

Modelling Concurrent Systems Notes

Made by Leon :)

1 Process Algebras

Definition 1.1.1: ACP, CCS, CSP

The syntax of ACP, CCS, and CSP is defined as:

Operation	ACP	CCS	CSP
Termination	ϵ	0	STOP
Deadlock	δ		
Action	a		
Sequential Composition	$P.Q$		
Action Prefixing		$a.P$	$a \rightarrow P$
Alternative Choice	$P + Q$	$P + Q$	$P \sqcap Q$
External Choice			$P \sqcap Q$
Internal Choice			$P \sqcap Q$
Parallel Composition	$P \parallel Q$	$P \mid Q$	$P \parallel_A Q$
Restriction	$\partial_H(P)$	$P \backslash a$	
Abstraction	$\tau_I(P)$		P/a
Relabelling		$P[f]$	$P[f]$

Differences between ACP, CCS, and CSP

- **Action:** CCS and CSP require Action Prefixing, while ACP can perform sequential composition on any process. This also requires CCS and CSP processes to feature the inaction 0/STOP, while ACP is not restricted to this.
- **Choice:** ACP and CCS have an operator which can perform both External and Internal Choice. CSP Differentiates internal choices from external ones, and internal actions within \sqcap do not count as a choice in CSP.
- **Parallel Composition:**
 - ACP actions follow a communication function to decide what to synchronise, i.e. $\gamma(a, b)$
 - CCS actions can only synchronise with its conjugate counterpart, i.e. a and \bar{a}
 - CSP actions can only synchronise over the same action, i.e. a and a
- **Restriction, Abstraction, Relabelling:**
 - Relabelling just doesn't exist in base ACP, lol
 - CCS combines communication and abstraction into one step - every synchronisation results in a τ .
 - CSP combines Parallel Composition and Restriction into one step, as CSP Parallel Composition doesn't feature left-over Left Merges.

Definition 1.1.2: The GSOS Format

General Structured Operational Semantics (GSOS) operations are compositional.

Rules of GSOS

- Its source has the form $f(x_1, \dots, x_{ar(f)})$ with $f \in \Sigma$ and $x_i \in V$
- The left hand sides of its premises are variables x_i with $1 \leq i \leq ar(f)$
- The right hand sides of its positive premises are variables that are all distinct, and that do not occur in its source
- Its target only contains variables that also occur in its source or premises

GSOS Semantics of ACP

$(a.P) \xrightarrow{a} P$	$P + Q \xrightarrow{a} P$	$P + Q \xrightarrow{a} Q$
$\frac{P \xrightarrow{a} P'}{P \parallel Q \xrightarrow{a} P' \parallel Q}$	$\frac{P \xrightarrow{a} P' \quad Q \xrightarrow{b} Q' \quad a b=c}{P \parallel Q \xrightarrow{a} P' \parallel Q'}$	
$\frac{Q \xrightarrow{a} Q'}{P \parallel Q \xrightarrow{a} P \parallel Q'}$	$\frac{P \xrightarrow{a} P' \quad (\alpha \notin A)}{\partial_H(P) \xrightarrow{a} \partial_H(P')}$	$\frac{\langle \mathcal{S}_X \mid \mathcal{S} \rangle \xrightarrow{a} P'}{\langle X \mid \mathcal{S} \rangle \xrightarrow{a} P'}$

GSOS Semantics of CSP

$(a \rightarrow P) \xrightarrow{a} P$	$P \sqcap Q \xrightarrow{\tau} P$	$P \sqcap Q \xrightarrow{\tau} Q$
$\frac{P \xrightarrow{a} P'}{P \sqcap Q \xrightarrow{a} P'}$	$\frac{P \xrightarrow{\tau} P'}{P \sqcap Q \xrightarrow{\tau} P' \sqcap Q}$	$\frac{Q \xrightarrow{a} Q'}{P \sqcap Q \xrightarrow{a} Q'}$
$\frac{Q \xrightarrow{\tau} Q'}{P \sqcap Q \xrightarrow{\tau} P \sqcap Q'}$	$\frac{P \xrightarrow{\alpha} P'}{f(P) \xrightarrow{f(\alpha)} f(P')}$	$\frac{P \xrightarrow{\alpha} P' \quad (\alpha \notin A)}{P \parallel_A Q \xrightarrow{\alpha} P' \parallel_A Q}$
$\frac{P \xrightarrow{a} P' \quad Q \xrightarrow{a} Q' \quad (a \in A)}{P \parallel_A Q \xrightarrow{a} P' \parallel_A Q'}$		$\frac{Q \xrightarrow{\alpha} Q' \quad (\alpha \notin A)}{P \parallel_A Q \xrightarrow{\alpha} P \parallel_A Q'}$
$\mu p.P \xrightarrow{\tau} P[\mu p.P/p]$		

