The background of the slide is a deep space image. It features a bright, glowing core of a galaxy or nebula in the upper center, with a soft purple and blue glow. Several bright stars are visible, each with a four-pointed diffraction pattern. A prominent, dark, diagonal streak, possibly a comet tail or a star trail, runs from the upper right towards the lower left. The overall color palette is dark, with blues, purples, and whites.

Dark Matter-Admixed White Dwarfs and their Thermonuclear Explosions – Alternative Probe to Astronomical Dark Matter

Physics Student Conference

21.9.2019

The background of the entire slide is a Hubble Deep Field image, showing a vast field of galaxies and stars against a black cosmic background. The galaxies are of various shapes and sizes, some appearing as bright, fuzzy patches and others as more distinct, elongated structures. The stars are small, bright points of light, some with visible diffraction spikes.

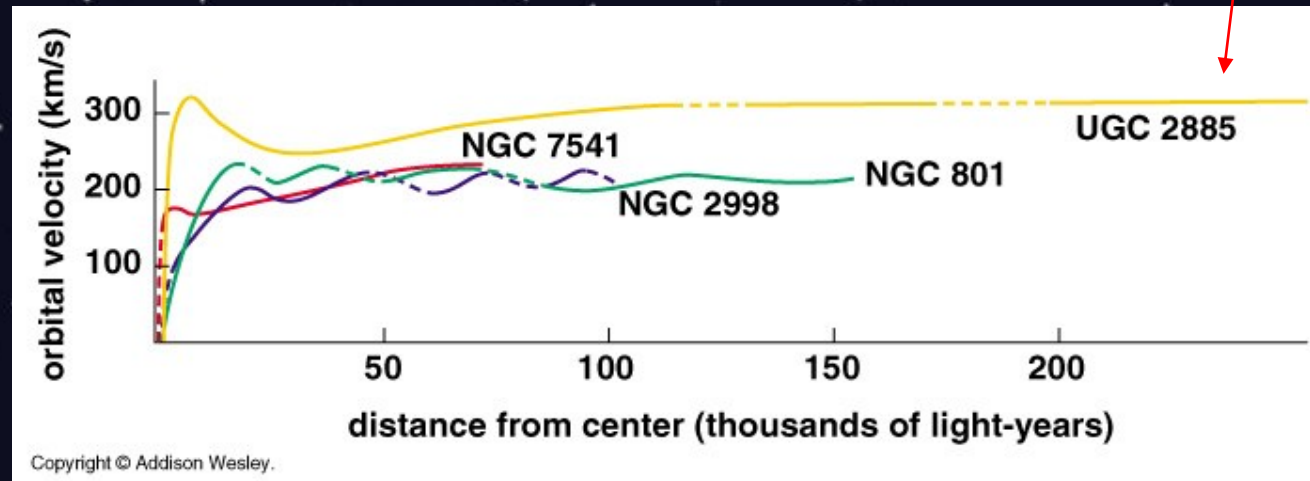
We are only small part of the universe....
Are the visible object represent all of the universe?

Could something not been seen yet plays a role in the universe?
We can find a way to observe them!

Hubble Deep Field Picture From
<https://www.spacetelescope.org>

The Dark Matter Problem

- Rotational velocity curves of galaxies shows asymptotically flatness
- Extended well beyond the visible region
- Maybe some “Dark” Matter (DM) exist?



Typical Galaxies Rotational
Velocity Curve
Taken From
<https://www.arizona.edu/>

Such DM could be accreted by stars

How would they affect the stars?

Outline Of Our Presentation

- Introduction and motivation – DM as the unseen of the universe
- Equilibrium structure of dark matter admixed white dwarf
- Thermonuclear explosions of dark matter admixed white dwarf
- Seeing in the future – Improvements on current explosions model
- An overall summary

A large, glowing white dwarf star is the central focus of the image. It has a bright, yellowish-white surface with visible mottled patterns and a soft, glowing aura. The star is set against a deep black background filled with numerous distant stars and faint, wispy nebulae in shades of purple and blue. The overall scene is a cosmic representation of a white dwarf in space.

Equilibrium Structure Of Dark Matter Admixed White Dwarf

The white dwarf concept picture taken from
<https://www.theverge.com>

Previous Literature Results

- Assumed **spin $\frac{1}{2}$ ideal fermi gas DM**
- DM particle mass **over $1\text{GeV}/c^2$**
- **Spherical Symmetric white** Dwarfs/Neutron Star

DM Admixed White Dwarfs (DMAWD)

- DM core surrounded by normal matter (NM)
- ???

