

Two uniform smooth spheres A and B of equal radii have masses m and 2m respectively. The two spheres are moving with equal speeds u on a smooth horizontal surface when they collide. Immediately before the collision, A's direction of motion makes an angle of 60° with the line of centres, and B's direction of motion makes an angle θ with the line of centres (see diagram). The coefficient of restitution between the spheres is e.

After the collision, the component of the velocity of A along the line of centres is v and B moves perpendicular to the line of centres. Sphere A now has twice as much kinetic energy as sphere B.

(a) Show that
$$v = \frac{1}{2}u(4\cos\theta - 1)$$
. [1]

(b) Find the value of
$$\cos \theta$$
. [4]

(c) Find the value of
$$e$$
. [2]