

The diagram shows the curve $y = xe^{2x} - 5x$ and its minimum point M, where $x = \alpha$.

(a) Show that
$$\alpha$$
 satisfies the equation $\alpha = \frac{1}{2} \ln \left(\frac{5}{1 + 2\alpha} \right)$. [3]

- (b) Verify by calculation that α lies between 0.4 and 0.5.
- (c) Use an iterative formula based on the equation in part (a) to determine α correct to 2 decimal places. Give the result of each iteration to 4 decimal places.