Definition 1.1.3: CSP Expansion Theorem

Let $P := \sum_{i \in I} \alpha_i P_i$ and $Q := \sum_{j \in J} \beta_j Q_j$. Then

$$P \mid Q = \sum_{i \in I} \alpha_i (P_i \mid Q) + \sum_{j \in J} \beta_j (P \mid Q_j) + \sum_{\substack{i \in I, j \in J \\ \alpha_i = \bar{\beta}_j}} \tau.(P_i \mid Q_j)$$

Any guarded CCS expression can be written into a bisimulation equivalent CCS expression of the form $\sum_{i \in I} \alpha_i.P_i$. This is called **head normal form**

Definition 1.1.4: CCS Axioms

- Axioms of CCS

$$(P + Q) + R = P + (Q + R) \quad (\text{associativity})$$

$$P + Q = Q + P \quad (\text{commutativity})$$

$$P + P = P \quad (\text{idempotence})$$

$$P + 0 = P \quad (0 \text{ is a neutral element})$$

- Axiomatisation of Rooted Weak Bisimulation

$$\alpha.\tau.P = \alpha.P \quad (\text{T1})$$

$$\tau.P = \tau.P + P \quad (\text{T2})$$

$$\alpha.(\tau.P + Q) = \alpha.(\tau.P + Q) + \alpha.P \quad (\text{T3})$$

- Axiomatisation of Branching Bisimilarity

$$\alpha.(\tau.(P + Q) + Q) = \alpha.(P + Q) \quad (\text{P})$$

- Axiomatisation of strong partial trace equivalence

$$\alpha.(P + Q) = \alpha.P + \alpha.Q$$

- Axiomatisation of weak partial trace equivalence

$$\tau.P = P$$

Definition 1.1.5: Axioms of ACP

is this really necessary.. who knows

2 Semantics and shit like that

Definition 2.0.1: Trace Semantics

- **Completed Trace:** A start to finish trace of a process.
- **Partial Trace:** From the start of a process to any point, including the end. Clearly, $CT(P) \subseteq PT(P)$
- **Strong vs Weak:** Weak PT and CT means that two processes are equivalent with all instances of τ omitted.
- **Infinite Trace Semantics:** Differs from different types of divergence. Stronger than CT and PT

Definition 2.0.2: Bisimulation Semantics

- **True Bisimulation** (\rightleftharpoons):
 - if sRt and $s \xrightarrow{a} s'$ then $\exists t'$ s.t. $t \xrightarrow{a} t'$ and $s'Rt'$
 - if sRt and $t \xrightarrow{a} t'$ then $\exists s'$ s.t. $s \xrightarrow{a} s'$ and $s'Rt'$
 - if sRt then $s \models p \iff t \models p$ for all $p \in P$
- **Branching Bisimilarity** ($=_{RBB}$)
 - if sRt and $s \xrightarrow{a} s'$ then either:
 - * $a = \tau$ and $s'Rt$
 - * $\exists t_1, t'$ such that $t \Rightarrow t_1 \xrightarrow{a} t'$, sRt_1 and $s'Rt'$
 - if sRt and $t \xrightarrow{a} t'$ then either:
 - * $a = \tau$ and $t'Rt$
 - * $\exists s_1, s'$ such that $s \Rightarrow s_1 \xrightarrow{a} s'$, s_1Rt and $s'Rt'$
 - if sRt and $s \models p$ then $\exists t_1$ s.t. $t \Rightarrow t_1 \models p$, and sRt_1
 - if sRt and $t \models p$ then $\exists s_1$ s.t. $s \Rightarrow s_1 \models p$, and s_1Rt
- Other notions:
 - **Rooted Branching Bisimilarity:** The same as Branching Bisimilarity except the first action is Strongly bisimilar. (This makes RBB a congruence on +)
 - **Delay Bisimilarity:** Same as *branching bisimilarity*, but with the requirements sRt_1 and s_1Rt dropped.
 - **Weak Bisimilarity:** The same as *delay bisimilarity* except the action requirements are also relaxed:
 - * If sRt and $s \xrightarrow{a} s'$ then either:
 - $a = \tau$ and $s'Rt$
 - $\exists t_1, t_2, t'$ such that $t \Rightarrow t_1 \xrightarrow{a} t_2 \Rightarrow t'$ and $s'Rt'$
 - * If sRt and $t \xrightarrow{a} t'$ then either:
 - $a = \tau$ and sRt'
 - $\exists s_1, s_2, s'$ such that $s \Rightarrow s_1 \xrightarrow{a} s_2 \Rightarrow s'$ and $s'Rt'$

Definition 2.0.3: Compositionality, Congruence

An equivalence \sim is a **congruence**^a for a language L if $P \sim Q$ implies that $C[P] \sim C[Q]$ for every context $C[\]$, where $C[\]$ is an L -expression with a **hole** in it, and $C[P]$ is the result of plugging in P for the hole. An alternative definition for a congruence \sim is if every n -ary operator f of L , we have

$$P_i \sim Q_i \text{ for } i = 1, \dots, n \text{ implies } f(P_1, \dots, P_n) \sim f(Q_1, \dots, Q_n)$$

The **Congruence closure** of a language, denoted \sim^c of a language is a modification to a language that isn't compositional to turn it compositional. The *congruence closure* of Branching Bisimilarity is Rooted Branching Bisimilarity.

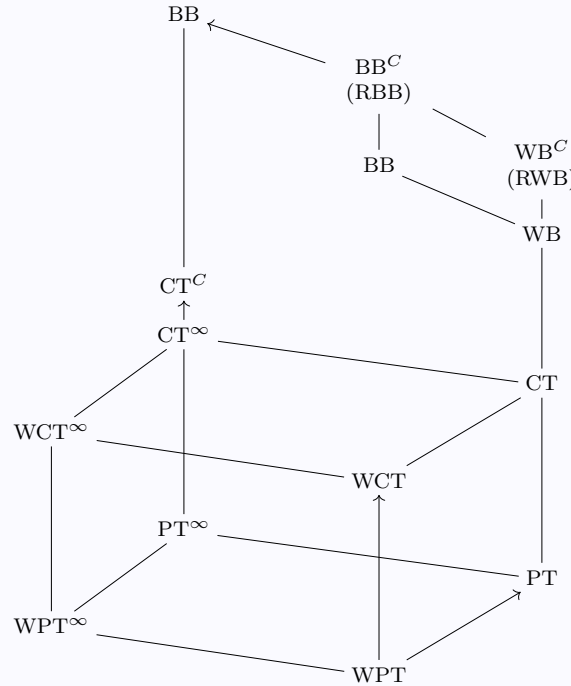
^aWe can also say the language is compositional for the equivalence

Definition 2.0.6: Failure Semantics

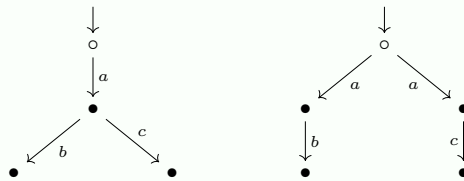
Definition 2.0.7: Consistent Colouring

Definition 2.0.8: Safety

Theorem 2.0.4: Semantic Equivalence Spectrum



Definition 2.0.5: The GOAT of Process algebra



3 Other models of Concurrency

Definition 3.0.1: Hennessy-Milner Logic

The syntax of HML is given by:

$$\phi, \psi ::= \top \mid \perp \mid \phi \wedge \psi \mid \phi \vee \psi \mid \neg \phi \mid \langle \alpha \rangle \phi \mid [\alpha] \phi$$

Infinitary HML (HML^∞) has an infinitary conjunction: $\bigwedge_{i \in I} \phi_i$ HML in set form. If a process P has a property Φ , we write $P \models \Phi$.