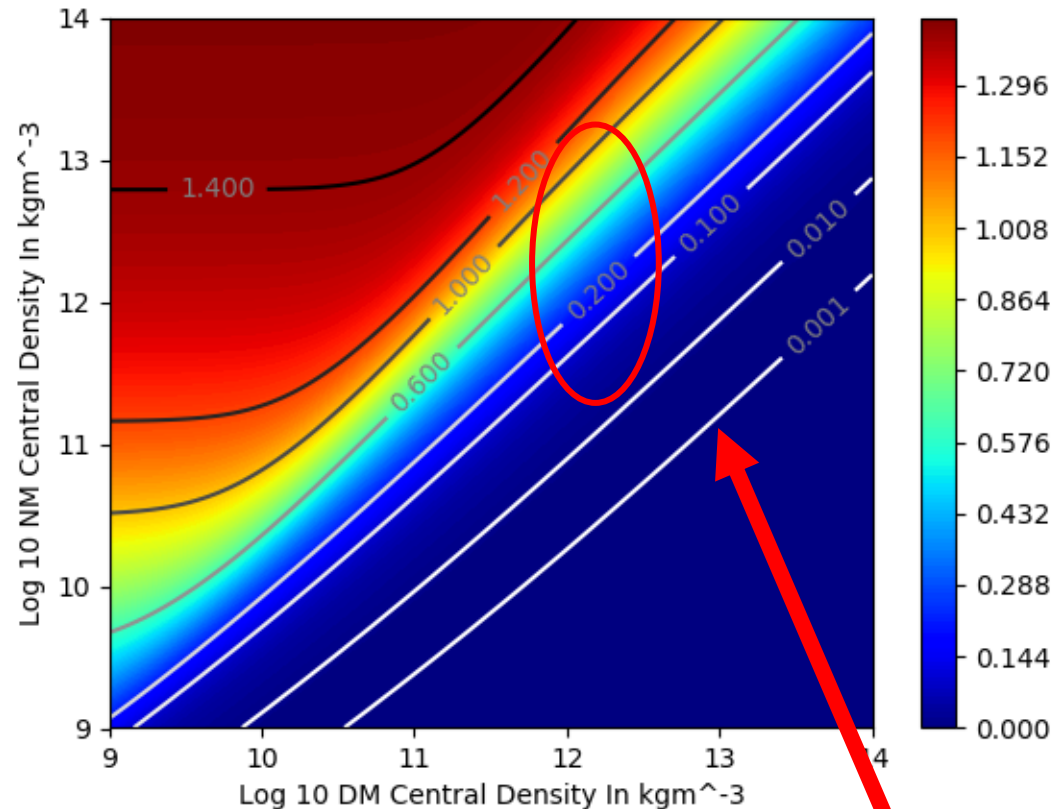
DM Admixed Neutron Stars (DANS)

- DM core surrounded by NM or vice versa
- Comparable DM And NM Mass And Radius

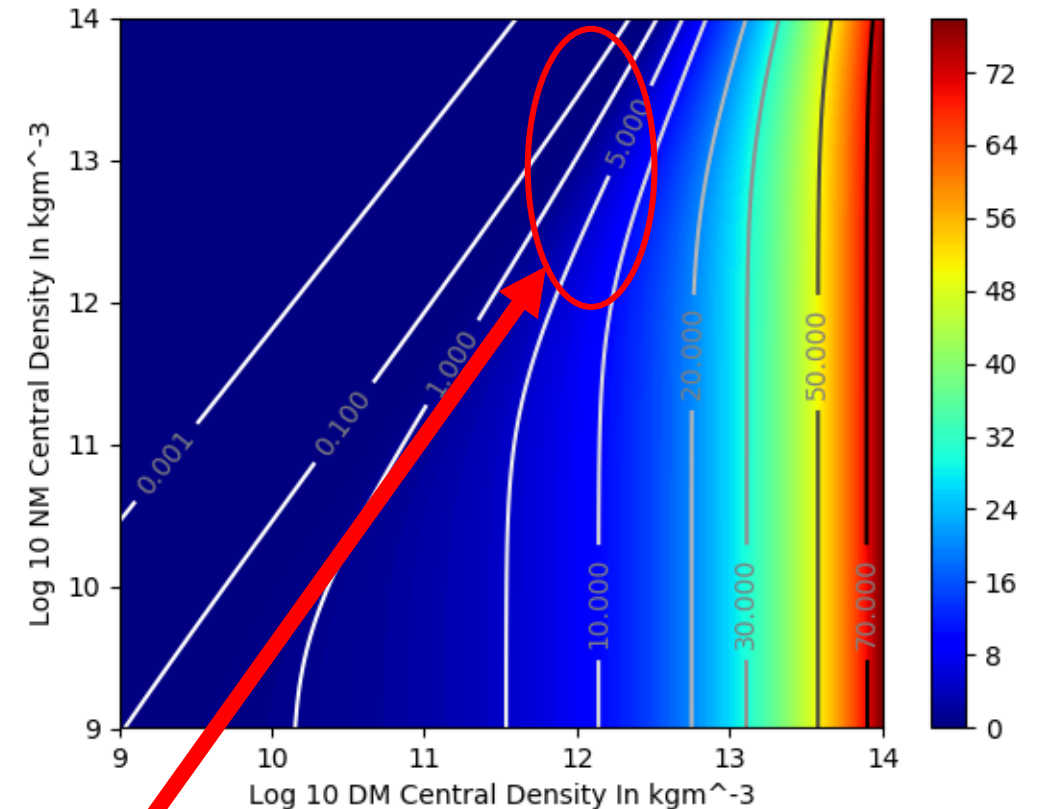
What would happen if lighter DM accreted into White Dwarf?

