

A particle  $P$  of mass  $0.4 \text{ kg}$  is projected horizontally along a smooth horizontal plane from a point  $O$ . At time  $t \text{ s}$  after projection the velocity of  $P$  is  $v \text{ m s}^{-1}$ . A force of magnitude  $0.8t \text{ N}$  directed away from  $O$  acts on  $P$  and a force of magnitude  $2e^{-t} \text{ N}$  opposes the motion of  $P$ .

(i) Show that  $\frac{dv}{dt} = 2t - 5e^{-t}$ . [2]

(ii) Given that  $v = 8$  when  $t = 1$ , express  $v$  in terms of  $t$ . [3]

(iii) Find the speed of projection of  $P$ . [2]