

Two uniform smooth spheres A and B of equal radii have masses m and km respectively. Sphere A is moving with speed u on a smooth horizontal surface when it collides with sphere B which is at rest. Immediately before the collision, A's direction of motion makes an angle θ with the line of centres (see diagram). The coefficient of restitution between the spheres is $\frac{1}{3}$.

(a) Show that the speed of B after the collision is
$$\frac{4u\cos\theta}{3(1+k)}$$
. [3]

70% of the total kinetic energy of the spheres is lost as a result of the collision.

(b) Given that
$$\tan \theta = \frac{1}{3}$$
, find the value of k .