NM and DM Masses Contour Plot

NM Mass In Solar Mass Contour Plot For DM Particle Mass $0.1\text{GeV}/c^2$



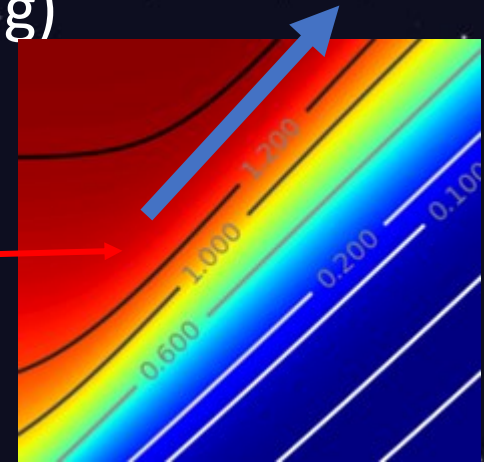
DM Mass In Solar Mass Contour Plot For DM Particle Mass $0.1\text{GeV}/c^2$



Closely packed contour lines where colors changes significantly

Closely Packed Contours And Its Effect

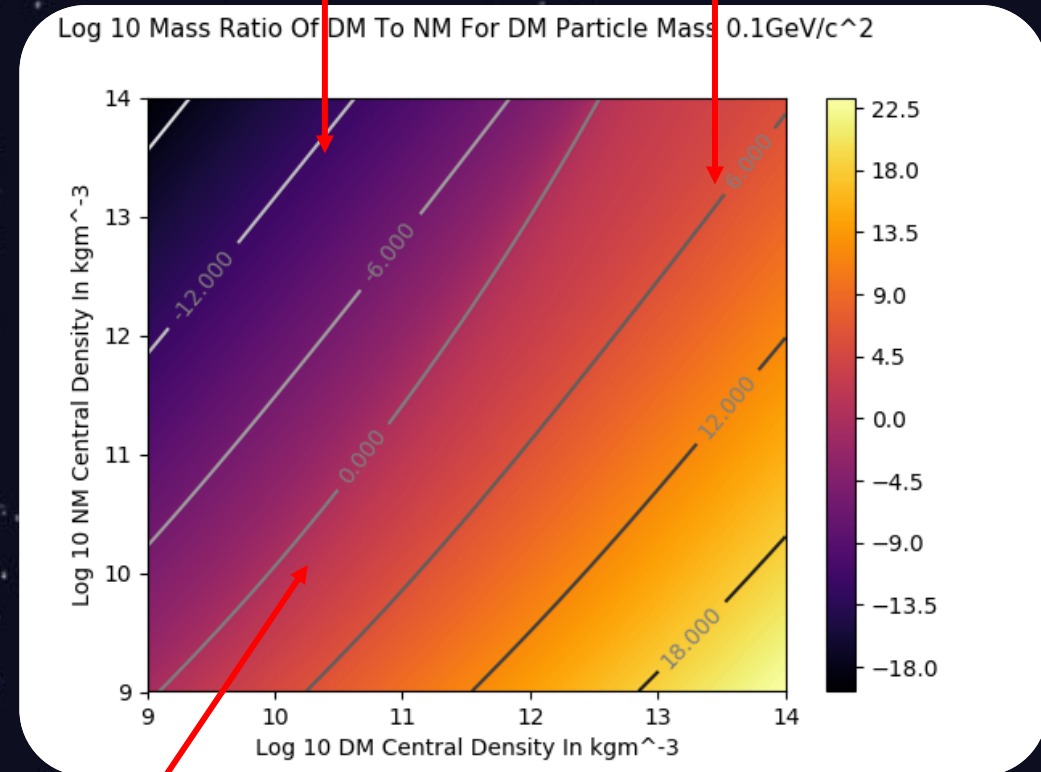
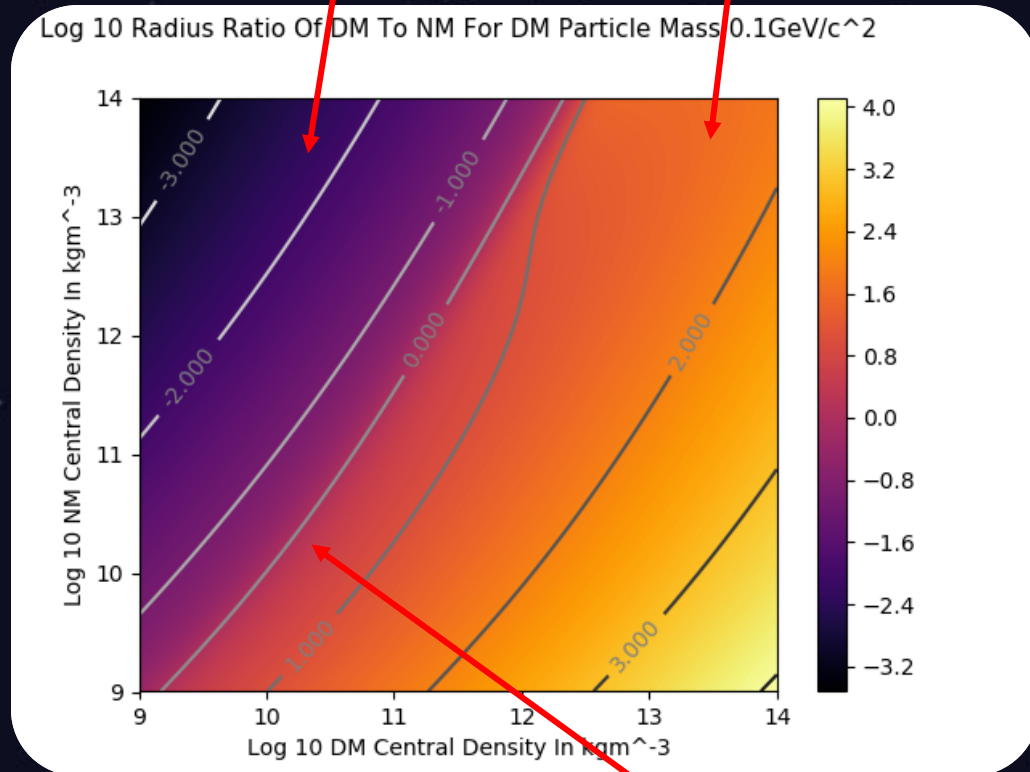
- Conserve NM mass, the DMAWD should lie on constant NM mass line
- When accreted DM mass small, almost no changes (NM dominating)
- Accreted DM mass increase, goes along contour lines...
- **NM central density increase** and radius decrease rapidly...



