Predicting Dow Jones Trading Volume

```
import pandas as pd
In [145...
          import numpy as np
          import seaborn as sns
          import matplotlib.pyplot as plt
          import io
          import requests
          import time
          import sys
          if not sys.warnoptions:
              import warnings
              warnings.simplefilter("ignore")
          warnings.filterwarnings('ignore')
          sns.set(font_scale = 1.)
          pd.set option('display.max columns', None)
In [207...
         from sklearn.compose import ColumnTransformer
          from sklearn.ensemble import RandomForestRegressor
          from sklearn.impute import SimpleImputer
          from sklearn.linear_model import ElasticNet
          from sklearn.neural_network import MLPRegressor
          from sklearn.tree import DecisionTreeRegressor
          from sklearn.metrics import r2_score
          from sklearn.model_selection import GridSearchCV, TimeSeriesSplit
          from sklearn.pipeline import Pipeline
          from sklearn.preprocessing import OneHotEncoder, StandardScaler
          from keras.wrappers.scikit learn import KerasRegressor
          import tensorflow as tf
          from tensorflow import keras
          from keras.models import Sequential
          from keras.layers import Dense, LSTM
          import xgboost as xgb
```

Data Visualization and Preparation

```
In [6]: url = "https://raw.githubusercontent.com/ucla-econ-425t/2023winter/master/slides/data/NYSE.csv"
s = requests.get(url).content.decode('utf-8')
nyse = pd.read_csv(io.StringIO(s), index_col = 0)
nyse
```

Out[6]	1:	day of week	DJ return	log volume	log volatility	train

date					
1962-12-03	mon	-0.004461	0.032573	-13.127403	True
1962-12-04	tues	0.007813	0.346202	-11.749305	True
1962-12-05	wed	0.003845	0.525306	-11.665609	True
1962-12-06	thur	-0.003462	0.210182	-11.626772	True
1962-12-07	fri	0.000568	0.044187	-11.728130	True
•••					
1986-12-24	wed	0.006514	-0.236104	-9.807366	False
1986-12-26	fri	0.001825	-1.322425	-9.906025	False
1986-12-29	mon	-0.009515	-0.371237	-9.827660	False
1986-12-30	tues	-0.001837	-0.385638	-9.926091	False
1986-12-31	wed	-0.006655	-0.264986	-9.935527	False

6051 rows × 5 columns

Autocorrelation

```
In [7]: from statsmodels.graphics.tsaplots import plot_acf, plot_pacf

plt.figure()
plot_acf(nyse['log_volume'], lags = 20)
plt.show()
```

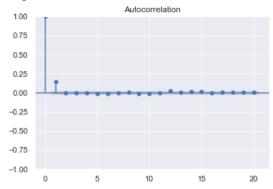
<Figure size 432x288 with 0 Axes>

```
Autocorrelation

0.75
0.50
0.25
0.00
-0.25
-0.50
-0.75
-1.00
0 5 10 15 20
```

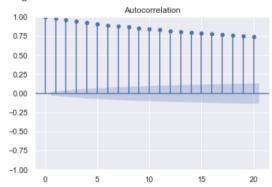
```
In [8]: plt.figure()
  plot_acf(nyse['DJ_return'], lags = 20)
  plt.show()
```

<Figure size 432x288 with 0 Axes>



```
In [9]:
    plt.figure()
    plot_acf(nyse['log_volatility'], lags = 20)
    plt.show()
```

<Figure size 432x288 with 0 Axes>



Create Lagged Variables

```
In [10]: L = 5
for s in range(1, L+1):
    nyse[f'DJ_return_lag{s}'] = nyse['DJ_return'].shift(s)
    nyse[f'log_volume_lag{s}'] = nyse['log_volume'].shift(s)
    nyse[f'log_volatility_lag{s}'] = nyse['log_volatility'].shift(s)

nyse = nyse.reindex(sorted(nyse.columns), axis = 1)
```

```
In [11]: nyse
```

:	DJ_return	DJ_return_lag1	DJ_return_lag2	DJ_return_lag3	DJ_return_lag4	DJ_return_lag5	day_of_week	log_volatility	log_volatility_lag1	log_volatil
date										
1962- 12-03	-0.004461	NaN	NaN	NaN	NaN	NaN	mon	-13.127403	NaN	
1962- 12-04	0.007813	-0.004461	NaN	NaN	NaN	NaN	tues	-11.749305	-13.127403	
1962- 12-05	0.003845	0.007813	-0.004461	NaN	NaN	NaN	wed	-11.665609	-11.749305	-13
1962- 12-06	-0.003462	0.003845	0.007813	-0.004461	NaN	NaN	thur	-11.626772	-11.665609	-11
1962- 12-07	0.000568	-0.003462	0.003845	0.007813	-0.004461	NaN	fri	-11.728130	-11.626772	-11
1986- 12-24	0.006514	-0.006150	-0.001385	0.008345	-0.002866	-0.009262	wed	-9.807366	-9.782214	_Ç
1986- 12-26	0.001825	0.006514	-0.006150	-0.001385	0.008345	-0.002866	fri	-9.906025	-9.807366	-S
1986- 12-29	-0.009515	0.001825	0.006514	-0.006150	-0.001385	0.008345	mon	-9.827660	-9.906025	- <u>g</u>
1986- 12-30	-0.001837	-0.009515	0.001825	0.006514	-0.006150	-0.001385	tues	-9.926091	-9.827660	- <u>g</u>
1986- 12-31	-0.006655	-0.001837	-0.009515	0.001825	0.006514	-0.006150	wed	-9.935527	-9.926091	- <u>9</u>