- $P \models \top$
- $P \not\models \perp$
- $P \models \Phi \wedge \Psi$ iff $P \models \Phi$ and $P \models \Psi$
- $P \models \Phi \vee \Psi$ iff $P \models \Phi$ or $P \models \Psi$
- $P \models [K]\Phi$ iff $\forall Q \in \{P' : P \xrightarrow{a} P' \text{ and } a \in K\}. Q \models \Phi$
- $P \models \langle K \rangle \Phi$ iff $\exists Q \in \{P' : P \xrightarrow{a} P' \text{ and } a \in K\}. Q \models \Phi$

Deadlock can be represented as $P \models [\text{Act}]\perp$, where Act is the set of all actions.

Definition 3.0.2: Preorder

A **preorder** is a relation that is *transitive* and *reflexive*, but not *symmetric*. Preorders are denoted with \sqsubseteq .

Preorders are used just like equivalence relations to compare specifications and implementations. We write

$$\text{Spec} \sqsubseteq \text{Impl}$$

For each preorder \sqsubseteq , there exists an associated equivalence relation \equiv called its **kernel**, defined by

$$P \equiv Q \iff (P \sqsubseteq Q \wedge Q \sqsubseteq P)$$

Definition 3.0.3: Simulation Equivalence

One process simulates the other when P can do all the same moves as Q . We write $P \sqsubseteq_S Q$ if Q can be simulated by P . Two processes are **simulation equivalent**, $P =_S Q$ if one simulates the other, and vice versa. This is two one-sided equivalences, and therefore is not the same as bisimulation, which needs both processes to be equivalent at the same time

Definition 3.0.4: Kripke Structure

Kripke Structures are defined on states rather than actions, called **atomic predicates**.

Let AP be a set of **atomic predicates**. A **Kripke structure** over AP is a tuple $(S, \rightarrow, \models)$ with S a set of states, $\rightarrow \subseteq S \times S$, the **transition relation**, and $\models \subseteq S \times AP$. The relation $s \models p$ says that predicate $p \in AP$ **holds in state** $s \in S$.

A **path** in a Kripke structure is a nonempty finite or infinite sequence s_0, s_1, \dots of states, such as $(s_i, s_{i+1}) \in \rightarrow$ for each adjacent pair of states s_i, s_{i+1} in the sequence. A path is **complete** if it is either infinite or ends in deadlock (a state without outgoing transitions)

Definition 3.0.5: Petri Nets

they exist

Definition 3.0.6: CTL

Computational Tree Logic is defined on

$$\phi, \psi ::= p \mid \top \mid \perp \mid \neg \phi \mid \phi \wedge \psi \mid \phi \vee \psi \mid \neg \phi \mid \phi \rightarrow \psi \mid$$

$$\text{EX}\phi \mid \text{AX}\phi \mid \text{EF}\phi \mid \text{AF}\phi \mid \text{EG}\phi \mid \text{AG}\phi \mid \text{E}\psi\text{U}\phi \mid \text{A}\psi\text{U}\phi$$

$p \in AP$ is an atomic predicate. CTL is defined on states, the relation \models between states s in a Kripke structure and CTL formulae ϕ is inductively defined by

