

Arrays

Hello Everyone



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Space complexity:

maximum space that is utilised by your program at any given point of time.

int → 4 Bytes

long → 8 bytes

{
 int x=2; → 4B
 long y=1*3; → 8B
}

Total = 4B + 8B = 12 B
↓
Memory

O(1)



4B(x)

1. void fun(int N){
 int x = N; → 4B
 int y = 2*x; → 4B
 long z = x+y; → 8B
}

$$\begin{aligned} &= 4B + 4B + 8B \\ &= 16B \\ &= O(1) \end{aligned}$$

2. func(int N){ // 4 bytes → iIP

 int arr[10]; // 40 bytes
 int x; // 4 bytes
 int y; // 4 bytes
 long z; // 8 bytes
 int[] arr = new int[N]; // 4*N bytes
}

$$\begin{aligned} &= 40B + 4B + 4B + 8B + 4N \\ &= 56B + 4NB \\ &= (\cancel{56} + 4N) \text{ Byte} \\ &= 4N \\ SC &= O(N) \end{aligned}$$



3. void fun(int N){ **|| 4 bytes || → i/p**

 int x = N; **|| 4 bytes**

 int y = x*x; **|| 4 Bytes**

 long z = y+y; **|| 8 Byte**

 int[] arr = new int[N]; **|| 4*N Byte**

 long[][] b = new long[N][N]; **|| 8*N*N Byte**

}

$$= (4 + 4 + 8 + 4N + 8N^2) B$$

$$= \cancel{(16 + 4N + 8N^2)} B$$

$$= \cancel{8N^2}$$

SC = O(N^2).

* input and output will not be considered as space complexity.

4. int maxArr(int arr[], int N){

 int ans = arr[0]; **→ 4B → O/p**

 for(i=0; i<N; i++){

 ans = Max(ans, arr[i]);

$$= 4B$$

4B

}

 return ans;

}

4*N Bytes ↘ i/p
 4Bytes



Introduction to Arrays

$A = [\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 2 & 8 & 10 & 12 & 20 \end{matrix}]$

→ Continuous memory allocation.

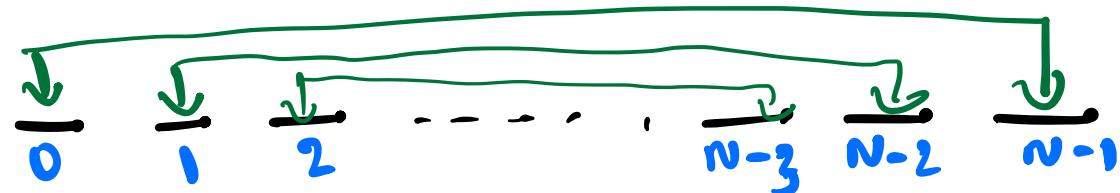
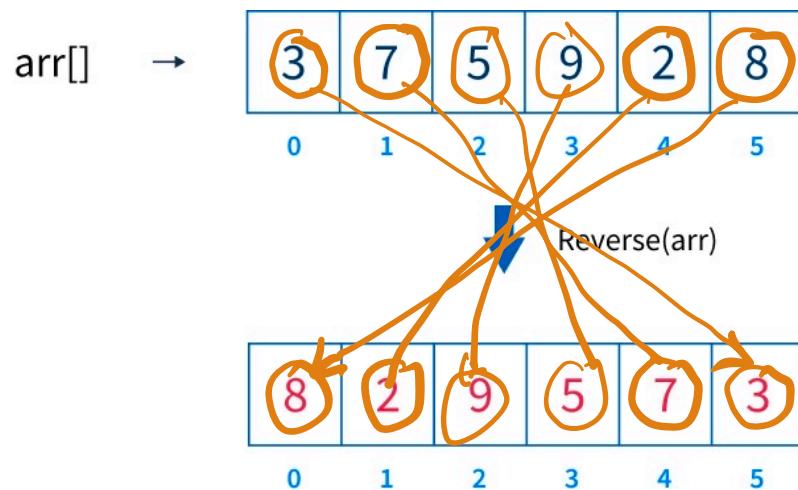
$A[2] \rightarrow (\text{addr. of } A) + (2 * 4B)$