Accreted DM increase NM central density significantly
Recall that typical Type Ia supernova density $\sim 10^9 gcm^{-3}$
A Type Ia supernova with lower NM mass?

NM / DM Radii and Masses Ratio Contour Plot

DM(NM) more massive then NM(DM) \rightarrow DM(NM) surrounding NM(DM)



The contour line 0 represent masses or radii are equal

What Can Be Known From The Ratio Plot?

Some other class of DMAWD...

DMAWD having ...

1. DM surrounding NM core
2. Comparable order of DM and NM radii and masses

Not found previously

Such DMAWD could also exist so that NM central density \sim Type Ia
What would happen if a Type Ia explosions happen ?



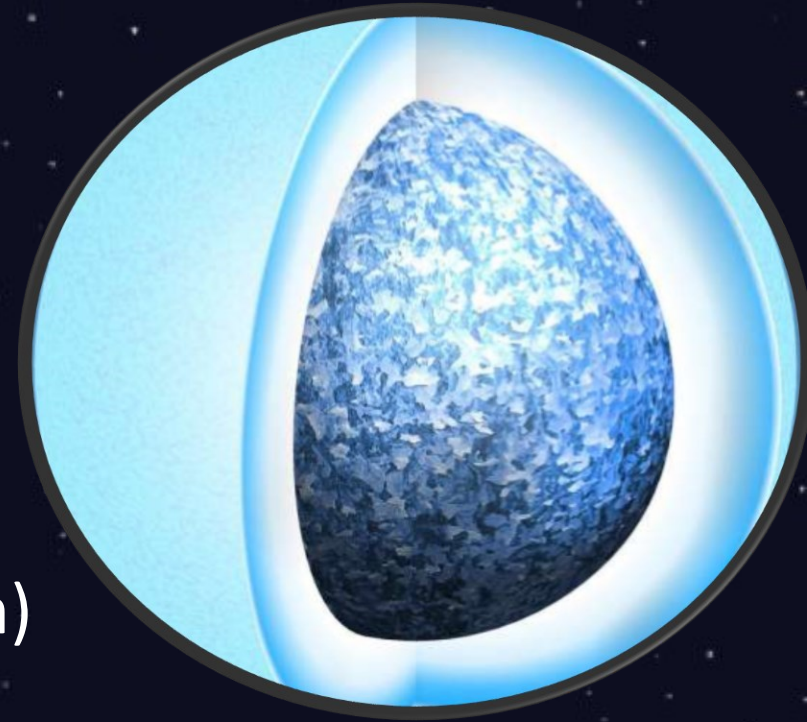


Thermonuclear Explosions of Dark Matter Admixed White Dwarfs

Picture References : [Nasa.gov](https://www.nasa.gov)

Setup Of Our Simple Type Ia Model

- One - dimensional
- Pure Carbon – 12 White Dwarf
- Immediate conversion $14C12 \rightarrow 3Ni56$
- Central Density - $3 \times 10^{12} \text{kgm}^{-3}$
- Temperature – Isothermal $10^8 K$ (electron conduction)
- Stellar equation of state by Timmes et al.
- Pure deflagration model
- $\vec{v}_n = \beta c_s$, c_s is the local sound speed



Picture References : Phys.org

Serve to compare with previous literature (Woosley, Holfich...)

