One end of a light elastic string, of natural length a and modulus of elasticity  $\lambda mg$ , is attached to a fixed point O. The string lies on a smooth horizontal surface. A particle P of mass m is attached to the other end of the string. The particle P is projected in the direction OP. When the length of the string is  $\frac{4}{3}a$ , the speed of P is  $\sqrt{2ag}$ . When the length of the string is  $\frac{5}{3}a$ , the speed of P is  $\frac{1}{2}\sqrt{2ag}$ .

Find the value of  $\lambda$ . [4]