- $s \models p, p \in AP$ iff $(s, p) \in \models$
- $s \models \top$ always holds, and $s \models \perp$ never
- $s \models \neg \phi$ iff $s \not\models \phi$
- $s \models \phi \wedge \psi$ iff $s \models \phi$ and $s \models \psi$
- $s \models \phi \vee \psi$ iff $s \models \phi$ or $s \models \psi$
- $s \models \phi \rightarrow \psi$ iff $s \not\models \phi$ or $s \models \psi$
- $s \models \text{EX}\phi$ iff there is a state s' with $s \rightarrow s'$ and $s' \models \phi$
- $s \models \text{AX}\phi$ iff for each state s' with $s \rightarrow s'$ one has $s' \models \phi$
- $s \models \text{EF}\phi$ iff some complete path starting in s contains a state s' with $s \models \phi$
- $s \models \text{AF}\phi$ iff each complete path starting in s contains a state s' with $s \models \phi$
- $s \models \text{EG}\phi$ iff all states s' on some complete path starting in s satisfy $s' \models \phi$
- $s \models \text{AG}\phi$ iff all states s' on all complete path starting in s satisfy $s' \models \phi$
- $s \models \text{E}\psi\text{U}\phi$ iff some complete path π starting in s contains a state s' with $s' \models \phi$, and each state s'' on π prior to s' satisfies $s'' \models \psi$
- $s \models \text{A}\psi\text{U}\phi$ iff each complete path π starting in s contains a state s' with $s' \models \phi$, and each state s'' on π prior to s' satisfies $s'' \models \psi$

Definition 3.0.7: LTL

Linear-Time Temporal Logic is defined on

$$\phi, \psi ::= p \mid \top \mid \perp \mid \neg \phi \mid \phi \wedge \psi \mid \phi \vee \psi \mid \neg \phi \mid \phi \rightarrow \psi \mid \text{X}\phi \mid \text{F}\phi \mid \text{G}\phi \mid \psi\text{U}\phi \mid$$

$p \in AP$ is an atomic predicate. The modalities X, F, G, U are called **next-state**, **eventually**, **globally**, and **until**. The relation \models between paths and LTL formulae, with $\pi \models \phi$ saying that the path π satisfies the formula ϕ , or that ϕ is valid on π , or **holds** on π , is inductively defined by

- $\pi \models p, p \in AP$ iff $(s, p) \in \models$
- $\pi \models \top$ always holds, and $\pi \models \perp$ never
- $\pi \models \neg \phi$ iff $s \not\models \phi$
- $\pi \models \phi \wedge \psi$ iff $\pi \models \phi$ and $\pi \models \psi$
- $\pi \models \phi \vee \psi$ iff $\pi \models \phi$ or $\pi \models \psi$
- $\pi \models \phi \rightarrow \psi$ iff $s \not\models \phi$ or $\pi \models \psi$
- $\pi \models \text{X}\phi$ iff $\pi' \models \phi$, where π' is the suffix of π obtained by omitting the first state
- $\pi \models \text{F}\phi$ iff $\pi' \models \phi$ for some suffix π'
- $\pi \models \text{G}\phi$ iff $\pi' \models \phi$ for each suffix π'
- $\pi \models \psi\text{U}\phi$ iff $\pi' \models \phi$ for some suffix π' of π , and $\pi'' \models \psi$ for each path $\pi'' \neq \pi'$ with $\pi \Rightarrow \pi'' \Rightarrow \pi'$

Here a path is seen as a state, namely the first state on that path, together with a future that has been chosen already when evaluating an LTL formula on that state. Traditionally, these judgements $\pi \models \phi$ were defined only for infinite paths π . When also applying them to finite paths, we only have to make one adaptation, namely $\pi \models \text{X}\phi$ never holds if π has only one state. So $\text{X}\phi$ says that there is a next state, and that ϕ holds in it. $s \models \phi$ iff $\pi \models \phi$ for all complete paths π starting in state s . Here a path is **complete** if it is either infinite or ends in deadlock.

Lemma 3.0.8: Comparing LTL to CTL

LTL and CTL can be shown to be incomparable by proving that there cannot exist an LTL formula that is equivalent to the CTL formula $\text{AGEF}a$, and by showing that there cannot exist a CTL formula equivalent to the LTL formula $\text{FG}a$

Theorem 3.0.9: Satisfaction of Strong Bisimilarity

- Two processes are strongly bisimilar iff they satisfy the same infinitary HML formulas. Therefore, to show that two processes are not strongly bisimilar, it suffices to find an infinitary HML formula that is satisfied by one, but not the other.
- Two processes P and Q satisfy the same CTL formulas if they are strongly bisimilar. For finitely branching processes, we have “iff”. For general processes, we have “iff” if we use CTL with infinite conjunctions.
- Two divergence-free processes satisfy the same $\text{CTL}_{\neg X}$ formulas if they are branching bisimulation equivalent. We have “iff” if we use $\text{CTL}_{\neg X}$ with infinite conjunctions.

