

1. Suppose that in a two-factor ANOVA (with factors A and B), a significant interaction is found. Suppose in addition that the  $F$ -test for factor A is significant. The latter result is potentially misleading because:

- (a) We must also consider the  $F$ -test for factor B.
- (b) The value of  $SSE$  might be too large.
- (c) The levels of factor A may only be significantly different from each other when a particular level of B is used.
- (d) We cannot be sure in this case whether or not the sums of squares add up to  $SST$ .
- (e) Interactions are hard enough to explain without having to explain a significant factor A effect as well.

2. Suppose one is using a  $\chi^2$  goodness-of-fit test to test the fit of a particular model that does not completely specify all the unknown parameters. The most *ideal* way to estimate the unknown parameters in this case is to:

- (a) Use the sample mean and variance.
- (b) Use the method of moments.
- (c) Use the method of maximum likelihood.
- (d) Use the method of minimum  $\chi^2$ .
- (e) Do so while watching the NFL playoffs.

3. A genetics experiment on characteristics of tomato plants provided the following data on the number of offspring expressing four phenotypes.

Phenotype	Frequency
1 - Tall, cut-leaf	926
2 - Dwarf, cut-leaf	293
3 - Tall, potato-leaf	288
4 - Dwarf, cut-leaf	104
Total	1611

It was of interest to test the following hypothesis, where  $\pi_i$  = the proportion of tomato plants expressing phenotype  $i$ ,  $i = 1, 2, 3, 4$ :

$$H_0 : \pi_1 = \frac{9}{16}, \quad \pi_2 = \frac{3}{16}, \quad \pi_3 = \frac{3}{16}, \quad \pi_4 = \frac{1}{16}.$$

The value of the  $\chi^2$  statistic for testing this hypothesis is 1.469. Which of the following statements is correct for a test with level  $\alpha = 0.1$ ?

- (a) The  $P$ -value is greater than 0.1 and so there is enough evidence to conclude that the phenotype proportions differ from those in  $H_0$ .
- (b) The  $P$ -value is greater than 0.1 and so there is not enough evidence to conclude that the phenotype proportions differ from those in  $H_0$ .
- (c) The  $P$ -value is less than 0.1 and so there is enough evidence to conclude that the phenotype proportions differ from those in  $H_0$ .
- (d) The  $P$ -value is less than 0.1 and so there is not enough evidence to conclude that the phenotype proportions differ from those in  $H_0$ .
- (e) Run for your lives! The killer tomatoes are attacking!

4. The 2008 General Social Survey produced the following count data for  $n = 955$  families:

Income	Marital Happiness		
	Not	Pretty	Very
Above	123	105	7
Average	291	151	17
Below	172	83	6

The value of the  $\chi^2$  statistic for testing independence of income and marital happiness is 12.84. Which of the following is the correct conclusion for a test with  $\alpha = 0.05$ ?

- (a) The  $P$ -value is smaller than 0.05 and we therefore conclude that income and marital happiness are independent.
- (b) The  $P$ -value is smaller than 0.05 and we therefore conclude that income and marital happiness are not independent.
- (c) The  $P$ -value is larger than 0.05 and we therefore conclude that income and marital happiness are not independent.
- (d) The  $P$ -value is larger than 0.05 and we therefore conclude that income and marital happiness are independent.
- (e) Having a high income is the secret to happiness in marriage.

5. In Small Town, USA, the ages and smoking status of adult residents are distributed as:

		Age		
		18–30	31–45	Over 45
Smoking status	Nonsmoker	2000	3500	3000
	Smokes < one pack a day	400	800	400
	Smokes $\geq$ one pack a day	200	450	150

An adult is randomly selected from Small Town, USA, and it turns out that this adult is *not* a nonsmoker. The probability that this person is between the ages of 31 and 45 is:

- (a) 4750/10,900.
- (b) 1250/10,900.
- (c) 450/800.
- (d) 800/1600.
- (e) 1250/2400.

6. An experimenter investigated the effects of two stimulant drugs, labeled A and B. She had a total of 20 rats, and randomly assigned 4 rats to each of the following five treatment groups: placebo, Drug A low, Drug A high, Drug B low, and Drug B high. Twenty minutes after injection of the drug, each rat's activity level was measured. This led to the following (partially filled) ANOVA table:

Source	df	Sum of squares	Mean square	$F$
Treatments		181.3		
Within treatments		159.0		
Total	19	340.3		

The value of the  $F$ -statistic for testing the hypothesis that the mean activity level is the same for all five treatments is:

- (a) 0.534.
- (b) 9.72.
- (c) 3.192.
- (d) 1.140 .
- (e) 4.276.

7. In Question 6, the type of experimental design used is:

- (a) A split-plot design.
- (b) A randomized block design.
- (c) A completely randomized design.
- (d) A crossover design.
- (e) None of the above.

8. In a simple linear regression analysis, the residuals are:

- (a)  $y_i - (\hat{\beta}_0 + \hat{\beta}_1 x_i)$ , for  $i = 1, \dots, n$ .
- (b) Used to check whether the variability of  $y$  tends to increase with  $x$ .
- (c) Used to check whether or not the relationship between the response variable  $y$  and the independent variable (or covariate)  $x$  is linear.
- (d) All of the above.
- (e) None of the above.

9. In a simple linear regression analysis based on a sample of 100 observations, the 95% confidence interval (CI) for the regression parameter  $\beta_1$  turned out to be (0.27, 0.52). Then, which of the following is the best and most meaningful interpretation of this CI?

- (a) About 95% of the time the true parameter  $\beta_1$  lies within this interval.
- (b) About 95% of the time the parameter estimate  $\hat{\beta}_1$  lies within this interval.
- (c) If one repeats the data collection process many times and constructs a 95% CI for  $\beta_1$  each time, then about 95% of these intervals will contain the parameter estimate  $\hat{\beta}_1$ .
- (d) If one repeats the data collection process many times and constructs a 95% CI for  $\beta_1$  each time, then about 95% of these intervals will contain the true parameter  $\beta_1$ .
- (e) About 95% of the time the true response variable lies within this interval.

10. I graded a quiz for 12 students in my class. Their scores (out of 10 points) are as follows:

7, 5, 5, 7, 7, 9, 8, 6, 9, 8, 6, 7.

Suppose I want to test the following hypotheses for the median ( $M$ ) of the population of my students' scores:  $H_0 : M = 6.5$  vs.  $H_a : M > 6.5$ , and suppose I use the Sign test to do so. Then, the  $Z$ -statistic and the approximate  $P$ -value for this Sign test are closest to:

- (a)  $Z$ -statistic = -1.1547;  $P$ -value  $\approx 0.125$ .
- (b)  $Z$ -statistic = -1.1547;  $P$ -value  $\approx 0.875$ .
- (c)  $Z$ -statistic = 1.1547;  $P$ -value  $\approx 0.875$ .
- (d)  $Z$ -statistic = 1.1547;  $P$ -value  $\approx 0.125$ .
- (e)  $Z$ -statistic = 1.1547;  $P$ -value  $\approx 0.25$ .