

A company produces packets of sweets. Two different machines, A and B , are used to fill the packets. The manager decides to assess the performance of the two machines. He selects a random sample of 50 packets filled by machine A and a random sample of 60 packets filled by machine B . The masses of sweets, x kg, in packets filled by machine A and the masses of sweets, y kg, in packets filled by machine B are summarised as follows.

$$\Sigma x = 22.4 \quad \Sigma x^2 = 10.1 \quad \Sigma y = 28.8 \quad \Sigma y^2 = 16.3$$

A test at the $\alpha\%$ significance level provides evidence that the mean mass of sweets in packets filled by machine A is less than the mean mass of sweets in packets filled by machine B . Find the set of possible values of α . [12]