Dark Matter Admixed SNela


- DM squeeze lower NM mass to high central density
- Sub-Luminous SNela? Leung et al. perform stationary DM simulation
- Extend to movable DM?

Parameters							
	DM Mass	NM Mass	DM Radius	NM Radius	DM Central Density	NM Central Density	DM Movable
DF10	$0.009M_{\odot}$	$1.37M_{\odot}$	370km	1830km	$3 \times 10^{10}\text{kgm}^{-3}$	$3 \times 10^{12}\text{kgm}^{-3}$	No
DF11	$0.07M_{\odot}$	$1.25M_{\odot}$	960km	1780km	$2 \times 10^{11}\text{kgm}^{-3}$	$3 \times 10^{12}\text{kgm}^{-3}$	Yes
DF12	$0.20M_{\odot}$	$1.13M_{\odot}$	1380km	1650km	$3 \times 10^{11}\text{kgm}^{-3}$	$3 \times 10^{12}\text{kgm}^{-3}$	Yes

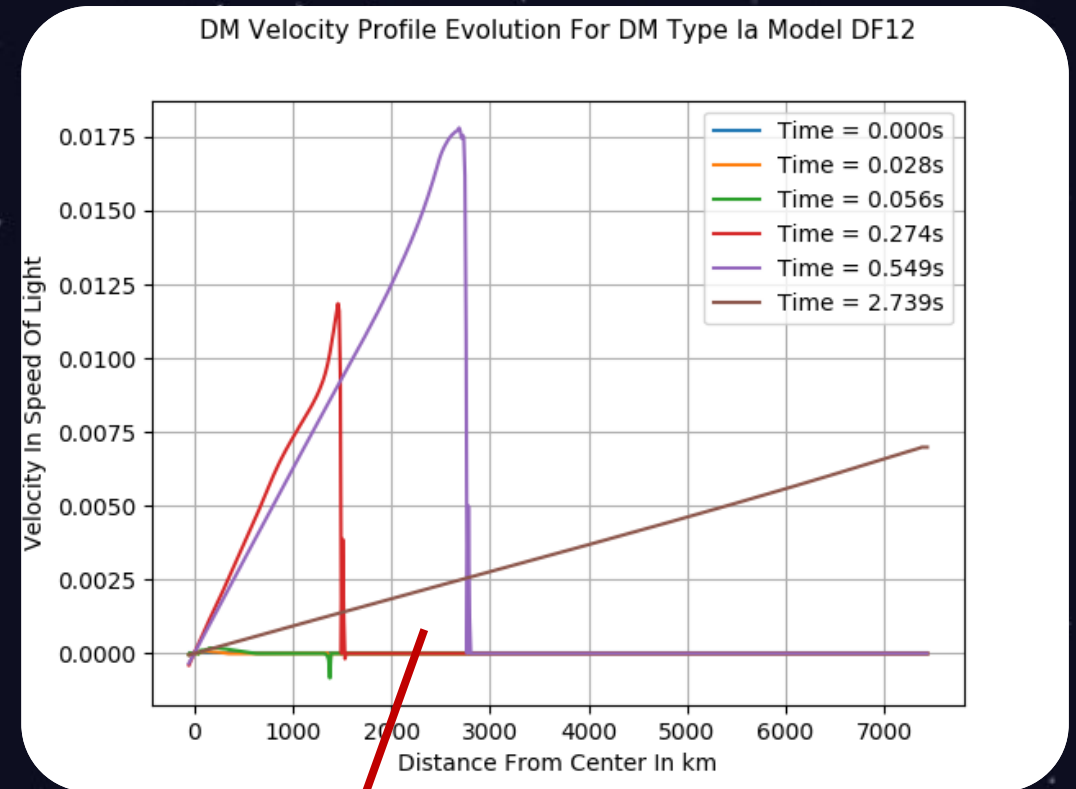
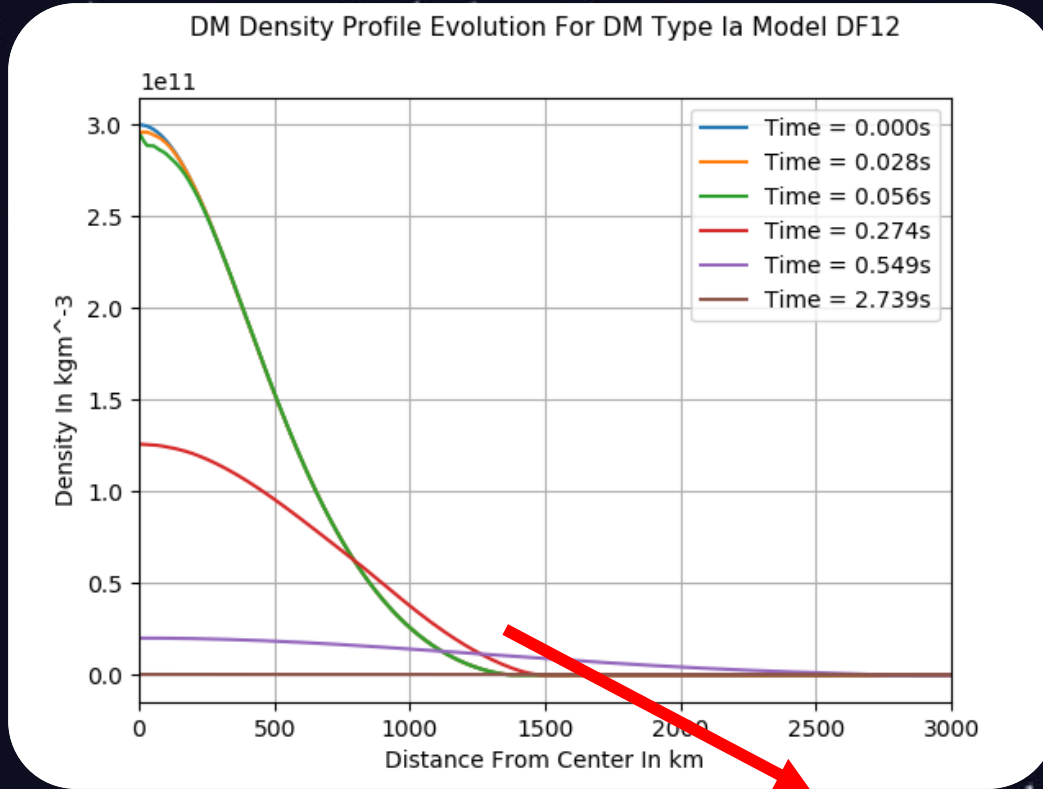
- Deflagration speed $0.75c_s$, initial position enclose $10^{-4}M_{\odot}$
- Lower NM mass - Less Nickel-56 or energy being produced?
- How would the DM behaved?

