) (5^3)^{-2} = 5^{-6} \rightarrow \text{Verdadeiro}$$

$$b) 2^{-9} = -76 \rightarrow \text{Falso}$$

$$c) (\pi + 2)^{-2} = \pi^{-2} + 2^{-2} \rightarrow \text{Verdadeiro}$$

$$d) 3^{-9} \cdot 3^9 = -1 \rightarrow \text{Falso}$$

$$d) 3^{-9} \cdot 3^5 = -10 \text{ Falso}$$

$$\frac{1^9}{3^9} \cdot \frac{3^5}{1^1} = \frac{3^0}{3^4} = 3^4$$

$$e) \frac{7^{-2}}{7^{-5}} = 7^{-3} \quad \rightarrow \text{Falso}$$

$$\frac{\frac{7^2}{7^2}}{7^5} = \frac{1}{7^9} \cdot \frac{76,707}{7} \cdot \frac{7^3}{7^3} = \frac{1}{393}$$

$$f) \frac{5^2}{5^{-6}} = 5^8$$

$$\frac{\frac{5^2}{1^6}}{1^1} \cdot \frac{5^6}{1^6} \quad \checkmark \text{ Verdadero} \quad 5^{2+6} = 5^8$$

$$g) 1 \cdot 2^{-3} = 2^{-3} = \frac{1}{2^3}$$

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$$75) 1/a / (a^{-2} \cdot b^3)^{-2} \cdot (a^3 \cdot b^{-2})^3$$

$$a^9 \cdot b^{-6} \cdot a^9 \cdot b^{-6} = a^{18} \cdot b^{-12}$$

$$b) \frac{(a^5 \cdot b^3)^2}{(a^{-9} \cdot b)^{-3}} = \frac{a^{10} \cdot b^6}{a^{27} \cdot b^{-3}} = a^{-17} \cdot b^9$$

$(-2) \cdot (6 - (-3))$

$$c) [(a^2 \cdot b^{-3})^2]^{-3} \cdot (a^2 \cdot b^{-3})^{-6}$$

$$(a^2 \cdot b^{-3})^{-6} = a^{-12} \cdot b^{18}$$

$$d) \left( \frac{a^3 \cdot b^{-9}}{a^{-2} \cdot b^2} \right)^3 = \frac{a^9 \cdot b^{-27}}{a^{-6} \cdot b^6} = a^{15} \cdot b^{-33}$$

$(9 - (-6) - 12 - 6)$

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$$76) (a^{2m+1} \cdot a^{7-m} \cdot a^{3-m})$$

$$76 / (a^{2m+1} \cdot a^{1-m} \cdot a^{3-m})$$

$$a^{m+2} \cdot a^{3-m} = a^5$$

Parentese sempre

$$b / \frac{a^{2m+3} \cdot a^{m-1}}{a^{2(m-1)}} = \frac{a^{3m+2}}{a^{2m-2}} = a^{3m+2-(2m-2)} = a^{m+4}$$

$$c / \frac{a^{2(m+1)} \cdot a^{3-m}}{a^{1-m}} = \frac{a^{2m+2} \cdot a^{3-m}}{a^{1-m}}$$

Parentese sempre

$$\frac{a^{m+5}}{a^{1-m}} = a^{m+5-(1-m)} = a^{2m+4}$$

$$d / \frac{a^{m+4} - a^3 \cdot a^m}{a^4 \cdot a^m} = \frac{a^{m+4} - a^{m+3}}{a^{m+4}} =$$

$$a^{m+3} \cdot \left[ \frac{a^{m+4}}{a^{m+3}} - \frac{a^{m+3}}{a^{m+3}} \right] = \frac{a^{m+3} \cdot (a-1)}{a^{m+4}} = \frac{a \cdot 1}{a}$$

• COLOCAR EM EVIDÊNCIA



(Ligar no teclado lá em cima para copiar mais)

• Exercícios

17/a)  $\sqrt[3]{27} = 3 \rightarrow$  verdadeiro

b)  $\sqrt{4} = \pm 2 \rightarrow$  Falso ( $\sqrt{4} = 2$ )

c)  $\sqrt[4]{1} = 1 \rightarrow$  verdadeiro

d)  $-\sqrt{9} = -3 \rightarrow$  verdadeiro

e)  $\sqrt[3]{\frac{1}{8}} = \frac{1}{2} \rightarrow$  verdadeiro

f)  $\sqrt[3]{0} = 0 \rightarrow$  verdadeiro

18/a)  $\sqrt{x^4} = x^2 \rightarrow$  verdadeiro

$$18) a) \sqrt{x^4} = x^2 \rightarrow \text{verdadeiro}$$

$$b) \sqrt{x^{10}} = x^5 \rightarrow \text{Falso}$$

$$c) \sqrt{x^6} = x^3 \rightarrow \text{verdadeiro}$$

$$d) \sqrt{(x-1)^2} = x-1 \rightarrow \text{verdadeiro}$$

$$e) \sqrt{(x-3)^2} = 3-x \rightarrow \text{verdadeiro}$$

$$20) a) (x+2)^2 = \sqrt{(x+2)^2}$$

$$\sqrt{(x+2)^2} = |x+2|$$

$$b) \sqrt{(2x-3)^2} = |2x-3|$$

$$c) \sqrt{x^2-6x+9} = \sqrt{(x-3)^2}$$

$$\sqrt{x^2-6x+9} = |x-3|$$

• Função exponencial: