

Personalization with Unobserved Heterogeneity

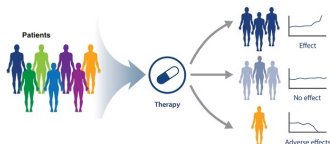
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RBC Royal Bank

Motivation for Personalization

- Personalization is founded on the premise that individuals have heterogeneous responses to actions.
- Personalization algorithms aim to improve decision-making by identifying and exploiting this heterogeneity.

Non-Personalized Paradigm



Personalized Paradigm



Unobserved and Heterogeneous Confounder (UHC)

- Treatment effect (T) varies according to the value of an unobserved confounder (U).

$$T := f(U) + N_T$$

$$Y := f(T, U, \mathbf{T} \times \mathbf{U}) + N_Y$$

- Presence of UHCs is arguably the most sensible assumption in practice.
- UHCs introduce challenges to personalization.

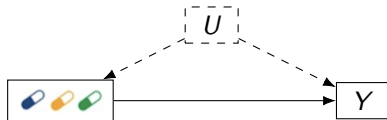


Figure: Observational setting.

Motivating Questions

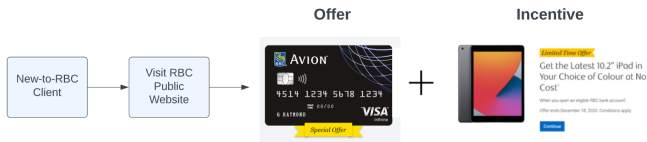
Given the goal of assigning the best treatment to each individual, and the context of UHCs:

- How should I express my objective function? What is a suitable causal estimand?
- What data do I need for identification?
- Is experimental data 'gold standard'?

Out-of-scope: Estimation (e.g., compare different estimators for personalization).

Business Setting

- **Business objective:** Sell a credit card to new-to-RBC clients.
- **Current campaign.** All new-to-RBC clients who visited the RBC public site get a credit card offer + iPad incentive.



- **Business Goal: Personalize the incentive.** Identify which new-to-RBC clients should receive an iPad incentive in the future to maximize the expected profitability of the campaign.

Data Generating Process

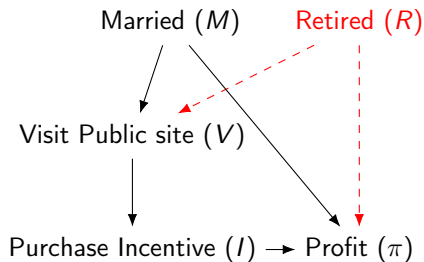


Figure: Observational setting.

Data Generating Process

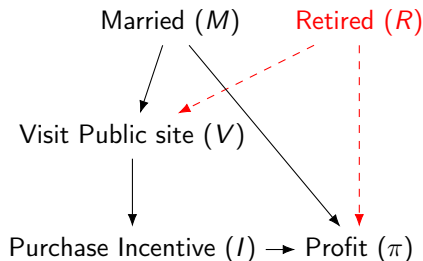


Figure: Observational setting.

$$P(R = 1) = 0.5, \quad P(M = 1) = 0.5$$

$$V := M \oplus R$$

$$I := V$$

	$R = 0$		$R = 1$	
	$M = 1$	$M = 0$	$M = 1$	$M = 0$
$I = 1$	25	50	45	5
$I = 0$	50	10	5	30

Table: $E[\pi|M, R, I]$. Highlighted cells reflect (new-to-RBC) client's 'natural' choice to visit the Public site or not.

Four Approaches to Personalizing the Incentive

Business Goal: Identify which new-to-RBC clients should receive an iPad incentive in the future to maximize the expected profitability of the campaign.

Data Scientist 1



Data Scientist 2



Data Scientist 3



Data Scientist 4



1. Associational Inference



$$\mathcal{D}_{\text{AI}}^*(M) = \operatorname{argmax}_{I \in \{0,1\}} E[\pi|I, M]$$

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$$E[\pi|I = 1, M = 1] = 25$$

$$E[\pi|I = 0, M = 1] = 5$$

$$E[\pi|I = 1, M = 0] = 5$$

$$E[\pi|I = 0, M = 0] = 10$$

	$R = 0$		$R = 1$	
	$M = 1$	$M = 0$	$M = 1$	$M = 0$
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$I = 1$	25	50	45	5
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Table: $E[\pi|M, R, I]$.