Theorem 3.0.10: De Nicola-Vaandrager

Translates Kripke structures :D

Definition 3.0.11: Partition Refining

Partition refining is an algorithm to turn a process into its minimal state, making it easier to compare bisimilarity. Works with

$$\text{split}(B, a, P)$$

where B is an equivalence class, a is an action, and P is the process. **split** splits an equivalence class into two, ones with the action and ones without it.

$$[\{s \xrightarrow{a} \bullet\}]_P$$

means “state s does action a outside the equivalence class in process P ”

Listing 1: Pseudocode for **split**

```
split(B, a, P) → ({Bi} a set of blocks)
  choose s ∈ B
  B1 = ∅ (B1 contains states equivalent to s*)
  B2 = ∅ (B2 contains states inequivalent to s*)
  for each s' ∈ B do
    begin
      if [{s'  $\xrightarrow{a}$  •}]P = [{s  $\xrightarrow{a}$  •}]P then
        B1 = B1 ∪ {s'}
      else
        B2 = B2 ∪ {s'}
    end
  if B2 = ∅ then
    return {B1}
  else
    return {B1, B2}
```

Methodology:

- Start with one equivalence class for all states
- Run **split** on the outermost states, this now splits into R_1 and R_2 , where R_2 are outside states
- Run **split** on states with outgoing actions to states in R_2 , this now splits R_1 into R_1 and R_3 , where R_3 are second-most outer states
- Keep on running until root state is partitioned
- If needed, the minimal graph will have exactly one of each equivalence class

Running partition refinement for Branching Bisimilarity

- When checking whether a state in block B has an α transition to block C , it is okay if we can move through block B by doing only τ -transitions, and then reach a state with an α transition to block C
- We never check τ -transitions from block B to block B (τ -transitions to another block are fair game though)

This implies running the rule on

$$[\{s \Rightarrow \xrightarrow{a} \bullet\}]_P$$

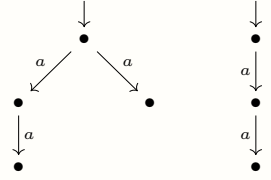
Definition 3.0.12: Alternating Bit Protocol

no idea this works tbh

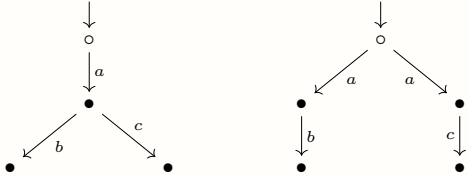
4 Example Catalogue

Example 4.0.1: Trace Semantics

A process that is PT equivalent but not CT equivalent

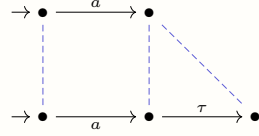


A process that is CT equivalent but not Bisimulation equivalent

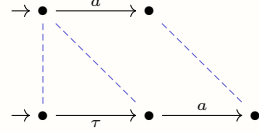


Example 4.0.2: Bisimulation Semantics

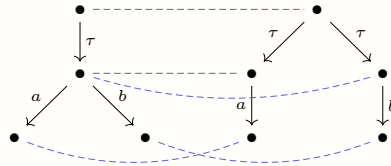
Two processes that are Branching Bisimulation equivalent



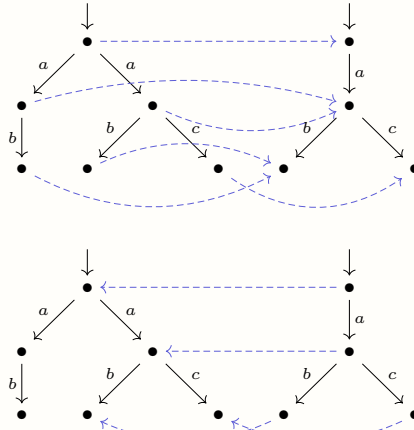
Two processes that are Branching Bisimulation equivalent but not Rooted BB equivalent



Two processes that are Weak Bisimulation equivalent but not Branching Bisimulation equivalent?



Two processes that are Simulation equivalent but not Bisimulation equivalent



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