The curve with equation  $y = e^{-ax} \tan x$ , where a is a positive constant, has only one point in the interval  $0 < x < \frac{1}{2}\pi$  at which the tangent is parallel to the x-axis. Find the value of a and state the exact value of the x-coordinate of this point.