< Question > : Print all elements of the array

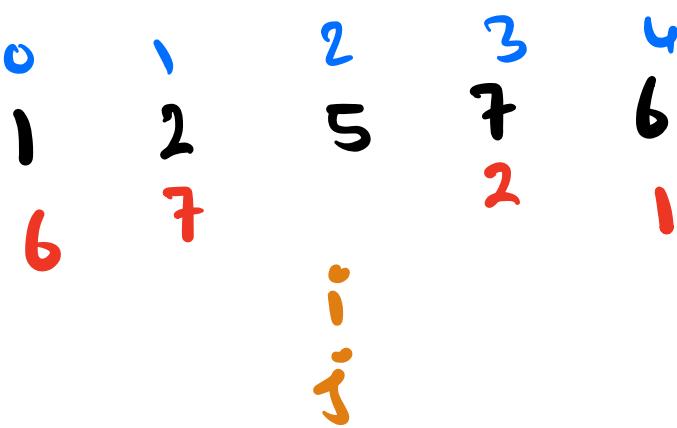
for i → 0 to N-1
print (A[i])
}



2. Reverse the given array



i < j





0	1	2	3	4	5
3	5	6	9	4	2
2	4	9	6	5	3

j i

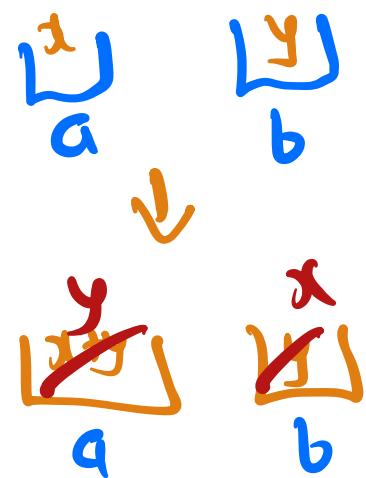
</> Code

```
i=0 , j=n-1  
while(i < j)  
{  
    temp = A[i];  
    A[i] = A[j];  
    A[j] = temp;  
    i++;  
    j--;  
}
```

TC: O(n)

SC: O(1)

swap a, b
without 3rd intv.



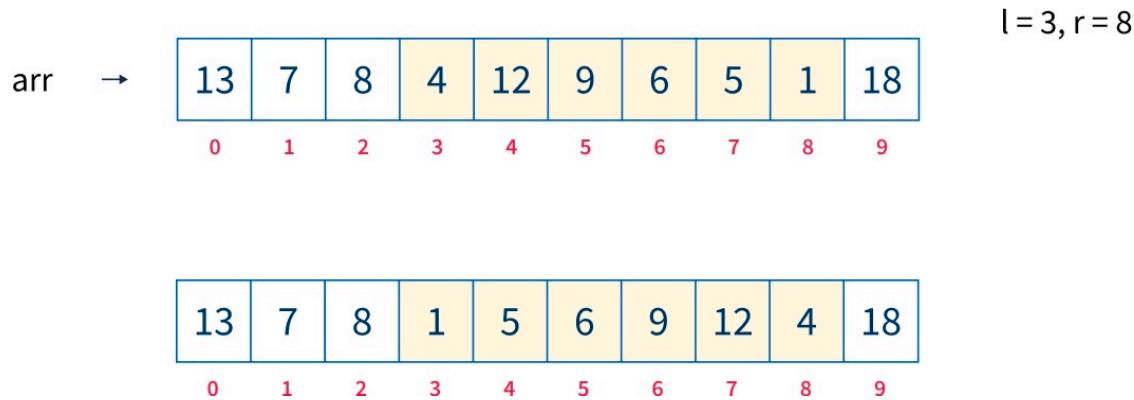
$$\begin{aligned}b &= a - b \\&= x + y - y\end{aligned}$$

$$b = x$$

$$\begin{aligned}a &= a - b \\&= x + y - x \\&= y\end{aligned}$$



3. Reverse part of an array



```
void reversePart(int []arr, int l, int r){
```

~~i = \cancel{l} , j = \cancel{r}~~

while ($i < j$)
{
 temp = arr[i];
 arr[i] = arr[j];
 arr[j] = temp;
 i++;
 j--;

```
}
```

TC: O(N)
SC: O(1)



Break : 10:16 PM

- * Given an array of size n , Rotate the array from right to left K times.

