

Personalization with Unobserved Heterogeneity

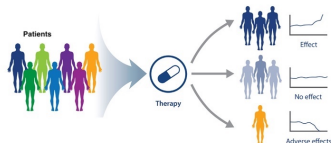
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RBC Royal Bank

Motivation for Personalization

- Personalization is founded on the premise that individuals have heterogeneous responses to actions.
- Personalization algorithms aim to improve decision-making by identifying and exploiting this heterogeneity.

Non-Personalized Paradigm



Personalized Paradigm



Unobserved and Heterogeneous Confounders

- Treatment effect (T) varies according to the value of unobserved confounders (U).

$$T := f(U) + N_T$$

$$Y := f(T, U, \mathbf{T} \times \mathbf{U}) + N_Y$$

- Likely the norm in observational settings.

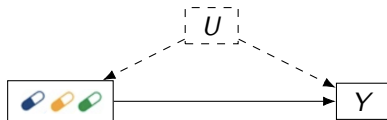


Figure: Observational setting.

Motivating Questions

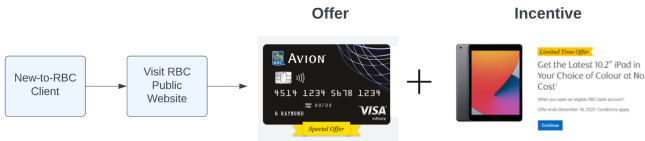
Given the high-level goal of personalization, and the context of unobserved heterogeneity:

- Alternatives to how I formulate this problem? For instance, what is a suitable causal estimand?
- What data do I need for identification?
- Is experimental data 'gold standard'?

Out-of-scope: Estimation (e.g., compare different estimators).

Motivating Example

- **Business objective:** Sell a credit card to new-to-RBC clients.
- **Current campaign.** All new-to-RBC clients who visited the RBC public site get a credit card offer + iPad incentive.



- **Business Goal: Personalize the incentive.** Identify which new-to-RBC clients should receive an iPad incentive in the future to maximize the expected profitability of the campaign.

Data Generating Process

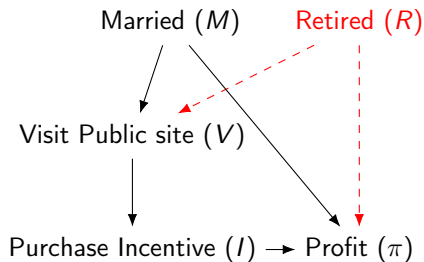


Figure: Observational setting.

Data Generating Process

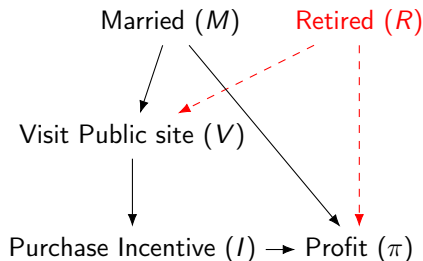


Figure: Observational setting.

$$P(R = 1) = 0.5, \quad P(M = 1) = 0.5$$

$$V := M \oplus R$$

$$I := V$$

	$R = 0$		$R = 1$	
	$M = 1$	$M = 0$	$M = 1$	$M = 0$
$I = 1$	0.25	0.50	0.45	0.05
$I = 0$	0.50	0.10	0.05	0.30

Table: $E[\pi|M, R, I]$. Highlighted cells reflect (new-to-RBC) client's 'natural' choice to visit the Public site or not.

Four Approaches to Personalizing the Incentive

Business Goal: Identify which new-to-RBC clients should receive an iPad incentive in the future to maximize the expected profitability of the campaign.

