

A particle P is projected with speed u at an angle α above the horizontal from a point O on a horizontal plane and moves freely under gravity. The horizontal and vertical displacements of P from O at a subsequent time t are denoted by x and y respectively.

- (a) Derive the equation of the trajectory of P in the form

$$y = x \tan \alpha - \frac{gx^2}{2u^2} \sec^2 \alpha. \quad [3]$$

The point Q is the highest point on the trajectory of P in the case where $\alpha = 45^\circ$.

- (b) Show that the x -coordinate of Q is $\frac{u^2}{2g}$. [3]

- (c) Find the other value of α for which P would pass through the point Q . [4]