$N=7$

1	2	3	4	5	6	7
0	1	2	3	4	5	6

$K=1$

7	1	2	3	4	5	6
0	1	2	3	4	5	6

$K=2$

6	7	1	2	3	4	5
0	1	2	3	4	5	6

$K=3$

5	6	7	1	2	3	4
0	1	2	3	4	5	6

$K=4$

4	5	6	7	1	2	3
0	1	2	3	4	5	6



$A = [\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 9 & 5 & 2 & 8 & 2 & 3 & 6 & 5 \end{matrix}]$

$K = 3$

$[\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 9 & 4 & 2 & 8 & 1 & 3 & 6 & 5 \end{matrix}]$

$\downarrow 1^{st}$ rotation

$[\begin{matrix} 5 & 9 & 4 & 2 & 8 & 1 & 3 & 6 \end{matrix}]$

$\downarrow 2^{nd}$

$[\begin{matrix} 6 & 5 & 9 & 4 & 2 & 8 & 1 & 3 \end{matrix}]$

$\downarrow 3^{rd}$

[3 6 5 9 4 2 8]

$$A = [\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ 9 & 6 & 8 & 3 & 4 & 9 & 1 \end{matrix}]$$

K=1 1 9 6 8 3 4 9

K=2 9 1 9 6 8 3 4

K=3 4 9 1 9 6 8 3

$K = K \% N \leftarrow$ length of arr

for i → 1 to K

d temp = A[n-i]

for j → N-2 to 0

A[j+1] = A[j]

A[0] = temp

TC: O(N*K)

SC: O(1)