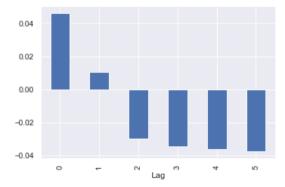
Correlation

4

```
In [14]: corr = nyse.filter(regex = 'log_volume*|DJ_return*|log_volatility*').corr()
    corr.style.background_gradient(cmap = 'coolwarm')
```

	DJ_return	DJ_return_lag1	DJ_return_lag2	DJ_return_lag3	DJ_return_lag4	DJ_return_lag5	log_volatility	log_volatility_lag1	log_volatility
DJ_return	1.000000	0.143388	-0.003597	-0.005304	-0.005528	-0.014239	0.026793	0.014177	0.0
DJ_return_lag1	0.143388	1.000000	0.143365	-0.003752	-0.005278	-0.005428	0.021996	0.026778	0.0
DJ_return_lag2	-0.003597	0.143365	1.000000	0.143336	-0.003744	-0.005249	0.017013	0.021991	0.02
DJ_return_lag3	-0.005304	-0.003752	0.143336	1.000000	0.143389	-0.003602	0.011547	0.016992	0.02
DJ_return_lag4	-0.005528	-0.005278	-0.003744	0.143389	1.000000	0.143372	0.000350	0.011551	0.0
DJ_return_lag5	-0.014239	-0.005428	-0.005249	-0.003602	0.143372	1.000000	-0.006393	0.000366	0.0
log_volatility	0.026793	0.021996	0.017013	0.011547	0.000350	-0.006393	1.000000	0.980054	0.96
log_volatility_lag1	0.014177	0.026778	0.021991	0.016992	0.011551	0.000366	0.980054	1.000000	0.98
log_volatility_lag2	0.013557	0.014163	0.026773	0.021972	0.016995	0.011565	0.960890	0.980054	1.00
log_volatility_lag3	0.010581	0.013561	0.014164	0.026780	0.021972	0.016994	0.943046	0.960892	0.98
log_volatility_lag4	0.008297	0.010570	0.013557	0.014149	0.026783	0.021983	0.926665	0.943046	0.96
log_volatility_lag5	0.009971	0.008303	0.010572	0.013568	0.014148	0.026778	0.910997	0.926668	0.94
log_volume	0.200892		0.108032	0.110325	0.090132	0.070240	0.046306	0.010394	-0.02
log_volume_lag1	0.047600			0.107846	0.110372	0.090282	0.036211	0.046288	0.0
log_volume_lag2	0.015934	0.047396			0.107921	0.110601	0.027911	0.036186	0.04
log_volume_lag3	0.008729	0.015730	0.047345			0.108141	0.021485	0.027885	0.03
log_volume_lag4	-0.004202	0.007997	0.015549	0.046402	0.201233		0.015350	0.021425	0.02
log_volume_lag5	0.002981	-0.004333	0.007959	0.015366	0.046438	0.201379	0.003120	0.015331	0.02
	DJ_return_lag1 DJ_return_lag2 DJ_return_lag3 DJ_return_lag5 log_volatility_lag1 log_volatility_lag2 log_volatility_lag3 log_volatility_lag4 log_volatility_lag5 log_volume_lag1 log_volume_lag2 log_volume_lag2 log_volume_lag3 log_volume_lag3	DJ_return 1.000000 DJ_return_lag1	DJ_return_lag1 0.143388 1.000000 DJ_return_lag2 -0.003597 0.143365 DJ_return_lag3 -0.005304 -0.003752 DJ_return_lag4 -0.005528 -0.005278 DJ_return_lag5 -0.014239 -0.005428 log_volatility 0.026793 0.021996 log_volatility_lag1 0.014177 0.026778 log_volatility_lag2 0.013557 0.014163 log_volatility_lag3 0.010581 0.013561 log_volatility_lag4 0.008297 0.010570 log_volatility_lag5 0.009971 0.008303 log_volume_lag1 0.047600 0.200776 log_volume_lag2 0.015934 0.047396 log_volume_lag3 0.008729 0.015730 log_volume_lag4 -0.004202 0.007997	DJ_return 1.000000 0.143388 -0.003597 DJ_return_lag1 0.143388 1.000000 0.143365 DJ_return_lag2 -0.003597 0.143365 1.000000 DJ_return_lag3 -0.005304 -0.003752 0.143336 DJ_return_lag4 -0.005528 -0.005278 -0.003744 DJ_return_lag5 -0.014239 -0.005428 -0.005249 log_volatility_lag1 0.026793 0.021996 0.017013 log_volatility_lag2 0.013557 0.014163 0.026773 log_volatility_lag3 0.010581 0.013561 0.014164 log_volatility_lag4 0.008297 0.010570 0.013557 log_volume 0.200892 0.211669 0.108032 log_volume_lag1 0.047600 0.200776 0.211648 log_volume_lag2 0.015934 0.047396 0.200756 log_volume_lag3 0.008729 0.015730 0.047345 log_volume_lag4 -0.004202 0.007997 0.015549	DJ_return 1.000000 0.143388 -0.003597 -0.005304 DJ_return_lag1 0.143388 1.000000 0.143365 -0.003752 DJ_return_lag2 -0.003597 0.143365 1.000000 0.143336 DJ_return_lag3 -0.005304 -0.003752 0.143336 1.000000 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 DJ_return_lag5 -0.014239 -0.005428 -0.005249 -0.003602 log_volatility 0.026793 0.021996 0.017013 0.011547 log_volatility_lag1 0.014177 0.026778 0.021991 0.016992 log_volatility_lag2 0.013557 0.014163 0.026773 0.021972 log_volatility_lag3 0.010581 0.013561 0.014164 0.026780 log_volatility_lag4 0.008297 0.010570 0.013557 0.014149 log_volume_lag4 0.0200892 0.211669 0.108032 0.110325 log_volume_lag1 0.047600 0.200776 0.211648 0.107846 <th>DJ_return 1.000000 0.143388 -0.003597 -0.005304 -0.005528 DJ_return_lag1 0.143388 1.000000 0.143365 -0.003752 -0.005278 DJ_return_lag2 -0.003597 0.143365 1.000000 0.143336 -0.003744 DJ_return_lag3 -0.005304 -0.005278 -0.003744 0.143389 1.000000 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1.000000 DJ_return_lag5 -0.014239 -0.005248 -0.005249 -0.003602 0.143372 log_volatility_lag1 0.026793 0.021996 0.017013 0.011547 0.000350 log_volatility_lag2 0.014177 0.026778 0.021991 0.016992 0.011551 log_volatility_lag3 0.010581 0.013561 0.014164 0.026780 0.021972 log_volatility_lag4 0.008297 0.010570 0.013557 0.014149 0.026783 log_volume_lag1 0.047600 0.200776 0.211648 0.107846 0.110372 <th< th=""><th>DJ_return 1.000000 0.143388 -0.003597 -0.005304 -0.005528 -0.014239 DJ_return_lag1 0.143388 1.000000 0.143365 -0.003752 -0.005278 -0.005428 DJ_return_lag2 -0.003597 0.143365 1.000000 0.143336 -0.003744 -0.005249 DJ_return_lag3 -0.005304 -0.003752 0.143336 1.000000 0.143389 -0.003602 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1.000000 0.143372 DJ_return_lag5 -0.014239 -0.005278 -0.003744 0.143389 1.000000 0.143372 1.000000 log_volatility 0.026793 0.021996 0.017013 0.011547 0.000350 -0.006393 log_volatility_lag1 0.014177 0.026778 0.021991 0.016992 0.011551 0.00366 log_volatility_lag3 0.010581 0.013561 0.014164 0.026780 0.021972 0.016995 0.011565 log_volume_lag4 0.00802 0.211669</th><th>DJ_return 1,00000 0,143388 -0,003597 -0,005304 -0,005528 -0,014239 0,026793 DJ_return_lag1 0,143388 1,00000 0,143365 -0,003752 -0,005278 -0,005428 0,021996 DJ_return_lag2 -0,003597 0,143365 1,000000 0,143336 -0,003744 -0,005249 0,017013 DJ_return_lag3 -0,005528 -0,005278 -0,003744 0,143389 1,000000 0,143372 0,00350 DJ_return_lag4 -0,005528 -0,005278 -0,003744 0,143389 1,000000 0,143372 0,000350 DJ_return_lag5 -0,014239 -0,005428 -0,005249 -0,003602 0,143372 1,000000 -0,006393 log_volatility 0,026793 0,021996 0,017013 0,011547 0,000350 -0,006393 1,000000 log_volatility_lag2 0,014163 0,026773 0,021972 0,016993 0,011565 0,960890 log_volatility_lag3 0,010581 0,013561 0,014164 0,026780 0,021972 <th< th=""><th>DJ_return 1,000000 0.143388 -0.003597 -0.005304 -0.005528 -0.014239 0.026793 0.014177 DJ_return_lag1 0.143388 1,000000 0.143365 -0.003752 -0.005278 -0.005428 0.021996 0.026778 DJ_return_lag2 -0.003597 0.143365 1,000000 0.143336 -0.003744 -0.005249 0.017013 0.021991 DJ_return_lag3 -0.005304 -0.003752 0.143336 1,000000 0.143389 -0.003602 0.011547 0.016992 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1,000000 0.143372 0.000350 0.011551 DJ_return_lag5 -0.014239 -0.005428 -0.005249 -0.003602 0.143372 1,000000 -0.06393 1,00000 log_volatility_lag5 0.026773 0.021991 0.016992 0.011551 0.00366 0.980054 1,00000 log_volatility_lag2 0.013557 0.014163 0.026773 0.021972 0.016995 0.011565 0.960890</th></th<></th></th<></th>	DJ_return 1.000000 0.143388 -0.003597 -0.005304 -0.005528 DJ_return_lag1 0.143388 1.000000 0.143365 -0.003752 -0.005278 DJ_return_lag2 -0.003597 0.143365 1.000000 0.143336 -0.003744 DJ_return_lag3 -0.005304 -0.005278 -0.003744 0.143389 1.000000 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1.000000 DJ_return_lag5 -0.014239 -0.005248 -0.005249 -0.003602 0.143372 log_volatility_lag1 0.026793 0.021996 0.017013 0.011547 0.000350 log_volatility_lag2 0.014177 0.026778 0.021991 0.016992 0.011551 log_volatility_lag3 0.010581 0.013561 0.014164 0.026780 0.021972 log_volatility_lag4 0.008297 0.010570 0.013557 0.014149 0.026783 log_volume_lag1 0.047600 0.200776 0.211648 0.107846 0.110372 <th< th=""><th>DJ_return 1.000000 0.143388 -0.003597 -0.005304 -0.005528 -0.014239 DJ_return_lag1 0.143388 1.000000 0.143365 -0.003752 -0.005278 -0.005428 DJ_return_lag2 -0.003597 0.143365 1.000000 0.143336 -0.003744 -0.005249 DJ_return_lag3 -0.005304 -0.003752 0.143336 1.000000 0.143389 -0.003602 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1.000000 0.143372 DJ_return_lag5 -0.014239 -0.005278 -0.003744 0.143389 1.000000 0.143372 1.000000 log_volatility 0.026793 0.021996 0.017013 0.011547 0.000350 -0.006393 log_volatility_lag1 0.014177 0.026778 0.021991 0.016992 0.011551 0.00366 log_volatility_lag3 0.010581 0.013561 0.014164 0.026780 0.021972 0.016995 0.011565 log_volume_lag4 0.00802 0.211669</th><th>DJ_return 1,00000 0,143388 -0,003597 -0,005304 -0,005528 -0,014239 0,026793 