

A particle  $P$  moving in a straight line has displacement  $x$  m from a fixed point  $O$  on the line at time  $t$  s. The acceleration of  $P$ , in  $\text{ms}^{-2}$ , is given by  $\frac{200}{x^2} - \frac{100}{x^3}$  for  $x > 0$ . When  $t = 0$ ,  $x = 1$  and  $P$  has velocity  $10 \text{ ms}^{-1}$  directed towards  $O$ .

(a) Show that the velocity  $v \text{ ms}^{-1}$  of  $P$  is given by  $v = \frac{10(1-2x)}{x}$ . [5]

(b) Show that  $x$  and  $t$  are related by the equation  $e^{-40t} = (2x-1)e^{2x-2}$  and deduce what happens to  $x$  as  $t$  becomes large. [5]