 $K=0$

5 3 7 9 1

 $K=1$

1 5 3 7 9

 $K=2$

9 1 5 3 7

 $K=3$

7 9 1 5 3

 $K=4$

3 7 9 1 5

 $K=5$

5 3 7 9 1

 $K=6$

1 5 3 7 9

 $K=7$

9 1 5 3 7

length
of arr
↓

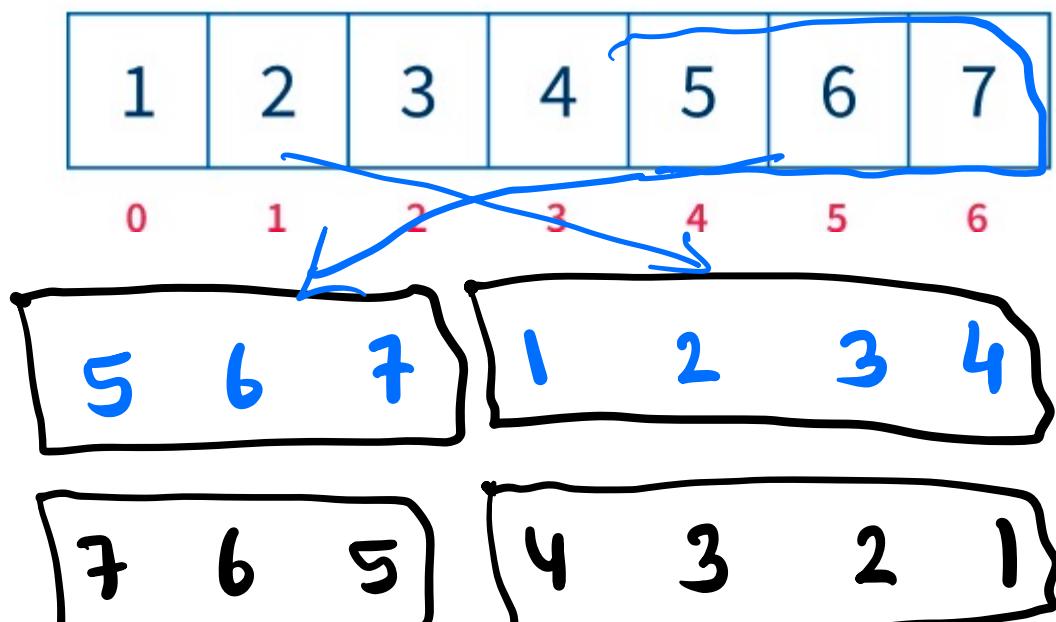
$K = K \% N$

$N=5$

K	0	5	10	15
0	6	11	16	
1	7	12	17	
2	8	13	18	
3	9	14	19	

Optimisation

$N=7$



$K=3$

Reverse

→ A 0 K-1 K n-1

Steps →

$$K = K \times n$$

TC

- 1) Reverse (A, 0, n-1) $\rightarrow O(n)$
2) Reverse (A, 0, K-1) $\rightarrow O(K)$
3) Reverse (A, K, n-1) $\rightarrow O(n-K)$

$$\text{Total } TC = O(n + K + n - K)$$

$$= O(2n)$$
$$= O(n)$$

$$SC = O(1)$$

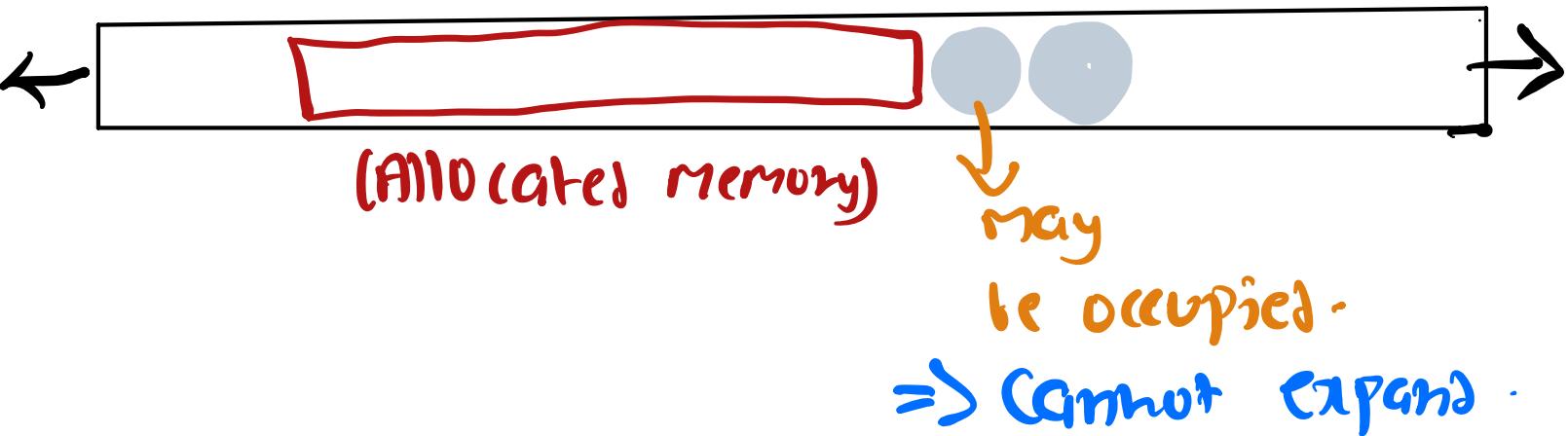
Dynamic Array:

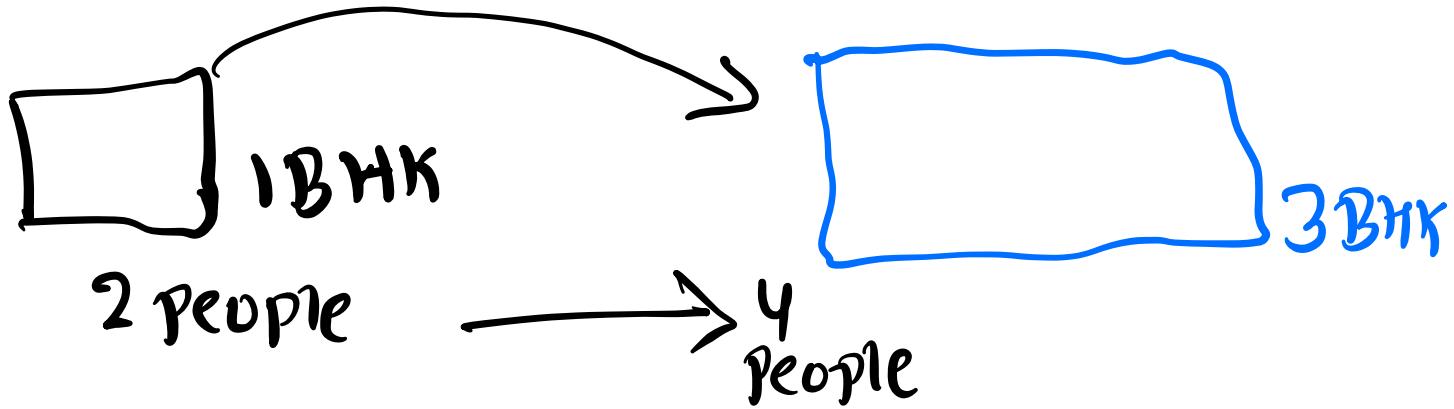
`int[] arr = new int[16]; // 10 length`
integer array will
be created.

Sometimes defining length at the start
might not be possible → dynamic
array.

Eg. Java arrayList
C++ vector
etc.

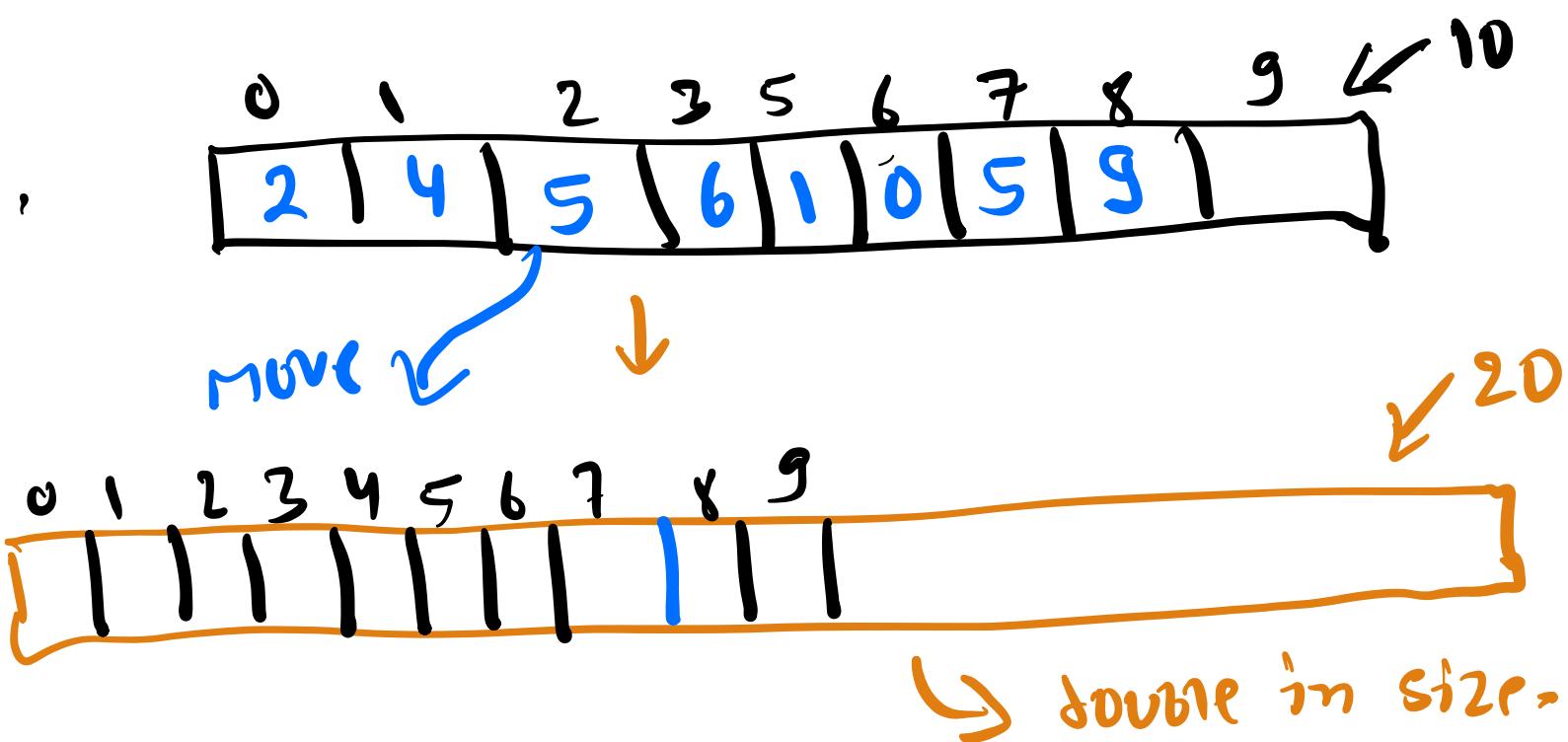
Memory:





