

A company has two machines,  $A$  and  $B$ , which independently fill small bottles with a liquid. The volumes of liquid per bottle, in suitable units, filled by machines  $A$  and  $B$  are denoted by  $x$  and  $y$  respectively. A scientist at the company takes a random sample of 40 bottles filled by machine  $A$  and a random sample of 50 bottles filled by machine  $B$ . The results are summarised as follows.

$$\Sigma x = 1120 \quad \Sigma x^2 = 31400 \quad \Sigma y = 1370 \quad \Sigma y^2 = 37600$$

The population means of the volumes of liquid in the bottles filled by machines  $A$  and  $B$  are denoted by  $\mu_A$  and  $\mu_B$ .

- (a) Test at the 2% significance level whether there is any difference between  $\mu_A$  and  $\mu_B$ . [8]
- (b) Find the set of values of  $\alpha$  for which there would be evidence at the  $\alpha\%$  significance level that  $\mu_A - \mu_B$  is greater than 0.25. [4]