DJ_return_lag1 0,143388 1,00000 0,143365 -0,003752 -0,005278 -0,005428 0,021996 DJ_return_lag2 -0,003597 0,143365 1,000000 0,143336 -0,003744 -0,005249 0,017013 DJ_return_lag3 -0,005528 -0,005278 -0,003744 0,143389 1,000000 0,143372 0,00350 DJ_return_lag4 -0,005528 -0,005278 -0,003744 0,143389 1,000000 0,143372 0,000350 DJ_return_lag5 -0,014239 -0,005428 -0,005249 -0,003602 0,143372 1,000000 -0,006393 log_volatility 0,026793 0,021996 0,017013 0,011547 0,000350 -0,006393 1,000000 log_volatility_lag2 0,014163 0,026773 0,021972 0,016993 0,011565 0,960890 log_volatility_lag3 0,010581 0,013561 0,014164 0,026780 0,021972 <th< th=""><th>DJ_return 1,000000 0.143388 -0.003597 -0.005304 -0.005528 -0.014239 0.026793 0.014177 DJ_return_lag1 0.143388 1,000000 0.143365 -0.003752 -0.005278 -0.005428 0.021996 0.026778 DJ_return_lag2 -0.003597 0.143365 1,000000 0.143336 -0.003744 -0.005249 0.017013 0.021991 DJ_return_lag3 -0.005304 -0.003752 0.143336 1,000000 0.143389 -0.003602 0.011547 0.016992 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1,000000 0.143372 0.000350 0.011551 DJ_return_lag5 -0.014239 -0.005428 -0.005249 -0.003602 0.143372 1,000000 -0.06393 1,00000 log_volatility_lag5 0.026773 0.021991 0.016992 0.011551 0.00366 0.980054 1,00000 log_volatility_lag2 0.013557 0.014163 0.026773 0.021972 0.016995 0.011565 0.960890</th></th<></th></th<>	DJ_return 1.000000 0.143388 -0.003597 -0.005304 -0.005528 -0.014239 DJ_return_lag1 0.143388 1.000000 0.143365 -0.003752 -0.005278 -0.005428 DJ_return_lag2 -0.003597 0.143365 1.000000 0.143336 -0.003744 -0.005249 DJ_return_lag3 -0.005304 -0.003752 0.143336 1.000000 0.143389 -0.003602 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1.000000 0.143372 DJ_return_lag5 -0.014239 -0.005278 -0.003744 0.143389 1.000000 0.143372 1.000000 log_volatility 0.026793 0.021996 0.017013 0.011547 0.000350 -0.006393 log_volatility_lag1 0.014177 0.026778 0.021991 0.016992 0.011551 0.00366 log_volatility_lag3 0.010581 0.013561 0.014164 0.026780 0.021972 0.016995 0.011565 log_volume_lag4 0.00802 0.211669	DJ_return 1,00000 0,143388 -0,003597 -0,005304 -0,005528 -0,014239 0,026793 DJ_return_lag1 0,143388 1,00000 0,143365 -0,003752 -0,005278 -0,005428 0,021996 DJ_return_lag2 -0,003597 0,143365 1,000000 0,143336 -0,003744 -0,005249 0,017013 DJ_return_lag3 -0,005528 -0,005278 -0,003744 0,143389 1,000000 0,143372 0,00350 DJ_return_lag4 -0,005528 -0,005278 -0,003744 0,143389 1,000000 0,143372 0,000350 DJ_return_lag5 -0,014239 -0,005428 -0,005249 -0,003602 0,143372 1,000000 -0,006393 log_volatility 0,026793 0,021996 0,017013 0,011547 0,000350 -0,006393 1,000000 log_volatility_lag2 0,014163 0,026773 0,021972 0,016993 0,011565 0,960890 log_volatility_lag3 0,010581 0,013561 0,014164 0,026780 0,021972 <th< th=""><th>DJ_return 1,000000 0.143388 -0.003597 -0.005304 -0.005528 -0.014239 0.026793 0.014177 DJ_return_lag1 0.143388 1,000000 0.143365 -0.003752 -0.005278 -0.005428 0.021996 0.026778 DJ_return_lag2 -0.003597 0.143365 1,000000 0.143336 -0.003744 -0.005249 0.017013 0.021991 DJ_return_lag3 -0.005304 -0.003752 0.143336 1,000000 0.143389 -0.003602 0.011547 0.016992 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1,000000 0.143372 0.000350 0.011551 DJ_return_lag5 -0.014239 -0.005428 -0.005249 -0.003602 0.143372 1,000000 -0.06393 1,00000 log_volatility_lag5 0.026773 0.021991 0.016992 0.011551 0.00366 0.980054 1,00000 log_volatility_lag2 0.013557 0.014163 0.026773 0.021972 0.016995 0.011565 0.960890</th></th<>	DJ_return 1,000000 0.143388 -0.003597 -0.005304 -0.005528 -0.014239 0.026793 0.014177 DJ_return_lag1 0.143388 1,000000 0.143365 -0.003752 -0.005278 -0.005428 0.021996 0.026778 DJ_return_lag2 -0.003597 0.143365 1,000000 0.143336 -0.003744 -0.005249 0.017013 0.021991 DJ_return_lag3 -0.005304 -0.003752 0.143336 1,000000 0.143389 -0.003602 0.011547 0.016992 DJ_return_lag4 -0.005528 -0.005278 -0.003744 0.143389 1,000000 0.143372 0.000350 0.011551 DJ_return_lag5 -0.014239 -0.005428 -0.005249 -0.003602 0.143372 1,000000 -0.06393 1,00000 log_volatility_lag5 0.026773 0.021991 0.016992 0.011551 0.00366 0.980054 1,00000 log_volatility_lag2 0.013557 0.014163 0.026773 0.021972 0.016995 0.011565 0.960890

```
0.200
0.175
0.150
0.125
0.100
0.075
0.050
0.025
0.000
```



