Two uniform smooth spheres A and B of equal radii have masses m and km respectively. The two spheres are on a horizontal surface. Sphere A is travelling with speed u towards sphere B which is at rest. The spheres collide. Immediately before the collision, the direction of motion of A makes an angle  $\alpha$  with the line of centres. The coefficient of restitution between the spheres is  $\frac{1}{2}$ .

(a) Show that the speed of *B* after the collision is  $\frac{3u\cos\alpha}{2(1+k)}$  and find also an expression for the speed of *A* along the line of centres after the collision, in terms of *k*, *u* and  $\alpha$ . [4]

After the collision, the kinetic energy of A is equal to the kinetic energy of B.

**(b)** Given that  $\tan \alpha = \frac{2}{3}$ , find the possible values of k.