



The diagram shows the curve  $y = (\ln x)^2$ . The  $x$ -coordinate of the point  $P$  is equal to  $e$ , and the normal to the curve at  $P$  meets the  $x$ -axis at  $Q$ .

- (i) Find the  $x$ -coordinate of  $Q$ . [4]
- (ii) Show that  $\int \ln x \, dx = x \ln x - x + c$ , where  $c$  is a constant. [1]
- (iii) Using integration by parts, or otherwise, find the exact value of the area of the shaded region between the curve, the  $x$ -axis and the normal  $PQ$ . [5]