Data split

Baseline Method

```
In [25]: r2_train_strawman = r2_score(y_other, X_other['log_volume_lag1'])
    print('Strawman train R2:', r2_train_strawman)

Strawman train R2: 0.4199386914132621

In [28]: r2_test_strawman = r2_score(y_test, X_test['log_volume_lag1'])
    print('Strawman test R2:', r2_test_strawman)

Strawman test R2: 0.18026287838158628
```

Elastic net

```
In [384... enet = ElasticNet(
    alpha = 1.0,
```

```
l1_ratio = 0.5,
            max_iter = 1000,
            warm_start = True,
            random_state = 425,
('model', enet)
         ])
         enet_pipe
Out[31]: Pipeline
          ▶ StandardScaler
            ▶ ElasticNet
In [32]: alpha_grid = np.logspace(start = -7, stop = 2, num = 20)
         11_ratio_grid = np.logspace(start = 0.0, stop = 1.0, num = 20)
         enet_params = {
             'model__alpha': alpha_grid,
            'model__l1_ratio': l1_ratio_grid
         enet params
Out[32]: {'model_alpha': array([1.00000000e-07, 2.97635144e-07, 8.85866790e-07, 2.63665090e-06,
                7.84759970e-06, 2.33572147e-05, 6.95192796e-05, 2.06913808e-04,
                6.15848211e-04, 1.83298071e-03, 5.45559478e-03, 1.62377674e-02,
                4.83293024e-02, 1.43844989e-01, 4.28133240e-01, 1.27427499e+00,
                3.79269019e+00, \ 1.12883789e+01, \ 3.35981829e+01, \ 1.000000000e+02]),
         In [33]: enet_search = GridSearchCV(
            enet_pipe,
            enet_params,
            cv = TimeSeriesSplit(5),
            scoring = 'r2',
            refit = True
In [43]: tic = time.time()
         enet_search.fit(X_other, y_other)
         toc = time.time()
         print('Execution time:', toc-tic, 'seconds')
         Execution time: 9.677505493164062 seconds
In [83]: cv_res_enet = pd.DataFrame({
           "alpha": enet_search.cv_results_['param_model__alpha'],
           "r2": enet_search.cv_results_["mean_test_score"]
         plt.figure()
         sns.relplot(
          data = cv_res_enet,
          x = "alpha",
y = "r2"
          ).set(
            xlabel = "alpha",
            ylabel = "R^2",
xscale = "log"
         plt.show()
         <Figure size 432x288 with 0 Axes>
```

```
0.5

0.4

0.3

0.2

0.1

0.0

10<sup>-6</sup>

10<sup>-4</sup>

10<sup>-2</sup>

10<sup>0</sup>

10<sup>2</sup>

alpha
```

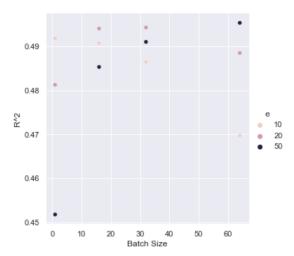
Multilayer Perceptron

mlp_pipe,

```
In [383... | mlp = MLPRegressor(
             hidden_layer_sizes = (10, 5),
             activation = 'tanh',
             solver = 'adam',
             batch_size = 16,
warm_start = True,
             random_state = 425
 In [98]: mlp_pipe = Pipeline(steps = [
                ('std', scalar),
                ('model', mlp)
           ])
           mlp_pipe
 Out[98]:
                 Pipeline
            ▶ StandardScaler
              ▶ MLPRegressor
 In [99]: hls_grid = [(5), (10), (12), (10, 5), (12, 6), (20, 10)]
bs_grid = [1, 5, 10, 12, 16, 20, 24, 28]
            mlp_params = {
              "model__hidden_layer_sizes": hls_grid,
              "model__batch_size": bs_grid
           mlp_params
Out[99]: {'model_hidden_layer_sizes': [5, 10, 12, (10, 5), (12, 6), (20, 10)],
             'model__batch_size': [1, 5, 10, 12, 16, 20, 24, 28]}
In [100...
          mlp_search = GridSearchCV(
```

```
mlp_params,
                cv = TimeSeriesSplit(5),
                scoring = 'r2',
                refit = True,
In [101...
          tic = time.time()
           mlp_search.fit(X_other, y_other)
           toc = time.time()
           print('Execution time:', toc-tic, 'seconds')
           Execution time: 735.2154622077942 seconds
In [102...
          cv_res_mlp = pd.DataFrame({
             "bs": np.array(mlp_search.cv_results_["param_model__batch_size"]),
"r2": mlp_search.cv_results_["mean_test_score"],
             "hls": mlp_search.cv_results_["param_model__hidden_layer_sizes"]
           plt.figure()
           sns.relplot(
             # kind = "line",
             data = cv_res_mlp,
             x = "bs",
             y = "r2"
             hue = "h1s"
             ).set(
                # xscale = "log",
               xlabel = "Batch Size",
