

A particle  $P$  of mass  $m$  is free to move on the smooth inner surface of a fixed hollow sphere of radius  $a$ . The centre of the sphere is  $O$  and the point  $C$  is on the inner surface of the sphere, vertically below  $O$ . The points  $A$  and  $B$  on the inner surface of the sphere are the ends of a diameter of the sphere. The diameter  $AOB$  makes an acute angle  $\alpha$  with the vertical, where  $\cos \alpha = \frac{4}{5}$ , with  $A$  below the horizontal level of  $B$ . The particle is projected from  $A$  with speed  $u$ , and moves along the inner surface of the sphere towards  $C$ . The normal reaction forces on the particle at  $A$  and  $C$  are in the ratio 8 : 9.

(i) Show that  $u^2 = 4ag$ . [6]

(ii) Determine whether  $P$  reaches  $B$  without losing contact with the inner surface of the sphere. [6]