

A uniform rod AB of length 2a and weight W rests against a smooth horizontal peg at a point C on the rod, where AC = x. The lower end A of the rod rests on rough horizontal ground. The rod is in equilibrium inclined at an angle of 45° to the horizontal (see diagram). The coefficient of friction between the rod and the ground is μ . The rod is about to slip at A.

(i) Find an expression for x in terms of a and μ . [5]

(ii) Hence show that
$$\mu \ge \frac{1}{3}$$
. [2]

(iii) Given that $x = \frac{3}{2}a$, find the value of μ and the magnitude of the resultant force on the rod at A.