The random variable X has probability generating function  $\mathbf{G}_{X}(t)$  given by

$$G_X(t) = ct(1+t)^5,$$

where c is a constant.

(a) Find the value of c. [1]

(b) Find the value of E(X). [2]

The random variable *Y* is the sum of two independent values of *X*.

(c) Write down the probability generating function of Y and hence find Var(Y). [4]

(d) Find P(Y = 5). [2]