



A light inextensible string is threaded through a fixed smooth ring  $R$  which is at a height  $h$  above a smooth horizontal surface. One end of the string is attached to a particle  $A$  of mass  $m$ . The other end of the string is attached to a particle  $B$  of mass  $\frac{6}{7}m$ . The particle  $A$  moves in a horizontal circle on the surface. The particle  $B$  hangs in equilibrium below the ring and above the surface (see diagram).

When  $A$  has constant angular speed  $\omega$ , the angle between  $AR$  and  $BR$  is  $\theta$  and the normal reaction between  $A$  and the surface is  $N$ .

When  $A$  has constant angular speed  $\frac{3}{2}\omega$ , the angle between  $AR$  and  $BR$  is  $\alpha$  and the normal reaction between  $A$  and the surface is  $\frac{1}{2}N$ .

**(a)** Show that  $\cos \theta = \frac{4}{9} \cos \alpha$ . [5]

**(b)** Find  $N$  in terms of  $m$  and  $g$  and find the value of  $\cos \alpha$ . [4]