Data Scientist 1



Data Scientist 2



Data Scientist 3



Data Scientist 4



1. Associational Inference

$$D_{AI}^*(M) = \operatorname{argmax}_{I \in \{0,1\}} E[\pi | I, M]$$

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$$E[\pi|I = 1, M = 0] = 0.05$$

$$E[\pi|I = 0, M = 0] = 0.10$$

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Decision Rule:

- If Visit Site \wedge Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 0.25$
- If Visit Site \wedge Not Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 0.30$

Expected profit = $\boxed{0.275} = (0.25+0.30)/2$.

2. Interventional Inference + Post-Visit Randomization

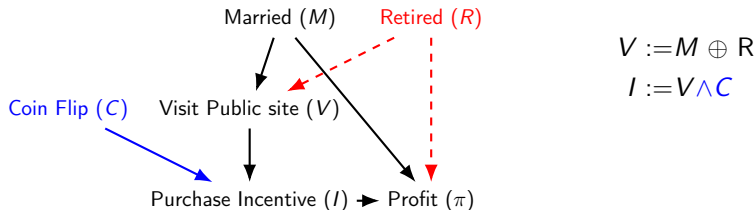


Figure: Causal DAG with post-visit randomization.

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Table: $E[\pi | M, R, I]$.

Decision Rule:

- If Visit Site \wedge Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = \mathbf{0.50}$
- If Visit Site \wedge Not Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = \mathbf{0.30}$

$$\text{Expected profit} = \boxed{0.40} = (0.50 + 0.30)/2.$$

3. Interventional Inference + Full Randomization

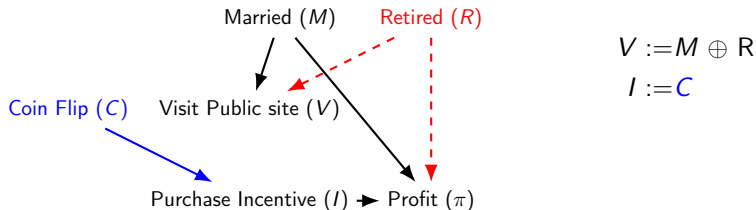


Figure: Causal DAG with A/B Test on all New-to-RBC clients.

3. Interventional Inference + Full Randomization

$$D_{\text{IFR}}^*(M) = \operatorname{argmax}_{I \in \{0,1\}} E[\pi | do(I), M]$$

$$E[\pi | do(I = 1), M = 1] = 0.350 = (0.25 + 0.45)/2$$

$$E[\pi | do(I = 0), M = 1] = 0.275 = (0.50 + 0.05)/2$$

$$E[\pi | do(I = 1), M = 0] = 0.275 = (0.50 + 0.05)/2$$

$$E[\pi | do(I = 0), M = 0] = 0.200 = (0.10 + 0.30)/2$$

	$R = 0$		$R = 1$	
	$M = 1$	$M = 0$	$M = 1$	$M = 0$
$I = 1$	0.25	0.50	0.45	0.05
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$I = 1$	0.25	0.50	0.45	0.05
$I = 0$	0.50	0.10	0.05	0.30

Table: $E[\pi | M, R, I]$.

Decision Rule:

- If Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = \mathbf{0.35}$
- If Not Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = \mathbf{0.275}$

$$\text{Expected profit} = \boxed{0.315} = (0.35 + 0.275)/2.$$

4. Counterfactual Inference

$$D_{CI}^*(M, I) = \operatorname{argmax}_{a' \in 0,1} E[\pi_{a'} | I = a, M]$$

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$$\begin{aligned} P(\pi_{a'}, M) &= P(\pi_{a'}, M, a') + P(\pi_{a'}, M, a) \\ &= P(\pi_{a'} | M, a') P(M, a') + P(\pi_{a'} | M, a) P(M, a) \end{aligned}$$

$$\begin{aligned} P(\pi_{a'} | M) &= P(\pi_{a'} | M, a') P(a' | M) + P(\pi_{a'} | M, a) P(a | M) \\ &= P(\pi | M, a') P(a' | M) + P(\pi_{a'} | M, a) P(a | M) \quad (\text{Consistency}) \end{aligned}$$

$$P(\pi_{a'} | M, a) = \frac{1}{P(a | M)} \left[P(\pi_{a'} | M) - P(\pi | M, a') P(a' | M) \right]$$

$$= \underbrace{\frac{1}{P(a | M)}}_{\text{observational}} \left[\underbrace{P(\pi | M, do(a'))}_{\text{experimental}} - \underbrace{P(\pi | M, a') P(a' | M)}_{\text{observational}} \right]$$

