

A random sample of 40 observations of a random variable  $X$  and a random sample of 50 observations of a random variable  $Y$  are taken. The resulting values for the sample means,  $\bar{x}$  and  $\bar{y}$ , and the unbiased estimates,  $s_x^2$  and  $s_y^2$ , for the population variances are as follows.

$$\bar{x} = 24.4 \quad \bar{y} = 17.2 \quad s_x^2 = 10.2 \quad s_y^2 = 11.1$$

Find a 90% confidence interval for the difference between the population means of  $X$  and  $Y$ . [5]