A 6-sided dice, A, with faces numbered 1, 2, 3, 4, 5, 6 is biased so that the probability of throwing a 6 is  $\frac{1}{4}$ . The random variable X is the number of 6s obtained when dice A is thrown twice.

(a) Find the probability generating function of X. [2]

A second dice, *B*, with faces numbered 1, 2, 3, 4, 5, 6 is unbiased. The random variable *Y* is the number of 6s obtained when dice *B* is thrown twice.

The random variable *Z* is the total number of 6s obtained when both dice are thrown twice.

**(b)** Find the probability generating function of *Z*, expressing your answer as a polynomial. [3]

(c) Find Var(Z). [3]

(d) Use the probability generating function of Z to find the most probable value of Z. [1]