4. Counterfactual Inference

$$E(\pi_{I=1}|M=1, I=0) =$$

$$\begin{aligned} & \frac{1}{P(I=0|M=1)} \left[E(\pi|M=1, do(I=1)) - \right. \\ & \quad \left. E(\pi|M=1, I=1)P(I=1|M=1) \right] \\ &= \frac{1}{1/2} (0.350 - 0.25 \times 1/2) = 0.45 \\ &> 0.05 = E(\pi_{I=0}|M=1, I=0). \end{aligned}$$

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$$E(\pi_{I=0}|M=0, I=1) = 0.30$$

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$$E(\pi_{I=1}|M=0, I=0) = 0.50$$

$$E(\pi_{I=0}|M=1, I=1) = 0.50$$

$$E(\pi_{I=0}|M=0, I=1) = 0.30$$

Decision Rule:

- If Not Visit Site \wedge Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 0.45$
- If Not Visit Site \wedge Not Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 0.50$
- If Visit Site \wedge Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 0.50$
- If Visit Site \wedge Not Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 0.30$

$$\text{Expected profit} = 0.4375 = (0.45 + 0.50 + 0.50 + 0.30)/4.$$

Summary of Methods

Criterion	Decision Rule	$E[\pi]$
EDC	<ul style="list-style-type: none">• If Visit Site \wedge Married \rightarrow Purchase Incentive• If Visit Site \wedge Not Married \rightarrow No Purchase Incentive	.2750
PVR	Never Purchase Incentive	.4000
ABT	Always Purchase Incentive	.3150
RDC	<ul style="list-style-type: none">• If Visit Site \wedge Married \rightarrow No Purchase Incentive• If Visit Site \wedge Not Married \rightarrow No Purchase Incentive• If Not Visit Site \wedge Married \rightarrow Purchase Incentive• If Not Visit Site \wedge Not Married \rightarrow Purchase Incentive	.4375
Oracle		.4375

Remarks

- If the goal is to learn personalized actions, experimental data alone is sub-optimal in the presence of unobserved confounders.
- Combining experimental and observational data under a Regret Decision Criterion (RDC) can provide information about the unobserved confounders, and hence outperform alternative optimization criteria.
- The expression derived from RDC works only in the binary treatment case. RDC-type randomization (Forney et al., 2017) was proposed to estimate counterfactual expressions empirically from an arbitrary number of treatments.

Estimating Treatment Effects: **Personalized Paradigm**

- A/B Tests are 'gold standard' in the One-Treatment-Fits-All paradigm because they remove the influence of unobserved confounders (unmeasured variables that influence both the treatment and the outcome).
- In the presence of unobserved confounders, experimental data is not 'gold standard' for estimating heterogeneous treatment effects (required for personalization)
- Experiments 'destroy' information that can be valuable to identify the values of unobserved confounders.
- Counterfactual-based decision making, which leads to a fusion of experimental and observational data, might be optimal for personalization.

References

- Elias Bareinboim, Andrew Forney, and Judea Pearl. 2015. Bandits with unobserved confounders: a causal approach. In Proceedings of the 28th International Conference on Neural Information Processing Systems - Volume 1 (NIPS'15).
 - ▶ Implementation: <https://github.com/leoguelman/mabuc>
- Forney, A., Pearl, J. ; Bareinboim, E.. (2017). Counterfactual Data-Fusion for Online Reinforcement Learners. Proceedings of the 34th International Conference on Machine Learning, in Proceedings of Machine Learning Research 70:1156-1164