

BF

The brainfuck language uses a simple machine model consisting of the program and instruction pointer, as well as an array of at least 30,000 byte cells initialized to zero; a movable data pointer (initialized to point to the leftmost byte of the array); and two streams of bytes for input and output (most often connected to a keyboard and a monitor respectively, and using the ASCII character encoding).

MODULE BF-SYNTAX

The syntax of the language consists in eight commands: > < + - . , []

SYNTAX *Ignore* ::= [token, onlyLabel, regex(`[^><+~\.\[\]\+]`)

SYNTAX *Instruction* ::= >
| <
+
.
, [onlyLabel]
[Instructions]
Ignore

A Brainfuck program consists in a list of commands. Brainfuck ignores all characters except the eight commands +-<>[],. so no special syntax for comments is needed. Unfortunately, because of K parsing issues, we assume that programs contain only the language instructions.

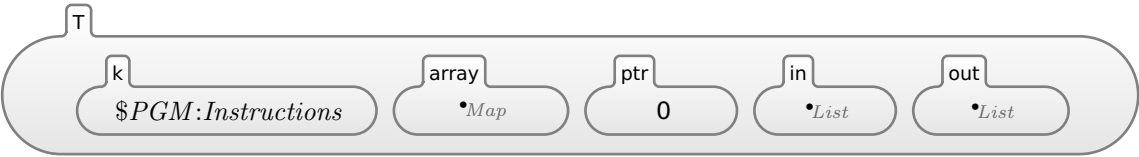
SYNTAX *Instructions* ::= List{Instruction, ""}

END MODULE

MODULE BF

The configuration of the language contains the K cell for Brainfuck programs, an array cell containing the byte array, a cell ptr for the instruction pointer and I/O streams.

CONFIGURATION:



Unroll intructions into KList.

RULE
$$\frac{I:Instruction\ Is:Instructions}{I \curvearrowright Is}$$

RULE
$$\frac{\bullet Instructions}{\bullet K}$$

Output the byte at the data pointer.

RULE
$$\frac{\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{'.()}{\bullet K} \quad \begin{array}{|c|} \hline array \\ \hline \end{array} \frac{P \mapsto V:Int}{P:Int} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{P:Int} \quad \begin{array}{|c|} \hline out \\ \hline \end{array} \frac{\bullet List}{ListItem(\text{chrChar}(V))}$$

Input the byte at the data pointer.

RULE
$$\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{',()}{\bullet K} \quad \begin{array}{|c|} \hline array \\ \hline \end{array} \frac{P \mapsto \text{---}}{V} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{P:Int} \quad \begin{array}{|c|} \hline in \\ \hline \end{array} \frac{ListItem(V:Int)}{\bullet List}$$

Increment the data pointer.

RULE
$$\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{>}{\bullet K} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{(P +_{Int} 1)}$$

Decrement the data pointer.

RULE
$$\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{<}{\bullet K} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{(P -_{Int} 1)}$$

Increment the byte at the data pointer

RULE
$$\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{+}{\bullet K} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{P:Int} \quad \begin{array}{|c|} \hline array \\ \hline \end{array} \frac{P \mapsto V:Int}{(V +_{Int} 1) \bmod_{Int} 256}$$

Decrement the byte at the data pointer

RULE
$$\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{-}{\bullet K} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{P:Int} \quad \begin{array}{|c|} \hline array \\ \hline \end{array} \frac{P \mapsto V:Int}{(V -_{Int} 1) \bmod_{Int} 256}$$

Brainfuck jumps ('[' and ']') are considered to be loops. Whenever the byte at the data pointer is not zero, execute the loops instructions.

RULE
$$\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{[Is:Instructions]}{Is \curvearrowright [Is]} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{P:Int} \quad \begin{array}{|c|} \hline array \\ \hline \end{array} \frac{P \mapsto V:Int}{P \mapsto V:Int} \quad \text{requires } V \neq_{Int} 0$$

RULE
$$\begin{array}{|c|} \hline k \\ \hline \end{array} \frac{[Is:Instructions]}{\bullet K} \quad \begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{P:Int}{P:Int} \quad \begin{array}{|c|} \hline array \\ \hline \end{array} \frac{P \mapsto 0}{P \mapsto 0}$$

RULE
$$\frac{I:Ignore}{\bullet K}$$

RULE
$$\begin{array}{|c|} \hline ptr \\ \hline \end{array} \frac{I:Int}{I:Int} \quad \begin{array}{|c|} \hline array \\ \hline \end{array} \frac{M:Map \quad \bullet Map}{I \mapsto 0} \quad \text{requires } \neg_{Bool}(I \text{ in keys}(M)) \wedge_{Bool}(I \geq_{Int} 0)$$

[structural]

END MODULE