Load factor: $(0.1) = 0.8$ (eg.)

Whenever 80% memory is occupied it double the size of a Memory.



if (current size * load factor) is full
find another location with double
size.

Doubt Session

Tausif

```
fun (int[][] arr, n)
```

1

$\downarrow \leftarrow O(1)$

```
return ans;
```

y

Vishal

```
for (int[] arr, int n)
```

|| $O(n)$
int[] arr;
computation.

$O(n)$

```
return ans;
```

$$SC: O(n^2)$$

$\mathcal{O}(n^2)$.

Sc: O(1)

$Sc: O(n)$

i=0 → a → 103

$$j=1 \rightarrow q \rightarrow 103$$

$i=2 \rightarrow a \rightarrow 103$



$\log n$ vs $n \log n$

```

for (i=0 ; i<=2N ; i++)
{
    int j = i
    while (j > 0)
    {
        j--;
    }
}

```

i	j	iteration
0	0	0
1	1	1
2	2[2]	2
3	3	3
4	4	4
50	50	50

$$\dots \cdot 2^N$$

$$2^N$$

$$2^N \swarrow \text{round off}$$

$$= 1 + 2 + 3 + \dots + 2^N$$

$$= \frac{2^n * (2^n + 1)}{2} \quad \left(\frac{n * (n+1)}{2} \right)$$

$$= \frac{4^n + 2^n}{2}$$

$$= \frac{4^n}{2} + \frac{2^n}{2}$$

$$\begin{array}{r} 0 \quad 1 \quad 2 \quad 3 \quad 4 \\ 1 \quad 3 \quad 5 \quad 7 \quad 9 \\ 3 \quad 1 \quad 5 \quad 7 \quad 9 \end{array}$$

$$i = 0$$

$$j = \underline{\underline{1}}$$

$$\begin{array}{c} 0 < 1 \\ \downarrow \quad \downarrow \\ 1 < 0 \quad X \end{array}$$

```
for(i=1; i<=n; i*=2)
```

2

```
    for(j=1; j<=n; j++)
```

{

j

i

1

2

j

[1 n]

[1 n]

iteration

n iterations

n iter

$$= 1 + 2t + 3t + 4t + \dots + t^{2^n}$$

$\Rightarrow x$

$$\frac{x * (x+1)}{2}$$

$$= \frac{x^2 + x}{2}$$

$$= \frac{x^2}{2} + \cancel{\frac{x}{2}} \rightarrow \text{lower order}$$

$$= x^2 * \cancel{\frac{1}{2}} \rightarrow \text{constant}$$

$$= x^2$$

x^2

$$= (2^n)^2 \quad \cancel{(2^3)}$$

$$= 4^n = (2 * 2 * 2)^2$$

$$= 2 * 2 * 2 * 2 * 2 * 2$$

$$= 4 * 4 * 4$$