The random variable X has probability generating function $G_X(t)$ given by

$$G_X(t) = ct(1+t)^5,$$

where c is a constant.

(a) Find the value of c.

(b) Find the value of E(X). [2]

The random variable Y is the sum of two independent values of X.

(c) Write down the probability generating function of Y and hence find Var(Y). [4]

(d) Find P(Y = 5).