

A particle P is projected with speed $u \text{ m s}^{-1}$ at an angle of θ above the horizontal from a point O on a horizontal plane and moves freely under gravity. The horizontal and vertical displacements of P from O at a subsequent time t s are denoted by x m and y m respectively.

- (a) Starting from the equation of the trajectory given in the List of formulae (MF19), show that

$$y = x \tan \theta - \frac{gx^2}{2u^2}(1 + \tan^2 \theta). \quad [1]$$

When $\theta = \tan^{-1} 2$, P passes through the point with coordinates (10, 16).

- (b) Show that there is no value of θ for which P can pass through the point with coordinates (18, 30).
[6]