The parametric equations of a curve are

$$x = 1 - \cos\theta, \qquad y = \cos\theta - \tfrac{1}{4}\cos 2\theta.$$

Show that $\dfrac{\mathrm{d}y}{\mathrm{d}x} = -2\sin^2\left(\tfrac{1}{2}\theta\right)$. [5]