

A particle  $P$  is projected from a point  $O$  on horizontal ground. At the instant  $t$  s after projection, the horizontal and vertically upwards displacements of  $P$  from  $O$  are  $x$  m and  $y$  m respectively. The equation of the trajectory of  $P$  is  $y = 3x - 0.05x^2$ .

- (i) Find the angle of projection and the initial speed of  $P$ . [3]
- (ii) Find the coordinates of  $P$  at the instant when  $OP$  makes an angle of  $45^\circ$  with the horizontal. [2]
- (iii) For the instant when  $P$  is at its greatest height above the ground, calculate this height and the corresponding value of  $t$ . [4]