               ylabel = "R^2"
           plt.show()
           <Figure size 432x288 with 0 Axes>
              0.52
              0.51
              0.50
           R^{\Lambda}2
                                                                   10
                                                                   12
              0.49
                                                                   (10, 5)
                                                                   (12, 6)
                                                                   (20, 10)
              0.48
              0.47
                  0
                          5
                                                      25
                                    Batch Size
In [103...
           r2_mlp_cv = mlp_search.best_score_
           r2_mlp_cv
           0.523593962772549
Out[103]:
          r2_mlp_tr = r2_score(
In [104...
               y_other,
                mlp_search.best_estimator_.predict(X_other)
           r2_mlp_tr
Out[104]: 0.5749142600453868
           r2_mlp_ts = r2_score(
In [105...
               y_test,
                mlp_search.best_estimator_.predict(X_test)
           r2_mlp_ts
Out[105]: 0.40707935871836953
           LSTM
          def lstm_data(data, lags):
In [302...
               X = np.zeros((len(data) - lags, lags, 1))
                y = data[lags:]
                for i in range(len(y)):
```

```
X[i] = data[i:i+lags].values.reshape(-1, 1)
               return X, y
           lags = 5
           X_other_lstm, y_other_lstm = lstm_data(nyse_other['log_volume'], lags)
           X_test_lstm, y_test_lstm = lstm_data(nyse_test['log_volume'], lags)
         X_other_lstm_scaled = scalar.fit_transform(X_other_lstm.reshape(-1, lags)).reshape(-1, lags, 1)
In [318...
           X_test_lstm_scaled = scalar.transform(X_test_lstm.reshape(-1, lags)).reshape(-1, lags, 1)
           y_other_lstm_scaled = scalar.fit_transform(y_other_lstm.values.reshape(-1, 1)).reshape(-1)
          y_test_lstm_scaled = scalar.transform(y_test_lstm.values.reshape(-1, 1)).reshape(-1)
In [359...
          def create_model():
               model = Sequential()
               model.add(LSTM(50, input_shape=(X_other_lstm_scaled.shape[1], X_other_lstm_scaled.shape[2]), activation='tanh'))
               model.add(Dense(1, activation='tanh'))
               model.compile(loss='mean_squared_error', optimizer='adam')
In [360... | lstm = KerasRegressor(build_fn=create_model, verbose=0)
          <keras.wrappers.scikit_learn.KerasRegressor at 0x1e7d67d3e20>
Out[360]:
In [361...
          lstm pipe = Pipeline(steps = [
              ('model', lstm)
           1stm_pipe
                Pipeline
Out[361]:
            ▶ KerasRegressor
In [369...
         e_grid = [10, 20, 50]
           bs_grid = [1, 16, 32, 64]
           lstm_params = {
               'model__epochs': e_grid,
               'model__batch_size': bs_grid
           1stm_params
Out[369]: {'model_epochs': [10, 20, 50], 'model_batch_size': [1, 16, 32, 64]}
In [370... lstm_search = GridSearchCV(
               lstm_pipe,
              lstm_params,
              cv = TimeSeriesSplit(5),
              scoring = 'r2',
               n_jobs= -1,
               verbose= 1,
               refit = True,
In [371...
         tic = time.time()
           lstm_search.fit(X_other_lstm_scaled, y_other_lstm_scaled)
           toc = time.time()
           print('Execution time:', toc-tic, 'seconds')
          Fitting 5 folds for each of 12 candidates, totalling 60 fits
          Execution time: 1688.1097552776337 seconds
In [372...
         cv_res_lstm = pd.DataFrame({
            "bs": np.array(lstm_search.cv_results_["param_model__batch_size"]),
"r2": lstm_search.cv_results_["mean_test_score"],
            "e": lstm_search.cv_results_["param_model__epochs"]
           plt.figure()
           sns.relplot(
            # kind = "line",
            data = cv_res_lstm,
            x = "bs",
            y = "r2"
            hue = "e'
               # xscale = "log",
               xlabel = "Batch Size",
               ylabel = "R^2"
           plt.show()
```



