

A particle P of mass m is attached to one end of a light inextensible string of length a . The other end of the string is attached to a fixed point O . The particle is held so that the string is taut, with OP horizontal. The particle is projected downwards with speed $\sqrt{\left(\frac{2}{5}ag\right)}$ and begins to move in a vertical circle. The string breaks when its tension is equal to $\frac{11}{5}mg$.

- (i) Show that the string breaks when OP makes an angle θ with the downward vertical through O , where $\cos \theta = \frac{3}{5}$. Find the speed of P at this instant. [6]
- (ii) For the subsequent motion after the string breaks, find the distance OP when the particle P is vertically below O . [6]