

## CS 330 : Discrete Computational Structures

Spring Semester, 2019

ASSIGNMENT #4

**Due Date:** Wednesday, February 20

**Suggested Reading:** Rosen Sections 2.1 - 2.3; Lehman et al. Chapter 4.1, 4.3, 4.4

These are the problems that you need to hand in for grading. Always explain your answers and show your reasoning.

1. [6 Pts] Prove that if  $A \subseteq B$  and  $C \subseteq D$ , then  $A \times C \subseteq B \times D$ .
2. [6 Pts] Use Venn diagrams to show that  $(B - A) \cup (C - A) = (B \cup C) - A$ .
3. [6 Pts] Use an iff argument to prove that  $(B - A) \cup (C - A) = (B \cup C) - A$ . Use logical equivalences in your proof.
4. [8 Pts] Disprove the statements below.
  - (a) If  $A - C = B - C$  then  $A = B$ .
  - (b) If  $A \cap C = B \cap C$  then  $A = B$ .
5. [8 Pts] Prove that if  $A - C = B - C$  and  $A \cap C = B \cap C$  then  $A = B$ .
6. [8 Pts] Prove that  $\overline{A \cup B} = \overline{A} \cap \overline{B}$ . To prove  $S = T$ , where  $S$  and  $T$  are sets, prove that each set is a subset of the other. To prove  $S \subseteq T$ , prove that if any element  $x$  is in  $S$  then it is in  $T$ . You *may not* use logical equivalences in your proof. Use general proof techniques like ‘proof by contradiction’ and ‘proof by cases’.
7. [4 Pts] Prove that  $f(n) = 5n + 12$  is one-to-one, where the domain and co-domain of  $f$  is  $\mathbb{Z}^+$ . Show that  $f$  is not onto.
8. [4 Pts] Prove that  $f(m, n) = 3mn$  is onto, where the domain of  $f$  is  $\mathcal{R} \times \mathcal{R}$  and the co-domain of  $f$  is  $\mathcal{R}$ . Show that  $f$  is not one-to-one.

For more practice, you are encouraged to work on the problems given in Rosen Sections 2.1 - 2.3 and Lehman et al. Chapter 4.1, 4.3, 4.4.