



One end of a light spring of natural length  $a$  and modulus of elasticity  $4mg$  is attached to a fixed point  $O$ . The other end of the spring is attached to a particle  $A$  of mass  $km$ , where  $k$  is a constant. Initially the spring lies at rest on a smooth horizontal surface and has length  $a$ . A second particle  $B$ , of mass  $m$ , is moving towards  $A$  with speed  $\sqrt{\frac{4}{3}ga}$  along the line of the spring from the opposite direction to  $O$  (see diagram).

The particles  $A$  and  $B$  collide and coalesce. At a point  $C$  in the subsequent motion, the length of the spring is  $\frac{3}{4}a$  and the speed of the combined particle is half of its initial speed.

**(a)** Find the value of  $k$ . [6]

At the point  $C$  the horizontal surface becomes rough, with coefficient of friction  $\mu$  between the combined particle and the surface. The deceleration of the combined particle at  $C$  is  $\frac{9}{20}g$ .

**(b)** Find the value of  $\mu$ . [4]