Toby has a bag which contains 6 red marbles and 3 green marbles. He randomly chooses 3 marbles from the bag, without replacement. The random variable X is the number of red marbles that Toby obtains.

(a) Find the probability generating function of X. [3]

Ling also has a bag which contains 6 red marbles and 3 green marbles. He randomly chooses 2 marbles from his bag, without replacement. The random variable Y is the number of red marbles that Ling obtains. It is given that the probability generating function of Y is - + + .

The random variable *Z* is the total number of red marbles that Toby and Ling obtain.

- (b) Find the probability generating function of Z, expressing your answer as a polynomial in t. [3]
- (c) Use the probability generating function of Z to find Var(Z). [4]