

Particles  $P$  and  $Q$  are projected in the same vertical plane from a point  $O$  at the top of a cliff. The height of the cliff exceeds 50 m. Both particles move freely under gravity. Particle  $P$  is projected with speed  $\frac{35}{2} \text{ m s}^{-1}$  at an angle  $\alpha$  above the horizontal, where  $\tan \alpha = \frac{4}{3}$ . Particle  $Q$  is projected with speed  $u \text{ m s}^{-1}$  at an angle  $\beta$  above the horizontal, where  $\tan \beta = \frac{1}{2}$ . Particle  $Q$  is projected one second after the projection of particle  $P$ . The particles collide  $T$  s after the projection of particle  $Q$ .

- (a) Write down expressions, in terms of  $T$ , for the horizontal displacements of  $P$  and  $Q$  from  $O$  when they collide and hence show that  $4uT = 21\sqrt{5}(T+1)$ . [4]
- (b) Find the value of  $T$ . [4]
- (c) Find the horizontal and vertical displacements of the particles from  $O$  when they collide. [3]