A particle *P* is projected with speed $u \text{ m s}^{-1}$ at an angle θ above the horizontal from a point *O* and moves freely under gravity. After 5 seconds the speed of *P* is $\frac{3}{4}u$.

(a) Show that
$$\frac{7}{16}u^2 - 100u\sin\theta + 2500 = 0$$
. [3]

(b) It is given that the velocity of *P* after 5 seconds is perpendicular to the initial velocity.

Find, in either order, the value of u and the value of $\sin \theta$.

[5]