DM Admixed SNela Model DF10 – DF12

Simulations Results				
	Nickel-56 Mass	Energy Production	DM Unbinding Time	NM Unbinding Time
DF9	$0.58M_{\odot}$	$1.47 \times 10^{44} \text{ J}$	-	0.12s
DF10	$0.58M_{\odot}$	$1.47 \times 10^{44} \text{ J}$	-	0.12s
DF11	$0.54M_{\odot}$	$1.36 \times 10^{44} \text{ J}$	1.05s	0.11s
DF12	$0.52M_{\odot}$	$1.30 \times 10^{44} \text{ J}$	0.95s	0.13s

- More DM admixed  less NM mass
- Hence less Nickel-56 and energy
- DM unbinding time later than NM
- DM freely expanding after NM exploded
- Reason – A weaker gravitational interaction between NM and DM

Density and Velocity Profiles For DM



- DM density decreasing, NO inversion
- Velocity profile radially increasing – Free expansion

NM explosion is able bring along DM

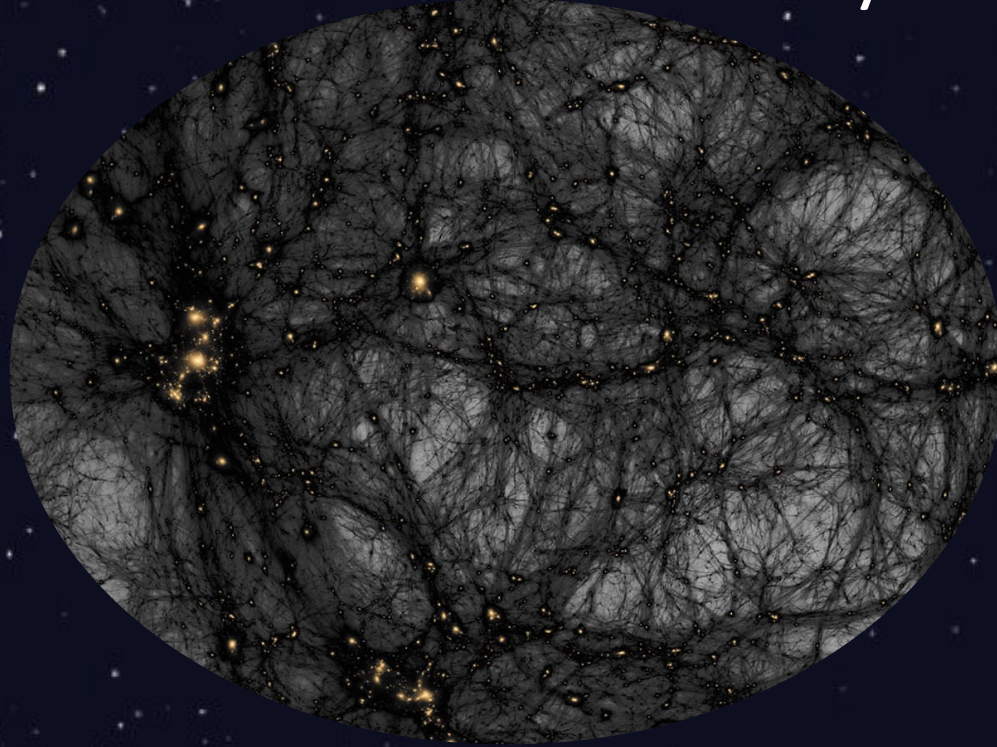
Extension To Higher DM Central Density



What if DM mass or radius start to be comparable
Or even **over dominate** that of NM?

Would a DM star left behind? Worth to explore

A Small Summary



- We discover two new class of DMAWD equilibrium structure
- We simulate a simple thermonuclear explosions of DMAWD
- With less NM mass comes with less Ni-56 produced – Sub luminous
- DMAWD with more massive DM worth to explore – Observable?

Picture References : Universe Today

SNela Model DF1 – DF9

These meet the requirement
 $0.5M_{\odot}$ Nickel-56 And 10^{44} J energy

	Simulations Results								
	DF1	DF2	DF3	DF4	DF5	DF6	DF7	DF8	DF9
Initial deflagration Position (M_{\odot})	0.01	0.001	0.0001	0.01	0.001	0.0001	0.01	0.001	0.0001
Deflagration Speed (c_s)	0.25	0.25	0.25	0.50	0.50	0.50	0.75	0.75	0.75
Unbinding Time (s)	0.15	0.24	0.29	0.09	0.14	0.16	0.07	0.10	0.12
Ni56 Mass (M_{\odot})	0.24	0.22	0.21	0.43	0.41	0.41	0.59	0.58	0.58
Energy Released (10^{44} J)	0.66	0.65	0.62	1.12	1.09	1.08	1.48	1.47	1.47

