

A bead of mass m moves on a smooth circular wire, with centre O and radius a, in a vertical plane. The bead has speed  $v_A$  when it is at the point A where OA makes an angle  $\alpha$  with the downward vertical through O, and  $\cos \alpha = \frac{3}{5}$ . Subsequently the bead has speed  $v_B$  at the point B, where OB makes an angle  $\theta$  with the upward vertical through O. Angle AOB is a right angle (see diagram). The reaction of the wire on the bead at B is in the direction OB and has magnitude equal to  $\frac{1}{6}$  of the magnitude of the reaction when the bead is at A.

Find, in terms of $m$ and $g$ , the magnitude of the reaction at $B$ .	[6]

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(b) Given	that $v_A = \sqrt{kag}$ , find	the value of $k$ .		[2]
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