Decision Rule:

- If Visit Site \wedge Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 25$
- If Visit Site \wedge Not Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 30$

Expected profit = $\boxed{27.5} = (25+30)/2$.

2. Interventional Inference + Post-Visit Randomization

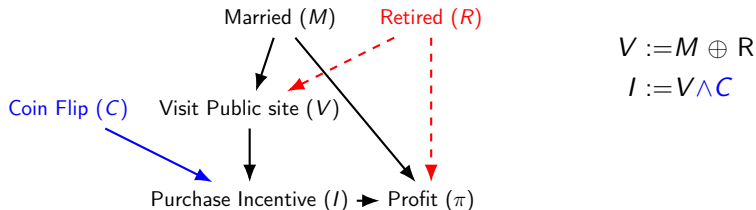


Figure: Causal DAG with post-visit randomization.

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$$E[\pi | \text{do}(I = 0), M = 1, V = 1] = 50$$

$$E[\pi | \text{do}(I = 1), M = 0, V = 1] = 5$$

$$E[\pi | \text{do}(I = 0), M = 0, V = 1] = 30$$

	$R = 0$		$R = 1$	
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	R = 0		R = 1	
	M = 1	M = 0	M = 1	M = 0
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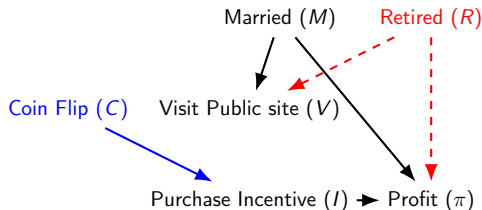
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Decision Rule:

- If Visit Site \wedge Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 50$
- If Visit Site \wedge Not Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 30$

Expected profit = $\boxed{40} = (50+30)/2$.

3. Interventional Inference + Full Randomization



$$V := M \oplus R$$

$$I := C$$

Figure: Causal DAG with Full Randomization.

3. Interventional Inference + Full Randomization



$$\mathcal{D}_{\text{IFR}}^*(M) = \operatorname{argmax}_{I \in \{0,1\}} E[\pi | do(I), M]$$

$$E[\pi | do(I = 1), M = 1] = 35.0 = (25 + 45)/2$$

$$E[\pi | do(I = 0), M = 1] = 27.5 = (50 + 5)/2$$

$$E[\pi | do(I = 1), M = 0] = 27.5 = (50 + 5)/2$$

$$E[\pi | do(I = 0), M = 0] = 20.0 = (10 + 30)/2$$

	$R = 0$		$R = 1$	
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	$R = 0$		$R = 1$	
	$M = 1$	$M = 0$	$M = 1$	$M = 0$
$I = 1$	25	50	45	5
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Table: $E[\pi | M, R, I]$.

Decision Rule:

- If Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 35$
- If Not Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 27.5$

$$\text{Expected profit} = \boxed{31.5} = (35 + 27.5)/2.$$

4. Regret Decision Criterion



Puzzled by $E[\pi|I, M] \neq E[\pi|do(I), M]$.

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$$\mathcal{D}_{\text{RDC}}^*(M, I) = \operatorname{argmax}_{a' \in 0,1} E[\pi_{I=a'}|I = a, M] \quad (1)$$

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Eq.1 is a population-level counterfactual known as the *Conditional Average Treatment Effect on the Treated* (CATT).

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Is this causal estimand identifiable?

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Is this causal estimand identifiable?

In general, identifiability of the CATT requires the causal graph (so I can condition on a set of covariates that satisfy the backdoor criterion).

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Is this causal estimand identifiable?

In general, identifiability of the CATT requires the causal graph (so I can condition on a set of covariates that satisfy the backdoor criterion).

An exception where we don't need the graph is when the treatment is binary and both experimental and observational data are available.

