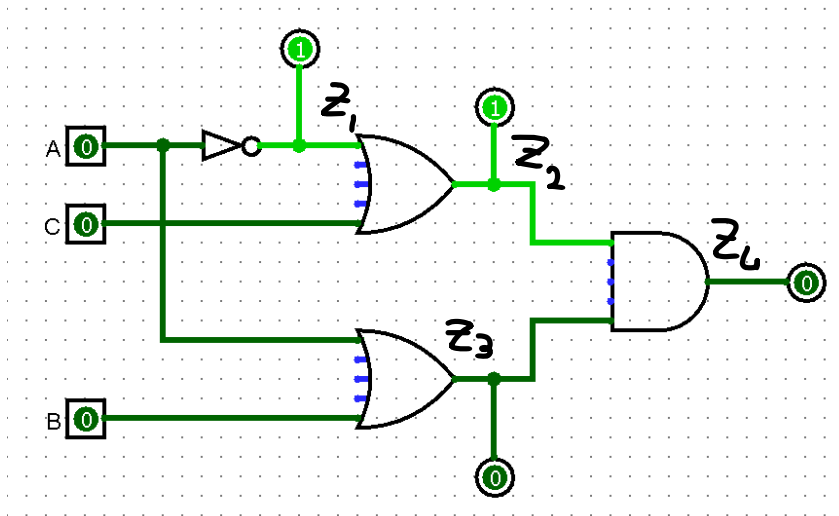


Esercizio 1



+ = OR, * = AND, ~ = NOT

$$Z1 = \sim A$$

$$Z2 = Z1 + C = \sim A + C$$

$$Z3 = A + B$$

$$Z4 = Z2 * Z3 = (\sim A + C) * (A + B)$$

A	B	C	Z1=~A	Z2=~A+C	Z3=A+B	Z4=Z2*Z3
0	0	0	1	1	0	0
0	0	1	1	1	0	0
0	1	0	1	1	1	1
0	1	1	1	1	1	1
1	0	0	0	0	1	0
1	0	1	0	1	1	1
1	1	0	0	0	1	0
1	1	1	0	1	1	1

Esercizio 2

La XNOR identifica quando i due bit in ingresso sono identici. In questo caso l'output vale 1, altrimenti 0.

A	B	Z=A XNOR B
0	0	1
0	1	0
1	0	0
1	1	1

$$Z = (\sim A * \sim B) + (A * B) = \sim(A + B) + (A * B)$$

Esercizio 3

$$X = \sim A + \sim(B + \sim C)$$

A	B	C	$\sim A$	$\sim C$	$B + \sim C$	$\sim(B + \sim C)$	$X = \sim A + \sim(B + \sim C)$
0	0	0	1	1	1	0	1
0	0	1	1	0	0	1	1
0	1	0	1	1	1	0	1
0	1	1	1	0	1	0	1
1	0	0	0	1	1	0	0
1	0	1	0	0	0	1	1
1	1	0	0	1	1	0	0
1	1	1	0	0	1	0	0

Esercizio 4

$$\text{DISTRIBUTIVA(AND)} = X * (Y + Z) = X * Y + X * Z$$

$$\text{ASSORBIMENTO II} = X * (-X + Y) = X * Y$$

$$E1 = \sim(\sim A * B * \sim C + A * B * \sim C) * A$$

$$E2 = (\sim B * A) + (A * C)$$

$$E1 = E2?$$

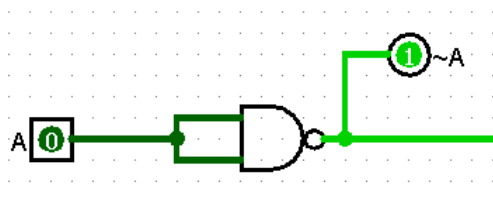
$$\begin{aligned} E1 &= \sim(\sim A * B * \sim C + A * B * \sim C) * A = \text{DISTRIBUTIVA(AND), COMMUTATIVA(AND)} = \sim((\sim A * B + A * B) * \sim C) * A = \\ &\text{DISTRIBUTIVA(AND), COMMUTATIVA(AND)} = \sim(((\sim A + A) * B) * \sim C) * A = \text{INVERSO(OR)} = \sim((1 * B) * \sim C) * A = \\ &\text{IDENTITA'(AND)} = \sim(B * \sim C) * A = \text{DeMorgan(AND)} = (\sim B + C) * A = \text{DISTRIBUTIVA(AND)} = \sim B * A + C * A = \\ &\text{COMMUTATIVA(AND)} = \sim B * A + A * C \end{aligned}$$

