

# FUN — Untyped — Environment

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Abstract

This is the  $\mathbb{K}$  semantic definition of the untyped FUN language. FUN is a pedagogical and research language that captures the essence of the functional programming paradigm, extended with several features often encountered in functional programming languages. Like many functional languages, FUN is an expression language; that is, everything, including the main program, is an expression. Functions can be declared anywhere and are first class values in the language. FUN is call-by-value here, but has been extended to a broader framework (a.k.a. *monads*) with other parameter-passing styles. To make it more interesting and to highlight some of  $\mathbb{K}$ 's strengths, FUN includes the following features: *monads*, *type checking* and *inference* is performed to ensure that the type constructors are used correctly. The execution will simply get stuck when they are misused. Moreover, since no type checking is performed, the data-types are not even declared in the untyped version of FUN.

- Functions and `let/letrec` binders can take multiple space-separated arguments, but these are designed to ones that only take one argument, by currying. For example, the expression

```
fun x y -> x y
let x y = y in x
```

are desugared, respectively, into the following expressions:

```
fun x -> fun y -> x y
let x = fun y -> y in x
```

- Functions can be defined using pattern matching over the available data-types. For example, the program

```
letrec max = fun [h] -> h
| [h1] -> let x = max t
in if h > x then h else x
in max [1, 3, 5, 2, 4, 0, -1, -5]
```

defines a function `max` that calculates the maximum element of a non-empty list, and the function

```
letrec ack = fun Pair (0, n) -> n + 1
| Pair (n, 0) -> ack Pair (n - 1, 1)
| Pair (n, n) -> ack Pair (n - 1, ack Pair (n, n - 1))
in ack Pair (2, 3)
```

calculates the Ackermann function applied to a particular pair of numbers. Patterns can be nested. Patterns can currently only be used in function definitions, and not directly in `let/letrec` binders. For example, this is not allowed:

```
letrec Pair (x, y) = Pair (1, 2) in x + y
```

But this is allowed:

```
let f Pair (x, y) = x + y in f Pair (1, 2)
```

because it is first reduced to

```
let f = fun Pair (x, y) -> x + y in f Pair (1, 2)
```

by uncursing of the `let` binder, and pattern matching is allowed in function arguments.- We include a `callcc` construct, for two reasons: first, several functional languages support this construct; second, some constructs from *monads* have difficulties defining in  $\mathbb{K}$ . Not  $\mathbb{K}$ .
- Finally, we include *mutables* by means of referencing an expression, getting the reference of a variable, dereferencing and assignment. We include these for the same reasons as above: there are languages which have them, and they are not easy to define in some semantic frameworks.

Like in many other languages, some of FUN's constructs can be degraded into a smaller set of basic constructs. We do that in our small, simple module, and then we only give semantics to the core constructs.

**Notes:** We recommend the reader to first consult the dynamic semantics of the LAMBDA++ language in the first part of the  $\mathbb{K}$  tutorial. To keep the comments below small and focused, we will not re-explain functional or  $\mathbb{K}$  features that have already been explained in there.

Syntax

## MODULE FUN-UNTYPED-SYNTAX

FUN is an expression language. The constructs below fall into several categories: names, arithmetic constructs, conventional functional constructs, patterns and pattern matching, data constructs, lists, references, and call-with-current-continuation (callcc). The arithmetic constructs are standard; they are present in almost all our  $\mathbb{K}$  language definitions. The meaning of FUN's constructs are discussed in more depth when we define their semantics in the next module.

The Syntactic Constructs

We start with the syntactic definition of FUN names. We have several categories of names: ones to be used for functions and variables, others to be used for data constructors, others for types and others for type variables. We will introduce them as needed, starting with the former category. We prefer the names of variables and functions to start with lower case letters. We take the freedom to tacitly introduce syntactic list-sequences for each nonterminal for which we need them.

SYNTAX *Name* ::= [*token*, *notInRules*, *autoReject*, *regex*([a-z][\_a-zA-Z0-9]\*)]

SYNTAX *Names* ::= List(*Name*, "...")

Expression constructs will be defined throughout the syntax module. Below are the very basic ones, namely the builtins, the names, and the parentheses used as brackets for grouping. Lists of expressions are declared strict, so all expressions in the list get evaluated whenever the list is on a position which can be evaluated:

SYNTAX *Exp* ::= *Int*  
| *Bool*  
| *String*  
| *Name*  
| (*Exp*) [*bracket*]

SYNTAX *Exprs* ::= List(*Exp*, "...") [*strict*]

We next define the syntax of arithmetic constructs, together with their relative priorities and left-to-non-associativities. We also tag all these rules with a new tag, "arith", so we can more easily define global syntax priorities later (at the end of the syntax module).

SYNTAX *Exp* ::= *Exp* + *Exp* [*strict*, *arith*]  
*Exp* / *Exp* [*strict*, *arith*]  
*Exp* \* *Exp* [*strict*, *arith*]  
*Exp* < *Exp* [*strict*, *arith*]  
*Exp* > *Exp* [*strict*, *arith*]  
*Exp* <= *Exp* [*strict*, *arith*]  
*Exp* >= *Exp* [*strict*, *arith*]  
*Exp* == *Exp* [*strict*, *arith*]  
*Exp* != *Exp* [*strict*, *arith*]  
| *Exp* [*strict*, *arith*]  
| *Exp* 66 *Exp* [*strict*], *arith*]  
| *Exp* [] *Exp* [*strict*], *arith*]

The conditional construct has the expected evaluation strategy, stating that only the first argument is evaluate:

SYNTAX *Exp* ::= if *Exp* then *Exp* else *Exp* [*strict*], []]

FUN's builtin lists are formed by enclosing comma-separated sequences of expressions (i.e., terms of sort *Exprs*) in square brackets. The list constructor `cons` adds a new element in the top of the list, `head` and `tail` get the first element and the tail subset of a list if they exist, respectively, and `get stuck` otherwise, and `not137?` tests whether a list is empty or not, syntactically. `Pair` (or `P`, `P2`, `P3`) is a constructor term holding two numbers, `Cons` (or `C`, `Cons` (2, `Cons` (3, `Cons` (4, `Cons` (5, `Cons` (6, `Cons` (7, `Cons` (8, `Cons` (9, `Cons` (10, `Cons` (11, `Cons` (12, `Cons` (13, `Cons` (14, `Cons` (15, `Cons` (16, `Cons` (17, `Cons` (18, `Cons` (19, `Cons` (20, `Cons` (21, `Cons` (22, `Cons` (23, `Cons` (24, `Cons` (25, `Cons` (26, `Cons` (27, `Cons` (28, `Cons` (29, `Cons` (30, `Cons` (31, `Cons` (32, `Cons` (33, `Cons` (34, `Cons` (35, `Cons` (36, `Cons` (37, `Cons` (38, `Cons` (39, `Cons` (40, `Cons` (41, `Cons` (42, `Cons` (43, `Cons` (44, `Cons` (45, `Cons` (46, `Cons` (47, `Cons` (48, `Cons` (49, `Cons` (50, `Cons` (51, `Cons` (52, `Cons` (53, `Cons` (54, `Cons` (55, `Cons` 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