

A particle of mass m is attached to one end of a light inextensible string of length a. The other end of the string is attached to a fixed point O. The point A is such that OA = a and OA makes an angle α with the upward vertical, where $\tan \alpha = \frac{12}{5}$. The particle is projected downwards from A with speed u perpendicular to the string and moves in a vertical plane (see diagram). The string becomes slack after the string has rotated through 270° from its initial position, with the particle now at the point B.

(i) Show that
$$u^2 = 2ag$$
. [5]

(ii) Find the maximum tension in the string as the particle moves from A to B. [4]