

(a) Express $3 \sin x + 2\sqrt{2} \cos\left(x + \frac{1}{4}\pi\right)$ in the form $R \sin(x + \alpha)$, where $R > 0$ and $0 < \alpha < \frac{1}{2}\pi$. State the exact value of R and give α correct to 3 decimal places. [4]

(b) Hence solve the equation

$$6 \sin \frac{1}{2}\theta + 4\sqrt{2} \cos\left(\frac{1}{2}\theta + \frac{1}{4}\pi\right) = 3$$

for $-4\pi < \theta < 4\pi$.

[5]