

Ellie is investigating the heights of two types of beech tree,  $A$  and  $B$ , in a certain region. She has chosen a random sample of 60 beech trees of type  $A$  in the region, recorded their heights,  $x$  m, and calculated unbiased estimates for the population mean and population variance as 35.6 m and  $4.95 \text{ m}^2$  respectively.

Ellie also chooses a random sample of 50 beech trees of type  $B$  in the region and records their heights,  $y$  m. Her results are summarised as follows.

$$\Sigma y = 1654 \quad \Sigma y^2 = 54\,850$$

Find a 95% confidence interval for the difference between the population mean heights of type  $A$  and type  $B$  beech trees in the region. [6]