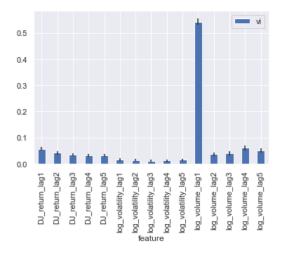
```
In [373...
         r2_lstm_cv = lstm_search.best_score_
          r2_lstm_cv
          0.49535823048267325
          r2_lstm_tr = r2_score(
In [374...
              y_other_lstm_scaled,
              lstm_search.best_estimator_.predict(X_other_lstm_scaled)
          r2 1stm tr
Out[374]: 0.5126004371056312
In [375...
          r2_lstm_ts = r2_score(
              y_test_lstm_scaled,
              lstm_search.best_estimator_.predict(X_test_lstm_scaled)
          r2_1stm_ts
          0.35193385562715396
Out[375]:
```

rf_params,

cv = TimeSeriesSplit(5), scoring = 'r2',

```
Random Forest
In [264...
         rf = RandomForestRegressor(
           n_estimators = 100,
criterion = 'squared_error',
            max_features = 'sqrt',
            oob_score = True,
            warm_start = True,
            random_state = 425
In [108...
          rf_pipe = Pipeline(steps = [
            ("model", rf)
            ])
          rf_pipe
Out[108]: •
                    Pipeline
           ▶ RandomForestRegressor
In [125...
          B_grid = np.linspace(start = 100, stop = 500, num = 15, dtype=int)
           m_grid = ['sqrt', 'log2', 1.0]
          rf_params = {
             "model__n_estimators": B_grid,
             "model__max_features": m_grid
          rf_params
Out[125]: {'model_n_estimators': array([100, 128, 157, 185, 214, 242, 271, 300, 328, 357, 385, 414, 442,
           'model__max_features': ['sqrt', 'log2', 1.0]}
         rf_search = GridSearchCV(
In [126...
              rf_pipe,
```

```
refit = True
In [127...
           tic = time.time()
            rf_search.fit(X_other, y_other)
            toc = time.time()
            print('Execution time:', toc-tic, 'seconds')
           Execution time: 1552.903362751007 seconds
In [128... cv_res = pd.DataFrame({
              "B": np.array(rf_search.cv_results_["param_model__n_estimators"]),
             "r2": rf_search.cv_results_["mean_test_score"],
"m": rf_search.cv_results_["param_model__max_features"]
            plt.figure()
            sns.relplot(
             # kind = "line",
              data = cv_res,
             x = "B",
y = "r2",
              hue = "m",
              ).set(
                xlabel = "B",
ylabel = "R^2"
            plt.show()
            <Figure size 432x288 with 0 Axes>
              0.534
              0.532
            ° 0.530
€
                                                                   sqrt
                                                                    log2
                                                                    1.0
              0.528
              0.526
                     100
                              200
                                        300
                                                  400
                                                           500
                                         В
In [129...
          r2_rf_cv = rf_search.best_score_
            r2_rf_cv
Out[129]: 0.5351289417184615
           rf_vi_df = pd.DataFrame({
In [130...
              "feature": X_other.columns,
              "vi": rf_search.best_estimator_['model'].feature_importances_,
             "vi_std": np.std([tree.feature_importances_ for tree in rf_search.best_estimator_['model'].estimators_], axis = 0)
             })
            plt.figure()
            rf_vi_df.plot.bar(x = "feature", y = "vi", yerr = "vi_std")
            plt.xticks(rotation = 90);
            plt.show()
            <Figure size 432x288 with 0 Axes>
```