4. Regret Decision Criterion



$$\mathcal{D}_{\text{RDC}}^*(M, I) = \operatorname{argmax}_{a' \in 0,1} E[\pi_{a'} | I = a, M]$$

$$\begin{aligned} P(\pi_{a'}, M) &= P(\pi_{a'}, M, a') + P(\pi_{a'}, M, a) \\ &= P(\pi_{a'} | M, a')P(M, a') + P(\pi_{a'} | M, a)P(M, a) \end{aligned}$$

$$\begin{aligned} P(\pi_{a'} | M) &= P(\pi_{a'} | M, a')P(a' | M) + P(\pi_{a'} | M, a)P(a | M) \\ &= P(\pi | M, a')P(a' | M) + P(\pi_{a'} | M, a)P(a | M) \text{ (Consistency)} \end{aligned}$$

$$P(\pi_{a'} | M, a) = \frac{1}{P(a | M)} \left[P(\pi_{a'} | M) - P(\pi | M, a')P(a' | M) \right]$$

$$= \underbrace{\frac{1}{P(a | M)}}_{\text{observational}} \left[\overbrace{P(\pi | M, do(a'))}^{\text{experimental}} - \underbrace{P(\pi | M, a')P(a' | M)}_{\text{observational}} \right]$$

4. Regret Decision Criterion



$$E(\pi_{I=1}|M=1, I=0) =$$

$$\begin{aligned} & \frac{1}{P(I=0|M=1)} \left[E(\pi|M=1, do(I=1)) - \right. \\ & \quad \left. E(\pi|M=1, I=1)P(I=1|M=1) \right]. \\ & = \frac{1}{1/2} (35 - 25 \times 1/2) = 45 \\ & > 5 = E(\pi_{I=0}|M=1, I=0). \end{aligned}$$

$$E(\pi_{I=1}|M=0, I=0) = 50$$

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	R = 0		R = 1	
	M = 1	M = 0	M = 1	M = 0
I = 1	25	50	45	5
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Table: $E[\pi|M, R, I]$.

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$$E(\pi_{I=1}|M=0, I=0) = 50$$

$$E(\pi_{I=0}|M=1, I=1) = 50$$

$$E(\pi_{I=0}|M=0, I=1) = 30$$

Decision Rule:

- If Not Visit Site \wedge Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 45$
- If Not Visit Site \wedge Not Married \rightarrow Purchase Incentive $\rightarrow E[\pi] = 50$
- If Visit Site \wedge Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 50$
- If Visit Site \wedge Not Married \rightarrow No Purchase Incentive $\rightarrow E[\pi] = 30$

$$\text{Expected profit} = \boxed{43.75} = (45 + 50 + 50 + 30)/4.$$

	R = 0		R = 1	
	M = 1	M = 0	M = 1	M = 0
I = 1	25	50	45	5
I = 0	50	10	5	30

Table: $E[\pi|M, R, I]$.

Summary of Methods

Criterion	Decision Rule	$E[\pi]$
\mathcal{D}_{AI}	<ul style="list-style-type: none"> • If Visit Site \wedge Married \rightarrow Purchase Incentive • If Visit Site \wedge Not Married \rightarrow No Purchase Incentive 	27.50
\mathcal{D}_{IPVR}	Never Purchase Incentive	40.0
\mathcal{D}_{IFR}	Always Purchase Incentive	31.50
\mathcal{D}_{RDC}	<ul style="list-style-type: none"> • If Visit Site \wedge Married \rightarrow No Purchase Incentive • If Visit Site \wedge Not Married \rightarrow No Purchase Incentive • If Not Visit Site \wedge Married \rightarrow Purchase Incentive • If Not Visit Site \wedge Not Married \rightarrow Purchase Incentive 	43.75
\mathcal{D}_{Oracle}		43.75

Remarks

- All approaches used population/sub-population level estimands. There's nothing personal about personalization!
- Experimental data are 'gold standard' in the non-personalized paradigm because they remove the influence of unobserved confounders.
- In the personalization paradigm with UHCs, experimental data are not necessarily 'gold standard' for identifying heterogeneous treatment effects:
 - ▶ Experiments 'destroy' uncoded knowledge about these confounders.
 - ▶ Interventional inference does not capture the information required to maximize payout.
- Counterfactual-based decision-making leads to a fusion of experimental and observational data, which might capture additional information about UHCs required to maximize payout.

Further Reading

- This presentation is fundamentally inspired by this paper:
 - ▶ Elias Bareinboim, Andrew Forney, and Judea Pearl. 2015. **Bandits with unobserved confounders: a causal approach**. In Proceedings of the 28th International Conference on Neural Information Processing Systems - Volume 1 (NIPS'15).
 - ▶ Implementation: <https://github.com/leoguelman/mabuc>.
- The expression derived from RDC works only in the binary treatment case.
 - ▶ RDC-type randomization (Forney et al., 2017) was proposed to estimate counterfactual expressions empirically from an arbitrary number of treatments.