

Find the complex numbers  $w$  which satisfy the equation  $w^2 + 2iw^* = 1$  and are such that  $\operatorname{Re} w \leq 0$ .  
Give your answers in the form  $x + iy$ , where  $x$  and  $y$  are real. [6]