

A factory produces small bottles of natural spring water. Two different machines, X and Y , are used to fill empty bottles with the water. A quality control engineer checks the volumes of water in the bottles filled by each of the machines. He chooses a random sample of 60 bottles filled by machine X and a random sample of 75 bottles filled by machine Y . The volumes of water, x and y respectively, in millilitres, are summarised as follows.

$$\sum x = 6345 \quad \sum (x - \bar{x})^2 = 243.8 \quad \sum y = 7614 \quad \sum (y - \bar{y})^2 = 384.9$$

\bar{x} and \bar{y} are the sample means of the volume of water in the bottles filled by machines X and Y respectively.

Find a 95% confidence interval for the difference between the mean volume of water in bottles filled by machine X and the mean volume of water in bottles filled by machine Y . [6]