

Let $f(x) = \frac{5x^2 + x + 27}{(2x + 1)(x^2 + 9)}$.

(i) Express $f(x)$ in partial fractions. [5]

(ii) Hence find $\int_0^4 f(x) \, dx$, giving your answer in the form $\ln c$, where c is an integer. [5]