Esercizio 5

$$E1 = (A \text{ NOR } B) * (C + \sim B) \text{ tramite solo porte NAND}$$

A	B	$Z = A \text{ NAND } B = \sim(A * B)$
0	0	1
0	1	1
1	0	1
1	1	0

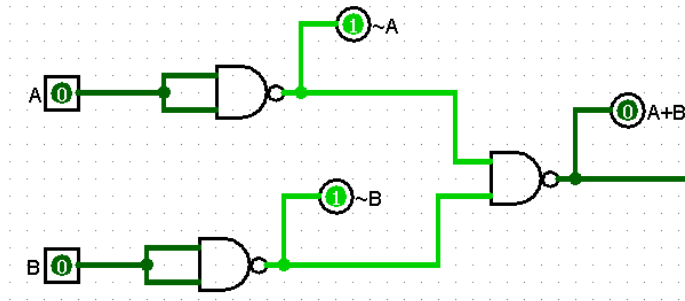
$$\sim A = A \text{ NAND } A$$



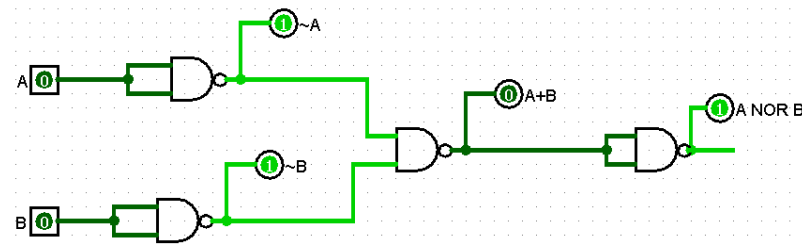
A	B	$Z = A \text{ NOR } B = \sim(A + B)$
0	0	1

0	1	0
1	0	0
1	1	0

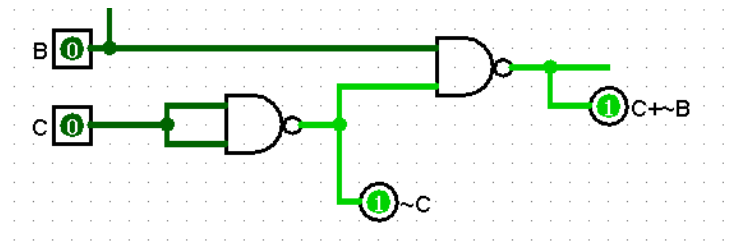
$$A+B = \sim\sim(A+B) = \text{DeMorgan(OR)} = \sim(\sim A * \sim B) = \sim A \text{ NAND } \sim B$$



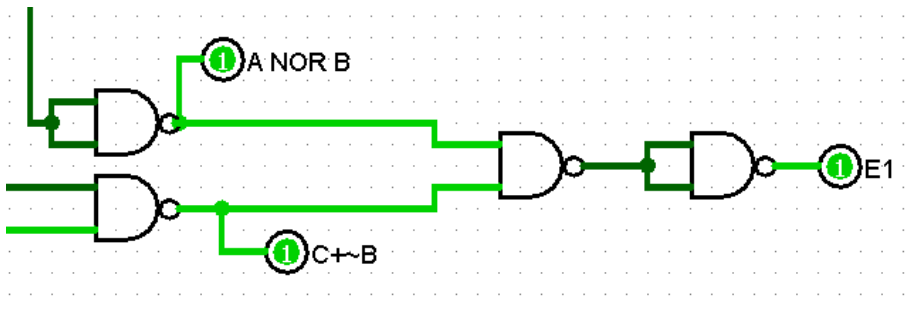
$$A \text{ NOR } B = \sim(A+B) = (\sim A \text{ NAND } \sim B) \text{ NAND } (\sim A \text{ NAND } \sim B) = ((A \text{ NAND } A) \text{ NAND } (B \text{ NAND } B)) \text{ NAND } ((A \text{ NAND } A) \text{ NAND } (B \text{ NAND } B))$$



$$C+\sim B = \sim C \text{ NAND } B$$



$$E1 = (A \text{ NOR } B) * (C+\sim B)$$



$$E2 = \sim A * \sim B$$

$$E1 = E2?$$

$$E1 = \sim(A+B) * (C+\sim B) = \text{DeMorgan(OR)} = (\sim A * \sim B) * (C+\sim B) = \text{DISTRIBUTIVA(AND)} = (\sim A * \sim B * C) + (\sim A * \sim B) = \text{DISTRIBUTIV A(AND)} = \sim A * \sim B * (C+1) = \text{ELEMENTO NULL(OR)} = \sim A * \sim B$$