- Differentiated by **deflagration speed** and **front location**
- Different Nickel-56, energy production, unbinding time

Faster propagation

OR

Further initial position

More energy + Nickel-56 + earlier unbinding



More energetic explosion

A photograph of a server room aisle. The room is dimly lit with a strong blue light emanating from the server racks. The racks are lined up on both sides of the aisle, receding into the distance. The floor is a light-colored, polished material. The ceiling has visible pipes and lighting fixtures. The overall atmosphere is futuristic and high-tech.

Appendix – Supplementary To Main Slide

Constructing DMAWD Model

Hydrostatic Equilibrium Equation Of DM and NM

$$\frac{dP_1(r)}{dr} = -\frac{\rho_1(r)G}{r^2} (M_1(r) + M_2(r))$$

$$\frac{dP_2(r)}{dr} = -\frac{\rho_2(r)G}{r^2} (M_1(r) + M_2(r))$$

$$\frac{dM_1(r)}{dr} = 4\pi r^2 \rho_1$$

$$\frac{dM_2(r)}{dr} = 4\pi r^2 \rho_2$$

- With M the mass, ρ the density, P the pressure, r the radius
- Subscript 1 and 2 belongs to DM and NM respectively
- DM and NM only acts through gravity
- Solving these sets of coupled equation with RK4 scheme

Assumption In Model Construction

- White dwarfs would have general relativity parameter

$$\frac{GM_{total}}{Rc^2} \sim 10^{-4}$$

- Safe to assume Newtonian gravity in most case
- DM particle mass ranging from $0.1\text{GeV}/c^2$ to $0.3\text{GeV}/c^2$
- DM and NM central Density ranging from 10^9 to 10^{14}
- Make sure they are degenerate

Make contour plots of DM/NM Mass And Radius


How Do We Classify Thermonuclear Explosion?

Deflagration

- Propagate **sub-sonically**
- Through **heat transfer process**
- Depends on **micro-physics**
- Release **less energy**

Detonation

- Propagate **super-sonically**
- Through generation of **shocks**
- Depends on **hydrodynamics**
- Release **more energy**

