

A particle P of mass 0.4 kg is released from rest at a point O on a smooth plane inclined at 30° to the horizontal. P moves down the line of greatest slope through O . The velocity of P is $v\text{ m s}^{-1}$ when its displacement from O is $x\text{ m}$. A retarding force of magnitude $0.2v^2\text{ N}$ acts on P in the direction PO .

(i) Show that $v \frac{dv}{dx} = 5 - 0.5v^2$. [2]

(ii) Express v in terms of x . [4]