Boosting

```
Pipeline

→ model: XGBRegressor

→ estimator: DecisionTreeRegressor

→ DecisionTreeRegressor
```

```
In [157... d_grid = [
    DecisionTreeRegressor(max_depth = 1),
    DecisionTreeRegressor(max_depth = 2),
    DecisionTreeRegressor(max_depth = 3),
    DecisionTreeRegressor(max_depth = 4)
    ]
    B_grid = np.linspace(start = 30, stop = 200, num = 20, dtype=int)
    lambda_grid = np.linspace(start = 0, stop = 1, num = 6)
    xgb_params = {
        "model__estimator": d_grid,
        "model__n_estimators": B_grid,
        "model__learning_rate": lambda_grid
    }
    xgb_params
```

```
Out[157]: {'model__estimator': [DecisionTreeRegressor(max_depth=1),
            DecisionTreeRegressor(max_depth=2),
            DecisionTreeRegressor(max_depth=3),
            DecisionTreeRegressor(max_depth=4)],
            'model__n_estimators': array([ 30, 38, 47, 56, 65, 74, 83, 92, 101, 110, 119, 128, 137,
                  146, 155, 164, 173, 182, 191, 200]),
            'model__learning_rate': array([0. , 0.2, 0.4, 0.6, 0.8, 1. ])}
          xgb_search = GridSearchCV(
In [158...
              xgb_pipe,
               xgb_params,
               cv = TimeSeriesSplit(5),
              scoring = 'r2',
               refit = True
In [159...
         tic = time.time()
           xgb_search.fit(X_other, y_other)
           toc = time.time()
           print('Execution time:', toc-tic, 'seconds')
           Execution time: 1512.7632925510406 seconds
         xgb_cv_res = pd.DataFrame({
In [160...
             "B": np.array(xgb_search.cv_results_["param_model__n_estimators"]),
            "r2": xgb_search.cv_results_["mean_test_score"],
            "lambda": xgb_search.cv_results_["param_model__learning_rate"],
            "depth": xgb_search.cv_results_["param_model__estimator"],
            })
           plt.figure()
           sns.relplot(
             # kind = "line",
            data = xgb_cv_res,
            x = "B"
             y = "r2",
             hue = "lambda",
            style = "depth"
            ).set(
               xlabel = "B",
              ylabel = "R^2"
           plt.show()
           <Figure size 432x288 with 0 Axes>
                 *****************
             n
                                                         lambda
             -1
                                                         0.0
                                                         0.2
                                                        0.4
                                                        • 0.60000000000000001
                                                        • 0.8
                                                         • 1.0
                                                         depth
             -3

    DecisionTreeRegressor(max_depth=1)

                                                           DecisionTreeRegressor(max_depth=2)
                                                           DecisionTreeRegressor(max_depth=3)
             -4
                                                           DecisionTreeRegressor(max_depth=4)
             -5
                25
                    50 75 100
                                   125 150 175 200
In [161...
          r2_xgb_cv = xgb_search.best_score_
           r2_xgb_cv
Out[161]: 0.5031755488035357
In [162...
          r2_xgb_tr = r2_score(
              y_other,
               xgb_search.best_estimator_.predict(X_other)
           r2_xgb_tr
Out[162]: 0.7920584557040472
In [163...
          r2_xgb_ts = r2_score(
              y_test,
               xgb_search.best_estimator_.predict(X_test)
```

```
)
r2_xgb_ts

0.3841513684639135
```

Comparison

```
        Out[381]:
        Model
        CV R^2
        Test R^2

        0
        Baseline
        0.419939
        0.180263

        1
        ENet
        0.556290
        0.412891

        2
        MLP
        0.523594
        0.407079

        3
        LSTM
        0.495358
        0.351934

        4
        Random Forest
        0.535129
        0.400074

        5
        Boosting
        0.503176
        0.384151
```

Elastic Net is has both the highest cross-validation and test R squared.

```
In []:
```