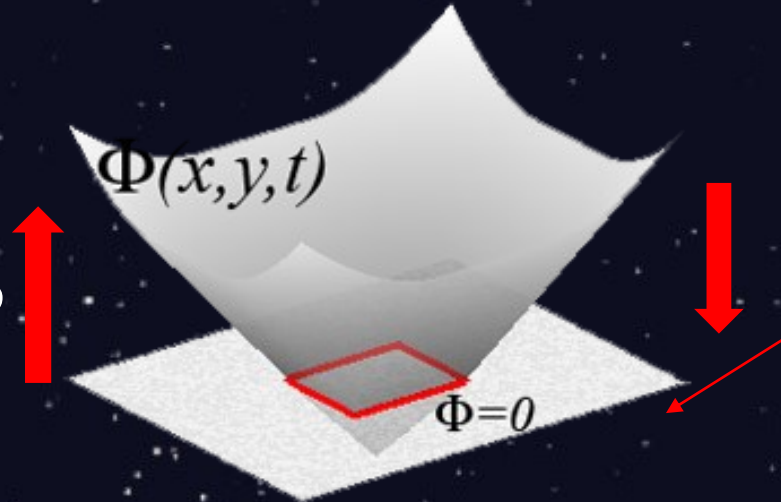
- 
- Their burning region (**front**) **separate ash and fuels**
 - **Very thin** in astrophysical contexts ($10^{-3}cm$ vs $\sim 10^3km$)

Good to approximate them as a discontinuous surface

The Level – Set Surface Capturing Method

- The surface is the zeroth level – set of a scalar field Φ

Motion of surface
governed by motion of Φ



The zeroth level - set

Picture References : profs.etsmtl.ca

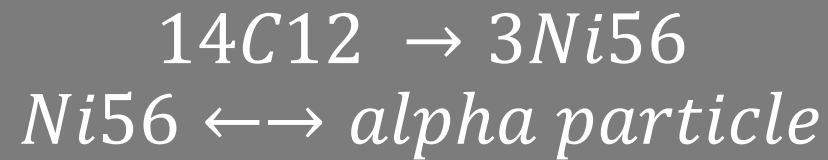
- In a mathematical way...

$$\{\vec{x}(t) | \Phi(\vec{x}(t), t) = 0\}$$

- Immediate advantage – Topological change handled naturally

Limitations – Unrealistic Nuclear Reaction

- We **need high deflagration speed** to produce sufficient Nickel-56
- **$>0.5c_s$ vs $0.3c_s$** as pointed by Woosley, Hoflich et al....
- Reinecke et al. say that **immediate conversion to Ni56 not realistic...**



- **Nuclear statistical equilibrium** shift towards Ni56 later
- Effect – less energetic explosion initially, **more time to burn C12...**
- How about other elements? E.g. **Intermediate mass elements?**

A large nuclear network between elements is needed

Limitations – Deflagration speed? DDT?

- Deflagration speed in local sound speed is unphysical?
- How about other choice of speed? But...

Laminar deflagration speed couldn't produce explosions

- **Convective** deflagration speed? **Turbulence** deflagration speed?
- Act to “**accelerate**” deflagration front
- Prompt Explosion - How about a transition detonation?

Deflagration to detonation transition(DDT) – One explosion model

- However, DDT in open system is still debatable...

Limitations – Light Curve + Microphysics

- Other important benchmark – **Light curve + Neutrino emission**
- Light curve – **a radiative transfer equation?**
- **Special relativistic hydro-dynamics?** (The velocity is so high)
- Amount Nickel – 56 and other **iron peak elements?**
- Need **electron capture** module, **reduce iron peak elements.**
- **NSE module** to calculate elements in burnt region?

Still a long way to go to produce a good model...

Appendix - deflagration/detonation speed?

- Timmes et al. solved energy equation to obtain...

$$\vec{v}_n = 92.0 \left(\frac{\rho}{2 \times 10^9} \right)^{0.805} \left[\frac{X_{c12}}{0.5} \right]^{0.889} \text{ km s}^{-1}$$

- Problems – Too slow for explosions
- Solutions – Accelerate it
- By means of turbulence, convection...

\vec{v}_n turbulence parameterized in fractal dimension?

- More realistic – Go to higher dimension
- Handle turbulence more carefully

Appendix - Why not pure detonation model?

- Pure detonation – burn much material at high density
- Too much iron peak elements
- Much less intermediate mass elements (Silicon, magnesium...)
- Some also argued that...
- Pure detonation is not possible to initiate

It is commonly argued that the initiation of detonations in degenerate C-O mixtures is impossible (e.g. Nomoto et al. 1976, 1984; Mazurek et al. 1977; Woosley et al. 1980). The argument was that constant volume explosions in C-O mixtures generate only weak shock waves, which cannot trigger a detonation.

Picture References : Khokhlov et al.

Appendix – What is DDT?

Pure detonation – Too much Ni56

Pure deflagration – Too weak

How about combine both?

- Khokhlov first proposed DDT
- Initially, a slow deflagration expand stars
- At critical condition, transit to detonation
- Observed on terrestrial combustion

What condition?(Density? Temperature?...)
Still unclear!

Appendix – What is Timmers EOS?

White dwarf – degenerate electron in finite temperature

- Needs finite temperature EOS with contribution from electron...
- Include pressure, density, specific energy from...

Electron, positron, photo, ideal gas ions



- A finite temperature EOS
- Solved by calculating the fermi integral exactly
- Included in terms of a free energy table
- Interpolate the free energy table – Get thermo variables...