A small object is projected horizontally with speed  $V \, \mathrm{m \, s^{-1}}$  from a point O above horizontal ground. At time  $t \, \mathrm{s}$  after projection, the horizontal and vertically upwards displacements of the object from O are  $x \, \mathrm{m}$  and  $y \, \mathrm{m}$  respectively.

(i) Express x and y in terms of t and hence show that the equation of the path of the object is  $y = -\frac{5x^2}{V^2}$ .

The object passes through points with coordinates (a, -a) and  $(a^2, -16a)$ , where a is a positive constant.

- (ii) Find the value of a. [3]
- (iii) Given that the object strikes the ground at the point where x = 5a, find the height of O above the ground. [2]