

A particle  $P$  of mass  $0.5 \text{ kg}$  is attached to one end of a light elastic string of natural length  $0.8 \text{ m}$  and modulus of elasticity  $16 \text{ N}$ . The other end of the string is attached to a fixed point  $O$ . The particle  $P$  is released from rest at the point  $0.8 \text{ m}$  vertically below  $O$ . When the extension of the string is  $x \text{ m}$ , the downwards velocity of  $P$  is  $v \text{ m s}^{-1}$  and a force of magnitude  $25x^2 \text{ N}$  opposes the motion of  $P$ .

(i) Show that, when  $P$  is moving downwards,  $v \frac{dv}{dx} = 10 - 40x - 50x^2$ . [2]

(ii) For the instant when  $P$  has its greatest downwards speed, find the kinetic energy of  $P$  and the elastic potential energy stored in the string. [6]